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Electroactive self-assembled monolayers: A versatile function to fit symmetric voltammetric peak.

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ABSTRACT

We propose a versatile function to fit adsorption voltammometric peak in order to extract the characteristic parameters as the full width at half maximum, the peak potential, the peak current and the surface coverage. Based on the generalized Gaussian function and supported by generalized lateral interactions model, this method has been tested on different electroactive self-assembled monolayers (i.e. ferrocene, bithiophene, tetraphiafulvalene and radical aminoxyl units).

1. Introduction

Current-voltage behaviours of electroactive self-assembled monolayers (SAMs) can be simple or complex with sharp, normal or broad shapes [1, 2] and one of the major obstacles facing those who wish to analyse raw data is how to extract characteristic parameters ($E_p$, $i_p$, and FWHM) from experimental cyclic voltamograms (CVs). The only alternative to CV peak analysis is often to use the graphical powerful analysis tools of the turnkey instrument control software (i.e. EC-Lab from Biologic, VersaStudio Software from Princeton Applied Research, etc.).

Previous works [3-7] have proposed to fit unusual CV peaks via usual or unusual functions such as Gaussian, Lorentzian, or Extreme function but these calculations were either very intricate or not based on a theoretical support.

Herein, we propose a versatile method to fit experimental peak in order to extract characteristic parameters ($E_p$, $i_p$, FWHM and $\Gamma$) of cyclic voltamograms (CVs), especially for non-ideal voltamograms where no algebraic equation does exist. This approach is compared to the extended Laviron’s interactions model [8, 9] and then to electrochemical data obtained from several electroactive SAMs.
2. Generalized lateral interactions model

In a previous work [8, 9], we have presented a theoretical study to complete the lateral interaction model proposed by E. Laviron [10], by extending this initial model to non-random distributions of electroactive sites adsorbed on surface. This model enables current-voltage behaviours to be simulated and allows extracting characteristics parameters of cyclic voltamograms (CVs) obtained from any surface distribution of electroactive SAM.

To summarize, the generalized lateral interactions model can be defined according to the main following hypotheses [9-12]:

- The electroactive centers are distributed on substrate with a unimodal statistical distribution of electroactive neighbours. A parameter \( \phi(\theta) \), between 0 and 1, defined for a normalized surface coverage \( \theta \), quantifies the segregation level of the electroactive centers. For a randomly distributed SAM, \( \phi(\theta) = \theta \), and when a segregation exists on the surface, \( \phi(\theta) > \theta \).

- The sum of normalized surface coverage \( \theta_o \) and \( \theta_r \) of oxidized (O) and reduced (R) species is constant and equal to \( \theta \),

- The surface occupied by one molecule of O is equal to the surface occupied by one molecule of R,

- The electrochemical rate constant \( k_s \) is independent of the coverage,

- \( a_{oo}, a_{rr} \) and \( a_{or} \) are the interaction constants between molecules of O, molecules of R and molecules of O and R, respectively. \( a_i \) is positive for an attraction and negative for a repulsion.

For a full reversible reaction \( (k_s \to \infty) \), CVs are reversible, and the characteristic parameters as full width at half maximum (FWHM), peak potential \( (E_p) \) and peak current \( (i_p) \) are defined as:

\[
E_p(\phi(\theta)) = E_0 + \frac{RT}{nF} S\phi(0)
\]  

(1)

\[
\text{FWHM}(\phi(\theta)) = \frac{2 RT}{nF} \left[ \ln \left( 1 + \frac{2 - G\phi(\theta)}{4 - G\phi(\theta)} \right) - G \frac{2 - G\phi(\theta)}{4 - G\phi(\theta)} \phi(\theta) \right]^{\frac{\phi(\theta)}{S}} \approx \frac{RT}{nF} \left( 2 \ln \left( 2 \sqrt{2} + 3 \right) - \frac{3 \sqrt{2}}{2} G\phi(\theta) \right)
\]  

(2)

\[
i_p(\phi(\theta)) = \frac{n^2 F^2 v A \Gamma_{\text{max}}}{RT} \frac{0}{2(2 - G\phi(\theta))}
\]  

(3)

with, \( G = a_{oo} + a_{rr} - 2a_{or} \) et \( S = a_{or} - a_{oo} \) (\(|G| \text{and} |S| \leq 2\))
G and S, play a primordial role and can be defined as "interaction" parameters of O and R, respectively. The parameter G defines the shape of the peak (FWHM) and the peak intensity \(i_p\) and the parameter S, the peak potential \(E_p\) as a function of \(\theta\).

