

Probing electron acceleration and x-ray emission in laser-plasma accelerators

Cédric Thaury, Kim Ta Phuoc, Sébastien Corde, P. Brijesh, Guillaume Lambert, S. P. D. Mangles, M. S. Bloom, S. Kneip, Victor Malka

To cite this version:

Cédric Thaury, Kim Ta Phuoc, Sébastien Corde, P. Brijesh, Guillaume Lambert, et al.. Probing electron acceleration and x-ray emission in laser-plasma accelerators. Physics of Plasmas, 2013, 20 (6) , pp.063101. 10.1063/1.4810791. hal-01163773

HAL Id: hal-01163773 <https://hal.science/hal-01163773v1>

Submitted on 13 Jul 2015

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

[Probing electron acceleration and x-ray emission in laser-plasma](http://dx.doi.org/10.1063/1.4810791) [accelerators](http://dx.doi.org/10.1063/1.4810791)

C. Thaury,¹ K. Ta Phuoc,¹ S. Corde,¹ P. Brijesh,¹ G. Lambert,¹ S. P. D. Mangles,² M. S. Bloom,² S. Kneip,² and V. Malka¹ ¹Laboratoire d'Optique Appliquée, ENSTA ParisTech-CNRS UMR7639-École Polytechnique ParisTech, Chemin de la Hunière, 91761 Palaiseau, France 2 Blackett Laboratory, Imperial College, London SW7 2AZ, United Kingdom

(Received 12 March 2013; accepted 2 May 2013; published online 10 June 2013)

While laser-plasma accelerators have demonstrated a strong potential in the acceleration of electrons up to giga-electronvolt energies, few experimental tools for studying the acceleration physics have been developed. In this paper, we demonstrate a method for probing the acceleration process. A second laser beam, propagating perpendicular to the main beam, is focused on the gas jet few nanosecond before the main beam creates the accelerating plasma wave. This second beam is intense enough to ionize the gas and form a density depletion, which will locally inhibit the acceleration. The position of the density depletion is scanned along the interaction length to probe the electron injection and acceleration, and the betatron X-ray emission. To illustrate the potential of the method, the variation of the injection position with the plasma density is studied. © 2013 AIP Publishing LLC. [[http://dx.doi.org/10.1063/1.4810791\]](http://dx.doi.org/10.1063/1.4810791)

Over the past decade, considerable progress has been made in the development of laser-plasma accelerators.¹ These accelerators can now deliver quasi-mono energetic electron beams² with energy up to 1 GeV (Ref. 3) and energy spread close to 1% .⁴ A significant step forward has also been achieved in the control and the stabilization of the accelerator using controlled injection techniques (e.g., colliding pulses injection, 5 down-ramp injection, $6,7$ or ionization injection⁸). However more improvements, in particular in terms of stability and energy spread, are needed for laser-plasma accelerators to compete with state of the art conventional accelerators. To further push the performance of laserplasma accelerators and enhance control over the interaction, a thorough knowledge of the details of the interaction is required.

In a laser plasma accelerator, electrons are injected in a relativistic plasma wave, which is excited in the WAKE of an intense laser pulse propagating in an underdense plasma. The electric field associated with the plasma wave has a very large amplitude of a few hundreds of gigavolt per meter. Electrons can therefore be accelerated to a few hundreds of MeV within just a few millimeters. Three phenomena play an important role in a laser plasma accelerator: the laser propagation; the electron injection; and the electron acceleration itself. All these phenomena are difficult to experimentally characterize, which can be largely traced back to the very small size of the accelerator and to the extremely fast (femtosecond) dynamics of the interaction. As a result, current knowledge of the laser-plasma interaction relies heavily on numerical simulations. This lack of experimental information could hinder the development of laser-plasma accelerators. New experimental tools were therefore recently developed to get more insight into the acceleration process. Among these, the observation of the shadow of a small aperture illuminated with Betatron X-ray radiation was used to map the acceleration length and injection position.^{9,10} The acceleration phase was also probed by varying the acceleration length, using different methods.^{5,11–13} Further information about the plasma wave was obtained from interferometric 14 and magnetic fields $15,16$ measurements. Techniques were also developed to determine whether electrons are trapped in the first plasma wave period, 17 whether they are trapped in two or more periods 18 and to determine the position of injection. 19 In this letter, we present a method for probing the acceleration. It relies on the use of a second laser beam to locally disrupt the accelerating structure and hence assess the influence of a given part of the plasma on electron acceleration and X-ray emission.

