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V.T. Renard, B. A. Piot, Xavier Waintal, G Fleury, D Cooper, et al.. Valley polarization assisted spin polarization in two dimensions. Nature Communications, 2015, 6, pp.7230. 10.1038/ncomms8230 . hal-01160304

HAL Id: hal-01160304 https://hal.science/hal-01160304v1

Submitted on 5 Jun 2015

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Valley polarization assisted spin polarization in two dimensions

V. T. Renard,¹ B. A. Piot,² X. Waintal,¹ G. Fleury,³ D. Cooper,⁴ Y.

Niida,⁵ D. Tregurtha,⁶ A. Fujiwara,⁷ Y. Hirayama,⁵ and K. Takashina⁶

¹Univ. Grenoble Alpes/CEA, INAC-SPSMS, F-38000 Grenoble, France

²Laboratoire National des Champs Magnétiques Intenses,

CNRS-UJF-UPS-INSA, 38042 Grenoble, France

³Service de Physique de l'État Condensé, DSM/IRAMIS/SPEC,

 $CNRS \ UMR \ 3680 \ CEA \ Saclay, \ 91191 \ Gif \ sur \ Yvette \ cedex, \ France$

⁴Univ. Grenoble Alpes/CEA Leti Minatec campus, F-38054 Grenoble, France

⁵Graduate School of Science, Tohoku University,

6-3 Aramakiaza Aoba, Aobaku, Sendai, 980-8578 Japan

⁶Department of Physics, University of Bath, Bath BA2 7AY, UK

⁷NTT Basic Research Laboratories, NTT Corporation, Atsugi-shi, Kanagawa 243-0198, Japan

(Dated: June 5, 2015)

Valleytronics is rapidly emerging as an exciting area of basic and applied research. In two dimensional systems, valley polarisation can dramatically modify physical properties through electron-electron interactions as demonstrated by such phenomena as the fractional quantum Hall effect and the metalinsulator transition. Here, we address the electrons' spin alignment in a magnetic field in siliconon-insulator quantum wells under valley polarisation. In stark contrast to expectations from a noninteracting model, we show experimentally that less magnetic field can be required to fully spin polarise a valley-polarised system than a valley-degenerate one. Furthermore, we show that these observations are quantitatively described by parameter free ab *initio* quantum Monte Carlo simulations. We interpret the results as a manifestation of the greater stability of the spin and valley degenerate system against ferromagnetic instability and Wigner crystalisation which in turn suggests the existence of a new strongly correlated electron liquid at low electron densities.

INTRODUCTION

The valley degree of freedom has a long history as a subject of pure and applied research since it is an intrinsic property of the band structure of silicon and germanium, the historical materials in microelectronics¹. Valley degeneracy had generally been viewed as a drawback as it limits the mobility of CMOS (Complementary Metal Oxide Semiconductor) devices due to intervalley scattering². Microelectronics manufacturers have consequently put much effort into manipulating valley bands through strain, to improve transport properties. This approach has been successful, and strained silicon has been in use in microelectronics since the 90 nm $node^3$.

More recently, however, the valley degree of freedom is becoming recognised as an opportunity, rather than a hindrance, and this is leading to the emergence of a field of research now known as valleytronics in which valleys are exploited in addition to charge and spin. Valleytronics has received a recent boost owing to the discovery of graphene and other new topical materials also possessing the valley degree of freedom and by the proposal of valley tronics devices^{4–10}. A vital ingredient to the development of valleytronics is valley polarization. Analogous to spin polarization in spintronics in which when achieved under equilibrium conditions, leads to key phenomenology such as ferromagnetism, valley polarization can also be expected to yield rich and useful physics.

Experimental research into the physical consequences of valley polarizing a two dimensional electron system in the steady state is led by studies of AlAs and Si based structures. It has been demonstrated that valley polarisation dramatically affects phenomena such as the fractional quantum Hall effect¹¹⁻¹⁴ and the metal insulator transition¹⁵⁻¹⁸, two effects in which electron-electron interactions are central. Pioneering experiments performed in AlAs indicate that valley polarisation also has a strong impact on another effect where electronelectron interactions play crucial roles : spin polarisation. It has been demonstrated that valley polarisation leads to a strong enhancement of spin susceptibility and symmetrically, spin polarisation enhances valley susceptibility^{19–21}.

In this article, we firstly confirm the enhancement of spin susceptibility by valley polarisation in silicon, which in contrast to AlAs has an isotropic inplane effective mass which simplifies interpretation of transport phenomena. More importantly, we explore a new regime in the interaction-disorder parameter space where a qualitatively new behaviour emerges. This is achieved by using electrically controlled valley polarisation in a simple two dimensional electron gas in foundry compatible silicon-oninsulator (100) MOSFETs^{22,23} (Metal Oxide Semiconductor Field Effect Transistors). We present magneto-resistance data which indicate that for low enough electron densities, valley polarising the twodimensional electron gas (2DEG) reduces the field of full spin polarisation. This represents not only a quantitative failure of the single particle picture but a qualitative one, in which the observed behaviour is opposite to the prediction of the non-interacting framework.

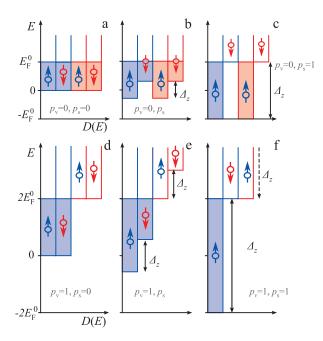


Figure 1. Energy diagram of a 2D electron gas of fixed electron density. The diagram depicts the four spin-split valley-split subbands. Up (resp. down) arrows correspond to spin up (down) electrons and blue (resp. red) color corresponds to valley + (resp. -). Depending on spin and valley polarisation, the system can be either (a) valley- and spin-degenerate or (b) valley-degenerate, partially spin-polarised or (c) valley-degenerate, spin-polarised or (d) valley-polarised, spin-degenerate or (e) valley-polarised, partially spin-polarised or (f) valley-polarised, spin-polarised.

RESULTS

Single particle picture

Let us first describe briefly how spin polarization is expected to respond to valley polarisation in a non-interacting 2DEG. In the non-interacting model, the density of states of a 2DEG is independent of energy and can be written as $g_{\rm s}g_{\rm v}D_0$ where $D_0 = m_{\rm b}/2\pi\hbar^2$, $g_{\rm s}$ and $g_{\rm v}$ are spin and valley degeneracies, $m_{\rm b}$ is the electron band mass and \hbar is the reduced Planck's constant. In a (001) silicon 2DEG, $g_{\rm s} = g_{\rm v} = 2$ and the system is composed of four independent spin-valley subbands with equal density of states D_0 , as depicted in Figure 1a. All states are filled up to the Fermi energy $E_{\rm F}^0 = n/g_{\rm s}g_{\rm v}D_0 \equiv$ $n/4D_0$ at zero temperature, where n is the electron sheet density.