3. The Generalized Gaussian Function (GG Function)

Known as the exponential power distribution, or the generalized Gaussian distribution, this distribution is a parametric family of symmetric distributions. It includes all normal and Laplace distributions, and in some limiting cases it includes all continuous uniform distributions on bounded intervals of the real line.

Applied to a CV peak, the generalized Gaussian function can be expressed as:

\[
i(E, a, b, c) = \frac{a}{2 \cdot b \cdot \Gamma(1+1/c)} e^{\frac{[E-E_p]}{b}} \text{ with } \left\{ \begin{array}{l} E_p, \text{ peak potential} \\ \Gamma, \text{ the Gamma function} \end{array} \right. (4)
\]

and the characteristic parameters are defined as:

\[
FWHM = 2 \cdot b \cdot \left[ \ln(2) \right]^\frac{1}{c}
\]

\[
i_p = \frac{a}{2 \cdot b \cdot \Gamma(1+1/c)}
\]

\[
\Gamma_{SG} = \frac{a}{n \cdot FA \cdot v} \text{ with } \left\{ \begin{array}{l} A, \text{ the electrode area} \\ v, \text{ the scan rate} \end{array} \right. (7)
\]

In order to avoid confusion with the Gamma function (\(\Gamma\)), the symbol of the surface coverage is named \(\Gamma_{SG}\) (i.e. \(\Gamma_{SG} = \Gamma_{max} \cdot \theta\)).

3. Discussions

3.1. Starting from an ideal case

Let us take the ideal but simplistic case (i.e. Langmuir model and \(G = S = 0\)): all adsorption sites are equivalent and there is no interaction between immobilized electroactive centers, leading to a CV shape independent of the surface coverage. In this particular case, an algebraic equation was formulated by Laviron [11] to describe the CVs, and allows us to verify the robustness of fits generally used.
Gaussian, Lorentzian and Extreme functions do not match the ideal case (Figure 1A and 1B) and astonishingly, some previous work have used these empirical functions to estimation $E_p$, $i_p$, FWHM and $\Gamma_{SG}$ parameters.

Conversely, the GG function provides a relevant fit (Figure 1C). Nonetheless it is important to note that the GG function requires 4 parameters and not 3, as Gaussian and Lorentzian functions, and that multiple minima can occur during the refinement because $b$ and $c$ seem to be dependent variables.

### 3.2. Dependence of $b$ and $c$

The dependence of $b$ and $c$ can be solved by finding a correlation between the generalized lateral interactions model and the GG function. Mathematically, equations 2 and 5 lead to:

$$\text{FWHM} = \frac{G \cdot \phi(\theta)^{1/2}}{nF} \left(2 \ln(2 \sqrt{2} + 3) - \frac{3 \sqrt{2}}{2} G \cdot \phi(\theta)\right) = 2 \cdot b \cdot \left[\ln(2)\right]^2$$

and equations 3 and 6 to:

$$i_p = \frac{n^2 F^2 A \Gamma_m \theta}{RT} \cdot \frac{a}{2 \left(2 - G \phi(\theta)\right)} = \frac{2 \cdot b \cdot \Gamma(1+1/c)}{2 \cdot 1/c}$$

From the equations 9 and 10, the parameter $b$ can be expressed as a function of the parameter $c$ via a simple relation and, remarkably, independent of $G \phi(\theta)$:

$$b = 2 \left[\frac{RT}{nF} \left(\frac{3 \sqrt{2} - 2 \ln(2 \sqrt{2} + 3)}{3 \sqrt{2} \cdot \Gamma(1+1/c) - 4 \cdot \left[\ln(2)\right]^2}\right)\right]$$