The experiment was performed at Laboratoire d'Optique Appliquée using the "Salle Jaune" Ti:Sa laser system, which delivers two laser pulses (main and disrupting beams) with a full width at half maximum (FWHM) duration of 35 fs and a linear polarization. The main laser pulse had an energy of 900 mJ. It was focused by a $F/15$ spherical mirror in a 3 mm supersonic helium gas jet. The FWHM focal spot size was $14 \times 18 \mu m^2$, and the peak intensity was about 4.6×10^{18} W cm⁻², corresponding to a normalized amplitude $a_0 = 1.5$. The disrupting pulse had an energy of 100 mJ. It made an angle of 90° with the main beam (see Fig. 1) and was focused into the gas jet with a $F/10$ plano-convex lens to an intensity of $\approx 7 \times 10^{17}$ W cm⁻². The intensity of the disrupting laser pulse was thus much larger than in experiments where the plasma channel created by a second pulse is used to trigger the electron injection $20,21$ (the electron density in the present experiment is also larger). The disrupting beam entered the plasma 2 ns before the main beam. Electron beam spectra were measured with a spectrometer consisting of a dipole magnet $(1.1 T$ over $10 \text{ cm})$ and a LANEX phosphor screen. Betatron X-ray beam profiles were measured using a X-ray CCD camera with 2048×2048 pixels of size 13.5 μ m × 13.5 μ m, situated 73 cm from the gas jet and protected from the laser light by a

FIG. 1. Experimental set up.

13 μ m Al filter. The density depletion created by the disrupting beam was observed using a Wollaston interferometer.

Figure 2 shows an interferogram of the plasma obtained a few picoseconds after the main beam has entered the gas jet. The plasma formed by the main beam is visible between the two dotted lines. The disrupting beam propagates perpendicular to the main beam and ionizes the helium gas along its path. With time, this plasma expands hydrodynamically, which creates a density depression at the center of the plasma column. This depletion zone is clearly observed in Fig. 2 (dotted circle). The full width of this zone is $\delta \approx 250 \ \mu m$. The amplitude of the depletion cannot be determined precisely because the phase shift is too large. We will show in the following that it is, however, sufficient to prevent electron injection and acceleration locally, in contrast with Refs. 20 and 21. The electron acceleration process can thus be probed by moving the position of the disrupting beam along the main beam path to inhibit the acceleration in a given zone of the plasma and hence assess the influence of this zone on the acceleration.

Figure 3 shows the beam charge Q and the peak electron energy E as a function of the disrupting beam position z , for an electron density $n_e = 10^{19}$ cm⁻³. In this experiment, electron spectra were broad (because of a long injection length due to relatively high densities). For $z \lesssim 1.6$ mm, the disrupting beam has no influence on the electron beam features $(E \text{ and } Q \text{ are the same as without disrupting beam}).$ This indicates that no electrons are injected in this part of the plasma. The intensity of the main laser pulse for $z \leq 1.6$ mm

FIG. 2. Interferometric image of the plasma obtained \approx 5.6 ps after the main laser pulse has entered the gas jet. The laser goes from right to left. The dotted red lines highlight the beam path. The width of the density depletion zone created by the disrupting beam (dashed blue circle) is $\delta = 255 \pm 15 \,\mu \text{m}$.

FIG. 3. Beam charge Q (a), peak electron energy E (b), betatron yield S and quantity S/Q (c) as a function of the position in the plasma for $n_e = 10^{19}$ cm⁻³. The position $z = 0$ corresponds to the entrance of the gas jet. The red dashed lines indicate the estimated injection and acceleration lengths. The black stars correspond to shots without the disrupting beam. The black dashed lines indicate the mean charge and energy without disrupting beam. Each point corresponds to an average over 5 to 27 shots. The error bars correspond to standard errors of the mean. (d) Schematic of possible injection and acceleration profiles.

is not sufficient to trigger the injection of electrons into the relativistic plasma wave. As the main laser pulse propagates in the plasma, it self-focuses and eventually reaches an intensity high enough to trigger the injection for $z \gtrsim 1.6$ mm. For 1.6 mm $\le z \le 2$ mm, Q is strongly reduced, which demonstrates that the disrupting beam inhibits locally the plasma wave and prevents electron injection in the depletion zone. From $z \approx 2$ mm, Q increases until it reaches its initial value for $z \gtrsim 2.2$ mm. The influence of the disrupting beam on the injection is thus less dramatic in this part of the plasma. An estimate of the injection length L_{inj} can be obtained from these measurements. The function $Q(z)$ is actually a convolution of the injection zone with the depletion profile. Assuming that the depletion profile can be described by a square function of width δ , we find that $L_{ini} \approx 0.4$ mm. Thus, the disrupting beam reduces the injection length by $\delta/L_{\text{ini}} \approx 70\%$, which is consistent with a decrease of Q from 72 pC down to 21 pC at minimum.

