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# Improvement of the chemical content prediction of a model powder system by reducing multiple scattering using polarized light spectroscopy

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**Abstract:** Near Infrared Spectroscopy (NIRS) is a powerful non destructive analytical method used to analyze major compounds in bulk materials and products and requiring no sample preparation. It is widely used in routine analysis and also in-line in industries, in-vivo with biomedical applications or in-field for agricultural and environmental applications. However, highly scattering samples subvert Beer-Lambert law's linear relationship between spectral absorbances and the concentrations. Instead of spectral pre-processing, which is commonly used by NIR spectroscopists to mitigate the scattering effect, we put forward an optical method, i.e. coupling polarized light with NIR spectrometry, to free spectra from scattering effect. This should allow us to retrieve linear and steady conditions for spectral analysis. When tested in Visible-NIR (VIS-NIR) range (400-800 nm) on model media - mixtures of scattering and absorbing particles - the set-up provided

21 significant improvements in absorber concentration estimation precision as well as in  
22 the quality and robustness of the calibration model.

23 **Index Heading:** Polarized Light Spectroscopy, Multiple Light Scattering, Diffuse  
24 Reflectance, Optical Properties, Chemical Content Prediction.

## 25 **1. Introduction**

26 Visible - Near infrared spectroscopy (VIS-NIRS) is a well-known technique used for  
27 measuring the chemical composition of a wide variety of media and products.  
28 Although VIS-NIRS has been quoted in articles for approximately 50 years<sup>1,2</sup> with  
29 this purpose, it really took off in the late 80's in agricultural and food applications  
30 (jumping from around 10 publications per year in the late 80's to 150 publications per  
31 year in the turn of century), and then in the 90's for pharmaceutical and biomedical  
32 applications. Today, it plays a major role in these sectors, as a routine laboratory  
33 method for in vivo or in-line monitoring system. On the one hand VIS-NIRS presents  
34 several advantages: VIS-NIR extinction coefficients are small compared to mid-  
35 infrared (MIR) ones, which allows light to penetrate deeper into objects and avoids  
36 time-consuming sample preparation; VIS-NIR light scattering makes it possible to  
37 analyze bulk samples with a retro-diffusion optical configuration, thus turning it into  
38 a non-destructive technique. In addition VIS-NIR optical components are low cost  
39 and with high Signal-to-Noise Ratio (SNR). On the other hand, VIS-NIRS has  
40 several drawbacks: the VIS-NIR spectrum is poorly resolved as it is made up of  
41 scattering effects and of wide low-intensity harmonics and combinations of MIR

42 fundamental absorption bands. Consequently, retrieving chemical information from  
43 VIS-NIR spectra is quite painstaking and requires advanced chemometrics: it is  
44 based on calibration models to be built between VIS-NIR spectra and known  
45 concentrations of a set of calibration samples. Traditionally, linear multivariate  
46 calibration methods such as Principal Component Regression (PCR) and Partial  
47 Least Square Regression (PLSR) are used in VIS-NIRS. However, scattering effects  
48 are troublesome in the VIS-NIR spectra of turbid media, defined by Shi and  
49 Anderson<sup>3</sup> as "*samples exhibiting multiple scattering events*". Scattering can be  
50 several orders of magnitude larger than absorption<sup>4</sup> and may invalidate the use of  
51 such data processing methods, which are themselves based on the underlying  
52 assumption of a linear Beer-Lambert law relationship between absorbance spectra  
53 and chemical concentration<sup>5</sup>. It is therefore necessary for VIS-NIR spectroscopists  
54 working on highly scattering media to use strategies to release VIS-NIR spectra from  
55 scattering effects. The most common strategy is spectral pre-treatment. These  
56 preprocessing step is specifically designed to reduce multiplicative and additive  
57 effects caused by variations in sample physical properties<sup>6,7</sup>. Among them, standard  
58 normal variate (SNV) often associated to detrend<sup>8</sup>, multiplicative signal correction  
59 (MSC)<sup>9</sup>, Extended MSC (EMSC)<sup>7</sup>, normalization or Optical Path Length Estimation  
60 and Correction (OPLEC)<sup>5,10</sup>. However, these approaches remain questionable: they  
61 consider that scattering is nearly constant over the wavelengths, which is not the  
62 case<sup>3</sup>; they may eliminate chemical-related information, which is very small with

63 regard to scattering effects<sup>11</sup>; they are inappropriate when light scattering varies  
64 greatly from sample to sample<sup>12</sup>.

65 Another option is to acquire the spectrum in a way that separates the part related to  
66 absorption from the part related to scattering. Specific experimental techniques,  
67 related to the application of light propagation theory and resolution of the Radiative  
68 Transfer Equation<sup>3</sup> have been proposed, including adding-doubling set-ups<sup>12-14</sup>,  
69 spatially-resolved spectroscopy<sup>15</sup>, time-resolved spectroscopy<sup>4,16</sup> and frequency-  
70 resolved spectroscopy<sup>17</sup>.