Applying a magnetic field parallel to the electron gas raises the bottom of the spin down bands compared to that of the spin up bands by the Zeeman splitting $\Delta_z = g\mu_{\rm B}B$ (Fig. 1b) where g is the Landé g-factor (g = 2 in Si) and $\mu_{\rm B}$ the Bohr magneton. Spin down electrons are consequently transferred to the spin up band: the system spin polarises. The spin (valley) polarisation is defined as $p_{\rm s} = (n_{\uparrow} - n_{\downarrow})/n$ (resp. $p_{\rm v} = (n_{+} - n_{-})/n$) with n_{\uparrow} and n_{\downarrow} being the spin up and spin down electron densities respectively $(n_{+} \text{ and } n_{-} \text{ are the electron})$ densities in the + and - valleys). At $p_v = 0$, full spin polarisation is achieved when $\Delta_z = 2E_{\rm F}^0$ (Fig. 1 c). It follows that the field $B_{\rm p}$ required for full spin polarisation should double when the system is valley polarised because the kinetic energy in the valley polarised system (Fig. 1d) is twice that of the unpolarised one (Fig. 1a). For more details on this single particle picture see Supplementary Discussion.

Experimental determination of B_{p}

The field of full spin polarisation $B_{\rm p}$ of a 2DEG can be extracted from measuring the electrical resistance under in-plane magnetic field. Spin polarisation has the effect of reducing the ability of the 2DEG to screen disorder, and as a consequence, increases the resistance due to enhanced scattering until, in the simplest case, the magneto-resistance (MR) saturates to a constant value²⁴. This is a signature that full spin polarisation is reached and the spin degree of freedom is completely frozen.

However, this situation is only rarely observed in experiments where it is more common to observe a

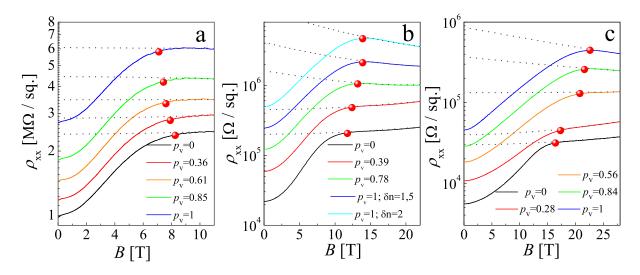


Figure 2. Magneto-resistance as function of valley polarisation. The MR of the 2DEG is plotted for increasing p_v at the density of $n = 1.6 \times 10^{15} \text{ m}^{-2}$ (a), $n = 2.5 \times 10^{15} \text{ m}^{-2}$ (b) and $n = 3.5 \times 10^{15} \text{ m}^{-2}$ (c), at T = 1.65 K (See Fig. 3 for a version of Fig. 2a in linear scale). The indicated values for p_v correspond to those at full spin polarisation. The field of full spin polarisation (plotted as red bullets) is estimated from the field where the MR has reached 97.5% of its high-field spin-independent behaviour (grey dotted lines). Values of δn are given in units of 10^{16} m^{-2} in panel b.

shoulder in the magnetoresistance $^{19,25-32}$ when the spin system freezes but the resistance continues to change due to spin-independent effects such as the coupling of the magnetic field to the electrons' orbital motion^{31,33}.

In the absence of a comprehensive description of the high field behaviour, we follow previous literature in empirically estimating $B_{\rm p}$ as the field where the MR has reached 97.5 % of its high field dependence^{19,28} (The behaviour in the spin polarized regime at high fields was fitted to a quadratic behaviour with no particular physical meaning. See dotted lines in Fig. 2). Results are shown as red dots in Fig. 2.

We note that we have also estimated $B_{\rm p}$ following other methods used in the literature²⁸ (inflexion point in the MR, intersection of the high field asymptote and tangent at the inflexion point etc.). All methods provided a qualitatively similar behaviour in the changes of $B_{\rm p}$ with valley polarisation. We have chosen the method described above as we believe it provides a better quantitative estimation of $B_{\rm p}$ compared to other methods which underestimate it.

Evolution of $B_{\mathbf{p}}$ with valley polarisation

At large density (Fig. 2b and c), we observe an increase of $B_{\rm p}$ with valley polarisation, a behaviour which is qualitatively consistent with the single particle picture (See Refs. 22 and 23 and Methods for details on the electrical control and determination of $p_{\rm v}$). It should be stressed, however, that quantitatively, the single-particle model fails completely. The values of $B_{\rm p}$ are always much lower than expected. Also, instead of the doubling of $B_{\rm p}$ from $p_v = 0$ to $p_v = 1$, we observe only a moderate increase of $B_{\rm p}$. For exemple, we measure $B_{\rm p}(p_{\rm v}=0)=11.75$ T and $B_{\rm p}(p_{\rm v}=1)=13.9$ T for $n=2.5\times10^{15}$ m⁻² while the single particule picture predicts $B_{\rm p}(p_{\rm v}=0)=28.85~{\rm T}$ and $B_{\rm p}(p_{\rm v}=1)=51.7~{\rm T}$ respectively. These observations are consistent with the strong enhancement of spin susceptibility with valley polarisation seen in $AlAs^{19-21}$. We note in addition, that the quantitative failure of the single-particle model has also been observed in numerous experiments where valley polarisation could not be tuned, regardless of valley degeneracy $^{25-32}$.

At lower density (Fig. 2a), the single particle picture fails qualitatively. Here, our data show that $B_{\rm p}$ moves to lower and lower magnetic field as valley polarisation is increased. That is, it becomes easier to spin polarise a valley-polarised electron gas than a valley degenerate one at low enough density.

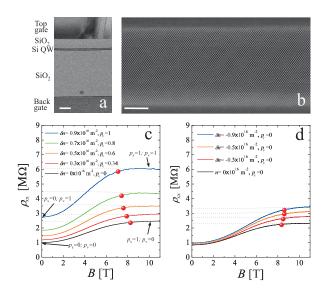


Figure 3. Exclusion of disorder as the origin of the reduction in $B_{\mathbf{p}}$. a) Bright field scanning TEM cross-section of a 16 nm SIMOX device made with the same recipe as our sample. The scale bar is 100 nm b) High Angle Annular Dark Field scanning TEM image of the quantum well. The image shows the very good and similar crystallographic quality of the top and buried interfaces. The scale bar is 5 nm c) Electrons are pressed against the back interface $\delta n > 0$. d) Electrons are pressed against the front interface for $\delta n < 0$. Red dots mark the field of full spin polarisation in both panels. Here, $n = 1.6 \times 10^{15}$ m⁻² in both panels while T = 1.6 K on the panel c and T = 1.7 K in the panel d. (This explains the small difference in resistivity at B = 0T and $\delta n = 0$.) The grey dashed lines correspond to the high-field behaviour used for the determination of $B_{\rm p}$.