From the equations 9 and 10, an relationship between $c$ and $G \phi(\theta)$ allows to estimate the boundary values $\left|G \phi(\theta)\right| < 1$ of $c$, according to:

$$(4 - 2G) \cdot \left[\ln(2)\right]^2 = \left(2 \ln(2 \sqrt{2} + 3) - \frac{3 \sqrt{2}}{2} G \phi(\theta)\right) \cdot \Gamma(1+1/c)$$

A numerical solving of the equation 12 shows that the parameter $c$ is strictly greater than 1 (i.e. close to 1.0166, 1.5691 and 2.0182 for $G \phi(\theta)$ equal to +1, 0 and -1, respectively).
To close this section, the GG function supported by lateral interactions model must be expressed as:

\[
i(E,a,c) = \frac{a}{2 \cdot b \cdot \Gamma(1+1/c)} e^{\left[ \frac{E_E \cdot E_a}{b} \right]^c} \quad \text{with} \quad \begin{cases} 
    c > 1 \\
    b = 2 \frac{RT}{nF} \left[ \frac{3 \sqrt{2} - 2 \ln \left( 2 \sqrt{2} + 3 \right)}{3 \sqrt{2} \cdot \Gamma(1+1/c) - 4 \cdot \left[ \ln(2) \right]^c} \right]
\end{cases}
\]  

(13)

Note that, for \( 3 > c > 1 \), \( b \) varies quasi linearly with \( c \) and can approximated to:

\[
b \approx \frac{RT}{nF} \left( \sqrt{2 \pi} \cdot c - \frac{5}{3} \right)
\]

(14)

### 3.2. GG function vs. generalized lateral interactions model

First of all, we simulated some CVs from generalized lateral interactions model with relevant \( G \) and \( S \) parameters in extreme cases (i.e. \( G = -S = +1 \) and \( G = -S = -1 \)) with \( \phi(\theta) > \theta \) (Figure 2A and 2B). Then, each CV shape was fitted with GG function (i.e. 3 and 4 unknown parameters) (Figure 2C and 2D). Then, the characteristic parameters (\( E_p \), \( I_p \), FWHM and \( \Gamma_{SG} \)) of each CV were extracted and, finally, plotted against \( \theta \) (Figure 2E and 2F) for comparison to expected values from generalized Laviron model.

The right agreement between mathematical shapes and modelled CV peaks in two extreme cases of phase segregation provides evidence of the versatility of GG function, for both 3 and 4 unknown parameters. The characteristic parameters are consistent with Laviron’s model in a wide range of surface coverage and we can notice that the values of FWHM for a peak fit with 3 parameters are less likely to agree with the Laviron’s model. This slight difference is due to the relationship between \( b \) and \( c \) (equation 11).

### 3.3 GG function vs. experimental CVs

It is well-known that the baseline can disturb the extraction of unknown parameters by peak fitting from experimental data and, herein, a monotonic polynomial function (i.e. \( g(x) = \pm \sum_{i=0}^{n} a_i \cdot x^i \) ) was selected for the baseline approximation in order to circumvent this problem.

#### 3.3.1 Different electroactive SAMs
Figure 3 shows that GG function peak fitting is successfully extracting $E_p$, $I_p$, FWHM and $\Gamma_{SG}$ of experimental electroactive SAMs ([i.e. ferrocene [13], bithiophene [14], tetrathiafulvalene [15] and radical aminoxyl [10] units], equally to one CV peak as to two. In the latter case, the two CV peaks were fitted with two GG functions of the same area (i.e. $a_1 = a_2$ – Figure 3C and 3D).

As expected, the usual slight dissymmetry of the CV peak of ferrocene SAM leads to a correct but no more result of the peak fitting (Figure 3B).

### 3.3.2 Mixed TEMPO SAMs

The robustness of the GG function peak fitting was tested through mixed SAMs (Figure 4). We opted for mixed Tempo:decanethiol SAMs, prepared by successive dilutions [8]. Such conditions lead to the random distributed (i.e. $\phi(\theta) = \theta$) electroactive centers on Au substrate and predict a linear dependence of peak potential (see equation 1) and FWHM (see equation 2) with the surface coverage [8].

