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Inconsistency Robustness for Logic Programs

Carl Hewitt

This article is dedicated to Alonzo Church and Stanislaw Jaśkowski

Abstract

This article explores the role of Inconsistency Robustness in the history and theory of Logic Programs. Inconsistency Robustness has been a continually recurring issue in Logic Programs from the beginning including Church's system developed in the early 1930s based on *partial* functions (defined in the lambda calculus) that he thought would allow development of a general logic without the kind of paradoxes that had plagued earlier efforts by Frege, *etc.*¹

Planner [Hewitt 1969, 1971] was a kind of hybrid between the procedural and logical paradigms in that it featured a procedural embedding of logical sentences in that an implication of the form (*p implies q*) can be procedurally embedded in the following ways:

Forward chaining

- **When asserted *p*, Assert *q***
- **When asserted $\neg q$, Assert $\neg p$**

Backward chaining

- **When goal *q*, SetGoal *p***
- **When goal $\neg p$, SetGoal $\neg q$**

Developments by different research groups in the fall of 1972 gave rise to a controversy over Logic Programs that persists to this day in the form of following alternatives:

1. **Procedural Interpretation:** Logic Programs using *procedural interpretation of logic-clause syntax for a program*ⁱ [Kowalski 2014]
2. **Procedural Embedding:** Logic Program in which *each computational step*ⁱⁱ is *logically inferred*ⁱⁱⁱ

ⁱ a Logic Program is written as $\Psi \Leftarrow (\Phi_1 \wedge \dots \wedge \Phi_n)$, which is logically equivalent to the disjunctive clause $\Psi \vee \neg \Phi_1 \vee \dots \vee \neg \Phi_n$ where Ψ and each of the Φ_i is either $P[t_1, \dots, t_m]$ or $\neg P[t_1, \dots, t_m]$ for some atomic predicate P and terms t_j .

ⁱⁱ *e.g.*, using the Actor Model of computation

ⁱⁱⁱ *e.g.*, using Direct Logic

This article argues for the second alternative based on the following considerations:

- Programs in logic-clause syntax are a special case of the second alternative because each computational step of a program in logic-clause syntax is logically inferred as backward chaining or forward chaining.
- Reducing propositions to logic-clause syntax can obscure their natural structure.
- Procedural interpretation of logic-clause syntax can obscure the natural structure of derivations.¹

Logic-clause syntax is far too limited to be of use for general Logic Programs.

Kowalski advocates a bold thesis: “*Looking back on our early discoveries, I value most the discovery that computation could be subsumed by deduction.*”² (Roman numeral superscripts in text are endnotes at the end of this article.)

However, mathematical logic cannot always infer computational steps because computational systems make use of arbitration for determining which message is processed next. Since reception orders are in general indeterminate, they cannot be inferred from prior information by mathematical logic alone. Therefore mathematical logic alone cannot in general implement computation. Logic Programs (like Functional Programs) are useful idioms even though they are not universal. For example Logic Programs can provide useful principles and methods for systems which are quasi-commutative and quasi-monotonic even though the systems themselves cannot be implemented using Logic Programs.

A fundamental principle of Inconsistency Robustness is to make contradictions explicit so that arguments for and against propositions can be formalized. In the Inconsistency Robustness paradigm, deriving contradictions is a progressive development and contradictions are not “game stoppers” that they would be using classical logic (in which reasoning about inconsistent information can make erroneous inferences). Contradictions can be helpful instead of being something to be “swept under the rug” by denying their existence or fruitlessly attempting complete elimination in systems of practice that are pervasively inconsistent.³

A contradiction is manifest when both a proposition and its negation are asserted even if by different parties, *e.g.*, New York Times said “*Snowden is a whistleblower.*”, but NSA said “*Snowden is not a whistleblower.*”⁴

¹ *e.g.*, Natural Deduction using Direct Logic

This paper explores the role of Inconsistency Robustness in the development and theory of Logic Programs, which is an interesting test case involving pervasive inconsistency in an area in which, traditionally, inconsistency was not supposed to occur.

Inconsistency Robustness

In this article, boxes like this one are used below to call out instances of inconsistency robustness.

Uniform Proof Procedures based on Resolution

By this it appears how necessary it is for nay man that aspires to true knowledge to examine the definitions of former authors; and either to correct them, where they are negligently set down, or to make them himself. For the errors of definitions multiply themselves, according as the reckoning proceeds, and lead men into absurdities, which at last they see, but cannot avoid, without reckoning anew from the beginning; in which lies the foundation of their errors...

[Hobbes *Leviathan*, Chapter 4]⁵

An important limitation of classical logic for inconsistent theories is that it supports the principle that from an inconsistency anything and everything can be inferred, e.g. “*The moon is made of green cheese.*”

For convenience, I have given the above principle the name IGOR⁶ for Inconsistency in Garbage Out Redux. IGOR can be formalized as follows in which a contradiction about a proposition Φ infers any proposition Ψ ,ⁱ i.e., $\Phi, \neg\Phi \vdash \Psi$.

Of course, IGOR *cannot* be part of inconsistency-robust logic because it allows *every* proposition to be inferred from a contradiction.

ⁱ Using the symbol \vdash to mean “infers in classical mathematical logic.” The symbol was first published in [Frege 1879].

The IGOR principle of classical logic may not seem very intuitive! So why is it included in classical logic?

- **Classical Proof by Contradiction:** $(\Psi \vdash \Phi, \neg\Phi) \Rightarrow (\vdash \neg\Psi)$, which can be justified in classical logic on the grounds that if Ψ infers a contradiction in a consistent theory then Ψ must be false. In an inconsistent theory. Classical Proof by Contradiction leads to explosion by the following proof in classical logic by which a contradiction about P infers any proposition Θ :

$$\underline{P, \neg P} \vdash \underline{\neg\Theta} \vdash \underline{P, \neg P} \vdash (\neg\neg\Theta) \vdash \Theta$$

- **Classical Contrapositive for Inference:** $(\Psi \vdash \Phi) \Rightarrow (\neg\Phi \vdash \neg\Psi)$, which can be justified in classical logic on the grounds that if $\Psi \vdash \Phi$, then if Φ is false then Ψ must be false. In an inconsistent theory. Classical Contrapositive for Inference leads to explosion by the following proof in classical logic by which a contradiction about P (*i.e.*, $\vdash P, \neg P$) infers any proposition Θ by the following proof:

Since $\vdash P, \neg\Theta \vdash P$ by monotonicity. Therefore $\neg P \vdash \Theta$ by Classical Contrapositive for Inference. Consequently $P, \neg P \vdash \Theta$.

- **Classical Extraneous \vee Introduction:**⁷ $\Psi \vdash (\Psi \vee \Phi)$, which in classical logic says that if Ψ is true then $\Psi \vee \Phi$ is true regardless of whether Φ is true.⁸ In an inconsistent theory, Extraneous \vee introduction leads to explosion via the following proof in classical logic in which a contradiction about P infers any proposition Θ :

$$\underline{P, \neg P} \vdash (\underline{P \vee \Theta}), \underline{\neg P} \vdash \Theta$$

- **Classical Excluded Middle:** $\vdash (\Psi \vee \neg\Psi)$, which in classical logic says that $\Psi \vee \neg\Psi$ is true regardless of whether Ψ is true. *Excluded Middle* is the principle of Classical Logic that for every proposition X the following holds: $\text{ExcludedMiddle}[X] \equiv X \vee \neg X$. However, Excluded Middle is not suitable for inconsistency-robust logic because it is equivalentⁱ to saying that there are no inconsistencies, *i.e.*, for every proposition X,

$$\text{Noncontradiction}[X] \equiv \neg(X \wedge \neg X)$$

Using propositional equivalences, note that

$$\text{ExcludedMiddle}[\Phi \vee \Psi] \Leftrightarrow (\Psi \vee \neg\Psi \vee \Phi) \wedge (\Phi \vee \neg\Phi \vee \Psi)$$

Consequently, $\text{ExcludedMiddle}[\Phi \vee \Psi] \Rightarrow (\Psi \vee \neg\Psi \vee \Phi)$, which means that the principle of Excluded Middle implies $\Psi \vee \neg\Psi \vee \Phi$ for all propositions Ψ and Φ . Thus the principle of Excluded Middle is not inconsistency robust because it implies every proposition Φ can be proved⁹ given any contradiction Ψ . [Kao 2011]

ⁱ using propositional equivalences

Classical Logic is unsafe for use with potentially inconsistent information.¹⁰

[Robinson 1965] developed a deduction method called resolution which was proposed as a uniform proof procedure using first-order logic for proving theorems which

Converted everything to clausal form and then used a method analogous to modus ponens to attempt to obtain a contradiction by adding the negation of the proposition to be proved.