71 Although powerful, these methods have their limitations, particularly when applied  
72 on highly turbid samples. First, they may require complex and sometimes expensive  
73 optical implementations, which may not be compatible with conventional  
74 spectrometers or with highly turbid samples (for which transmission measurement is  
75 not possible). Secondly, as they rely on the estimation of absorption and scattering  
76 coefficients achieved by model inversion, parameters describing the studied medium  
77 (sample thickness, refractive index, particle size and shape...) must be known or  
78 approximated, which may be a troublesome task as they are often unknown in  
79 complex media<sup>12,18</sup>.

80 Whereas separating absorption and scattering from a VIS-NIR signal is still an open  
81 research issue on highly turbid samples, the main demand from VIS-NIR  
82 spectroscopists is *merely* for spectra with reduced impact of scattering in order to  
83 better fit Beer-Lambert's Law conditions<sup>19,20</sup>.

84 Light polarization subtraction is a simple technique to reduce directly the effects of  
85 multi-scattering on the measured signal<sup>20,21</sup>. This approach has been based on the fact  
86 that, when light interacts with matter, a small number of scattering events do not  
87 significantly modify the polarization status of the beam whereas multiple scattering  
88 leads to depolarization<sup>18,22</sup>. Polarization subtraction technique<sup>19,23-25</sup> was used to  
89 select light beams that retain initial polarization and which are therefore less  
90 impacted by multiple scattering events.

91 Although this technique has gained interest in the field of biomedical<sup>20,21,25</sup>, where it  
92 is used to optically target subsurface organelles (particles suspended in water) and  
93 tissues (layered samples), it is either poorly understood or not used by NIR  
94 spectroscopists working with agricultural, food, pharmaceutical and other industrial  
95 samples. To our knowledge, polarized NIRS techniques have never been applied to  
96 routine or in-line analysis to reduce scattering effects on spectra on turbid media.

97 In this paper, the effectiveness of this multi-scattering correction based on the  
98 polarization subtraction is evaluated using a two-component model powder system.  
99 The objectives of this paper were to assess the effect of multi-scattering correction (i)  
100 on the performances of a calibration model and (ii) on the robustness of the  
101 prediction model built from the corrected spectra for predicting the absorber's  
102 concentration of powder samples

## 103 **2. Theoretical Model : Polarization subtraction**

Capital bold characters will be used for matrices, e.g. **X**; non bold characters will be used for column vectors, e.g. *X*

Polarization subtraction technique<sup>23-25</sup> is based on the polarization-maintaining property of weakly scattered light. When polarized light illuminates a scattering medium, weakly scattered light will emerge in its original polarization state<sup>21,26-28</sup>, while multiple scattered light will emerge with random polarization. In the case of linearly polarized source, the light that is remitted in the same polarization channel as the input illumination is composed by light that has maintained its original polarization state plus a component from the randomly polarized heavily scattered light (cf equation 1). Light that emerges in the orthogonal polarization channel contains only randomly polarized light, approximately equal to the randomly polarized component in the original polarization state (cf equation 2).

$$I_{\parallel}(\lambda) = \frac{\Omega}{2\pi} \cdot I_0(\lambda) \cdot S(\lambda) + \frac{\Omega}{2\pi} \cdot I_0(\lambda) \cdot \alpha(\lambda) \cdot M(\lambda) \quad (1)$$

$$I_{\perp}(\lambda) = \frac{\Omega}{2\pi} \cdot I_0(\lambda) \cdot \beta(\lambda) \cdot M(\lambda) \quad (2)$$

Where  $I_{\parallel}(\lambda)$  and  $I_{\perp}(\lambda)$  are the light scattered by the media with parallel and perpendicular polarization respect to the polarization of the illumination light.  $I_0(\lambda)$  is the intensity of the illumination light.  $\Omega$  is the collection solid angle, residual term of the integration on the solid angle<sup>23-25</sup>, of the optical device.  $S(\lambda)$  and  $M(\lambda)$  are the probabilities of light undergoing single and multiple scattering respectively.

Since all light undergoes scattering :

$$S(\lambda) + M(\lambda) = 1 \quad (3)$$

Finally,  $\alpha(\lambda)$  and  $\beta(\lambda)$  are the multiple light scattered ratio by the media with the parallel and perpendicular polarization respect to the polarization of the illumination light. The sum  $\alpha(\lambda)$  and  $\beta(\lambda)$  must be one:

$$\alpha(\lambda) + \beta(\lambda) = 1 \quad (4)$$

By subtracting (1) to (2), the intensity of light undergoing single scattering ( $I_{ss}(\lambda)$ ) is equal to :

$$I_{ss}(\lambda) = I_{\parallel}(\lambda) - I_{\perp}(\lambda) = \frac{\Omega}{2\pi} \cdot I_0(\lambda) \cdot [S(\lambda) + (\alpha(\lambda) - \beta(\lambda)) \cdot M(\lambda)] \quad (5)$$

In conclusion, the part of the single-scattering effect in the signal is preserved and the multi-scattering effect is highly reduced.

