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▶ **To cite this version:**

Laura Chaix, Rafik Ballou, Andres Cano, Sylvain Petit, Sophie de Brion, et al.. Helical bunching and symmetry lowering inducing multiferroicity in Fe langasites. Physical Review B, 2016, 93 (21), pp.214419. 10.1103/PhysRevB.93.214419 . hal-01163057v2

HAL Id: hal-01163057
https://hal.science/hal-01163057v2

Submitted on 2 Jun 2016

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Helical bunching and symmetry lowering inducing multiferroicity in Fe langasites

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(Dated: June 2, 2016)

The chiral Fe-based langasites represent model systems of triangle-based frustrated magnets with a strong potential for multiferroicity. We report neutron scattering measurements for the multichiral $Ba_3MFe_3Si_2O_{14}$ (M = Nb, Ta) langasites revealing new important features of the magnetic order of these systems: the bunching of the helical modulation along the c-axis and the in-plane distortion of the 120° Fe-spin arrangement. We discuss these subtle features in terms of the microscopic spin Hamiltonian, and provide the link to the magnetically-induced electric polarization observed in these systems. Thus, our findings put the multiferroicity of this attractive family of materials on solid ground.

PACS numbers: 75.85.+t, 75.25.-j, 75.30.Ds, 75.30.Gw

The quest for novel magnetic orders that promote multiferroicity and strong magnetoelectric coupling drives a considerable amount of current research (see e.g. [1–4] for recent reviews). In this respect, Fe-based langasites are propitious materials displaying an original "multichiral" magnetic order in which a 120° Fe-spin arrangement undergoes an additional helical modulation [5–8]. In fact, the magnetoelectric effect in these systems has been demonstrated at both static [9] and dynamical levels [10]. In addition, Zhou *et al.* [11] have reported the emergence of ferroelectricity at the onset of magnetic order. This ferroelectricity has subsequently been confirmed by Lee et al. [12], who have also demonstrated the magnetic-field manipulation of the electric polarization. However, these works report two different ferroelectric axis at zero-field and, above all, leave the precise mechanism promoting such a ferroelectricity unidentified.

Magnetically-induced ferroelectricity in many multiferroic cycloidal magnets is due to the spin-orbit coupling (SOC) via the so-called inverse Dzyaloshinskii-Moryia (DM) mechanism [13–15]. However, this mechanism is ineffective for the reported helical magnetic structure of the langasites [16, 17]. An electric polarization observed in magnetic helices rather than cycloids has been theorized [18], as well as observed experimentally in $RbFe(MoO_4)_2$ for instance [16, 17, 19]. However, the invoked mechanisms still rely on the SOC and appear inapplicable in the langasite case. Bulaevskii *et al.* [3, 20, 21] have discussed another fundamental mechanism that can generically operate in triangle-based frustrated magnets. The proposed mechanism is independent of SOC as it simply relies, in the language of Mott insulators, on high-order hopping-term contributions that enable the redistribution of the electronic charge. This purely electronic mechanism can be supplemented by a contribution from lattice degrees of freedom [3]. In any case, it requires a distortion of the perfect 120°-spin structure and, despite its generality, has not been verified experimentally so far.

In this paper, we carefully analyze neutron scattering experiments to revise the magnetic structure of the $Ba_3MFe_3Si_2O_{14}$ (M = Nb, Ta) langasites. We discover additional features indicating the bunching of the helicoidal modulation and significant deviations from the 120°-spin structure in these systems. In order to explain these features, we propose an extended spin Hamiltonian incorporating different magnetic anisotropies. These extra terms prove to be crucial for understanding the magnetically-induced ferroelectricity in the Fe langasites. Furthermore, we find that this ferroelectricity emerges from a magnetoelectric coupling that is equivalent to the Bulaevskii *et al.* proposal at the phenomenological level.