Resolution uniform proof procedures were used to generate some simple proofs [Wos, et. al. 1965; Green 1969; Waldinger and Lee 1969; Anderson and Bledsoe 1970; *etc.*]. In the resolution uniform proof procedure theorem proving paradigm, the use of procedural knowledge was considered to be “*cheating.*”¹¹

Kowalski (also see [Decker 2003, 2005, 2010]) advocates that inference for inconsistent information systems¹² be performed using resolution theorem proving.¹³ Unfortunately, in the presence of inconsistent information, resolution theorem provers can prove propositions using invalid arguments.

For example, consider the following illustration:ⁱ

A resolution theorem prover proved $\Psi \vee \Phi$ and as a consequence it was added to the information system. Sometime afterward, another resolution theorem prover proved Φ making use of the previously proved $\Psi \vee \Phi$. Unfortunately, Φ was proved by resolution theorem proving using an invalid argument because¹⁴

- The first resolution theorem prover proved $\Psi \vee \Phi$ becauseⁱⁱ $\vdash \Psi$ ⁱⁱⁱ where Ψ holding has no bearing^{iv} on whether Φ holds.^v
- Using an invalid argument,^{vi} the second resolution theorem proved Φ using the previously proved $\Psi \vee \Phi$ because^{vii} $\vdash \neg \Psi$ ^{viii}.

The above illustration illustrates how resolution theorem proving can prove propositions^{ix} using invalid arguments.

For a large information base Ω of theories of practice (*e.g.*, a climate models, theories of the human brain, etc.), Kowalski advocates use of the resolution set of support strategy¹⁵ as follows: In proving a proposition Φ , the set of support strategy chooses resolutions involving resolving $\neg \Phi$ with Ω and resolving the resulting clauses with each other and with $\neg \Phi$.¹⁶

ⁱ The illustration below is presented in general terms for simplicity of exposition because presenting a detailed example involves significant complexity with lots of irrelevant details. An important point is that resolution theorem provers rely on overlap of vocabulary in deciding on which propositions to resolve. Consequently, they can become entangled in irrelevancy when deriving a contradiction when two propositions (having no bearing on whether the other holds) share vocabulary.

ⁱⁱ unknown to the resolution theorem prover

ⁱⁱⁱ even though the resolution theorem prover could *not* prove Ψ in the time that it took to prove $\Psi \vee \Phi$

^{iv} unknown to the resolution theorem prover although Ψ and Φ have some common vocabulary, which can lead a resolution theorem prover astray

^v Unfortunately, the following rule of classical logic is not inconsistency robust: $\Psi \vdash \Psi \vee \Phi$. However, a resolution theorem prove must honor *all* of the rules of classical logic.

^{vi} because the resolution theorem provers unknowingly used $\vdash \Psi, \neg \Psi$ as the basis for the proof of Φ although Ψ holding has no bearing on Φ holding even though they have some common vocabulary

^{vii} unknown to the resolution theorem prover

^{viii} even though the resolution theorem prover could *not* prove $\neg \Psi$ in the time that it took to prove Φ

^{ix} for pervasively inconsistent information systems of practice, *e.g.*, theories for climate change and the human brain

Any proposition X can be provedⁱ by interacting with a resolution theorem proverⁱⁱ from an information base containing propositions \mathcal{G} and $\neg\mathcal{G}$ ⁱⁱⁱ as follows:

- 1) $\mathcal{G} \vdash_{\text{setOfSupport}} (\mathcal{G} \vee X)$ because $\mathcal{G}, \underline{\neg(\mathcal{G} \vee X)} \vdash_{\text{ResolutionTheoremProver}} \text{False}$ ^{iv}
- 2) $\mathcal{G} \vee X, \neg\mathcal{G} \vdash_{\text{setOfSupport}} X$ because $\mathcal{G} \vee X, \neg\mathcal{G}, \underline{\neg X} \vdash_{\text{ResolutionTheoremProver}} \text{False}$ ^v
- 3) A resolution theorem prover *using set of support* working on an information base containing both \mathcal{G} and $\neg\mathcal{G}$ can be used to first prove $\mathcal{G} \vee X$ using **1)** and then can be used to prove X using **2)**.

Direct Logic was developed to address limitations¹⁷ of classical logic as a foundation for Computer Science:

- Classical Direct Logic is intended to be thought to be consistent by an overwhelming consensus of working professional mathematicians. See [Hewitt 2013] for discussion of Classical Direct Logic.
- Inconsistency Robust Direct Logic is for pervasively inconsistent theories of practice, e.g., theories for climate modeling and for modeling the human brain. Classical Direct Logic can be freely used in theories of Inconsistency Robust Direct Logic. See [Hewitt 2010] for discussion of Inconsistency Robust Direct Logic.

Inconsistency Robust Direct Logic is the state of the art for possibly inconsistent information.^{vi} However, enforcing the constraint that a resolution theorem prover use only the rules of Inconsistency Robust Direct Logic is inefficient as well as extraordinarily complicated and awkward. Consequently, resolution theorem provers are unsuitable for inconsistency robust reasoning.

ⁱ using an invalid argument because it used inconsistent assumptions

ⁱⁱ using the set of support strategy

ⁱⁱⁱ a resolution theorem prover using set of support might not realize that \mathcal{G} and $\neg\mathcal{G}$ are inconsistent because if they are not in the set of support, they will not be resolved and it might not be immediately apparent from their clausal forms that they are inconsistent.

^{iv} set of support is underlined

^v set of support is underlined

^{vi} Many other paraconsistent logics have been proposed that are partially inconsistency robust.

Inconsistency Robustness: Resolution

Using resolution as the only rule of inference is problematical because it can obscure the natural structure of propositions and the natural structure of derivations using Natural Deduction. Also, Resolution Theorem Proving can prove propositions using invalid arguments for systems of practice because of pervasive inconsistencies.

Procedural Embedding redux

In the late 1960's, the two major paradigms for constructing semantics software systems were procedural and logical. The procedural paradigm was epitomized by Lisp [McCarthy *et. al.* 1962] which featured recursive procedures that operated on list structures including property lists that were updated imperatively. The logical paradigm was epitomized by uniform Resolution Theorem Provers [Robinson 1965].

Planner

Inconsistency Robustness: Uniform Proof Procedures

Uniform proof procedures using resolution was intended be a general theorem proving paradigm. But it suffered immense inefficiency in practice. Changing an axiomatization to improve performance was considered to be "cheating."

Planner [Hewitt 1969, 1971] was a kind of hybrid between the procedural and logical paradigms in that it featured a procedural embedding of logical sentences in that an implication of the form (p *implies* q) can be procedurally embedded in the following ways:ⁱ

Forward chaining

- **When asserted** p , **Assert** q
- **When asserted** $\neg q$, **Assert** $\neg p$

Backward chaining

- **When goal** q , **SetGoal** p
- **When goal** $\neg p$, **SetGoal** $\neg q$

ⁱ In modern notation [see appendix of this paper]:

Forward chaining

When $\vdash \Psi \rightarrow \vdash \Phi$

When $\vdash \neg \Phi \rightarrow \vdash \neg \Psi$

Backward chaining

When $\Vdash \Phi \rightarrow \Vdash \Psi$

When $\Vdash \neg \Psi \rightarrow \Vdash \neg \Phi$

Planner was the first programming language based on using explicit assertions and goals processed using pattern-directed invocation. The development of Planner was inspired by the work of Jaśkowski [1934], Newell and Simon [1956], McCarthy [1958], McCarthy *et. al.* [1962], Minsky [1958], Polya [1954], and Popper [1935, 1963].

Planner represented a rejection of the resolution uniform proof procedure paradigm in favor of Procedural Embedding making use of new program language constructs¹⁸ for computation including using explicit assertions and goals that invoked programs.

A subset called Micro-Planner was implemented by Gerry Sussman, Eugene Charniak and Terry Winograd as an extension to Lisp primarily for pragmatic reasons since it saved memory space and processing time (both of which were scarce) by comparison with more general problem solving techniques, *e.g.*, [Polya 1957]:

- Lisp was well suited to the implementation of a Micro-Planner interpreter.
- The full functionality of Lisp libraries were immediately available for use by Micro-Planner programs.
- The Lisp compiler could be used to compile Lisp programs used by Micro-Planner applications to make them smaller and run faster. (It was unnecessary to first implement a Micro-Planner compiler.)