Exclusion of disorder as the cause of the reduction of $B_{\mathbf{p}}$ with valley polarisation

One cause for this observation could be an increase in disorder which is known to reduce B_p^{28} . At first sight, this explanation might seem plausible since valley polarisation is achieved by pressing the 2DEG against the buried Si/SiO₂ interface (see Methods) and hence the 2DEG experiences higher disorder due to interface roughness. The amplitude of this effect can be estimated in our device where transport can also be investigated at the top Si/SiO₂ interface. At this interface, valley splitting is negligible²³ but disorder is comparable as demonstrated by our high resolution Transmission Electron

Microscope (TEM) images (Fig. 3) and independent measurements with holes which do not possess the valley degree of freedom and show similar mobility at both interfaces³⁴. This enables us to separate the effects of disorder and valley polarisation which are mixed at the buried interface.

Figures 3c and d show the magnetoresistance of the 2DEG for comparable magnitudes of out-ofplane electric bias (estimated from the phenomenological parameter δn . See Methods) when electrons are pressed against the buried or front Si/SiO₂ interface. The magnitude of the bare disorder potential increases with $|\delta n|$, while valley polarisation is enhanced only for $\delta n > 0$.²³ Insight into the variation of the bare disorder with $\delta n > 0$ is found from the comparison of the resistance at ($p_{\rm s} = 1; p_{\rm v} = 0$) and ($p_{\rm s} = 0; p_{\rm v} = 1$) (highlighted in Fig. 3c).

Spin and valley degeneracy can be treated as formally equivalent in the "screening" description of transport described in Ref. 24. Therefore, in the absence of variation of disorder due to the process of polarising, one should expect the same increase of resistance due to equivalent reduction of screening regardless of which degeneracy is lifted¹⁷.

We find that the resistances are indeed almost the same at $(p_s = 1; p_v = 0)$ and $(p_s = 0; p_v = 1)$. Therefore, we conclude that the major part of the increase in resistance with $\delta n > 0$ seen in Fig. 3a at B=0 T can be attributed to a reduced screening due to valley polarisation and not to a significant increase of bare disorder. Furthermore, the increase of disorder with $\delta n > 0$ can be estimated to be about 10% from the observed 10% difference between the resistance at $(p_s = 0; p_v = 1)$ and $(p_s = 1; p_v = 0)$. This estimation of the variation of disorder with $|\delta n|$ is confirmed by transport at the front interface where the entire change in resistance must be attributed to a change in disorder. The data at B = 0 T in Fig. 3d reveal a 14 % increase in the resistance for $\delta n = -0.9 \times 10^{16} \ {\rm m}^{-2}$ (comparable in amplitude to that necessary for full valley polarisation at the buried interface). The weak dependence of disorder on $\delta n < 0$ is well illustrated in the resistance map shown in Fig. 4 where contours of constant resistance run parallel to the constant density lines in the relevant regime of density.

Importantly, Fig. 3d shows that the field of full spin polarisation is almost unchanged when electrons are pressed against the front interface. That is, the 14% change in the bare disorder with δn in this experiments is not sufficient to cause a substantial change in $B_{\rm p}$. We even note a small initial increase of $B_{\rm p}$ which might be attributed to the removal of a small valley splitting at symmetry ($\delta n = 0$) as

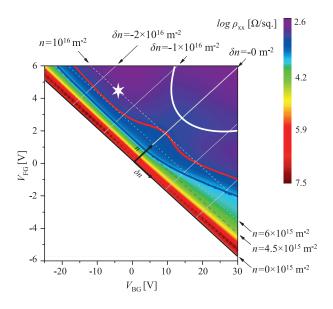


Figure 4. Two dimensional map of the resistance. Resistance of the sample as function of front and back gate voltages in a log scale. The white line materialises the upper spatial subband edge. The red curve represents the $\rho_{xx} = 1600\Omega$ iso-resistance obtained for $(n = 10^{16} \text{m}^{-2}, \delta n = 0 \text{ m}^{-2})$ while the blue one represents the $\rho_{xx} = 6000\Omega$ iso-resistance obtained for $(n = 4.5 \times 10^{15} \text{m}^{-2}, \delta n = 0 \text{ m}^{-2})$. The mobility was measured at the white star (see Methods for more details).

electrons are moved away from the buried interface. Alternatively, this small increase could be due to a broadening of the spin band edge due to the increased disorder felt by the 2DEG. Either way, we can conclude from this that the increase of the bare disorder with $|\delta n|$ cannot explain the behaviour seen in Fig. 2a, leaving valley polarisation as the only culprit.

As a final confirmation, we have checked that increasing δn above full valley polarisation does not lead to any further change in $B_{\rm p}$ (see the upper curve in Fig. 2b) despite the fact that, as already mentioned, the bare disorder potential continues to slowly increase with δn . This has also been confirmed in other samples. This set of experiments, therefore, allows us to conclude that valley polarisation itself is responsible for the reduction of $B_{\rm p}$ observed in Fig. 2.

Quantum Monte Carlo simulations

The reduction in $B_{\rm p}$ compared to single particle expectations is interpreted as resulting from electron-electron Coulomb interactions which favour spin alignment and this has already been confirmed theoretically^{35–40}. However, it is particularly challenging to make quantitatively reliable predictions for $B_{\rm p}$. Even in the absence of disorder, Hartree Fock or random phase approximation (RPA) calculations do not capture the crucial role of correlations at low density and one has to resort to quantum Monte Carlo (QMC) simulations.³⁹ In our lowdensity intrinsically disordered system, the interplay of disorder and interactions further complicates the problem.

Here, we use a Green's function quantum Monte Carlo approach, known to fully account for the effect of interactions in the presence of disorder⁴¹, to predict quantitatively the values of $B_{\rm p}$ in the interacting 2DEG with and without valley polarisation (See Methods and ref. 41).

The energy per electron for a given spin polarisation state p_s is given by:⁴¹

$$E = E_0 + E_{\rm p} p_{\rm s}^2.$$
 (1)

We calculate the energy E_0 of the spin unpolarised and the energy $E(p_s = 1)$ of the spin polarised system to obtain the energy per electron needed to fully spin polarise the system $E_{\rm p} = E(p_{\rm s} = 1) - E_0$. The predicted field of full spin polarisation is then calculated as $B_{\rm p} = 4E_{\rm p}/(g\mu_{\rm B})$. The resulting $B_{\rm p}$ as function of electron density can be easily compared to those extracted from the experiments with no adjustable parameter: the only input for the simulation being the amplitude W of the bare disorder (which we can estimate from the peak mobility of the sample) and the electron density (See methods and Ref. 41 for more details on how disorder is taken into account in the model). This approach has been firmly validated by the successful quantitative comparison to the experimental measurements of seven different studies in Si at $p_{\rm v} = 0.41$. Here, we have extended those calculations to the case of $p_{\rm v}~=~1~{\rm using}~\mu_{peak}~=~8000~{\rm cm}^2{\rm V}^{-1}{\rm s}^{-1}$ measured in our sample as a single input parameter for both $B_{\rm p}(p_{\rm v}=0)$ and $B_{\rm p}(p_{\rm v}=1)$ (see Methods for the determination of μ_{peak}). Assuming that a single input parameter μ_{peak} determined at $p_v = 0$ is enough to describe all the data seems reasonable since we have demonstrated that the bare disorder only varies weakly with $|\delta n|$.