The Fe langasites crystallize in the non-polar non-centrosymmetric space group P321, in which the magnetic Fe^{3+} ions ($S = 5/2$) form a triangular lattice of triangles in the ab-plane (see Fig. 1). The magnetic order of these systems, observed below the Néel temperature T_N, has been rationalized within the spin Hamiltonian [6, 7, 22–24]:

$$\mathcal{H} = \sum_{(ij)} J_{ij}\mathbf{S}_i \cdot \mathbf{S}_j + \sum_{(ij)_\triangle} D(\mathbf{S}_i \times \mathbf{S}_j)_z. \qquad (1)$$

Here the first term takes into account the exchange

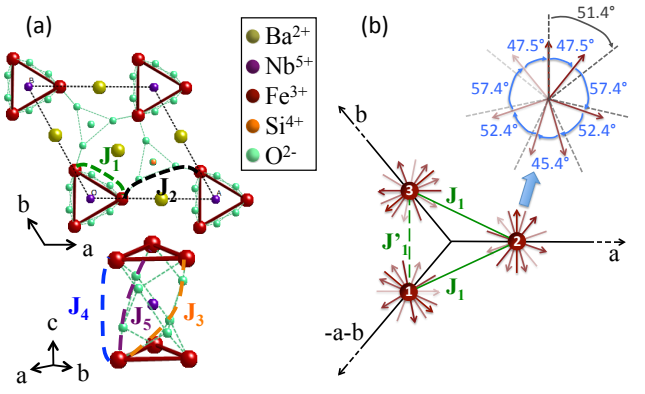


FIG. 1: (Color online) (a) $Ba_3NbFe_3Si_2O_{14}$ crystallographic structure in the ab-plane and along the c-axis, with five magnetic exchange paths J_1 to J_5. (b) Schematic representation of the revisited magnetic structure projected along the c-axis. The 3-fold axis is broken leading to different J_1 interactions (case of an isosceles triangle represented). The bunching of the helices in the Nb compound is reported through the successive angles between consecutive magnetic moments along c, deviating from the regular angle $2\pi\tau$=51.4°.

interactions, where the sum runs over the spin pairs connected by different paths shown in Fig. 1 (a). The nearest- and next-nearest-neighbor interactions J_1 and J_2 in the ab-plane are both antiferromagnetic. This generates magnetic frustration within the Fe triangles and causes the 120° spin structure. Among the three antiferromagnetic exchange couplings between adjacent ab-planes, the strongest one is J_3 or J_5 depending on the structural chirality. These couplings generate the helical modulation of the 120° structure along the c-axis. The propagation vector of this modulation depends on the balance between the inter-plane interactions J_3, J_4 and J_5. The second term in Eq. (1), where the sum runs over intra-triangle spins, corresponds to the additional DM interactions with the DM vector (D) along the c-axis, which is allowed by symmetry. This DM term restricts the spins to the ab-plane and favors one intra-triangle chirality as observed experimentally [22, 23, 25]. Alternatively, a weak easy-axis single-ion anisotropy can have similar effect [26].

We have revised this structure by carrying out single-crystal neutron scattering measurements on two members of the Fe langasite family with Nb or Ta on the 1a Wyckoff site. The two single-crystals, grown by floating-zone method in an image furnace [9], display opposite structural chiralities [25]. The experiments were done on two spectrometers installed at the Institut Laue Langevin: IN5 time-of-flight spectrometer using unpolarized neutrons, and CRG-CEA IN22 triple-axis spectrometer, equipped with CRYOPAD, using polarized neutrons and allowing longitudinal polarization analysis. The dynamical structure factors were measured on IN5 at 1.5 K, for both crystals in rotation about the a zone axis, with an incident wavelength of 4 Å. The Nb compound was also measured on IN22 at 2 K with a final wavevector fixed to 2.66 $Å^{-1}$ and at zero energy transfer in order to get a quantitative determination of the elastic structure factors of the magnetic satellites. The crystal was oriented with the a zone axis vertical so as to probe the (b*, c*) scattering plane. Two types of measurements were carried out using different monochromator-analyser configurations: Heusler-Heusler (H-H) and Graphite-Heusler (G-H). The former allows us to discriminate the magnetic and chiral contributions from the nuclear one, whereas the latter increases the incident neutron flux and allows us to determine the chiral scattering from an unpolarized beam [7], hence with a larger flux.