Computers were expensive. They had only a single slow processor and their memories were very small by comparison with today. So Planner adopted some efficiency expedients including the following:ⁱ

- Backtracking [Golomb and Baumert 1965] was adopted to economize on the use of time and storage by working on and storing only one possibility at a time in exploring alternatives. In several ways, backtracking proved unwieldy helping to fuel the great control structure debate. Hewitt investigated some preliminary alternatives in his thesis.
- A unique name assumption was adopted by assuming that different names referred to different objects, which saved space and time. For example names like Peking and Beijing were assumed to refer to different objects.
- A closed world assumption could be implemented by conditionally testing whether an attempt to prove a goal exhaustively failed. Later this capability was given the misleading name “negation as failure” because for a goal G it was possible to say: “if attempting to achieve G exhaustively fails then assert (*Not* G).”ⁱⁱ

ⁱ Prolog later also adopted these same efficiency expedients.

ⁱⁱ satirized as “*the less that can proved, the more that can be assumed!*”

- Being a hybrid language, Micro Planner had two different syntaxes, variable binding mechanisms, etc. So it lacked a certain degree of elegance. In fact, after Hewitt's lecture at IJCAI'71, Allen Newell rose from the audience to remark on the lack of elegance in the language! However, variants of this syntax have persisted to the present day.

Micro-Planner was used in Winograd's natural-language understanding program SHRDLU [Winograd 1971], Eugene Charniak's story understanding work, work on legal reasoning [McCarty 1977], and some other projects. This generated a great deal of excitement in the field of Artificial Intelligence.

Inconsistency Robustness: Procedural Embedding

Planner was designed as a program language for Procedural Embedding. However, efficiency expedients were made in its implementation that unfortunately resulted in inflexible problem solving strategies as well as awkward, limited reasoning capabilities.

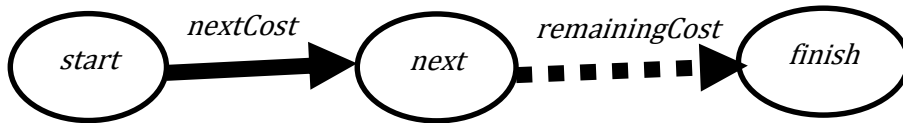
Although Winograd made an impressive demo, the successors of Planner and SHRDLU were incapable of practically realizing Procedural Embedding because of limited hardware performance and lack of effective software frameworks and tooling. Because of decades of subsequent progress, it has become feasible to develop practical, principled systems for Procedural Embedding.

Logic Programs in ActorScript are a further development of Planner. For example, suppose there is a ground-complete predicate¹⁹ `Link[aNode, anotherNode, aCost]` that is true exactly when there is a path from `aNode` to `anotherNode` with `aCost`.

```
When  $\vdash$  Path[aNode, aNode, aCost]  $\rightarrow$ 
    // when a goal is set for a cost between aNode and itself
     $\vdash$  aCost=0  $\mid$  // assert that the cost from a node to itself is 0
```

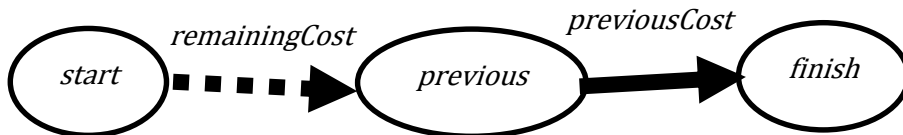
The following goal-driven Logic Program works forward from `start` to find the cost to `finish`:²⁰

```
When  $\vdash$  Path[start, finish, aCost]  $\rightarrow$ 
     $\vdash$  aCost=Minimum {nextCost + remainingCost
        |  $\vdash$  Link[start, next $\neq$ start, nextCost],
        Path[next, finish, remainingCost]}  $\mid$ 
    // a cost from start to finish is the minimum of the set of the sum of the
    // cost for the next node after start and
    // the cost from that node to finish
```



The following goal-driven Logic Program works backward from `finish` to find the cost from `start`:

```
When  $\vdash$  Path[start, finish, aCost]  $\rightarrow$ 
     $\vdash$  aCost= Minimum {remainingCost + previousCost
        |  $\vdash$  Link[previous $\neq$ finish, finish, previousCost],
        Path[start, previous, remainingCost]}  $\mid$ 
    // the cost from start to finish is the minimum of the set of the sum of the
    // cost for the previous node before finish and
    // the cost from start to that Node
```



Note that the above Logic Programs work together concurrently providing information to each other.

Control Structure Controversies

Peter Landin introduced a powerful co-routine control structure using his J (for Jump) operator that could perform a nonlocal goto into the middle of a procedure invocation [Landin 1965]. In fact the J operator enabled a program to jump back into the middle of a procedure invocation even after it had already returned!

Drew McDermott and Gerry Sussman called Landin's concept “*Hairy Control Structure*” and used it in the form of a nonlocal goto for the Conniver program language [McDermott and Sussman 1972]. Hewitt and others were skeptical about hairy control structure. Pat Hayes [1974] remarked: *Their* [Sussman and McDermott] *solution, to give the user access to the implementation primitives of Planner, is however, something of a retrograde step (what are Conniver's semantics?)*

The difficulties using backtracking in Planner and Conniver were useful in that they provoked further research into control structures for procedural embedding.

Inconsistency Robustness: Control Structures

There was there germ of a good idea (previously emphasized in Polya [1957] and “progressive deepening” [de Groot 1965]) in Conniver; namely, using co-routines to computationally shift focus to another branch of investigation while keeping alive the one that has been left Scott Fahlman used this capability of Conniver to good effect in his planning system for robot construction tasks [Fahlman 1973] to introduce a set of higher-level control and communications operations for its domain. However, the ability to jump back into the middle of procedure invocations seemed awkward and confusing. Hairy Control Structure didn't seem to be what was needed as the foundation to solve the difficulties in communication that were a root cause of the control structure difficulties.

Control structures are patterns of passing messages

In November 1972. Alan Kay visited MIT and gave an inspiring lecture that explained some of his ideas for Smalltalk-72 building on the message-passing of Planner, Simula [Dahl and Nygaard 1967] as well as the Logo work of Seymour Papert with the “little person” model of computation used for teaching children to program (*cf.* [Whalley 2006]).

The Actor model [Hewitt, Bishop, and Steiger 1973] was a new model of computation that differed from previous models of computation in that it was

grounded by the laws of physics so that it could be completely general in terms of control structure.²¹ It took some time to develop practical program languages for the Actor model.

Work on Planner was temporarily suspended in favor of intensive investigation of the Actor model.¹

Inconsistency Robustness: Message Passing

Planner aimed to extend what could be programmed using logical methods but did not take a stand about the theoretical limits of these methods. However, once the Actor model was invented in late 1972, it became clear that logical inference alone would not suffice for computation because the order of Actor message reception could not always be logically inferred.

[Hewitt 1976] reported

... we have found that we can do without the paraphernalia of "hairy control structure" (such as possibility lists, non-local gotos, and assignments of values to the internal variables of other procedures in CONNIVER.)... The conventions of ordinary message-passing seem to provide a better structured, more intuitive foundation for constructing the communication systems needed for expert problem-solving modules to cooperate effectively. (emphasis in original)

Edinburgh Logic for Computable Functions

Like Planner,²² Edinburgh Logic for Computable Functions [Milner 1972; Gordon, Milner, and Wadsworth 1979] was capable of both forward chaining as well as backward chaining. This was accomplished by a purely functional program operating on a special data type called "Theorem" to produce new theorems by forward and backward chaining. Sub-goaling strategies (called tactics) were represented as higher-order functions taking strategies as arguments and returning them as results with goal failure implemented using exceptions.

Inconsistency Robustness: Logic for Computable Functions

Edinburgh Logic for Computable Functions was a notable advance in that its logical soundness was guaranteed by the type system. However, its problem solving generality is limited since it was not concurrent because it was purely functional.

¹ Work on Logic Programs later resumed in the Scientific Community Model [see section below].

Procedural Embedding versus Procedural Interpretation of Logic-clause Syntax

At Edinburgh, Pat Hayes and Bob Kowalski collaborated on resolution theorem proving. Then Hayes visited Stanford where Bruce Baumgart published his *Micro-Planner Alternate Reference Manual* in April 1972. Hayes says that from the time that he learned about Micro-Planner it seemed obvious to him that it was based on controlled deduction.²³

When he returned to Edinburgh, he talked about his insight with anyone who would listen and gave internal seminars at two of the major departments at Edinburgh concerned with logic. In the third department, Hayes point seemed irrelevant because they were busy getting their hands on the latest “magic machinery” for controlling reasoning using Popler [Davies 1973], a derivative of Planner. Hayes wrote a joint paper with Bruce Anderson on “*The Logicians Folly*” against the resolution uniform proof procedure paradigm [Anderson and Hayes 1972].