The result of the calculation is displayed in Fig-

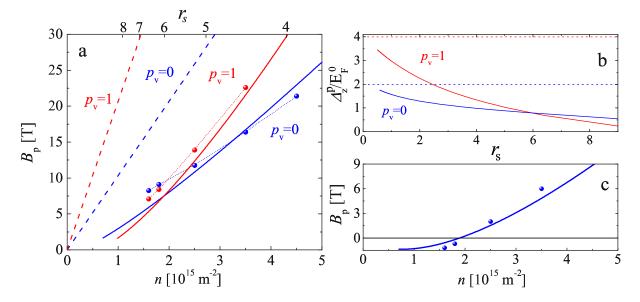


Figure 5. Comparison between experiments and quantum Monte Carlo simulations. a) Density dependence of $B_{\rm p}$. $(\cdots \bullet \cdots)$ Experimental values, (- -) non-interacting theory, (-) result of the quantum Monte Carlo simulation. b) Ratio of the Zeeman energy at full spin polarisation and $E_{\rm F}^0$ as function of $r_{\rm s}$. Dashed lines correspond to the non-interacting case while solid lines correspond to the prediction in the presence of interaction and disorder (The calculation are performed for the mobility of our sample). c) Density dependence of $\Delta B_{\rm p} = B_{\rm p}(p_{\rm v} = 1) - B_{\rm p}(p_{\rm v} = 0)$. Experimental measurements (•) and theory (--).

In both valley-degenerate and valleyure 5a. polarised cases the calculation predicts a much lower field of full spin polarisation than the single particle model. Importantly, the curves corresponding to $B_{\rm p}(p_{\rm v}=0)$ and $B_{\rm p}(p_{\rm v}=1)$ cross so that at low density the full spin polarisation is predicted to occur at a lower field in a valley polarised system. The full dependence of this effect from low to high interaction is illustrated in Fig. 5b. This figure shows the predicted ratio of the Zeeman splitting at full spin polarisation and the non-interacting Fermi energy $E_{\rm F}^0$ as function of the interaction parameter $r_{\rm s} = 1/(\pi n)^{1/2} a_{\rm B}$ (here $a_{\rm B}$ is the Bohr radius) using the mobility of our sample. At low $r_{\rm s}$ the behaviour is that of a non-interacting system. The effect of interaction becomes more and more important as $r_{\rm s}$ increases and the curves corresponding to $p_{\rm v} = 1$ and $p_{\rm v} = 0$ eventually cross over at around $r_{\rm s} = 6$.

For a more quantitative comparison between experiments and theory, the experimental values of $B_{\rm p}$ are plotted in Fig. 5a and in Fig. 5b the experimental difference $\Delta B_{\rm p} = B_{\rm p}(p_{\rm v} = 1) - B_{\rm p}(p_{\rm v} = 0)$ is plotted together with the prediction. The theory describes the experiments very well with no adjustable parameters, demonstrating that the theory captures the essential physics behind the behaviour of $B_{\rm p}$.

DISCUSSION

As a first remark we should point out that the possibility of observing the new behaviour reported here results from the cooperative effect of disorder and interaction. Indeed, the calculations in the disorder free system indicate that electron-electron interactions are the leading effect in reducing the polarisation energies. Evidence for the crossing of $B_{\rm p}(p_{\rm v}=0)$ and $B_{\rm p}(p_{\rm v}=1)$ curves is also seen for clean systems (See Fig. 6 and Fig. 2 in Ref. 39 where it is observed that the spin susceptibility enhancement $\chi/\chi_0(p_{\rm v}=1)>2\chi/\chi_0(p_{\rm v}=0)$ for large enough $r_{\rm s},$ a feature reminiscent of the crossing of $B_{\rm p}$ curves). However, in Si, this crossing is expected to occur at around $n = 10^{15} \text{ m}^{-2}$, too low to be accessed experimentally in our valley tunable samples. By further enhancing the effects of electron-electron interactions disorder shifts by a small amount, all curves to larger densities, just enough to allow the observation of the new phenomenology. The weak dependence on disorder implies that our comparison is robust against errors in the determination of the bare disorder potential. This accounts for why $B_{\rm p}$ is found to be independent of $\delta n < 0$ in Fig. 3d and justifies the use of a single input parameter to describe both $p_{\rm v} = 0$ and $p_{\rm v} = 1$. Nevertheless, including disorder is necessary to achieve quantitative comparison. This effect of disorder may explain why, in previous experiments in AlAs at similar values of $r_{\rm s}$, only the enhancement of spin susceptibility and not the reduction of $B_{\rm p}$ with valley polarisation was observed¹⁹. Indeed, in AlAs the mobility was five times larger than in our samples and therefore the crossing would be shifted to larger $r_{\rm s}$. However, the crossing must have been approached very close since the criteria $\chi/\chi_0(p_v = 1) > 2\chi/\chi_0(p_v = 0)$ is almost reached in Fig. 3 of Ref. 19. In addition, we should also point out that the comparison between QMC calculations and experimental results in valley tunable AlAs is complicated by the mass anisotropy in the system as concluded in Ref.42. The situation is more simple in narrow AlAs quantum wells where effective mass is isotropic⁴³ and QMC works well.³⁵

As a second remark we note that our study further confirms that QMC is an appropriate theory to predict the polarisation energies of two-dimensional electron gasses. Previous studies have shown that the disorder free QMC describes correctly the measurements in AlAs (apart from $p_v = 1$ in valley tunable AlAs with anisotropic effective mass) and GaAs if the finite thickness of the system is included^{35,39}. We have also shown in Ref. 41 that the QMC including disorder describes the available experimental data in silicon at $p_v = 0$. Therefore, QMC is able to determine the polarisation energies of most investigated samples without adjustable parameters.

As a concluding remark we now discuss our result in a more general context. Early QMC simulations⁴⁴ on clean 2DEGs at B = 0 T showed that the energy of the spin and valley polarised system becomes lower than that of the two component system in the region $r_{\rm s} \gtrsim 20$ before Wigner crystallisation at $r_{\rm s}$ \sim 34. A ferromagnetic instability had therefore been expected in the valley polarised system. In contrast, and in qualitative contradiction with results from Hartree-Fock calculations, no such instability was observed in the QMC simulations for the valley and spin degenerate system which was found to be the stable phase all the way up to Wigner crystallisation at $r_{\rm s} \sim 42$ (See Fig. 1 in Ref. 44). Our experiments and quantum Monte Carlo simulations confirm and demonstrate that this scenario remains valid in real disordered systems, rather than it being only a special case of hypothetical disorderfree systems. Results from simulations displayed in Fig. 5a show that $B_{\rm p}(p_{\rm v}=1)$ is approaching 0 at a finite electron density indicating a ferromagnetic instability in the valley polarized system. The instability occurs at a lower $r_{\rm s}$ in our disordered