### 3. Materials and Methods

#### 3.1 Instrumentation

In the experimental setup (figure 1), a halogen light source (150 W, Leica Cls ) was coupled with a 940  $\mu\text{m}$  core diameter optical fiber (numerical aperture (N.A) 0.22, Sedi & ATI). The light delivered by the fiber was collimated by an aspheric lens (F220SMA-B - Thorlabs). The incident beam was a 2 cm diameter circular spot with 1° divergence. The incident and reflected beam were polarized through two broad-band (400 nm - 800nm) polarizers (NT52-557, Edmunds Optics). Incident light was



148 linearly polarized and reflected light was collected in a narrow cone ( $1^\circ$ ). The output  
149 from the analyzer was coupled inside an optical fiber (N.A 0.22, Sedi & ATI) by an  
150 aspheric lens (F220SMA-B - Thorlabs). This fiber was connected to a spectrometer  
151 (MMS1, Zeiss) featuring a detection range of 400 nm - 800 nm, with 3 nm  
152 resolution. A constant angle of  $70^\circ$  was maintained between the excitation and  
153 collection arms. This angle was chosen to optimize intensity of the reflected beam  
154 and to avoid specular reflection.

### 155 **3.2 Experimental design and sample preparation**

156 Powdered samples mixing sand (Fontainebleau sand VWR International) and  
157 coloring dyes (brilliant blue FCF-E133 and chlorophyllin E141, purchased from  
158 Colorey, respectively named E133 and E141 in the text) were prepared. Two sand  
159 particle size classes were used:  $S_1$  with a diameter less than 250  $\mu\text{m}$  and  $S_2$  with a  
160 diameter greater than 250  $\mu\text{m}$ . Sand play the role of a scattering but non absorbing  
161 matrix. One or both of the coloring dyes have been added at different densities to the  
162 sand, playing the role of absorbing substance in the mixture. Note that absorbers in  
163 powdered form also have scattering properties. Particle sizes of the coloring powders  
164 were less than 50 $\mu\text{m}$ , with E133 being about three times smaller than E141.

165 Overall, 42 samples were prepared for spectral acquisition composing a calibration  
166 set and 12 samples were prepared, afterward and with the same procedure to create  
167 an independent test set.

168 The range of sample's colorant densities (in g.L-1) is specified in figure 2.

Each sample was directly prepared in an airtight plastic container of 100 mL by adding the precisely weighted corresponding amount of colorant in 20 g of sand using an analytical balance (Kern 770). The maximum dye volume added was not higher than 4% of the total sand volume. Considering that the pore volume for sand is about 40%, and that the dye particles are between 5 to 10 times smaller than the sand, one can make the assumption that the dye would fill the interstices between the sand particles and therefore not increase the initial volume of sand. The density of the colorant  $d_{\text{dye}}$  in a sample was obtained from :

$$d_{\text{dye}} = \frac{m_{\text{dye}} \cdot d_{\text{sand}}}{m_{\text{sand}}} \quad (6)$$

With  $m_{\text{dye}}$  the added mass of dye,  $d_{\text{sand}}$  the density of sand (which differ for  $S_1$  and  $S_2$ ) and  $m_{\text{sand}}$  the mass of sand (here 20 g). The colorant density ranged from [0 - 18 g.L<sup>-1</sup>].

To ensure homogeneity of the mixture, the sample was agitated after preparation and again just before it was carefully transferred in an adapted 5 cm of diameter cup to get an even and horizontal surface.

### 3.3 Spectral acquisition

For each sample, light was measured with the polarized spectrometer with parallel and perpendicular respect to the polarization of the illumination light. Dark current ( $I_b$ ) was recorded from all measured spectra and subtracted.

A broadband dielectric mirror (BB3-E02, Thorlabs) was used as a reference ( $I_0$ ) to standardize spectra from non-uniformities of all components of the instrumentation (light source, fibers, lens, polarizer and spectrometer).

191 From these measurements and the equation (5), a raw reflectance ( $R_w$ ) and a  
192 corrected reflectance ( $R_c$ ), for each sample, were calculated :

$$193 \quad R_w(\lambda) = \frac{(I_{\parallel}(\lambda) - I_{b\parallel}(\lambda)) + (I_{\perp}(\lambda) - I_{b\perp}(\lambda))}{(I_{o\parallel}(\lambda) - I_{b\parallel}(\lambda))} \quad (7)$$

$$194 \quad R_c(\lambda) = \frac{(I_{\parallel}(\lambda) - I_{b\parallel}(\lambda)) - (I_{\perp}(\lambda) - I_{b\perp}(\lambda))}{(I_{o\parallel}(\lambda) - I_{b\parallel}(\lambda))} = \frac{I_{ss}(\lambda) - (I_{b\parallel}(\lambda) + I_{b\perp}(\lambda))}{(I_{o\parallel}(\lambda) - I_{b\parallel}(\lambda))} \quad (8)$$

195

196 With  $I_{\parallel}(\lambda)$  and  $I_{\perp}(\lambda)$  the intensities of light scatters by the media with parallel and  
197 perpendicular polarization respect to the polarization of the illumination light and  
198  $I_{o\parallel}(\lambda)$  and  $I_{o\perp}(\lambda)$ , the intensities of light reflected by the standard mirror with  
199 parallel polarization respect to the polarization of the illumination light (as the  
200 perpendicular component emerging from the mirror is zero).  $I_{b\parallel}(\lambda)$  and  $I_{b\perp}(\lambda)$  are the  
201 dark current intensities recorded for each measurement.

202

### 203 **3.4 Multivariate analysis**

204 All computations and multivariate data analysis were performed with Matlab  
205 software v. R2012b (The Mathworks Inc., Natick, MA, USA).