Gerry Sussman and Seymour Papert visited Edinburgh spreading the news about Micro-Planner and SHRDLU casting doubt on the resolution uniform proof procedure approach that had been the mainstay of the Edinburgh Logicians. According to Maarten van Emden [2006]

The run-up to the workshop [Machine Intelligence 6 organized by Donald Michie in 1970] was enlivened by telegrams from Seymour Papert at MIT announcing on alternating days that he was (was not) coming to deliver his paper entitled "The Irrelevance of Resolution", a situation that caused Michie to mutter something about the relevance of irresolution. The upshot was that a student named Gerry Sussman appeared at the appointed time. It looked as if this was going to be his first talk outside MIT. His nervousness was compounded by the fact that he had been instructed to go into the very bastion of resolution theorem proving and tell the assembled experts how totally misguided they were in trying to get anything relevant to AI with their chosen approach.

I had only the vaguest idea what all this was about. For me theorem proving was one of the things that some people (including Kowalski) did, and I was there for the programming. If Bob and I had anything in common, it was search. Accordingly I skipped the historic Sussman lecture and arrived late for the talk scheduled to come after Sussman's. Instead, I found an unknown gentleman lecturing from a seat in the audience in, what I thought a very English voice. It turned out that a taxi from the airport had delivered Seymour Papert after all, just in time for the end of Sussman's lecture, which was now being re-done properly by the man himself.

The effect on the resolution people in Edinburgh of this frontal assault was traumatic. For nobody more so than for Bob Kowalski. Of course there was no shortage of counter objections, and the ad hoc creations of

MIT were not a pretty sight. But the occasion hit hard because there was a sense that these barbarians had a point.

The above developments generated tension among the Logicians at Edinburgh. These tensions were exacerbated when the UK Science Research Council commissioned Sir James Lighthill to write a report on the AI research situation. The resulting report [Lighthill 1973; McCarthy 1973] was highly critical although SHRDLU [Winograd 1971] was favorably mentioned. “Resolution theorem-proving was demoted from a hot topic to a relic of the misguided past. Bob [Kowalski] doggedly stuck to his faith in the potential of resolution theorem proving. He carefully studied Planner.” [Bruynooghe, Pereira, Siekmann, and van Emden 2004]

van Emden [2006] recalled:

Kowalski's apparent research program narrowed to showing that the failings so far of resolution inference were not inherent in the basic mechanism. He took great pains to carefully study PLANNER and CONNIVER. And painful it was. One of the features of the MIT work was that it assumed the audience consisted of LISP programmers. For anybody outside this circle (Kowalski most definitely was not a LISP programmer), the flavour is repellent.

According to [Kowalski 2014]

Pat Hayes and I had been working in Edinburgh on a book [Hayes and Kowalski, 1971] about resolution theorem-proving, when he returned from a second visit to Stanford (after the first visit, during which he and John McCarthy wrote the famous situation calculus paper [McCarthy and Hayes, 1968]). He was greatly impressed by Planner, and wanted to rewrite the book to take Planner into account. I was not enthusiastic, and we spent many hours discussing and arguing about the relationship between Planner and resolution theorem proving. Eventually, we abandoned the book, unable to agree.

In the fall of 1972 at MIT, there was universal dissatisfaction with the adequacy of micro-Planner. Consequently, to further the development of Procedural Embedding, the Actor Model was invented, which provided a rigorous basis for defining both:

- *Functional Program:* Actors do not change
- *Logic Program:* Each computational step is logically inferred.

Hayes reported that he was astonished when Kowalski wrote back from Marseilles saying that he and Colmerauer had a revolutionary idea that Horn clauses could be interpreted as backward-chaining programs. Feeling that his ideas were being unfairly appropriated by Kowalski, Hayes complained to the head of their unit Bernard Meltzer and still feeling unsatisfied wrote a summary and exegesis of his ideas in a paper for the proceedings of a summer

school in Czechoslovakia with the idea of recording the priority of his ideas [Hayes 1973].

However, Kowalski felt that his work with Colmerauer bore little resemblance to anything that had been discussed previously in Edinburgh by Hayes claiming that Hayes' ideas (and the paper that he published) were based on using equations for computation (in the spirit of the work in Aberdeen [Foster and Elcock 1969]).

Kowalski [2008] recalled:

In the meanwhile, critics of the formal approach, based mainly at MIT, began to advocate procedural representations of knowledge, as superior to declarative, logic-based representations. This led to the development of the knowledge representation and problem-solving languages Planner and micro-Planner. Winograd's PhD thesis (1971), using micro-Planner to implement a natural language dialogue for a simple blocks world, was a major milestone of this approach. Research in automated theorem-proving, mainly based on resolution, went into sharp decline.

The battlefield between the logic-based and procedural approaches moved briefly to Edinburgh during the summer of 1970 at one of the Machine Intelligence Workshops organized by Donald Michie (van Emden, 2006). At the workshop, Papert and Sussman from MIT gave talks vigorously attacking the use logic in AI, but did not present a paper for the proceedings. This created turmoil among researchers in Edinburgh working in resolution theorem-proving. However, I was not convinced that the procedural approach was so different from the SL resolution system I had been developing with Donald Kuehner (1971).

During the next couple of years, I tried to reimplement Winograd's system in resolution logic and collaborated on this with Alain Colmerauer in Marseille. This led to the procedural interpretation of Horn clauses (Kowalski 1973/1974) and to Colmerauer's development of the programming language Prolog.

In the fall of 1972, *Prolog* (an abbreviation for “**PRO**grammation en **LOG**ique” (French for *programming in logic*)), was developed as a subset of micro-Planner that restricted programs to Horn-clause syntax¹ using backward chaining and consequently had a simpler more uniform syntax than Planner.²⁴ However, the restriction to Horn-clause syntax tremendously restricted the expressive power of Prolog.

¹ Horn-clause syntax for a logic program is of the form $\Psi \Leftarrow (\Phi_1 \wedge \dots \wedge \Phi_n)$ which is logically equivalent to the disjunctive clause $\Psi \vee \neg \Phi_1 \vee \dots \vee \neg \Phi_n$ where Ψ and each of the Φ_i is $P[t_1, \dots, t_n]$ for some atomic predicate P and terms t_i .

Like Planner, Prolog provided the following:

- An indexed data base of propositions (limited by Prolog to positive predicates with ground arguments) and pattern-directed backward-chaining procedures (limited by Prolog to Horn-clause syntax).
- The Unique Name Assumption, by means of which different names are assumed to refer to distinct entities, *e.g.*, Peking and Beijing are assumed to be different in order to save space and time.
- The Closed World Assumption (available and used in practice in micro-Planner to save space and time although it was not strictly required by micro-Planner).

Prolog was fundamentally different in intent from Planner as follows:

- Planner was designed for **Procedural Embedding using explicit goals and assertions processed by pattern-directed procedures**. *Correctness can be checked when an assertion is made that a proposition holds in a theory using a rule of inference*. Theories do not limit the problem solving methods that can be used.¹
- Prolog was designed a **backward-chaining interpretation of Horn-clause syntax**. Consequently, a goal established by a Prolog backward-chaining program was intended to be a logical consequence of the *propositional interpretation* of the Prolog program syntax *without any additional checking*. A theory expressed in Prolog limits the problem solving method that can be used to backward chaining of Horn-clause syntax programs whose propositional content is the Horn clauses²⁵ of the theory.

A number of Logic Program features of Micro-Planner were omitted from Prolog including the following:²⁶

- Using explicit assertions processed by pattern-directed procedures (*i.e.*, “forward chaining”)
- Logical negation, *e.g.*, (not (human Socrates))
- Explicit goals and subgoals that are distinct from assertions²⁷

In summary, Prolog was basically a subsetⁱⁱ of Planner that restricted programs to a backward chaining interpretation of Horn clauses.

ⁱ *e.g.*, the full range of techniques in [Polya 1957] should be available.

ⁱⁱ excepting that Prolog used unification instead of the pattern matching used in Planner. However, in practice unification is often partially turned off in Prolog programs (at the potential cost of incorrect results) because unification can be expensive.

According to [Kowalski 2014]:

“... it was widely believed that logic alone is inadequate for problem solving, and that some way of controlling the theorem-prover is needed for efficiency. Planner combined logic and control in a procedural representation that made it difficult to identify the logical component. Logic programs with SLD resolution also combine logic and control, but make it possible to read the same program both logically and procedurally. I later expressed this as Algorithm=Logic+Control ($A=L+C$) [Kowalski, 1979a], influenced by Pat Hayes' [1973] Computation=Controlled Deduction.

The most direct implication of the equation is that, given a fixed logical representation L , different algorithms can be obtained by applying different control strategies, i.e. $A_1=L+C_1$ and $A_2=L+C_2$. Pat Hayes [1973], in particular, argued that logic and control should be expressed in separate languages, with the logic component L providing a pure, declarative specification of the problem, and the control component C supplying the problem solving strategies needed for an efficient algorithm A . Moreover, he argued against the idea, expressed by $A_1=L_1+C$ and $A_2=L_2+C$, of using a fixed control strategy C , as in Prolog, and formulating the logic L_i the problem to obtain a desired algorithm A_i .”