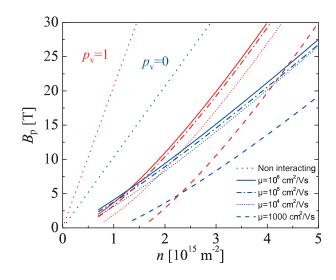


Figure 6. **Density dependence of** $B_{\mathbf{p}}$. Theoretical dependence of $B_{\mathbf{p}}$ in a single particle picture and in presence of interactions for various values of disorder (quantum Monte-Carlo simulation).

system compared to the clean one^{44} . In contrast, no sign of such instability is seen in the curve for $B_{\rm p}(p_{\rm v}=0)$ down to the lowest electron densities we have studied. Experimentally, the mobility of our sample obviously does not allow us to reach the very low densities necessary for the observation of spontaneous spin polarisation or Wigner crystallisation. Yet, the crossing of the curves $B_{\rm p}(p_{\rm v}=0)$ and $B_{\rm p}(p_{\rm v}=1)$ provides strong experimental evidence of the higher stability of the spin-valley degenerate system because they demonstrate that interactioninduced spin alignment is much less efficient in the valley unpolarised system than in the valley polarised system. The strong enhancement of spin susceptibility with valley polarisation in AlAs¹⁹ also supports this interpretation. The excellent agreement between the theory and our experiments suggests that the result can be extrapolated to cleaner spin-valley degenerate systems with greater interaction. In those systems, in the absence of ferromagnetic instability, we anticipate the presence of a strongly correlated electron liquid. This may result in a rich physics which might soon be accessed exploiting recent developments in high mobility silicon $systems^{45,46}$.

METHODS

Samples and control of valley polarisation

The samples consists of a $SiO_2/Si(100)/SiO_2$ quantum well of nominally 10nm thick silicon with front- and back-gate oxide thicknesses of 75 nm and 380 nm respectively. The fabrication proceedure of this sample is described in Ref. 22. A degenerately phosphorus-doped polysilicon layer was used as front gate while the substrate was used as a back gate.

It is well known that valley degeneracy can be lifted at the (001) Si/SiO₂ interface in Si MOSFETs and that the valley splitting can be increased by increasing the out-of-plane electric field, which in traditional MOSFETs can be controlled by changing the substrate bias¹. The magnitude of this valley splitting is found also to depend on the way in which the $Si-SiO_2$ interface is prepared, and the use of a buried-oxide interface using SIMOX (Separation by IMplantation of Oxygen) technology²² allows us to enhance the valley splitting up to tens of meV^{23} . The coupling responsible for the bare single-particle splitting is induced predominantly by the large interface electric field^{47,48} but there remain uncertainties as to the exact microscopic details that give rise to the particularly large values in SIMOX buried-oxide interfaces^{47–49}.

Experimentally, the valleys splitting is determined by fitting Shubnikov de Haas oscillations with an empirical expression for valley splitting²³:

$$\Delta_{\rm v} = \alpha \delta n \tag{2}$$

where, δn is an empirical measure of the out-ofplane electrostatic potential asymmetry controlled by front and back gates:

$$\delta n = n_{\rm B} - n_{\rm F} \tag{3}$$

where $n_{\rm F}$ and $n_{\rm B}$ are electron densities contributed by respective gates. Both $n_{\rm F}$ and $n_{\rm B}$ can take positive or negative values where negative values represent a density reduction due to a depleting bias from the corresponding gate so that the total electron density is given by

$$n = n_{\rm B} + n_{\rm F}.\tag{4}$$

The numerical factor α which is of the order of 0.5 meV/10¹⁵m⁻² determines how much the valley splitting changes with δn when δn is positive. That is, when the quantum well is biased in such a way that the electrons are pulled towards the back (SIMOX

buried-oxide) interface. On the other hand, when δn is negative, the electrons are pushed against the front interface, which is formed by standard thermal oxidation, where we find the valley splitting to be negligibly small. Thus, by pressing the electrons against the buried-oxide interface (positive δn) we can increase the valley splitting continuously, and independently control the electron density n. The out-of-plane potential necessarily affects the disorder, however, but the effects of this can be independently examined by applying a negative δn for which there is no valley splitting¹⁷.

For fitting the Shubnikov de Haas oscillations, we fix the perpendicular magnetic field and compare the valley splitting $\Delta_{\rm v}$ against the cyclotron energy $\hbar\omega_c$, or more accurately, we map the number of occupied Landau levels of the two valleys as function of $(\delta n, n)$. Straightforwardly applying the singleparticle model only yields a value for $\alpha m_{\rm b}$ but not α , in the same manner as coincidence experiments under tilted field only provide values for $gm_{\rm b}$ and not g. The bare effective mass only provides a crude conversion of the valley splitting to an energy scale²³, and would represent a good measure of the valley splitting in the absence of interactions that alter the effective density of states.

Valley polarisation is then estimated at full spin polarisation from the equation:

$$p_{\rm v} = \frac{\Delta_{\rm v} D_0}{n};$$

$$p_{\rm s} = 1,$$

(5)

The determination of valley polarisation does not, therefore, rely on separating α and $m_{\rm b}$ since in Eqs. 5, $\Delta_{\rm v}$ never appears on its own but always as a product with D_0 . It follows that this equation remains a valid method of determining the valley polarisation even in the presence of strong interactions. See Supplementary Discussion for more details.

Electrical Measurements

The samples were cooled in a Variable Temperature Insert with a base temperature of 1.6 K inserted into a 30 T resistive magnet. A standard four-terminal lock-in technique was used to measure the resistivity ρ_{xx} and ρ_{xy} of a sample with a Hallbar geometry. The current was kept below 5 nA to avoid electron heating. The samples were aligned parallel to the applied magnetic field with an *in-situ* rotator, eliminating the Hall resistance.

Determination of the mobility

The comparison of the theory to the experimental data requires the determination of the mobility of the sample in the Drude regime (conductivity $>> e^2/h$, see the next section). In practice one should measure the resistance at high density to obtain this quantity. However, this is not straightforward in our case because for densities larger than $n = 5 \times 10^{15} \text{ m}^{-2}$, electrons start to experience scattering from localized states in the upper spatial subband which become $populated^{34}$. Fortunately, the mobility at high density in the absence of the influence of the upper spatial subband can still be determined in our sample. To do so, we exploit the fact that pressing the electron gas to the front interface at negative δn does not increase valley splitting but narrows the effective width of the out-of-plane electronic wavefunction. This pushes the upper spatial subband to higher energies and suppresses its influence. This is illustrated by the solid white line in Fig. 4 which demarcates the onset of occupation of the upper subband. As the out-of-plane electric bias (δn) is increased, the density n at which it starts to fill increases, reflecting the increasing confinement energy 23 . The suppression of scattering by localized states in the upper spatial subband is evidenced by the reduction of resistance with δn for densities about 10^{16} m⁻². For densities relevant to the present study, scattering by localized states in the upper subband is absent as shown by the blue constant resistance contour in Fig. 4 which is parallel to the constant density line for all negative $-2 \times 10^{16} \mathrm{m}^{-2} < \delta n < 0$. For even larger electric fields $\delta n < -2 \times 10^{16} \text{m}^{-2}$ the electron gas experiences the roughness of the front interface³⁴ and the resistance starts to increase so that the iso-resistance lines deviate from constant density lines. We conclude that the mobility at high density and in absence of the influence of the upper spatial subband can be estimated in the regime $-2 \times 10^{16} \text{m}^{-2} <$ $\delta n < -1 \times 10^{16} \text{m}^{-2}$. Therefore, we estimated μ for $n = 10^{16} \text{ m}^{-2}$ and $\delta n = -1.5 \times 10^{16} \text{m}^{-2}$ marked by a star in the Fig. 4, where $\rho = 760\Omega$ leading to $\mu = 8000 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}.$