206

### 207 **3.5 Linear unmixing**

208 The first step of Classical Least Square (CLS)<sup>29</sup> was used to extract the reflectance  
209 *pure spectra* of the absorbers from the reflectance spectra of the mixtures. Also  
210 called **K**-matrix, this linear unmixing assumes that a spectrum is a linear combination  
211 of the pure component's spectra. The whole calibration set **R** (42 samples mixing the

absorbers at different concentrations) and  $\mathbf{C}$ , the matrix of sample components concentrations, were used to compute the linear least square estimated  $\hat{\mathbf{K}}$ -matrix of the two pure active components (E133 and E141) composing  $\mathbf{K}$  knowing that:

$$\hat{\mathbf{K}} = \mathbf{RC}^T(\mathbf{CC}^T)^{-1} \quad (9)$$

Both the raw reflectance spectra ( $\mathbf{R}_w$ ) and the corrected reflectance spectra ( $\mathbf{R}_c$ ) were used to compute respectively  $\hat{\mathbf{K}}_w$  and  $\hat{\mathbf{K}}_c$  containing the demixed pure spectra of E133 and E141.

### 3.6 Calibration

Partial Least Square (PLS)<sup>30</sup> algorithm was used to model the chemical composition of the powder mixture using  $\mathbf{R}_w$  and  $\mathbf{R}_c$ . A general PLS model was built using the whole calibration set (42 samples) to predict the samples of the independent test set (12 samples). Secondly, to assess the robustness of the prediction models regarding sand particle size, a PLS model was built with the samples set  $S_2$  and tested on the independent test set  $S_1$  (figure 2). The number of latent variables was determined by comparing performances by leave-one-out cross-validation<sup>31</sup>. Performances ( $R^2$ , Standard Error of prediction corrected from the bias (SEPC)) and number of latent variables of the different prediction models built with uncorrected and corrected signals were compared when applied on the test set.

## 4. Results and discussion

## 234 **4.1 Spectra analysis**

### 235 *Bulk colorant*

236 The raw spectra  $R_w(\lambda)$  and the corrected spectra  $R_c(\lambda)$  of the pure powder colorant  
237 E133 and E141 are represented in figure 3 (a) and (b).

238 First comment is that the polarization subtraction reduces the global reflectance  
239 intensity of the measured signal (by 10 times). It is an expected result as only a small  
240 part of the signal is selected: the single-scattered one. Despite this reflectance loss,  
241 the corrected spectrum is not noisy and contains information about the sample.

242 Between 400 nm and 700 nm, the raw spectrum and the corrected spectrum have  
243 similar shapes. For example, the spectroscopic signature of the colorant E133  
244 appears to be purple (as seen in powdered form), mixing a reflectance peak at 450  
245 nm (Blue) and at 650 nm (Red). However, these peaks are more marked in the  
246 corrected spectra. For the raw spectrum, crushing peaks can be explained by a strong  
247 increase in reflectance after 750 nm. This sharp increase in reflectance, in a spectral  
248 range where the colorant does not absorb, is due to the multi-scattering. However,  
249 this effect seems to be less important for E141 than for E133. In the corrected  
250 spectra, this effect is strongly reduced (figure 3 (b)).

251

### 252 *Sand and dye mixtures*

253 Figures 3 (c) and (d) show respectively the raw spectra and the corrected spectra of  
254 sand  $S_1$  mixing coloring powder E133 at different densities. When mixed with the  
255 colorant, sand is responsible for high multi-scattering as it is not absorbing the light.

256 This physical phenomenon comes on top of the chemical information contained in  
257 the spectra and masks the spectral features of the absorber. The shape of the raw  
258 spectra of coloring powder E133 (figure 3 (a)) and the shapes of the raw reflectance  
259 of the sand-dye mixture (figure 3 (c)) are completely different. The multiplicative  
260 effect due to scattering is not wavelength dependent and depends on the number of  
261 scatterers in the sample. Therefore, the more dye, the more scatterers and,  
262 consequently the higher the reflectance. The order of the raw spectra is consistent  
263 with the dye's concentration, but for a physical reason.

264 By applying the correction, the spectral features of the colorant are enhanced as it  
265 can be seen on figure 3 (d). The signature of the corrected spectra is similar to the  
266 spectral signal of the colorant E133 in powdered form (figure 3 (b)). The reflectance  
267 peaks at 450 nm and at 650 nm clearly appear, but more important, because linked to  
268 the dye's concentration, the wavelength regions where absorbance occurs (400- 430  
269 nm and 500 – 650 nm) are now visible. In these regions, the spectrum ordering is  
270 consistent with the dye concentration, contrary to the other areas where low  
271 absorbance occurs and reveals more complex reflectance patterns.

272 Figures 3 (e) and (f) show respectively the raw spectra and the corrected spectra of  
273 sand  $S_1$  mixing this time coloring powder E141 at different densities. By comparing  
274 the raw reflectance intensities of the sand - E133 mixtures (figure 3 (c)) and sand -  
275 E141 mixtures (figure 3 (e)), containing the same ranges of dye's densities, it appears  
276 that the level of  $R_w$  is two-times higher for E133 than for E141. As stated in section  
277 'Experimental design and sample preparation', the particle size of E141 is, at least,

three-times larger than E133. This difference in particle diameter has a direct impact on the elastic scattering phenomenon occurring during light-matter interaction. First, for the same density of dye, small particles scatter more than larger particles<sup>21</sup>. Secondly, the scattering angle differs between small and large particles: the larger the diameter, the smaller the scattering angle. Combining these two properties, the overall reflectance intensity will be higher for smaller particles, which is the case of raw reflectance of the Sand-E133 mixture.