The evolution of the peak electron energy E in Fig. 3(b) is somewhat different from that of the electron charge Q. The energy remains small for a longer length than Q , and it comes back to its initial value only for $z \ge 2.4$ mm (instead of \approx 2 mm for Q). For 2 mm \approx z \approx 2.4 mm, very few electrons are injected but electrons that have been injected earlier are still accelerated in the plasma wave. Focusing the disrupting beam in this region shortens the total acceleration and hence reduces the peak electron energy E. For $z \ge 2.4$ mm, the disrupting beam has no effect on E, which suggests that the laser intensity has decreased down to a level at which it can no more sustain a plasma wave, so that the acceleration stops. The acceleration length L_{acc} is estimated to be $L_{acc} \approx 0.6$ mm. The shortening of the acceleration length due to the disrupting beam is $\delta/L_{acc} \approx 40\%$, in good agreement with the decrease of E from 150 MeV down to 87 MeV. A schematic of possible injection and acceleration profiles that would be consistent with the experimental measurements is displayed in Fig. 3(d).

Also shown in Fig. 3 is the X-ray emission yield (energy in the beam integrated over angles and frequencies) due to betatron transverse oscillations of relativistic electrons into the plasma wave. 22 The variations of the X-ray yield S (left axis in Fig. $3(c)$ and of the electron charge Q (Fig. $3(a)$) are very similar, which indicate that S depends mainly on the electron charge. Some influence of the electron peak energy E is however noticed for $z \ge 1.9$ mm. To assess more quantitatively the influence of E on S , we plotted in Fig. $3(c)$ (right axis) the betatron yield by unit of charge S/Q. As anticipated, the quantity $S/Q(z)$ is observed to vary approximately as $E(z)$ (Fig. $3(b)$). However, the dependence of S on E is much weaker than reported in previous works.²³ The betatron yield is divided only by 1.5 when the electron energy is decreased from 150 MeV down to 85 MeV, while in Ref. 23 the betatron yield around 3 keV is divided by more than 10 for the same variation of E . Three main reasons can explain this difference. First, the interaction regime is different. The electron spectrum is broad, while in Ref. 23, quasi-monoenergetic electron beams were accelerated. In Fig. $3(c)$, the variation of the betatron yield with the electron energy is thus convolved with the electron spectrum, which tends to smooth the variations of S with E. Second, S in Fig. $3(c)$ is integrated over a large spectral bandwidth, while in Ref. 23, a narrow spectral window is selected. The betatron critical energy and hence the whole betatron spectrum shifts to higher frequencies when E increases. As the quantum efficiency of the X-ray camera decreases for $E \ge 3$ keV, our detection system tends to underestimate the increase of the betatron yield with the electron energy. Finally, the amplitude of the betatron oscillations is increased in the density depletion, which can enhance the betatron emission.²⁴ This effect may counterbalance the decrease of S due to the shortening of the acceleration length and thus may contribute to explain the weak dependence of S on E . To estimate the significance of this last effect and demonstrate an enhancement of the betatron emission, the ratio δ/L_{acc} should be decreased. More generally, the strong similarity between the variations of S , Q , and E confirms the strong correlation between relativistic electrons and betatron X -rays.²³ It shows also that the measure of X-ray emission can provide information on the acceleration.

We observed in Fig. 3 that for an electron density $n_e = 10^{19}$ cm⁻³, the injection begins at $z \approx 1.6$ mm from the gas jet entrance. In other words, 1.6 mm is required for the laser to reach an intensity sufficient to trigger the injection. As the laser propagation is largely determined by selffocusing and self-compression, both depend on the plasma density n_e , the injection position z_{inj} is also expected to vary with n_e . To check this, $z_{inj}(n_e)$ is plotted in Fig. 4 for 7×10^{18} cm⁻³ $< n_e < 1.6 \times 10^{19}$ cm⁻³. These data are compared with the position of the peak laser intensity z_{peak} obtained from WAKE simulations.²⁵ WAKE is a twodimensional cylindrical relativistic particle code. It describes the interaction of a laser pulse with an underdense plasma using the quasi-static approximation. The laser pulse is gaussian in time and space with a FWHM duration of 35 fs and a focal spot size of 16 μ m FWHM. The measured density profile is modeled by a trapezoid with 700 μ m ramps and a full length of 3.5 mm. The laser is focused 500 μ m beyond the gas jet center.