Quantum Monte Carlo simulations

The model we consider is a generalization of the Anderson model to the many-body problem (see Ref. 41 and 51 for details). The system is made of N spin up/down electrons with Coulomb interaction

on a disordered lattice of $L_x \times L_y$ sites. The electrons either populate a single valley $(p_v = 1)$ or are equally split up into two degenerate valleys $(p_v = 0)$. Their spin configuration sets the value of the spin polarisation $p_{\rm s}$. Formally, the spin and valley degrees of freedom are treated strictly in the same way as an internal electronic degree of freedom. In the continuum limit $\nu \equiv N/L_x L_y \ll 1$ (where lattice effects are negligible) and in the thermodynamics limit $N \gg 1$, the physics of a given (p_s, p_v) configuration is entirely controlled by two dimensionless parameters $r_{\rm s} = m_{\rm b} e^2 / (4\pi\epsilon\hbar^2\sqrt{\pi n}) \ (m_{\rm b} = 0.19m_e \text{ effective}$ mass, e electron charge, $\epsilon = 7.7\epsilon_0$ dielectric constant) and $1/k_F l$ (k_F Fermi momentum, l mean free path, both taken for the spin- and valley-degenerate system) which characterize respectively the interaction strength and the disorder strength in the system. Experimentally, it is difficult to estimate $k_F l$ for low density systems because conductivity is no longer a good estimate of disorder. We overcome this issued by observing that for white noise disorder of amplitude W (as assumed in our model), $k_F l \propto n$. Therefore, $\eta \equiv r_s \sqrt{k_F l}$ does not depend on n and depends only on W^{41} . One can estimate η in the high density regime where electronic interactions are negligible. In that regime, the conductance g of the system is $g = (2e^2/h)k_F l$ which gives $\eta = \sqrt{\mu}e^{3/2}m/(4\pi\epsilon\hbar^{3/2})$ where $\mu = g/(en)$ is the mobility of the sample. Thus, the two input parameters r_s and $k_F l$ of our model can be estimated from the mobility of the sample measured at high density and from the experimental values of electronic densities.

We use the Green's Function Monte Carlo method⁵⁰ in the fixed-node approximation to compute the energy per particle $E(p_s)$ of the ground state of our model at zero temperature⁴¹. The polarisation energy E_p is deduced from $E_p = E(p_s = 1) - E(p_s = 0)$ and averaged over 50 to 200 samples depending on the disorder strength. To extrapolate data at the thermodynamic and continuum limit, finite N- and ν -effects are carefully investigated. We thus observed large but controlled lattice effects without interaction that disappear as interaction is switched on $(r_{\rm s} \gtrsim 0.5)$. Small finite size effects in N are also present but they rapidly fade with the disorder amplitude. The resulting extrapolated data, as well as their fits given below. are finally obtained with a precision of the order of $\pm 0.02 E_{\rm F}^0$ (for $k_F^0 l_0 \ge 1.5$) and $\pm 0.04 E_{\rm F}^0$ (for $0.3 < k_F^0 l_0 < 1.5$) at $p_v = 0$, and roughly twice larger at $p_{\rm v} = 1$.

Without interaction $(r_s = 0)$, our data are in per-

fect agreement with the second-order perturbative formula $E_p/E_{\rm F}^0 = 1/2 [1] + \log 2/(\pi k_F^0 l_0)$ for $p_{\rm v} = 0$ $[p_{\rm v} = 1]$, at least for weak disorder $(k_F^0 l_0 \gtrsim 0.4)$. In the presence of (even small) interaction, first the effect of disorder is reversed making easier the spin polarisation of the system and second, the $1/k_F^0 l_0$ correction to E_p is no longer valid (except for tiny disorder). We find that our E_p data are very well described by the following formula,

$$E_p(k_F^0 l_0, r_{\rm s}) = E_p^{cl}(r_{\rm s}) + \frac{\beta(r_{\rm s})}{\sqrt{k_F^0 l_0}} E_{\rm F}^0 + A_5 E_{\rm F}^0, \quad (6)$$

where the polarisation energy of the clean system E_p^{cl} and the parameter β are both fitted with Padé approximates,

$$E_p^{cl}(r_{\rm s}) = \frac{A_0 + A_1 r_{\rm s}}{A_2 + A_3 r_{\rm s} + A_4 r_{\rm s}^2} E_{\rm F}^0 \tag{7}$$

$$\beta(r_{\rm s}) = \frac{B_0 + B_1 r_{\rm s}^2}{B_2 + B_3 r_{\rm s} + B_4 r_{\rm s}^2}, \qquad (8)$$

the fitting parameters A_i and B_i being given in Table I. We note that Eq. 7 for E_p^{cl} is in very good agreement with previous Quantum Monte Carlo calculations performed for the valley-polarized sys tem^{52} and the valley-degenerate system³⁹. Equation 8 – and in particular the fact that β 's sign flips at $r_{\rm s} \approx 0.3$ (for $p_{\rm v} = 0$) and $r_{\rm s} \approx 1.2$ (for $p_{\rm v} = 1$) - mainly depicts the opposite effects of disorder at very weak and stronger interactions. The last parameter A_5 adjusts the origin of the linear disorder correction in $1/\sqrt{k_F^0 l_0}$, to roughly take into account the actual quadratic correction in $1/\sqrt{k_F^0 l_0}$ at weak disorder. At extremely weak disorder, $1/(k_F^0 l^0) \lesssim$ 0.04, A_5 shall be taken equal to 0 and E_p evaluated by E_p^{cl} . We point out that Eqs. 6-8 are no more than one simple way to report our data, valid (at least) for $0.25[0.5] \leq r_{\rm s} \leq 10$ (at $p_{\rm v} = 0 [p_{\rm v} = 1]$) and $k_F^0 l_0 \ge 0.3$ as long as the output E_p is positive.

Deducing the polarisation magnetic field $B_{\rm p}$ from E_p is straightforward, once noticing that the energy E of the ground state is quadratic in $p_{\rm s}$,

$$E(p_{\rm s}) = E(0) + E_p p_{\rm s}^2$$
. (9)

This statement is obvious in the absence of disorder and interaction where we have $E_p = E_{\rm F}^0/2 [E_{\rm F}^0]$ for $p_{\rm v} = 0 \ [p_{\rm v} = 1]$. Numerically, it turns out to remain valid with good precision for intermediate disorder and interaction strength ($0 \le r_{\rm s} \le 10, k_F^0 l_0 > 1$). In particular, Eq. 9 is satisfied in the disorder and interaction regime explored in the present experiment. Then, when an in-plane magnetic field *B* is applied, a Zeeman term $-g\mu_{\rm B}Bp_{\rm s}/2$ has to be added to the right hand side of Eq. 9. Minimizing the energy *E* with respect to $p_{\rm s}$ gives the spin polarisation of the system at zero temperature, $g\mu_{\rm B}B/(4E_p)$, from which we get $B_{\rm p} = 4E_p/(g\mu_{\rm B})$.