A right agreement between GG peak and experiment shape was observed in the full range of surface coverage (Figure 4A). The electrochemical parameters ($E_p$, $I_p$, FWHM and $\Gamma_{SG}$) extracted from GG function peak fitting agree with those obtained in reference 8 via the Biologic EC-Lab Software, although with slight differences (Figures 4B, 4C and 4D) and the surface coverage dependence of $E_p$, FWHM and $I_p$ provides direct estimations of interaction parameters G and S. We can notice that 3 or 4 unknown parameters peak fitting produced very similar results, although the surface coverages from 4 parameters seem undervalued.

So, what is better for GG function peak fitting of experimental data? It is a GG function with 3 unknown parameters because the variations of c and b with surface coverage from 3 or 4 parameters peak fitting (Figures 4E and 4F) display a greater dispersion of estimated c values in the case of 4 unknown parameters.

### 4. Conclusion

We propose a versatile function to fit adsorption voltammetric peak in order to extract the characteristic parameters as the full width at half maximum, the peak potential, the peak current and the surface coverage. This work suggests to fit adsorption voltammetric peak with a 3 parameters GG function in order to finely estimate electrochemical parameters. It should be borne in mind that such calculations require experimental data with the respect of drastic experimental conditions (pure solvent, supporting electrolyte and compounds, substrate with very low roughness, ohmic drop compensation …).
Finally, this approach is dedicated to SAMs but it should also apply to a few electroactive layers.