As expected, z_{inj} and z_{peak} both decrease when n_e increases. However, for $a_0 = 1.5$ the position z_{peak} is significantly smaller than z_{inj} . To get a better agreement between z_{inj} and z_{peak} smaller a_0 have to be used. Figure 4 also suggests that z_{inj} saturates at low density. This effect is not observed in simulations for the considered parameters. Such discrepancies between experiment and simulations were also observed in previous works, 10 where experimental data were compared to three dimensional particle-in-cell simulations. They may be due to an imperfect modeling of the experimental conditions (e.g., the modeling of the laser pulse by a Gaussian), $2⁶$ and to fact that wake does not describe the complex injection dynamics.27 Nevertheless, these discrepancies demonstrate a need for innovative tools to study laser plasma acceleration. An accurate knowledge of the dynamics of injection is clearly required before control of the injection, in particular, in the wavebreaking regime.

In conclusion, we demonstrated a method for probing the electron injection and acceleration lengths, as well as X-ray emission, in laser-plasma accelerators. This probing technique is similar to the one described in Ref. 12 where a second laser beam, focused on a line, is used to modify the acceleration length. Our technique presents several

FIG. 4. Injection position z_{inj} and peak laser intensity position z_{peak} as a function of the plasma density. The squares are experimental injection positions. The red lines correspond to the position of the peak laser intensity obtained from wAKE simulations performed for $a_0 = 1.5$ and $a_0 = 1$.

advantages. First, a local disruption provides information that cannot be obtained by changing the acceleration length. In particular, the method described in Ref. 12 does not allow to measure the injection profile, because for very short plasma lengths the electron energy is too low for electrons to be detected. With the method proposed here, only the part of the plasma where electrons are injected is disrupted. Electrons are still accelerated on a substantial length, allowing to probe the injection region. Second, the disrupting laser beam can be much less energetic than the machining beam in Ref. 12, because it is focused on a point rather than on a line. The setup is also simpler and easier to align. For instance, in Ref. 12 the line focus and the main beam path have to be perfectly superimposed, while here the position of the disrupting beam can be easily changed to probe a different region. The main advantage of the line focus setup is to allow the creation of structured plasmas for optimizing the acceleration.²⁸

Compared to the method presented in Ref. 10, our new technique has the disadvantages that it is multi-shot, requires a second beam, and modifies the interaction. It has, however, several advantages. The main one is that it provides direct and separate information on injection and acceleration, without using any model. Moreover, the earlier method¹⁰ needs a small aperture mask to be placed close to the accelerator exit. This can be difficult to achieve in many cases. Further the aperture mask erodes a bit after each shot, which hinders the precision of the measure. The new method is free of such limitations. Finally, the limit on resolution of the new method is likely to be less stringent. To improve this resolution, different disrupting beam features (intensity, spot size, duration) and delays between the disrupting and the main beams should be tested.

The research leading to these results has received funding from the European Research Council (PARIS ERC project) and LASERLAB-EUROPE (grant agreements No. 284464 and No. 228334, EC's Seventh Framework Programme).