For the corrected spectra  $R_c$ , there is no significant difference in the intensity level between sand - E133 mixtures (figure 3 (d)) and sand - E141 mixtures (figure 3 (f)). This is coherent with the fact that the method corrects the spectra from multi-scattering, which is mainly due to the sand particles but also, and in a significant manner, to the powdered colorant.

#### 4.2 Extraction of the absorber's pure spectra

Figure (4) presents the demixed pure spectra  $\hat{K}$  extracted from the reflectance spectra ( $R_w$  and  $R_c$ ). The linear unmixing (figure 4 (a)) applied to raw spectra ( $R_w$ ) provided estimated pure spectra ( $\widehat{K_{w\_E133}}(\lambda)$  and  $\widehat{K_{w\_E141}}(\lambda)$ ) that are very different from the raw spectra  $R_{w\_E133}(\lambda)$  and  $R_{w\_E141}(\lambda)$  measured directly on the powders. The shape of these spectra are not matching and the correlation coefficients, between  $\widehat{K_{w\_E133}}(\lambda)$  and  $R_{w\_E133}(\lambda)$  and between  $\widehat{K_{w\_E141}}(\lambda)$  and  $R_{w\_E141}(\lambda)$ , are respectively equal to 0.59 and 0.74.

299 Linear unmixing assumes that a spectrum is a linear combination of the pure  
300 components spectra. From these results, the failure to recover the absorber's pure  
301 spectrum from the raw reflectance spectra, support the fact that interactions in the  
302 mixture are responsible of non-linearities which are directly responsible of the non-  
303 linearities in the relationship between the absorbance and the absorbing power of the  
304 sample. It is well known<sup>20,32</sup> that scattering and absorbance are not independent  
305 phenomenon. Scatter increases the mean free path of photons, which increases the  
306 chances of being absorbed.

307 On the contrary, the computation of the  $\widehat{\mathbf{K}}_c$ -matrix is successful and matches the pure  
308 colorant corrected reflectance spectrum. Estimated pure spectra ( $\widehat{K_{c\_E133}}(\lambda)$  and  
309  $\widehat{K_{c\_E141}}(\lambda)$ ) are very close to  $R_{c\_E133}(\lambda)$  and  $R_{c\_E141}(\lambda)$  measured directly on the  
310 powder and corrected. The correlation coefficients are respectively 0.98 and 0.93. As  
311 the method corrects the signal from a physical phenomenon (multi-scattering), one  
312 can affirm that the observed interactions in the raw spectra are of optical nature (and  
313 not chemical interactions). Regarding these results and this consideration,  
314 polarization subtraction correction induces, by reducing the multi-scattering effect, a  
315 better linear relationship between the light attenuation and the absorption the dyes.  
316 The recovered spectra  $\widehat{\mathbf{K}}_c$  are corrected from the physical interactions occurring in  
317 the mixture.

318

### 319 **4.3 Calibration model**

320 *General model*



321 Table 1 shows the quality parameter of the prediction models of the test set  
322 absorber's densities comparing the raw and the corrected spectra.

323 First, with the raw spectra  $R_w(\lambda)$ , the quality of the E133 prediction model is  
324 distinctly poorer than the quality of the E141 prediction model. The number of latent  
325 variables is much higher for E133 as well as the  $SEP_c$ . On the contrary, the figures of  
326 merit for the E141 model are good. Again, E133 and E141 behave differently. As  
327 stated before, multiscattering effect is more important when E133 is present in the  
328 mixture (with or without E141) because of a smaller particle diameter. Hence, non-  
329 linearities between absorbance and absorber's concentration are more important and  
330 the PLS model is limited in building a performant linear prediction model for E133.

331 When the models are built with the corrected reflectance spectra  $R_c(\lambda)$ , the figure of  
332 merit of the absorber's density prediction models are good and of the same level for  
333 E133 and E141. In both cases, the number of latent variables is decreasing. The  
334 improvement is less important for E141 but significant for E133. And both models  
335 have a lower standard error of prediction compared to the  $R_w(\lambda)$  prediction models  
336 for the two colorants. In section 'Sand and dye mixture', we stated that the proposed  
337 method mainly reduced the effect of multiscattering due to sand particles, enhancing  
338 the part of the signal related to chemical absorbance. In  $R_w(\lambda)$ , while this information  
339 is present, it is masked by the multi-scattering and the PLS needs more latent  
340 variable to extract this chemically related information to build a model.