The intensity maps at zero energy cut measured on IN5 for the Nb and Ta compounds are shown in Figs. 2(a) and (b) respectively. The Néel temperature of these compounds are nearly identical (27 K for Nb and 28 K for Ta), while the propagation vectors are $\vec{\tau} = (0, 0, 0.1429)$ and $(0, 0, 0.1385)$ respectively [9, 27]. The latter is obtained from the position of the magnetic satellites at $Q = |\vec{H} \pm \vec{\tau}|$ in Figs. 2. In addition to these first-order satellites, we clearly observe higher-order satellites at $Q = |\vec{H} \pm 2\vec{\tau}|$ and $Q = |\vec{H} \pm 3\vec{\tau}|$ in both compounds suggesting that the helical modulation is distorted.

Polarized neutron measurements with longitudinal polarization analysis on the Nb compound allowed us to extract the nuclear (σ_N), the magnetic (σ_M) and the chiral (σ_{ch}) scattering [25], hence to identify the nuclear and/or magnetic nature of these extra peaks. This analysis reveals that the second-order satellites are mainly of nuclear origin. This is usually attributed to magnetoelastic effects and will not be further discussed. In contrast, the magnetic contribution is dominant in the third-order satellites [see Fig. 2(c)], which confirms the deformation of the magnetic helices.

This deformation allows further explanation of the subtle details in the spin-wave spectrum. As we can see in Fig. 3, the spectra of the Nb and Ta compounds display two branches emerging from the magnetic satellites [22]. The high energy branch corresponds to spin components in the ab-plane while the low-energy branch is associated to spin components along the c-axis. The main features of this spectrum were initially captured by the model of Eq. 1 using the standard Holstein-Primakov formalism in the linear approximation (see Fig. 4 of ref. 22). However, this simple model fails to reproduce a spectral weight extinction observed in the ab-branch around 2.3 meV in both compounds, and a tiny extinction around 1.7 meV in the c-branch, visible only in the Ta compound (red and orange arrows respectively in Fig. 3) [25].

In order to reproduce the deformation of the helices leading to all these features, we have considered a straightforward extension of Eq. 1. We included extra single-ion anisotropy terms with respect to a local 2-fold z_{loc} axes, *i.e.* along a, b and $-a-b$ for the three ions of