[Hayes 1974] complained that procedural interpretation was “*alien semantics*” for logical propositions that was analogous to “... *throwing out the baby and keeping the bathwater*.” In other words, Hayes was arguing for Procedural Embedding as in Planner, whereas Kowalski was arguing for fixed control structure as in resolution uniform proof procedures.

Furthermore, there are concerns about the adequacy of logic-clauseⁱ syntax to express Logic Programs.

ⁱ Logic-clause syntax for a logic program is of the form $\Psi \leftarrow (\Phi_1 \wedge \dots \wedge \Phi_n)$ [logically equivalent to the disjunctive clause $\Psi \vee \neg \Phi_1 \vee \dots \vee \neg \Phi_n$] where Ψ is of the form $P[t_1, \dots, t_n]$ or the form $\neg P[t_1, \dots, t_n]$ for some atomic predicate P and terms t_i . (Logic-clause syntax is a slight generalization of Horn-clause syntax in that it allows predicates to be negated.)

Inconsistency Robustness: Expressiveness of Logic Programs

Procedural Embedding (starting with Planner) allows the distinction between propositions and programs:

- Propositional information does not have to be reformulated using logic-clause syntax (which can obscure the natural structure of propositions).
- Logic Programs can be more expressive and powerful when not restricted to logic-clause syntax. For example, Logic Programs in ActorScript use Natural Deduction.
- Procedural Embedding can implement problem solving methods that cannot be implemented using Logic Programs (see this article on “Is Computation Subsumed by Deduction?”)
- Assertions have provenance that justify their inference in a theory.

Scientific Community Model²⁸

Research on the Scientific Community Model [Kornfeld and Hewitt 1981, Kornfeld 1981]. involved the development of a program language named Ether that invoked procedural plans to process goals and assertions concurrently by dynamically creating new rules during program execution. Ether also addressed issues of conflict and contradiction with multiple sources of knowledge and multiple viewpoints.

The Scientific Community Model builds on the philosophy, history and sociology of science. It was originally developed building on work in the philosophy of science by Karl Popper and Imre Lakatos. In particular, it initially made use of Lakatos' work on proofs and refutations. Subsequently development has been influenced by the work of Geof Bowker, Michel Callon, Paul Feyerabend, Elihu M. Gerson, Bruno Latour, John Law, Karl Popper, Susan Leigh Star, Anselm Strauss, and Lucy Suchman.

In particular Latour's Science in Action had great influence. In the book, Janus figures make paradoxical statements about scientific development. An important challenge for the Scientific Community Model is to reconcile these paradoxical statements.

Scientific research depends critically on monotonicity, concurrency, commutativity, and pluralism to propose, modify, support, and oppose scientific methods, practices, and theories. Scientific Communities systems

have characteristics of monotonicity, concurrency, commutativity, pluralism, skepticism and provenance:

- **monotonicity**: Once something is published it cannot be undone. Scientists publish their results so they are available to all. Published work is collected and indexed in libraries. Scientists who change their mind can publish later articles contradicting earlier ones.
- **concurrency**: Scientists can work concurrently, overlapping in time and interacting with each other.
- **quasi-commutativity**: Publications can be read regardless of whether they initiate new research or become relevant to ongoing research. Scientists who become interested in a scientific question typically make an effort to find out if the answer has already been published. In addition they attempt to keep abreast of further developments as they continue their work.
- **pluralism**: Publications include heterogeneous, overlapping and possibly conflicting information. There is no central arbiter of truth in scientific communities.
- **skepticism**: Great effort is expended to test and validate current information and replace it with better information.
- **provenance**: The provenance of information is carefully tracked and recorded.

Inconsistency Robustness: Scientific Community Model

The above characteristics are limited in real scientific communities. Publications are sometimes lost or difficult to retrieve. Concurrency is limited by resources including personnel and funding. Sometimes it is easier to re-derive a result than to look it up. Scientists only have so much time and energy to read and try to understand the literature. Scientific fads sometimes sweep up almost everyone in a field. The order in which information is received can influence how it is processed. Sponsors can try to control scientific activities. In Ether the semantics of the kinds of activity described in this paragraph are governed by the Actor model.

Scientific research includes generating theories and processes for modifying, supporting, and opposing these theories. Karl Popper called the process "conjectures and refutations", which although expressing a core insight, has been shown to be too restrictive a characterization by the work of Michel Callon, Paul Feyerabend, Elihu M. Gerson, Mark Johnson, Thomas Kuhn, George Lakoff, Imre Lakatos, Bruno Latour, John Law, Susan Leigh Star, Anselm Strauss, Lucy Suchman, Ludwig Wittgenstein, etc.. Three basic kinds of participation in Ether are proposing, supporting, and opposing. Scientific communities are structured to support competition as well as cooperation.

These activities affect the adherence to approaches, theories, methods, etc. in scientific communities. Current adherence does not imply adherence for all future time. Later developments will modify and extend current understandings. Adherence is a local rather than a global phenomenon. No one speaks for the scientific community as a whole.

There are a number of controversies involved in the history of Logic Programs in which different researchers took contradictory positions that are addressed in following sections of this article including, "Is computation subsumed by deduction?" and "Did Prolog-style clause programs contribute to the failure of the Japanese Fifth Generation Project (ICOT)?" and "What is a Logic Program?"

Is Computation Subsumed by Deduction?

"...a single formalism suffices for both logic and computation, and logic subsumes computation."

[Kowalski 2014]

The challenge to the generality of Logic Programs as a foundation for computation was officially thrown in *The Challenge of Open Systems* [Hewitt 1985] to which [Kowalski 1988b] replied in *Logic-Based Open Systems*. This was followed up with [Hewitt and Agha 1988] in the context of the Japanese Fifth Generation Project (see section below). All of this was in opposition to Kowalski's thesis: “*Looking back on our early discoveries, I value most the discovery that computation could be subsumed by deduction.*”²⁹

In concrete terms, we cannot observe the internals of the mechanism by which the reception order of messages is determined. Attempting to do so affects the results and can even push the indeterminacy elsewhere. Instead of observing the internals of arbitration processes, we await outcomes. The reason that we await outcomes is that we have no alternative because of indeterminacy. Because of indeterminacy in the physical basis of computation, no kind of deductive mathematical logic can always infer which message will be received next and the resulting computational steps. Consequently, Logic Programs can make inferences about computation but not in general implement computation. Nevertheless, Logic Programs (like Functional Programs) can be a useful idiom.

Inconsistency Robustness: Universality of Deduction

Contrary to Kowalski, computation in general cannot be subsumed by deduction. Mathematical models of computation do not determine particular computations as follows: Arbiters can be used in the implementation of the reception order of messages, which are subject to indeterminacy. Since reception orders are in general indeterminate, they cannot be inferred from prior information by mathematical logic alone. Therefore mathematical logic alone cannot implement computation in open systems.

Actor systems can perform computations that are impossible by mathematical deduction as illustrated by the following nondeterministic Actor systemⁱ that can compute an integer of unbounded size implemented as follows using ActorScript™:

```

Unbounded.[ ]:Integer ≡
  Let aCounter ← Counter[ ]. // let aCounter be a new Counter
  □ aCounter.go[ ], // send aCounter a go message and concurrently
  □ aCounter.stop[ ]
  // return the value of sending aCounter a stop message

Actor Counter[ ]
  count := 0 // the variable count is initially 0
  continue := True. // the variable continue is initially True
  stop[ ]:Integer →
    count // return count
    afterward continue := false
    // continue is false for the next message received
  go[ ]:Void →
    continue ♦
    True: // if continue is True,
    Hole ..go[ ] // send go[ ] to this counter after
    afterward count := count+1
    // incrementing count
    False: Void // if continue is False, return Void

```

By the semantics of the Actor model of computation [Clinger 1981; Hewitt 2006], Unbounded.**[]** will result in computing an integer of unbounded size.

The procedure Unbounded above can be axiomatized as follows:

$$\begin{aligned}
& \forall [n:\mathbf{Integer}] \rightarrow \\
& \exists [aRequest:\mathbf{Request}, anInteger:\mathbf{Integer}] \rightarrow \\
& \text{Unbounded sent}_{aRequest} [] \Rightarrow \\
& \text{Sent}_{Response_{aRequest}} \text{Returned}[anInteger] \wedge anInteger > n
\end{aligned}$$

However, the above axiom does *not* compute any actual output! Instead the above axiom simply asserts the *existence* of unbounded outputs for Unbounded.**[]**.