Figure 6 presents the result of the numerical calculations of the magnetic field of full spin polarisation for various values of disorder. This figure shows that even in the presence of weak disorder ($\mu = 10^6$ cm²V⁻¹s⁻¹), the magnetic field of full spin polarisation is expected to be much lower than in the non-interacting picture.

i	0	1	2	3	4	5
$A_i(p_v = 0)$	27.93	9.83	56.5	46	1.77	0.019
$A_i(p_v = 1)$	23.4	-0.5	24.4	7.75	0.27	0
$B_i(p_v = 0)$	2.70	-24.81	42.4	-11.5	246.9	
$B_i(p_v = 1)$	54.28	-39.30	348	170.5	267	

TABLE I. Coefficients for the estimation of polarisation energies. A_i and B_i parameters of Eqs. 7 and 8 for the valley-degenerate ($p_v = 0$) and valley-polarized ($p_v = 1$) system.

The code to perform this simulations has been parallelised and ported on CEA Computing Center for Research and Technology (CCRT) massive parallel clusters. About 100000 CPU hours have been required for the present study. The code is available upon request.

TEM images

The High Angle Annular Dark Field scanning TEM images were measured using a probeaberration corrected FEI Titan microscope operated at 200 kV. A 100-nm-thick specimen was prepared by focused ion beam milling at 5 kV to reduce the surface damage. The HAADF STEM images are sensitive to Z-contrast and the vertical bright dumbbell structures are typical of aberration corrected images of silicon samples oriented in the < 110 >direction and show silicon atoms separated by 1.36 Angstroms in projection.

¹ Ando T., Fowler A. B. & Stern F. Electronic properties of two-dimensional systems *Rev. Mod. Phys.* 54,

^{437 (1982).}

- ² Schaffler F. High-mobility Si and Ge structures Semicond. Sci. Technol. **12** 15151549 (1997).
- ³ Ghani, T., et al. A 90nm high volume manufacturing logic technology featuring novel 45nm gate length strained silicon CMOS transistors. *IEDM Tech. Dig.* 978-980 (2003)
- ⁴ Gunawan, O. *et al.* Valley susceptibility of an interacting two-dimensional electron system. *Phys. Rev. Lett.* **97**, 186404 (2006).
- ⁵ Rycerz, A., J. Tworzydl, J., & Beenakker, C., W., J. Valley filter and valley valve in graphene. *Nature Phys.* **3** 172 (2007).
- ⁶ Culcer, D., Saraiva, A., L., Koiller, B., Hu, X., & Das Sarma, S. Valley-Based noise-resistant quantum computation using Si quantum dots. *Phys. Rev. Lett.* **108**, 126804 (2012).
- ⁷ Behnia, K. Polarized light boosts valleytronics. Nature Nanotech. 7, 488-489 (2012).
- ⁸ Isberg, J. *et al.* Generation, transport and detection of valley-polarised electrons in diamond. *Nature Mater.* **12**, 760-764 (2013).
- ⁹ Jones, A. M., *et al.* Optical generation of excitonic valley coherence in monolayer WSe₂. *Nature Nanotech.* **8**, 634-638 (2013).
- ¹⁰ Xu, X., Yao. W. & Heinz, T Spin and pseudospins in layered transition metal dichalcogenides. *Nature Phys.* **10**, 343-350 (2014).
- ¹¹ Shkolnikov, Y. P., Misra, S., Bishop, N. C., De Poortere, E. P. & M. Shayegan Observation of quantum Hall valley skyrmions. *Phys. Rev. Lett.* **95**, 066809 (2005).
- ¹² Bishop, N. C. *et al.* Valley polarization and susceptibility of composite fermions around a filling factor $\nu = 3/2$. *Phys. Rev. Lett.* **98**, 266404 (2007).
- ¹³ Padmanabhan, M., Gokmen, T., & Shayegan, M. Ferromagnetic fractional quantum Hall states in a valleydegenerate two-dimensional electron system. *Phys. Rev. Lett.* **104**, 016805 (2010).
- ¹⁴ Gokmen, T. Padmanabhan, M., & Shayegan, M. Transference of transport anisotropy to composite fermions. *Nature Phys.* 6, 621624 (2010).
- ¹⁵ Gunawan, O. *et al.* Spin-valley phase diagram of the two-dimensional metal-insulator transition. *Nature Phys.* **3**, 388 - 391 (2007).
- ¹⁶ Takashina, K. *et al.* Impact of valley polarization on the resistivity in two dimensions. *Phys. Rev. Lett.* **106**, 196403 (2011).
- ¹⁷ Takashina, K. *et al.* Spin and valley polarisation dependence of resistivity in two dimensions. *Phys. Rev. B* 88, 201301(R) (2013).
- ¹⁸ Renard, V. T. *et al.* Metallic behaviour in SOI quantum wells with strong intervalley scattering. Sci. Rep. **3**, 2011 (2013).
- ¹⁹ Shkolnikov, Y., P., Vakili, K., De Poortere, E. P., & Shayegan M. Dependence of spin susceptibility of a two-dimensional electron system on the valley degree of freedom. *Phys. Rev. Lett.* **92**, 246804 (2004).
- ²⁰ Padmanabhan, M., Gokmen, T., & Shayegan M. Enhancement of valley susceptibility upon complete spin

polarisation. Phys. Rev. B 78, 161301(R) (2008).