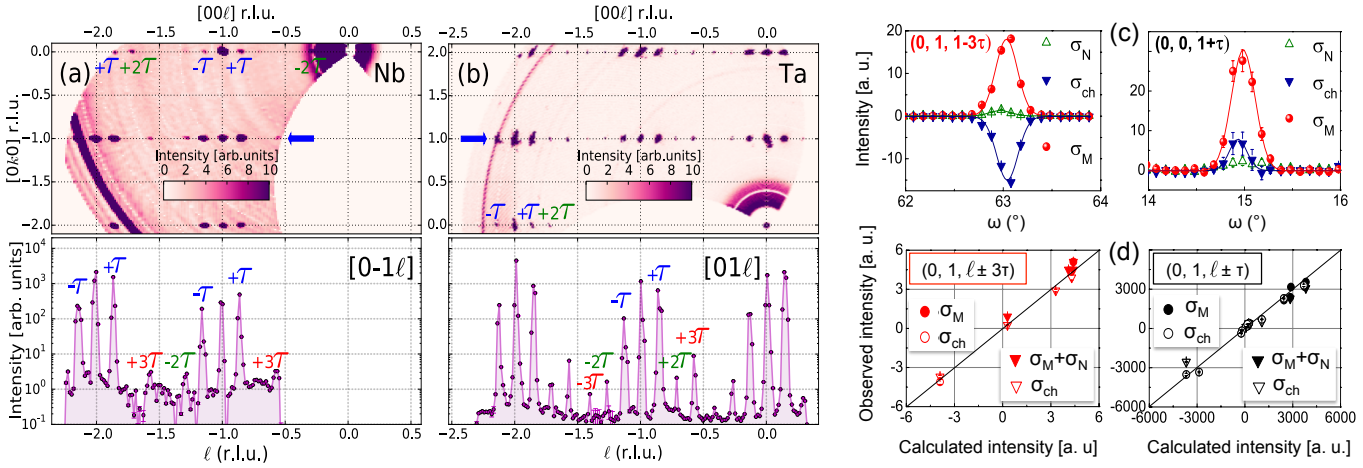


FIG. 2: (color online) Zero energy cut (integrated from -0.1 to 0.1 meV) from IN5 measurements at 1.5 K, on the Nb (a) and Ta (b) compounds. The blue arrows on the energy maps indicated the [0 ±1 ℓ]* directions of the Q-1D cuts shown below in vertical log scale. (c)-(d) summarize the measurements performed on the Nb compound at 2 K on IN22 with polarized neutrons. (c) shows the magnetic (red), nuclear (green) and chiral (blue) elastic contributions from scans obtained by rotating the crystal (ω-scans) with the H-H configuration. The solid lines are gaussian fits. The magnetic and chiral contributions measured in the H-H (circles) and G-H (triangles) configurations for the main (0, 1, $\ell \pm \tau$) and extra (0, 1, $\ell \pm 3\tau$) satellites, versus the calculated contributions using the model given in the caption of Fig. 3, are displayed in (d). Note that the G-H configuration cannot separate the magnetic from nuclear scattering, but we checked that $\sigma_M + \sigma_N \approx \sigma_M$ for these satellites.

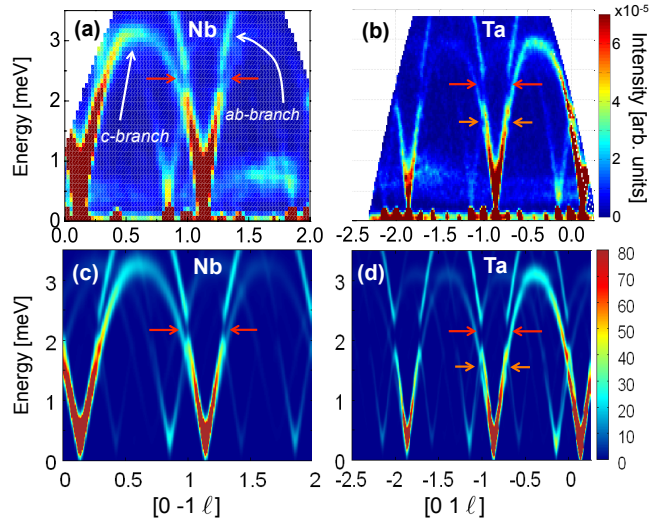


FIG. 3: (Color online) Spin-waves spectra of Nb (a) and Ta (b) measured along the [0 -1 ℓ]* and [0 1 ℓ]* directions respectively at 1.5 K on IN5. Below: Spin-waves calculations with the following parameters for the Nb(c)/Ta(d): J_1 = 0.85/0.85 ± 0.1 meV, J_2 = 0.24/0.24 ± 0.05 meV, J_3 = 0.053/0.22 ± 0.03 meV, J_4 = 0.017/0.014 ± 0.05 meV and J_5 = 0.24/0.053 ± 0.05 meV, D= -0.028/-0.028 ±0.005 meV, easy-plane anisotropy K = 0.045/0.053 ± 0.005 meV. The red/orange arrows show the spectral weight extinctions.

a triangle respectively:

$$H_{sia} = K \sum_i S^2_{z_{loc},i}. \qquad (2)$$

We first determine the magnetic ground state of the extended Hamiltonian by means of a real-space mean-field energy minimization. Then we compute the corresponding magnetic and chiral elastic scatterings for the first and third order magnetic satellites, and finally we compute the corresponding spin-wave spectrum [25].

A quantitive determination of the parameters of the revised Hamiltonian can be achieved for the Nb compound. The intensity of the the first-order (0, k, $\ell \pm \tau$) and extra (0, k, $\ell \pm 3\tau$) satellites (Figs. 2 (d)) increases with the single-ion anisotropy and agrees with the experiments (see Fig. 2) for $|K|$=0.045±0.05 meV. This term is also at the origin of the anti-crossings observed in the spin-waves (at 2.3 meV for the *ab*-branches and at 1.7 meV for the *c*-branches): these spectral weight extinctions occur at the crossing point of branches with the same symmetry, emerging from the $+\tau$ and $-\tau$ elastic magnetic satellites, which are mixed by the single ion anisotropy KS_z^2 [25, 28]. The anti-crossings are more pronounced in the Ta case (see Fig. 3 (b)) which qualitatively agrees with a higher value of K [25]. Another signature of the presence of tiny anisotropies is a gap in the *c*-branch, which reaches its energy minimum at ≈ 0.4 meV for Nb [26] and ≈ 0.2 meV for Ta as shown in Fig. 4 (a). The variation of this gap is actually opposite for the easy-plane ($K > 0$) and for the easy-axis ($K < 0$) anisotropies. In the latter case, the *c*-gap increases with increasing $|K|$ and is already around 1 meV for K=0.045 meV, which is larger than the values observed experimentally. These values are actually compatible with an easy-plane anisotropy combined with a DM term (with $D < 0$): the *c*-gap increases when $|D|$