ⁱ using the ActorScript programming language [Hewitt 2010a]

Theorem. The nondeterministic function defined by Unbounded (above) cannot be implemented by a nondeterministic Logic Programⁱ.

*Proof.*³⁰

The task of a nondeterministic Logic Program P is to start with an initial set of axioms and prove $\text{Output}=n$ for some numeral n . Now the set of proofs of P starting from initial axioms will form a tree. The branching points will correspond to the nondeterministic choice points in the program and the choices as to which rules of inference to apply. Since there are always only finitely many alternatives at each choice point, the branching factor of the tree is always finite. Now König's lemma says that if every branch of a finitary tree is finite, then so is the tree itself. In the present case this means that if every proof of P proves $\text{Output}=n$ for some numeral n , then there are only finitely many proofs. So if P nondeterministically proves $\text{Output}=n$ for every numeral n , it must contain a nonterminating computation in which it does not prove $\text{Output}=n$ for some numeral n .

The following arguments support unbounded nondeterminism in the Actor model [Hewitt 1985, 2006]:

- There is no bound that can be placed on how long it takes a computational circuit called an *arbiter* to settle. Arbiters are used in computers to deal with the circumstance that computer clocks operate asynchronously with input from outside, e.g., keyboard input, disk access, network input, etc. So it could take an unbounded time for a message sent to a computer to be received and in the meantime the computer could traverse an unbounded number of states.
- Electronic mail enables unbounded nondeterminism since mail can be stored on servers indefinitely before being delivered.
- Communication links to servers on the Internet can be out of service indefinitely.

ⁱ the lambda calculus is a special case of Logic Programs

The following Logic Programs procedurally embed information about Unbounded:

```

When  $\vdash$  aRequest anActor sent aMessage  $\rightarrow$ 
    // When asserted that anActor is sent aRequest with aMessage
     $\vdash$  aRequest anActor received aMessage ! // assert that anActor received aRequest
When  $\vdash$  aResponse Sent aResult  $\rightarrow$ 31
     $\vdash$  aResponse Received aResult ! // assert that aResult is received for aResponse
When  $\vdash$  aRequest Unbounded received []  $\rightarrow$ 
    // When asserted that Unbounded is sent []
 $\vdash$  Unbounded1[aRequest] Counter sent [],32
 $\vdash$  ResponseUnbounded1[request] Received Returned[aCounter:Counter]  $\rightarrow$ 
    // Set a goal that aCounter is returned for the request Unbounded1[aRequest].
 $\vdash$  Unbounded2[aRequest] aCounter sent go [],
 $\vdash$  Unbounded3[aRequest] aCounter sent stop [],
 $\vdash$  ResponseUnbounded2[request] Received Returned[Void]  $\rightarrow$ 
 $\vdash$  ResponseUnbounded3[request] Received Returned[anInteger:Integer]  $\rightarrow$ 
 $\vdash$  ResponseaRequest Returned[anInteger] !
When  $\vdash$  aRequest Counter received []  $\rightarrow$ 
 $\vdash$  ResponseaRequest Returned[aCounter],
 $\vdash$  ResponseaRequest currentCount anAccount = 0,
 $\vdash$  ResponseaRequest continue aCounter = True !
When  $\vdash$  aRequest aCounter:Counter received Stop []  $\rightarrow$ 
 $\vdash$  ResponseaRequest Sent Returned[currentCount aRequest],
When  $\vdash$  aRequest currentCount aCounter = n  $\rightarrow$ 
 $\vdash$  ResponseaRequest currentCount aCounter = n,
 $\vdash$  ResponseaRequest continue aCounter = False !
When  $\vdash$  aRequest aCounter:Counter received go []  $\rightarrow$ 
 $\vdash$  aRequest  $\rightarrow$  continue aCounter  $\rightarrow$  // Set a goal that continue aCounter = False
 $\vdash$  ResponseaRequest Sent Returned[Void],
 $\vdash$  ResponseaRequest Unchanged aRequest currentCount aCounter,
 $\vdash$  ResponseaRequest Unchanged aRequest continue aCounter,
 $\vdash$  aRequest continue aCounter  $\rightarrow$  // Set a goal that continue aCounter = True
 $\vdash$  Counter1[aRequest] aCounter sent go [],
 $\vdash$  Counter1[aRequest] Left,
    // Assert that the cheese has been left at Counter1[aRequest]
 $\vdash$  aRequest currentCount aCounter = anInteger
 $\vdash$  Counter1[aRequest] currentCount aCounter = anInteger + 1,
 $\vdash$  ResponseCounter1[request] Received Returned[anInteger:Integer]  $\rightarrow$ 
 $\vdash$  ResponseaRequest Sent Returned[anInteger] !

```

Note that the above logic programs do *not* make use of global³³ time.ⁱ

Inconsistency Robustness: Modeling Change

Direct Logic can be used to model change in a way that is physically realizable as opposed to systems that make use of physically unrealizable global time:

1. *Global State Spaces*: a computation can be represented as a global state that determines all information about the computation. It can be nondeterministic as to which will be the next global state, *e.g.*, in simulations where the global state can transition nondeterministically to the next state as a global clock advances in time, *e.g.*, Simula [Dahl and Nygaard 1967].ⁱ
2. *Actors*: a computation can be represented as a configuration. Information about a configuration can be indeterminate. For example, there can be arbiters that are meta-stable and messages in transit that will be delivered at some indefinite (unbounded) time.

The Japanese 5th Generation Project (ICOT)

Beginning in the 1970's, Japan took the DRAM market (and consequently most of the integrated circuit industry) away from the previous US dominance. This was accomplished with the help of the Japanese VLSI project that was funded and coordinated in good part by the Japanese government Ministry of International Trade and Industry (MITI) [Sigurdson 1986].

Project Inception

MITI hoped to repeat this victory by taking over the computer industry. However, Japan had come under criticism for “copying” the US. One of the MITI goals for ICOT was to show that Japan could innovate new computer technology and not just copy the Americans.

Trying to go all the way with Prolog-style clause programs

ICOT tried to go all the way with Prolog-style clause programs. Kowalski later recalled “*Having advocated LP [Logic Programs] as a unifying foundation for computing, I was delighted with the LP [Logic Program] focus of the FGCS [Fifth Generation Computer Systems] project.*” [Fuchi,

ⁱ which is physically unrealizable

Kowalski, Ueda, Kahn, Chikayama, and Tick 1993] By making Prolog-style clause programs (mainly being developed outside the US) the foundation, MITI hoped that the Japanese computer industry could leapfrog the US. “*The [ICOT] project aimed to leapfrog over IBM, and to a new era of advanced knowledge processing applications.*” [Sergot 2004]

Unfortunately, ICOT misjudged the importance of direct message passing, e.g., in the Actor Model [Hewitt, Bishop, and Steiger 1973] which had been developed in reaction to the limitations of Planner.

ICOT had to deal with the concurrency and consequently developed concurrent program languages based on Prolog-style clauses [Shapiro 1989] similar³⁴ to the above Logic Program. However, it proved difficult to implement clause-procedure invocation in these languages as efficiently as procedures in object-oriented program languages. Simula-67 originated a hierarchical class structure for objects so that message handling procedures (methods) and object instance variables could be inherited by subclasses. Ole-Johan Dahl [1967] invented a powerful compiler technology using dispatch tables that enabled message handling procedures in subclasses of objects to be efficiently invoked. The compiler technology originally developed for Simula³⁵ far out-performed the ICOT compilers for Prolog-style clause languages developed by ICOT.

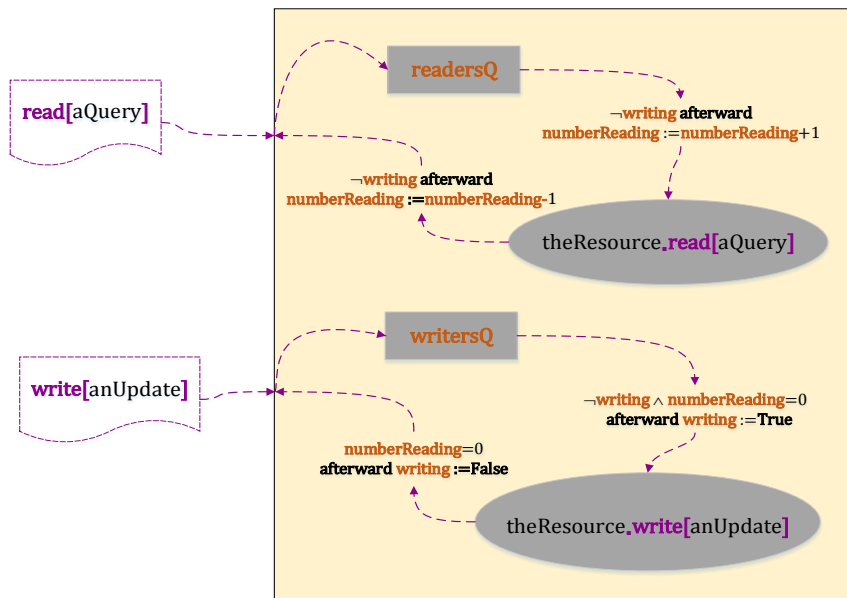
The clausal syntax used by ICOT was awkward because it only allowed relational syntax for procedure calls and consequently was not compositional requiring the use of multiple ports for communication.³⁶

Using clausal syntax, ICOT encountered difficulties dealing with concurrency, *e.g.*, readers-writers concurrency. Concurrency control for readers and writers in a shared resource is a classic problem. The fundamental constraint is that readers are allowed to operate concurrently but a writer is not allowed to operate concurrently with other writers and readers.