341 Here, the different behavior of the two dyes is not obvious anymore. This agrees with  
342 the hypothesis that the correction method equalizes the mean free photon path

343 between all the samples, regardless of the particle size and shape of the sample's  
344 constituents. For the two absorbers, the number of latent variables, which is an  
345 indicator of the complexity of the models, is still high (respectively 5 and 4 for E133  
346 et E141 with the corrected spectra  $R_c(\lambda)$ ) for samples mixing only two different  
347 absorbers. Theoretically, two PLS components should be sufficient. This agrees with  
348 the initial assumption that the polarization subtraction method highly reduces the  
349 multi-scattering but does not remove it completely. In addition, these results are  
350 consistent with the conclusions of section 'Extraction of the absorber's pure spectra',  
351 stating that the correction method restores, in a significant manner, the linear  
352 relationship between the spectra and the absorber's density in the powdered samples.  
353 To conclude, as the PLS models using the corrected spectra show good prediction  
354 capacities, it fulfills the assumption that even if the corrected signal intensity is  
355 highly reduced, the remaining information is of better quality in terms of signal  
356 sensitivity.

357

#### 358 *Robustness assessment*

359 Table 2 presents the results of the calibration model built with samples of one  
360 particle size ( $S_2 > 250 \mu\text{m}$ ) and tested on samples with another particle size ( $S_1 < 250$   
361  $\mu\text{m}$ ).

362 First, the models built with  $R_w(\lambda)$  show, as previously observed, better predictions  
363 for E141 than for E133, but, in overall, lower quality than in table 1. This confirms a  
364 different behavior of E133 and E141, but also that the sand particle size has an effect

365 in the quality of the predictions. A change in the physical structure of the samples  
366 usually leads to low prediction performances because of the scattering impact on the  
367 signal.

368 When built with the corrected spectra, again, the prediction of E133 highly improves,  
369 while the gain is less significant for E141, which is also consistent with the previous  
370 conclusions. But overall, the predictions are good, confirming that the corrected  
371 spectra, composed by the single scattered part of the total reflectance signal, becomes  
372 less dependent to physical changes in the sample.

373 The polarization subtraction method selects by optical means only, part of  
374 information related to the powdered absorbers concentration, while discarding the  
375 unwanted effect of multi-scattering on the signal. The measured signal becomes less  
376 dependent of the particle size changes of the samples and therefore improves both  
377 quality and robustness of the prediction models.

378

## 379 **5. Conclusion**

380 This study demonstrates the effectiveness of the polarized light subtraction method,  
381 applied to a two component model powder system, which improves the performance  
382 of multivariate calibration models.

383 By selecting only the light which has conserved the initial polarization and therefore  
384 being less impacted by scattering events, the collected photons all have the same  
385 mean free pathlength. As a consequence, the linear relationship between the spectra  
386 and the absorbers concentration is restored.

387 Then it is possible, by using Linear Unmixing to recover the pure spectra of the dyes.  
388 These recovered spectra are corrected from the physical interactions occurring in the  
389 mixture.

390 When the corrected spectra are used to build the PLS models, all the general quality  
391 parameters and the parsimony improve, especially for highly scattering media.  
392 Although the overall signal intensity is reduced after optical correction, the  
393 remaining information in the corrected signal is sufficient and of better quality to  
394 build a good prediction model, thus meaning that the signal sensitivity increases.  
395 Inevitably there is a trade-off between making more accurate measurements and a  
396 reduction of SNR.

397 After the polarization correction, the measured signal becomes less dependent to  
398 physical changes (particle sizes) which also improve the robustness of the prediction  
399 models.

400 This "plug and play" optical method offers the potential to be easy to implement to a  
401 commercial spectrophotometry system and does not significantly increase the  
402 measurement time.

403

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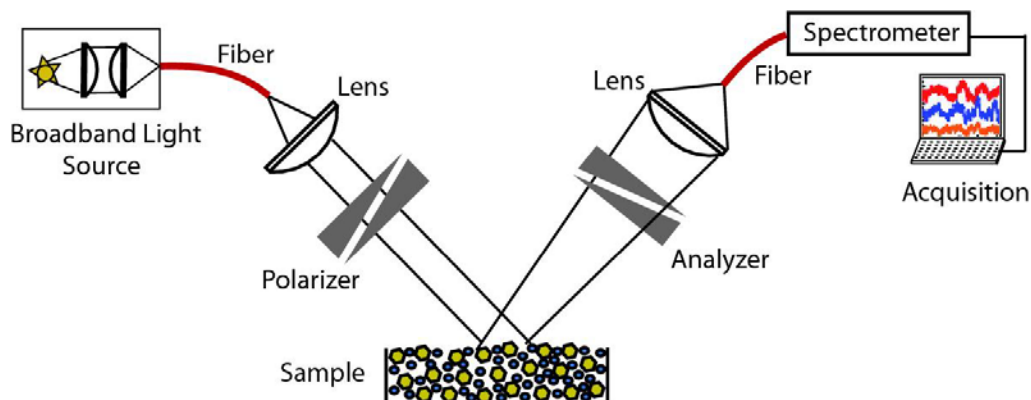


Figure 1: Schematic diagram of polarized light spectroscopy system.