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References

Figure 1. A comparison of peak fitting from an ideal CV \((n = 1, k = 1000 \text{ s}^{-1}, E_0 = 0.500 \text{ V}, T = 293 \text{ K}, v = 0.1 \text{ V.s}^{-1}, A = 0.2 \text{ cm}^2, \text{FWHM} = 0.089 \text{ V} \text{ and } \Gamma_{SG} = 5.00 \times 10^{-10} \text{ mol.cm}^{-2}\). (A) Fit vs. Lorentzian function (3 unknown parameters): \(E_0 = 0.500 \text{ V}, \text{FWHM} = 0.074 \text{ V} \text{ and } \Gamma_{SG} = 6.15 \times 10^{-10} \text{ mol.cm}^{-2}\). (B) Fit vs. a Gaussian function (3 unknown parameters): \(E_0 = 0.500 \text{ V}, \text{FWHM} = 0.095 \text{ V} \text{ and } \Gamma_{SG} = 4.85 \times 10^{-10} \text{ mol.cm}^{-2}\). (C) Fit vs. a GG function (4 unknown parameters): \(E_0 = 0.500 \text{ V}, \text{FWHM} = 0.088 \text{ V} \text{ and } \Gamma_{SG} = 4.95 \times 10^{-10} \text{ mol.cm}^{-2}\). Note that \(E_0 = 0.500 \text{ V}, \text{FWHM} = 0.086 \text{ V} \text{ and } \Gamma_{SG} = 5.02 \times 10^{-10} \text{ mol.cm}^{-2}\) for a GG function at 3 unknown parameters.
Figure 2. Evaluation of GG function peak fitting on calculated CVs from generalized Laviron model \((n = 1, k = 1000 \text{s}^{-1}, E_0 = 0.500 \text{V}, T = 293 \text{K}, v = 0.1 \text{V.s}^{-1}, A = 0.2 \text{cm}^2,\) in the case of two phase segregations \((G=+1, -1; S=G)\). (A) (line) calculated CVs for 5.00, 3.95, 2.95, 2.20, 1.50, 0.85, 0.52, 0.25 and 0.05 \(10^{-10} \text{mol.cm}^{-2}\) [9] for \(G=+1\). (dotted) Fit vs. a GG function \((4 \text{ unknown parameters})\). (B) (line) calculated CVs for 5.00, 3.95, 2.95, 2.20, 1.50, 0.85, 0.52, 0.25 and 0.05 \(10^{-10} \text{mol.cm}^{-2}\) [9] for \(G=-1\). (dotted) Fit vs. a GG function \((4 \text{ unknown parameters})\). (C) Fitted surface coverage, fitted apparent potential, fitted FWHM and fitted peak intensity vs. modelled surface coverage from a GG function peak fit in two cases: 3 (●) and 4 (▲) unknown parameters, then compared (line) to generalized Laviron model (see equations 1-3) for \(G=+1\). (D) Fitted surface coverage, fitted apparent potential, fitted FWHM and fitted peak intensity vs. modelled surface coverage from a GG function peak fit in two cases: 3 (●) and 4 (▲) unknown parameters, then compared (line) to generalized Laviron model (see equations 1-3) for \(G=-1\).
Figure 3. Evaluation of GG function peak fitting on experimental CVs of different electroactive SAMs. (A) CV of Tempo SAM in 0.1 M nBu$_4$NPF$_6$/CH$_2$Cl$_2$, at 0.1 V.s$^{-1}$ and 293 K [8]. Electrochemical parameters deduced of peak fitting: $E_0 = 0.515$ V, FWHM = 0.118 V, $\Gamma_{SG} = 5.33 \times 10^{-10}$ mol.cm$^{-2}$. (B) CV of Ferrocene SAM in 0.1 M nBu$_4$NPF$_6$/CH$_3$CN, at 0.1 V.s$^{-1}$ and 293 K [13]. Electrochemical parameters deduced of peak fitting: $E_0 = 0.375$ V, FWHM = 0.079 V, $\Gamma_{SG} = 3.60 \times 10^{-10}$ mol.cm$^{-2}$. (C) CV of TTF SAM in 0.1 M Bu$_4$NPF$_6$/CH$_2$Cl$_2$ at 0.1 V.s$^{-1}$, at 0.1 V.s$^{-1}$ and 293 K [15]. Electrochemical parameters deduced of two peaks fitting: $E_{01} = 0.232$ V, FWHM$_1 = 0.123$ V, $E_{02} = 0.547$ V, FWHM$_2 = 0.057$ V, $\Gamma_{SG} = 3.12 \times 10^{-10}$ mol.cm$^{-2}$. (D) CV of Bithiophene SAM in 0.1 M Bu$_4$NPF$_6$/CH$_2$Cl$_2$ at 0.1 V.s$^{-1}$, at 0.1 V.s$^{-1}$ and 293 K [14]. Electrochemical parameters deduced of two peaks fitting: $E_{01} = 0.700$ V, FWHM$_1 = 0.100$ V, $E_{02} = 0.996$ V, FWHM$_2 = 0.039$ V, $\Gamma_{SG} = 0.92 \times 10^{-10}$ mol.cm$^{-2}$. Note that the two CV peaks were fitted with two GG functions of the same area (i.e. $a_1 = a_2$).
Figure 4. Comparison of GG function peak fitting and experimental CVs of mixed Tempo SAMs, prepared with random distributed electroactive centers on Au substrate (see reference 8). Note that 3 and 4 unknown parameters peak fitting were symbolized by (●) and (▲), respectively then compared to results (represented by ★) from reference 8.

(A) (line) Experimental CVs of Tempo SAM in 0.1 M nBu4NPF6/CH2Cl2, prepared from different Tempo:decanethiol ratios, leading to 4.7 (i.e. θ = 100 %), 3.7, 2.8, 2.1, 1.4 and 0.8 \(10^{-10}\) mol.cm\(^{-2}\) [XX]. Note that these surface coverages were deduced by integration of the voltammetric signal. (dotted) Fit vs. a GG function (4 unknown parameters). (B) Fitted apparent potential vs. fitted surface coverage. Estimation of S parameter from equation 1. (C) Fitted FWHM vs. fitted surface coverage. Estimation of G parameter from equation 2. (D) Fitted peak intensity vs. fitted surface coverage. Estimation of \(i_p\) parameter from equation 3. (E) Fitted b and calculated b (see equation 11) vs. fitted surface coverage. (F) Fitted c vs. fitted surface coverage, displaying a greater dispersion of estimated c values in the case of 4 unknown parameters peak fitting.