The interface for the readers/writer guardian is the same as the interface for the shared resource:

Interface ReadersWriter with `read[Query] → QueryAnswer,`
`write[Update] → Void`

Cheese diagram for **ReadersWriter** implementations:



Note:

1. At most one activity is allowed to execute in the cheese.ⁱ
2. The cheese has holes.ⁱⁱ
3. The value of a variableⁱⁱⁱ cannot change in the cheese.^{iv}

ⁱ Cheese is yellow in the diagram

ⁱⁱ A hole is grey in the diagram

ⁱⁱⁱ A variable is orange in the diagram

^{iv} Of course, other external Actors can change.

**Inconsistency Robustness:
Clausal Concurrent Programming Languages**

The combination of efficient inheritance-based virtual procedure invocation (pioneered in Simula) together with class libraries and browsers (pioneered in Smalltalk) provided better tools than the slower pattern-directed invocation of the FGCS Prolog-style clause programs. Consequently, the ICOT program languages never took off and instead object-oriented program languages like Java and JavaScript became the mainstream.

Downfall

The technical managers at ICOT were aware of some of the pitfalls that had tripped up previous Artificial Intelligence (AI) researchers. So they deliberately avoided calling ICOT an AI Project. Instead they had the vision of an integrated hardware/software system [Uchida and Fuchi 1992]. However, the Prolog-style clause-program paradigm turned not to be a suitable foundation because of poor modularity and lack of efficiency by comparison with direct message passing [Hewitt and Agha 1988]. Another problem was that multi-processors found it difficult to compete in the marketplace because at the time single processors were rapidly increasing in speed and connections between multiple processors suffered long latencies.

The reliance on Prolog-style clause procedures was a principle contributing cause to the failure of ICOT to achieve commercial success.

Inconsistency Robustness: ICOT

MITI's Fifth Generation strategy backfired because Japanese companies refused to productize ICOT hardware.

However, the architects of ICOT did get some things right:

- The project largely avoided the Mental Agent paradigm [Hewitt 2009]
- The project correctly placed tremendous emphasis on research in concurrency and parallelism as an emerging computing paradigm.

What is a Logic Program?

“It would be like saying Prolog and SLD-Resolution is the only way to do Logic Programming. To some extent, the LP [“Logic Programming”] community's insistence on clinging to this “exclusive method” has contributed to the relative disinterest in LP following its development in the 1980's and 1990's.” [Ait-Kaci 2009] (Emphasis added.)

Developments by different research groups in the fall of 1972 gave rise to a controversy over Logic Programs that persists to this day in the form of following alternatives:

1. Logic Programs using *procedural interpretation of logic-clause syntax for procedures* [Kowalski 2014]ⁱ
2. Logic Programs in which *each computational step*ⁱⁱ is logically inferredⁱⁱⁱ

This article argues for the second conception based on the following considerations:

- Logic-clause syntax is inadequate to express Logic Programs, e.g., logic-clause syntax lacks the ability to construct sets using $\{x \mid \Vdash \Phi[x]\}$, where Φ is a ground-complete predicate.
- Programs in logic-clause syntax are a special case of the second alternative because each computational step of a program in logic-clause syntax is logically inferred by forward chaining and backward chaining.
- Reducing propositions to logic-clause syntax can obscure their natural structure
- Procedural interpretation of logic-clause syntax for procedures can obscure the natural structure of proofs.^{iv}

Logic Programs need to deal with both of the following:

- *Mathematical Theories* that are thought to be consistent by the overwhelming consensus of professional working mathematicians, e.g. Hilbert spaces, homology theory, *etc.*

ⁱ Logic-clause syntax for a logic program is $\Psi \Leftarrow (\Phi_1 \wedge \dots \wedge \Phi_n)$ where Ψ and each of the Φ_i is either $P[t_1, \dots, t_m]$ or $\neg P[t_1, \dots, t_m]$ for some atomic predicate P and terms t_j .

ⁱⁱ in the Actor Model of computation

ⁱⁱⁱ e.g. using Direct Logic

^{iv} e.g. ActorScript Logic Programs using Inconsistency Robust Natural Deduction in Direct Logic

- *Theories of Practice* that are pervasively inconsistent, *e.g.*, theories of climate change and the human brain. Mathematical theories are often freely used *within* theories of practice.

Going beyond the limitations of logic-clause syntax, there is a core subset of Logic Program constructs that are applicable to both Classical Direct Logic and Inconsistency Robust Direct Logic.ⁱ

Inconsistency Robustness: Characterization of Logic Programs

Developments by different research groups in the fall of 1972 gave rise to a controversy over Logic Programs that persists to this day in the form of following alternatives:

1. Each computational step (*e.g.* as defined in the Actor Model) of a Logic Program is logically inferred (*e.g.* in Direct Logic) with explicit assertions and goals processed using pattern-directed invocation.
2. A Logic Program is expressed using logic-clause syntax that is interpreted as both a backward-chaining program and a forward-chaining program.

ⁱ See appendix of this article.

Logic Programs versus Kowalski's "Logic Programming"

Kowalski has for a long time advocated "Logic Programming" characterized as follows:³⁷

The driving force behind logic programming is the idea that a single formalism suffices for both logic and computation, and that logic subsumes computation. ...

Logic programming aims ... to unify different areas of computing by exploiting the greater generality of logic [over computational modelsⁱ]. It does so by building upon and extendingⁱⁱ one of the simplest, yet most powerful logics imaginable, namely the logic of Horn clauses.

Kowalski's Logic Programming is a scientific research programme in the sense of [Lakatos 1980]. According to [Kowalski 2006]:

Admittedly, I have been messianic in my advocacy of Logic, and I make no apologies for it. Pushing Logic as hard as I could has been my way of trying to discover its limits.

Kowalski's version of Logic Programming has the following limitations:

- based on the following mistaken assumptions:
 - "that logic subsumes computation"ⁱⁱⁱ
 - that Horn clauses are the basis for a powerful logic^{iv}
- lacks inconsistency-robust inference because it is based on classical logic making use of resolution theorem proving^v
- lacks the precision of a well-defined scientific concept.^{vi}

ⁱ e.g., Turing Machines, relational model of data base queries, the Actor Model, etc.

ⁱⁱ using logic-clause syntax for a Logic Program, e.g., $\Psi \Leftarrow (\Phi_1 \wedge \dots \wedge \Phi_n)$ where Ψ and each of the Φ_i is either $P[t_1, \dots, t_m]$ or $\neg P[t_1, \dots, t_m]$ for some atomic predicate P and terms t_j .

ⁱⁱⁱ Contrary to Kowalski, there are computations that cannot be performed using logical inference. See discussion earlier in this article.

^{iv} Contrary to Kowalski, the logic-clause generalization of Horn-clause syntax is inadequate for expressing Logic Programs as explained earlier in this article. Also, Horn clauses do *not* form the basis for the most powerful logic because they are based on first-order logic, which has unintended models of axioms. For example, first-order logic cannot even characterize the integers up to isomorphism. See discussion in article 1-2 in this volume.

^v As explained earlier in this article, resolution theorem provers can make invalid inferences using inconsistent axioms.

^{vi} which could be fixed by defining the concept as "programming using Logic Programs" for a well-defined definition of a Logic Program.