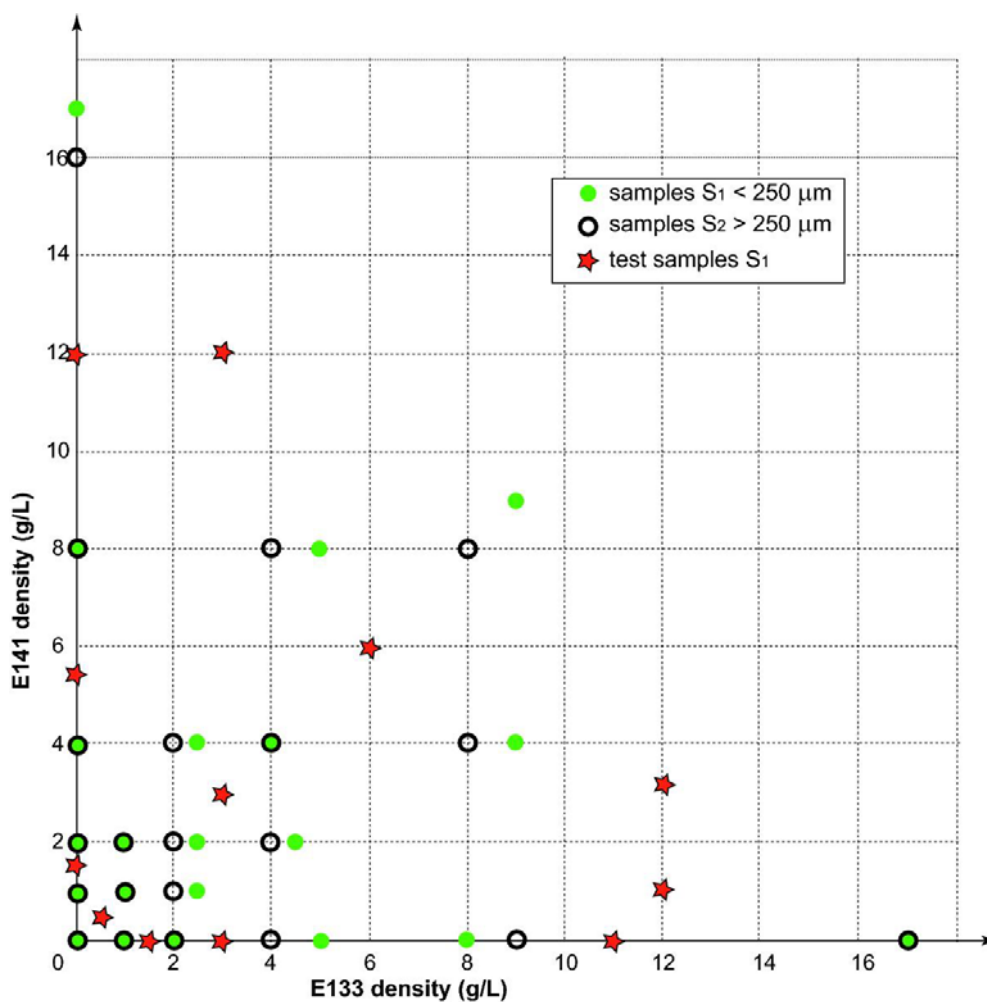
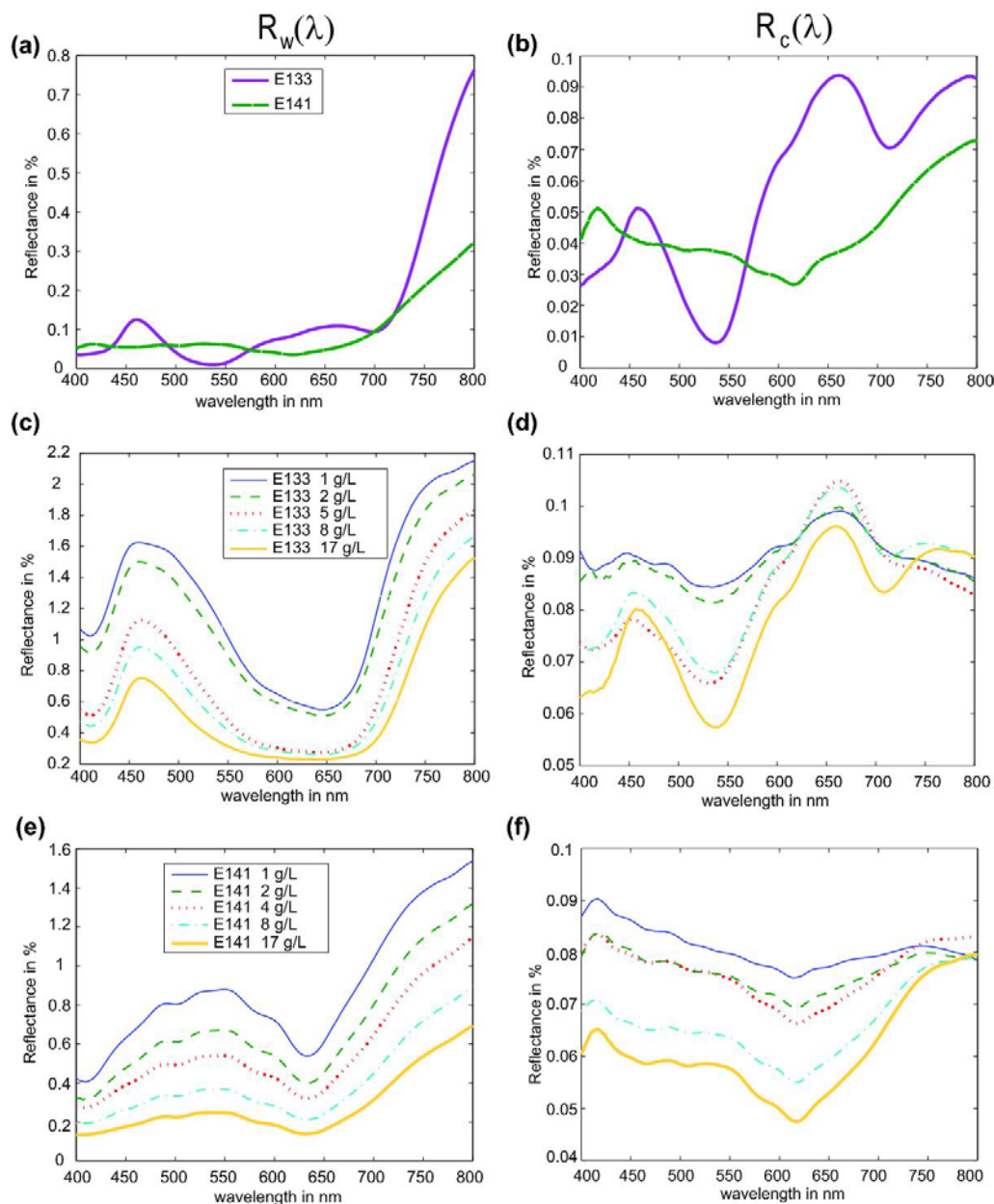