- 2 J. Faure, Y. Glinec, A. Pukhov, S. Kiselev, S. Gordienko, E. Lefebvre, J. P. Rousseau, F. Burgy, and V. Malka, [Nature \(London\)](http://dx.doi.org/10.1038/nature02963) 431, 541 (2004); S. P. D. Mangles, C. D. Murphy, Z. Najmudin, A. G. R. Thomas, J. L. Collier, A. E. Dangor, E. J. Divall, P. S. Foster, J. G. Gallacher, C. J. Hooker, D. A. Jaroszynski, A. J. Langley, W. B. Mori, P. A. Norreys, F. S. Tsung, R. Viskup, B. R. Walton, and K. Krushelnick, [Nature \(London\)](http://dx.doi.org/10.1038/nature02939) 431, 535 (2004); C. G. R. Geddes, C. Toth, J. van Tilborg, E. Esarey, C. B. Schroeder, D. Bruhwiler, C. Nieter, J. Cary, and W. P. Leemans, [Nature](http://dx.doi.org/10.1038/nature02900) [\(London\)](http://dx.doi.org/10.1038/nature02900) 431, 538 (2004).
- W. P. Leemans, B. Nagler, A. J. Gonsalves, C. Toth, K. Nakamura, C. G. R. Geddes, E. Esarey, C. B. Schroeder, and S. M. Hooker, [Nat. Phys.](http://dx.doi.org/10.1038/nphys418) 2, 696 (2006).
- 4 C. Rechatin, J. Faure, A. Ben-Ismail, J. Lim, R. Fitour, A. Specka, H. Videau, A. Tafzi, F. Burgy, and V. Malka, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.102.164801) 102, 164801 (2009).
- 5 J. Faure, C. Rechatin, A. Norlin, A. Lifschitz, Y. Glinec, and V. Malka, [Nature \(London\)](http://dx.doi.org/10.1038/nature05393) 444, 737 (2006).
- ⁶K. Schmid, A. Buck, C. M. S. Sears, J. M. Mikhailova, R. Tautz, D. Herrmann, M. Geissler, F. Krausz, and L. Veisz, [Phys. Rev. ST Accel.](http://dx.doi.org/10.1103/PhysRevSTAB.13.091301) [Beams](http://dx.doi.org/10.1103/PhysRevSTAB.13.091301) 13, 091301 (2010).
- A. J. Gonsalves, K. Nakamura, C. Lin, D. Panasenko, S. Shiraishi, T. Sokollik, C. Benedetti, C. B. Schroeder, C. G. R. Geddes, J. van Tilborg, J. Osterhoff, E. Esarey, C. Toth, and W. P. Leemans, [Nat. Phys.](http://dx.doi.org/10.1038/nphys2071) 7, 862–866 (2011).
- 8 B. B. Pollock, C. E. Clayton, J. E. Ralph, F. Albert, A. Davidson, L. Divol, C. Filip, S. H. Glenzer, K. Herpoldt, W. Lu, K. A. Marsh, J. Meinecke, W. B. Mori, A. Pak, T. C. Rensink, J. S. Ross, J. Shaw, G. R. Tynan, C. Joshi, and D. H. Froula, *[Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.045001)* **107**, 045001 (2011).
- ⁹G. Genoud, K. Cassou, F. Wojda, H. E. Ferrari, C. Kamperidis, M. Burza, A. Persson, J. Uhlig, S. Kneip, S. P. D. Mangles, A. Lifschitz, B. Cros, and
- C.-G. Wahlström, [Appl. Phys. B: Lasers Opt.](http://dx.doi.org/10.1007/s00340-011-4639-4) 105, 309 (2011). ¹⁰S. Corde, C. Thaury, K. T. Phuoc, A. Lifschitz, G. Lambert, J. Faure, O. Lundh, E. Benveniste, A. Ben-Ismail, L. Arantchuk, A. Marciniak, A. Stordeur, P. Brijesh, A. Rousse, A. Specka, and V. Malka, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.215004)
- 107, 215004 (2011). $11J$. Faure, C. Rechatin, A. F. Lifschitz, X. Davoine, E. Lefebvre, and V.
- Malka, [IEEE Trans. Plasma Sci.](http://dx.doi.org/10.1109/TPS.2008.927430) 36, 1751 (2008). ¹²C.-T. Hsieh, C.-M. Huang, C.-L. Chang, Y.-C. Ho, Y.-S. Chen, J.-Y. Lin,
- J. Wang, and S.-Y. Chen, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.96.095001) ⁹⁶, 095001 (2006). 13S. Kneip, S. R. Nagel, S. F. Martins, S. P. D. Mangles, C. Bellei, O. Chekhlov, R. J. Clarke, N. Delerue, E. J. Divall, G. Doucas, K. Ertel, F. Fiuza, R. Fonseca, P. Foster, S. J. Hawkes, C. J. Hooker, K. Krushelnick, W. B. Mori, C. A. J. Palmer, K. T. Phuoc, P. P. Rajeev, J. Schreiber, M. J. V. Streeter, D. Urner, J. Vieira, L. O. Silva, and Z. Najmudin, [Phys. Rev.](http://dx.doi.org/10.1103/PhysRevLett.103.035002)