increases and decreases when K increases. The Nb c-gap is reproduced for D=-0.028 meV and K=0.045 meV (see Fig. 4(b)). The smaller gap of the Ta compound is in turn compatible with a larger K than in the Nb one (see Fig. 4(c)). This analysis yields the extended model given in the caption of Fig. 3 with a set of parameters reproducing the spin-waves for the Nb and Ta compounds (see Figs. 3(c-d)). Moreover, in the Nb case these parameters are fully compatible with the magnetic structure factors and with the Electron Spin Resonance measurements [23] that have been reanalyzed carefully [25]. In real space, this revised model globally corresponds to a deviation of the angle between adjacent spins along the helix axis away from the ideal $2\pi\tau = 51.4°$ value: It gets smaller near the local easy-planes and larger far from them (see Fig. 1 (b)). Thus, we conclude that the magnetic structure of the Fe langasites corresponds to a bunched helix, as reported in some rare-earth intermetallics [29].

Next, we analyze in more detail the first-order satellites along the [0 0 ℓ]* line. These (0, 0, $\ell \pm \tau$) satellites are clearly visible in our data (see Fig. 2), where they display the same temperature dependence as the (0, 1, $\ell \pm \tau$) magnetic ones [25]. In fact, the longitudinal polarization analysis confirms their magnetic origin (see Fig. 2(c)). The observation of these satellites is very surprising since, in the case of a perfect 120° spin arrangement within the Fe triangles, there should be an extinction of the magnetic structure factor along the [0 0 ℓ]* line. We note, that the forbidden (0, 0, τ) satellite has also been observed by magnetic resonant X-ray diffraction (together with 2τ and 3τ satellites in the first Brillouin zone) [30]. This was attributed to a modulated out-of plane (butterfly) component of the magnetization produced by the in-plane intra-triangle DM vector. However, neutrons are blind to this component along [0 0 ℓ]* since they are only sensitive to the magnetic components perpendicular to the scattering vector Q. Thus, the observation of these (0, 0, $\ell \pm \tau$) satellites in our neutron experiments clearly demonstrates that the relative orientation of the magnetic moments within the triangles deviates from 120°, hence suggesting that the intra-triangle J_1 interactions are not equivalent. Our neutron data cannot single out whether the distortion of this triangular arrangement is local (helically modulated from planes to planes) or global. However, only the latter case, implying a loss of the 3-fold symmetry axis of the $P321$ structure, is compatible with a macroscopic polarization measured along the two-fold axis. The loss of the 3-fold axis was already invoked from Mössbauer experiments and x-ray magnetic diffraction [27, 30], and was an important ingredient for explaining the magnetoelectric excitations revealed by means of THz spectroscopy [10]. In addition, it is compatible with the phonon spectrum [31]. This finding has strong implications on the multiferroic properties of these systems, as we discuss in the following.