Figure 2: Experimental design presenting the dye densities in  $\text{g.L}^{-1}$  of 42 samples for the calibration set and 12 samples for the independent test set.





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466 Figure 3: (a) Raw reflectance spectra of coloring powder E133 and E141. (b)  
467 Corrected reflectance spectra of coloring powder E133 and E141 (c) Raw  
468 reflectance spectra of sand  $S_1$  + coloring powder E133 mixed at different densities.  
469 (d) Corrected reflectance spectra of sand  $S_1$  + coloring powders E133 mixed at  
470 different densities.(e) Raw reflectance spectra of sand  $S_1$  + coloring powder E141  
471 mixed at different densities.(f) Corrected reflectance spectra of sand  $S_1$  + coloring  
472 powders E141 mixed at different densities.  
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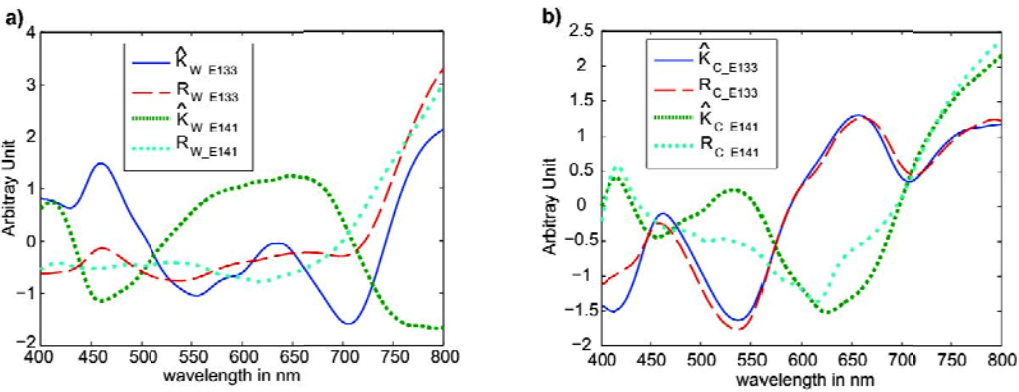


Figure 4 : Comparison of the raw and the corrected spectra acquired on the two coloring powders ( $R_{W\_E133}(\lambda)$ ,  $R_{W\_E141}(\lambda)$  and  $R_{C\_E133}(\lambda)$ ,  $R_{C\_E141}(\lambda)$ ) with the demixed pure spectrum ( $K_{W\_E133}(\lambda)$ ,  $K_{W\_E141}(\lambda)$  and  $K_{C\_E133}(\lambda)$ ,  $K_{C\_E141}(\lambda)$ ) extracted respectively from ( $\mathbf{R}_w$ ) and ( $\mathbf{R}_c$ ) with Linear unmixing.

Table 1: Figure of merit of the calibration models

	Cal set (n)	Test set (n)	Spectra	Predicted absorber	PLS factors	R <sup>2</sup>	SEPC (% g.L <sup>-1</sup> )
General model	S <sub>1</sub> +S <sub>2</sub> (42)	S <sub>1</sub> (12)	$\mathbf{R}_w$	E133	8	0.75	2.52
				E141	5	0.91	1.3
			$\mathbf{R}_c$	E133	5	0.91	1.41
				E141	4	0.93	1.12

Table 2: Figure of merit of the calibration model built with samples of one particle size (S<sub>2</sub>) and tested on samples with another particle size (S<sub>1</sub>)

	Cal set (n)	Test set (n)	Spectra	Predicted absorber	PLS factors	R <sup>2</sup>	SEPC (% g.L <sup>-1</sup> )
General model	S <sub>2</sub> (21)	S <sub>1</sub> (12)	$\mathbf{R}_w$	E133	5	0.69	3.33
				E141	5	0.83	1.79
			$\mathbf{R}_c$	E133	4	0.91	1.72
				E141	3	0.93	1.73