- [Lett.](http://dx.doi.org/10.1103/PhysRevLett.103.035002) **103**, 035002 (2009). $14N$. H. Matlis, S. Reed, S. S. Bulanov, V. Chvykov, G. Kalintchenko, T. Matsuoka, P. Rousseau, V. Yanovsky, A. Maksimchuk, S. Kalmykov, G. Shvets, and M. C. Downer, [Nat. Phys.](http://dx.doi.org/10.1038/nphys442) 2, 749 (2006).
¹⁵M. C. Kaluza, H.-P. Schlenvoigt, S. P. D. Mangles, A. G. R. Thomas, A.
- E. Dangor, H. Schwoerer, W. B. Mori, Z. Najmudin, and K. M.
- Krushelnick, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.105.115002) 105, 115002 (2010). ¹⁶A. Buck, M. Nicolai, K. Schmid, C. M. S. Sears, A. Sävert, J. M. Mikhailova, F. Krausz, M. C. Kaluza, and L. Veisz, [Nat. Phys.](http://dx.doi.org/10.1038/nphys1942) 7, 543 (2011). $17S$. P. D. Mangles, A. G. R. Thomas, M. C. Kaluza, O. Lundh, F. Lindau,
- A. Persson, F. S. Tsung, Z. Najmudin, W. B. Mori, C. G. Wahlstrom, and K. Krushelnick, *Phys. Rev. Lett.* **96**, 215001 (2006).
- ¹⁸Y. Glinec, J. Faure, A. Norlin, A. Pukhov, and V. Malka, *[Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.98.194801)*
- **98**, 194801 (2007).
¹⁹A. G. R. Thomas, S. P. D. Mangles, Z. Najmudin, M. C. Kaluza, C. D.
- Murphy, and K. Krushelnick, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.98.054802) ⁹⁸, 054802 (2007). 20J. Faure, C. Rechatin, O. Lundh, L. Ammoura, and V. Malka, [Phys.](http://dx.doi.org/10.1063/1.3469581)
- [Plasmas](http://dx.doi.org/10.1063/1.3469581) 17, 083107 (2010). ²¹P. Brijesh, C. Thaury, K. T. Phuoc, S. Corde, G. Lambert, V. Malka, S. P.
- D. Mangles, M. Bloom, and S. Kneip, [Phys. Plasmas](http://dx.doi.org/10.1063/1.4725421) 19, 063104 (2012). ²²A. Rousse, K. Ta Phuoc, R. Shah, A. Pukhov, E. Lefebvre, V. Malka, S. Kiselev, F. Burgy, J. P. Rousseau, D. Umstadter, and D. Hulin, [Phys. Rev.](http://dx.doi.org/10.1103/PhysRevLett.93.135005)
- [Lett.](http://dx.doi.org/10.1103/PhysRevLett.93.135005) 93, 135005 (2004).
²³S. Corde, K. T. Phuoc, R. Fitour, J. Faure, A. Tafzi, J. P. Goddet, V.
- Malka, and A. Rousse, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.255003) 107, 255003 (2011). ²⁴K. Ta Phuoc, E. Esarey, V. Leurent, E. Cormier-Michel, C. G. R. Geddes, C. B. Schroeder, A. Rousse, and W. P. Leemans, [Phys. Plasmas](http://dx.doi.org/10.1063/1.2918657) 15,
- 063102 (2008). ²⁵P. Mora and T. M. Antonsen, Jr., [Phys. Plasmas](http://dx.doi.org/10.1063/1.872134) 4, 217 (1997).
- ²⁶J. Vieira, S. F. Martins, F. Fiúza, C. K. Huang, W. B. Mori, S. P. D. Mangles, S. Kneip, S. Nagel, Z. Najmudin, and L. O. Silva, [Plasma Phys.](http://dx.doi.org/10.1088/0741-3335/54/5/055010)
- [Controlled Fusion](http://dx.doi.org/10.1088/0741-3335/54/5/055010) 54, 055010 (2012). $27S$. Kalmykov, S. A. Yi, V. Khudik, and G. Shvets, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.103.135004) 103,
- 135004 (2009). 28T.-S. Hung, Y.-C. Ho, Y.-L. Chang, S.-J. Wong, H.-H. Chu, J.-Y. Lin, J. Wang, and S.-Y. Chen, [Phys. Plasmas](http://dx.doi.org/10.1063/1.4729902) 19, 063109 (2012).

¹E. Esarey, C. B. Schroeder, and W. P. Leemans, [Rev. Mod. Phys.](http://dx.doi.org/10.1103/RevModPhys.81.1229) 81, 1229 (2009).

Physics of Plasmas is copyrighted by the American Institute of Physics (AIP). Redistribution of journal material is subject to the AIP online journal license and/or AIP copyright. For more information, see http://ojps.aip.org/pop/popcr.jsp