- ²¹ Gokmen, T., Padmanabhan, M., & Shayegan M. Contrast between spin and valley degrees of freedom. *Phys. Rev. B* **81**, 235305 (2010).
- ²² Takashina, K., Fujiwara, A., Horiguchi, S., Takahashi, Y. & Hirayama, Y. Valley splitting control in SiO₂/Si/SiO₂ quantum wells in the quantum Hall regime. *Phys. Rev. B* **69**, 161304 (2004).
- ²³ K. Takashina *et al.* Valley polarization in Si(100) at zero magnetic field. *Phys. Rev. Lett.* **96**, 236801 (2006).
- ²⁴ Dolgopolov, V., T., & Gold, A. Magnetoresistance of a two-dimensional electron gas in a parallel magnetic field. *JETP lett.* **71**, 42-46 (2000).
- ²⁵ Okamoto, T., Hosoya, K., Kawaji, S. & Yagi, A. Spin degree of freedom in a two-dimensional electron liquid. *Phys. Rev. Lett.* 82, 3875-3878 (1999).
- ²⁶ Tutuc, E., De Poortere, E., P., Papadakis, S. J., & Shayegan M. In-plane magnetic field-induced spin polarization and transition to insulating behavior in two-dimensional hole Systems. *Phys. Rev. Lett.* 86, 2858-2861 (2001).
- ²⁷ Shashkin, A., A., Kravchenko S., V., Dolgopolov, V., T., & Klapwijk, T, M. Indication of the ferromagnetic instability in a dilute two-dimensional electron system. *Phys. Rev. Lett.* **87**, 086801 (2001).
- ²⁸ Pudalov, V., M., Brunthaler, G., Prinz, A., & Bauer G. Weak anisotropy and disorder dependence of the in-plane magnetoresistance in high-mobility (100) Siinversion layers. *Phys. Rev. Lett.* 88, 076401 (2002).
- ²⁹ Lai, K;, Pan, W., Tsui, D., C., Lyon, S. A., Mhlberger, M., & Schaffler F. Two-dimensional metal-insulator transition and in-plane magnetoresistance in a high-mobility strained Si quantum well. *Phys. Rev. B* **72**, 081313 (2005).
- ³⁰ Boukari, H., Perez, F., Ferrand, D., Kossacki, P., Jusserand, B. & Cibert, J. Spin susceptibility enhancement in a two-dimensional hole gas. *Phys. Rev.* B 73, 115320 (2006).
- ³¹ Piot, B., A., Maude, D., K., Gennser, U., Cavanna, A., & Mailly D. Interplay among spin, orbital effects, and localization in a GaAs two-dimensional electron gas in a strong in-plane magnetic field. *Phys. Rev. B* 80, 115337 (2009).
- ³² Kapustin *et al.* Spin susceptibility and polarisation field in a dilute two-dimensional electron system in (111) silicon. *Phys. Rev. B* **79**, 205314 (2009).
- ³³ Das Sarma, S. & Hwang, H., E. Parallel magnetic field induced giant magnetoresistance in low density quasitwo-dimensional layers. *Phys. Rev. Lett.* **84**, 5596 (2000).
- ³⁴ Electron and hole mobilities at a Si/SiO2 interface with giant valley splitting. Niida, Y., Takashina, K., Fujiwara, A., & Hirayama, Y. Appl. Phys. Lett **102**, 191603 (2013).
- ³⁵ De Palo, S., Botti, M., Moroni, S., & Senatore, G. Effects of thickness on the spin susceptibility of the two dimensional electron Gas. *Phys. Rev. Lett.* **94**, 226405 (2005).

- ³⁶ Zhang Y., & Das Sarma S. Density-dependent spin susceptibility and effective mass in interacting quasitwo-dimensional electron systems. *Phys. Rev. B.* 72, 075308 (2005).
- ³⁷ Zhang, Y. , & Das Sarma S. Nonlinear 2D Spin Susceptibility in a Finite Magnetic Field: Spin-Polarization Dependence. *Phys. Rev. Lett.* **96**, 196602 (2006).
- ³⁸ Das Sarma S., Hwang, E., H., & Li Q. Valleydependent many-body effects in two-dimensional semiconductors. *Phys. Rev. B.* 80, 121303(R) (2009).
- ³⁹ Correlation energy and spin susceptibility of a twovalley two-dimensional electron gas. Marchi, M., De Palo, S., Moroni, S., & Senatore G. *Phys. Rev. B* 80, 035103 (2009).
- ⁴⁰ Subaşi, A., L., & Tanatar B. Effects of a parallel magnetic field on the ground-state magnetic properties of a two-dimensional electron gas. *Phys. Rev. B* 78, 155304 (2008).
- ⁴¹ Fleury, G., & Waintal X. Energy scale behind the metallic behaviors in low-density Si MOSFETs. *Phys. Rev. B* **81**, 165117 (2010).
- ⁴² Gokmen, T. *et al.* Spin susceptibility of interacting two-dimensional electrons with anisotropic effective mass. *Phys. Rev. B* **76**, 233301 (2007).
- ⁴³ Vakili, K. *et al.* Spin susceptibility of two-dimensional electrons in narrow AlAs quantum wells. *Europhys. Lett.* **92**, 226401 (2004).
- ⁴⁴ Conti, S. & Senatore, G. Electron correlation and charge transfer instability in bilayer two-dimensional electron gas. *Europhys. Lett.* **36**, 695-700 (1996).
- ⁴⁵ Lu, T. M., Pan, W., Tsui, D. C., Lee, C. -H. & Liu, C. H. Fractional quantum Hall effect of two-dimensional electrons in high-mobility Si/SiGe field-effect transistors. *Phys. Rev. B* **85**, 121307(R) (2012).
- ⁴⁶ Kott, T. M., Hu, B., Brown, S. H. & Kane, B. Valleydegenerate two-dimensional electrons in the lowest Landau level. *Phys. Rev. B* **89**, 041107(R) (2014).
- ⁴⁷ Saraiva A.L., Calderon M.J., Hu X., Das Sarma S. & Koiller B. Physical mechanisms of interface-mediated intervalley coupling in Si *Phys. Rev. B* **80**, 081305(R) (2009).
- ⁴⁸ Saraiva A.L., Calderon M.J., Capaz R.B., Hu X., Das Sarma S. and Koiller B. Intervalley coupling for interface-bound electrons in silicon: An effective mass study *Phys. Rev. B* 84, 155320 (2011).

- ⁴⁹ Saraiva A.L., Koiller B. & Friesen M. Extended interface states enhance valley splitting in Si/SiO₂. *Phys. Rev. B* 82, 245314 (2010).
- ⁵⁰ Trivedi, N., & Ceperley D. M. Ground-state correlations of quantum antiferromagnets : a Green-function Monte Carlo study. *Phys. Rev. B* **41**, 4552 (1990).
- ⁵¹ Waintal, X. On the quantum melting of the twodimensional Wigner crystal. *Phys. Rev. B* **73**, 075417 (2006).
- ⁵² Attaccalite, C., Moroni, S., Gori-Giorgi, P., & Bachelet, G. B. Correlation energy and spin polarisation in the 2D electron gas *Phys. Rev. Lett.* 88, 256601 (2002).

ACKNOWLEDGEMENTS

We acknowledge the support from the 7th framework programme Transnational Access (contract N 228043-EuroMagNET II Integrated Activities Ref. GSC09-210) and the support from the CEA-CCRT supercomputing facilities. VTR acknowledges support from the Nanoscience Fundation of Grenoble. XW is founded by the ERC consolidator grant Meso-QMC. DC is supported by the ERC starting Grant Holoview. KT and DT are supported by the EPSRC of the UK(EP/I017860/1). AF acknowledges the support by the Funding Program for Next Generation World-Leading Researchers of JSPS (GR103). YH acknowledges support from JST programs.

AUTHORS CONTRIBUTION

VTR, BAP and KT designed the experiments. AF fabricated the samples. VTR, BAP, YN, DT and KT performed the transport measurements which were discussed by all the authors. XW and GF performed the quantum Monte Carlo simulations. DC performed TEM measurements. VTR, KT, GF and XW co-wrote the manuscript and all authors commented on it. KT coordinated the collaboration.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.