The P321 space group of the Fe langasites allows the

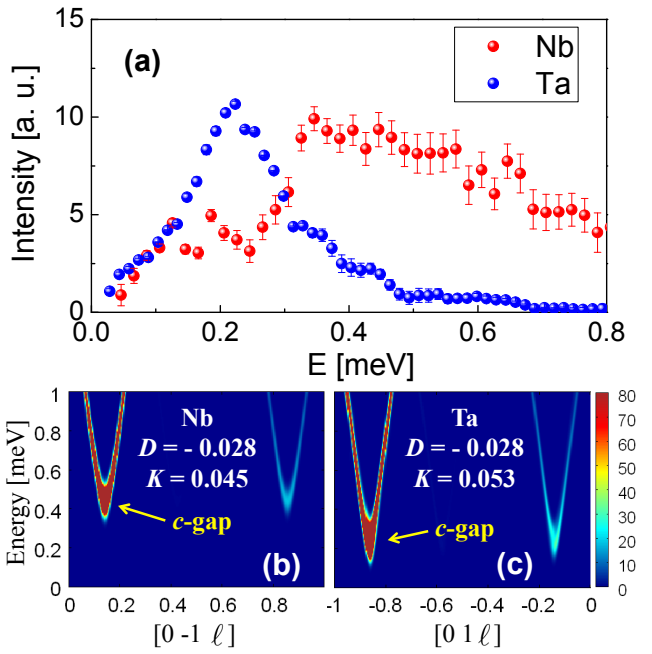


FIG. 4: (Color online) (a) Neutron scattering intensity versus the energy at the magnetic satellite position for Ta and Nb, obtained from 1D Q-cut (integration ranges $\Delta h = \Delta k = \Delta l = 0.05$) measured on IN5 with a wavelength of 8 Å. Below: Calculated scattering intensity of the c-branch only showing the c-gap of the Nb (b) and Ta (c) compounds using the revised model with the parameters of the caption of Fig. 3.

magnetoelectric coupling of the form:

$$F_{ME} = \alpha\{P_x(\mathbf{S}_1-\mathbf{S}_2)\cdot\mathbf{S}_3 - \frac{1}{\sqrt{3}}P_y[(\mathbf{S}_1+\mathbf{S}_2)\cdot\mathbf{S}_3 - 2\mathbf{S}_1\cdot\mathbf{S}_2]\}.$$

where y and x stand for the a-axis and its perpendicular direction in the ab-plane, and $\mathbf{S}_1$ to $\mathbf{S}_3$ are the three spins on a triangle (see Fig. 1). This coupling can have a purely electronic origin as discussed in [20] or emerge from magnetostriction effects in the symmetric Heisenberg exchange [3]. In any case, at the phenomenological level, its form is identical to the one discussed in [3, 20, 21]. The presence of such a coupling means that a spin-induced electric polarization has to be expected whenever the spin arrangement deviates from the perfect 120° structure [32]. This polarization will lie in the ab-plane. Thus, the new magnetic structure deduced from our experiments is compatible with the polarisation measurements of Lee *et al.* [12] rather than those of Zhou *et al.* [11]. This is also in tune with the DFT-based calculations reported in [33], in which a magnetically-induced polarization was also obtained in the ab-plane due to the reduction of symmetry of the magnetic structure to C2'. In this work, however, this reduction was the result of spin-orbit coupling (likely via symmetric anisotropic exchange), and the precise magnetoelectric coupling behind such an electric polarization was not identified.

The enhancement of the electric polarization in the

ab-plane by the application of a magnetic field has also been reported in [12]. This can be understood on the basis of the above coupling, although its connection with the revised magnetic structure is more subtle. In this case, the 120° spin-structure of each triangle is additionally deformed by the Zeeman coupling, which induces a (weak) ferromagnetic component and thus an extra local contribution to the electric polarization. In the perfect helical structure, however, these individual field-induced electric polarizations coming from the different layers of the helix rotate along the c axis in such a way that they cancel each other. In the bunched helical structure, in contrast, this rotation is modified so that the cancelation is avoided, which eventually enables an overall finite polarization induced by the magnetic field. This will happen even if the initial (zero-field) structure corresponds to a perfect 120° arrangement within the Fe triangles. Thus, the magnetic-field induced electric polarization essentially relies on the bunching of the helix along the c-axis.

By carrying out neutron scattering experiments, we have identified subtle features in the magnetic order of Fe langasites, with drastic consequences on their properties. The first feature is a bunching of the helical modulation related to single-ion magnetocrystalline anisotropy, and the second one is the distortion of the 120° spin structure. At the phenomenological level, we have established that the magnetically-induced electric polarization at zero and finite magnetic fields results from a generic magnetoelectric coupling that is equivalent to that put forward by Bulaevskii *et al.* Our study thus sets the basis for understanding the multiferroic properties of Fe langasites representing model-case magnetically-induced ferroelectrics in triangle-based frustrated magnets. Finally, the close relation between the multifaceted chiral properties of the Fe langasites and their multiferroic potential is expected to motivate further studies.

Acknowledgments

We would like to acknowledge A. Hadj-Azzem and J. Debray for their help in the preparation of the samples, and P. Bordet, S. Grenier and O. Cépas for fruitful discussions. This work was financially supported by Grant No. ANR-13-BS04-0013-01.

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