Overview

Contradiction	Outcome
Kowalski advocates using resolution theorem proving to make inferences about inconsistent information systems. Unfortunately, using resolution theorem provers allows inferring every proposition from an inconsistent information system.	Using Direct Logic, inconsistent-robust inference allows inference about inconsistent information systems without enabling inference of every sentence.
Planner was intended to be a general purpose programming language for the procedural embedding of knowledge. Partly as a result of limitations of contemporary computers, pragmatic decisions were made in the implementation of Planner that limited its generality.	Programming languages (like ActorScript) have been developed that incorporate general Logic Programs.
Kowalski, <i>et. al.</i> advocated that Horn-clause syntax for programs be used as the foundation of Logic Programs. But Horn-clause syntax for programs (and slightly more general logic-clause syntax) lack the generality and modularity needed for Logic Programs.	Programming languages (like ActorScript) are not restricted to logic-clause syntax for Logic Programs.
The Japanese Fifth Generation Project (ICOT) attempted to create a new computer architecture based on logic-clause programs.	ICOT failed to gain commercial traction although it was an important research project.
Kowalski claims that mathematical logical deduction subsumes computation. However, there are computations that cannot be implemented using deduction (<i>i.e.</i> Logic Programs) and there are important applications that cannot be implemented using only Logic Programs.	Actor programming languages (like ActorScript) use direct message passing to Actors and are not restricted to just Logic Programs.
Previously, change was modeled in Logic Programs using a global time that is physically meaningless.	The Actor model enables change in computation to be modeled by causal partial orders of message-passing events.

The above examples are intended to be case studies in Inconsistency Robustness in which information is formalized, contradictions are derived using Inconsistency Robust reasoning, and arguments are formalized for and

against contradictory propositions. A challenge for the future is to automate the reasoning involved in these case studies.

Conclusion

Max Planck, surveying his own career in his Scientific Autobiography [Planck 1949], sadly remarked that 'a new scientific truth does not triumph by convincing its opponents and making them see the light, but rather because its opponents eventually die, and a new generation grows up that is familiar with it.'

[Kuhn 1962]

A fundamental principle of Inconsistency Robustness is to make contradictions explicit so that arguments for and against propositions can be formalized. This paper has explored the role of Inconsistency Robustness in the history and theory of Logic Programs by making contradictions explicit and using them to explicate arguments. The development of Logic Programs has been shown to be a productive area for applying principles of Inconsistency Robustness.

The examples presented in this paper are intended to be case studies in Inconsistency Robustness in which information is formalized, contradictions are derived using Inconsistency Robust reasoning, and arguments are formalized for and against contradictory propositions with developments that included:

- Some arguments were dropped.
- Some arguments triumphed.
- Arguments were combined and improved.
- New arguments were developed

A challenge for the future is to automate the reasoning involved in these case studies.³⁸

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Appendix. Inconsistency Robust Logic Programs

Notation of Direct Logic

The aims of logic should be the creation of “*a unified conceptual apparatus which would supply a common basis for the whole of human knowledge.*”
[Tarski 1940]

In Direct Logic, unrestricted recursion is allowed in programs by using recursive definitions.

There are uncountably many Actors.³⁹ For example, `CreateReal.a[]` can output any real numberⁱ between 0 and 1 whereⁱⁱ

`CreateReal.a[]` \equiv [(0 **either** 1), **VPostpone** `CreateReal.a[]`]

where

- `CreateReal.a[]` is the result of sending the Actor `CreateReal` the message `[]`
- (0 **either** 1) is the nondeterministic choice of 0 or 1,
- [*first*, *rest*] is the list that begins with *first* and whose remainder is *rest*, and
- **Postpone** *expression* delays execution of *expression* until the value is needed.

Each `CreateReal.a[]` is one of uncountably many Actors.

There are uncountably many propositions (because there is a different proposition for every real number). Consequently, there are propositions that are not the abstraction of any element of a denumerable set of sentences. For example, $p \equiv [x:\mathbb{R}] \rightarrow ([y:\mathbb{R}] \rightarrow (y=x))$ defines a different predicate $p[x]$ for each real number x , which holds for only one real number, namely x .ⁱⁱⁱ

ⁱ using binary representation.

ⁱⁱ Typically, a result returned by the non-deterministic procedure `Real` is not computable in the sense there is no computable deterministic procedure that can compute its digits.

ⁱⁱⁱ For example $(p[3])[y]$ holds if and only if $y=3$.

It is important to distinguish between sentences, and propositions. Sentencesⁱ (which without free variables) can be abstracted into propositions that can be asserted. Furthermore, termsⁱⁱ can be abstracted into Actors (*i.e.* objects in mathematics).

Abstraction and parsing are becoming increasingly important in software engineering. *e.g.*,

- The execution of code can be dynamically checked against its documentation. Also Web Services can be dynamically searched for and invoked on the basis of their documentation.
- Use cases can be inferred by specialization of documentation and from code by automatic test generators and by model checking.
- Code can be generated by inference from documentation and by generalization from use cases.

Abstraction and parsing are needed for large software systems so that that documentation, use cases, and code can mutually speak about what has been said and their relationships.

For example:

Proposition<N>

e.g. $\forall [n:\mathbb{N}] \rightarrow \exists [m:\mathbb{N}] \rightarrow m > n$

i.e., for every N there is a larger N

Sentence<N>

e.g. $((\forall [n:\mathbb{N}] \rightarrow ((\exists [m:\mathbb{N}] \rightarrow (m > n))))))$

i.e., the sentence that for every N there is a larger N

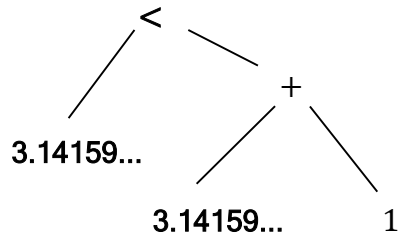
ⁱ which are grammar tree structures

ⁱⁱ which are grammar tree structures

In Direct Logic, a sentence is a grammar tree (analogous to the ones used by linguists). Such a grammar tree has terminals that can be constants. And there are uncountably many constants, *e.g.*, the real numbers:

Of course, because the digits of 3.14159... are computable, there is a expression_1 such that $\lfloor \text{expression}_1 \rfloor = 3.14159\dots$ that can be used to create the sentence $(\text{expression}_1 < (\text{expression}_1 + 1))$.

However the sentence $(\text{expression}_1 < (\text{expression}_1 + 1))$ is not the same as $(3.14159\dots < (3.14159\dots + 1))$ because it does not have the same vocabulary and it is a much larger sentence that has many terminals whereas $(3.14159\dots < (3.14159\dots + 1))$ has just 3 terminals:



Consequently, sentences *cannot* be enumerated.

Note: Type theory of Classical Direct Logic is much stronger than constructive type theory with constructive logic⁴⁰ because Classical Direct Logic has all of the power of Classical Mathematics.

Notation of Direct Logic

- *Type* i.e., a **Type** is a *discrimination* of the following:
 - **Boolean**:**Type** \langle **Boolean** \rangle ⁴¹ and **N**⁴²:**Type** \langle **N** \rangle
 - **Proposition** \langle σ \rangle , **Sentence** \langle σ \rangle , **Proof** \langle σ \rangle , **Sets** \langle σ \rangle :**Type** \langle σ \rangle
 - **Type** \langle σ \rangle :**Type**² \langle σ \rangle ⁱ
 - $\sigma_1 \oplus \sigma_2$ ⁱⁱ, $[\sigma_1, \sigma_2]$ ⁴³:**Type** \langle $\sigma_1 \oplus \sigma_2$ \rangle
 - $[\sigma_1] \mapsto \sigma_2$ ⁱⁱⁱ:**Type** \langle $[\sigma_1] \mapsto \sigma_2$ \rangle ^{iv} and $\sigma_2^{\sigma_1}$ ^v:**Type** \langle $\sigma_2^{\sigma_1}$ \rangle ^{vi}
 - **True**, **False**:**Boolean** and **0**, **1**:**N**
- *Propositions*, i.e., a **Proposition** is a *discrimination* of the following:
 - If Φ :**Proposition** \langle σ \rangle , then $\neg\Phi$:**Proposition** \langle σ \rangle .
 - If Φ, Ψ :**Proposition** \langle σ \rangle , then $\Phi \wedge \Psi$, $\Phi \vee \Psi$, $\Phi \Rightarrow \Psi$, $\Phi \Leftrightarrow \Psi$:**Proposition** \langle σ \rangle .
 - If p :**Boolean** and Φ, Ψ :**Proposition** \langle σ \rangle , then $(p \Leftrightarrow \text{True} \text{;} \Phi_1 \boxtimes \text{False} \text{;} \Phi_2)$:**Proposition** \langle σ \rangle .⁴⁴
 - If x_1, x_2 : σ , then $x_1 = x_2$, $x_1 \sqsubseteq x_2$, $x_1 \sqsubset x_2$:**Proposition** \langle σ \rangle .
 - If x_1 : σ_1 and x_2 : σ_2 , then $x_1 \in x_2$, $x_1 ? x_2$:**Proposition** \langle $\sigma_1 \oplus \sigma_2$ \rangle .
 - If x : σ_1 , and p :**Proposition** \langle σ_2 \rangle ^{σ_1} , then $p[x]$:**Proposition**² \langle σ_2 \rangle .^{vii}
 - If p :**Proof** \langle σ \rangle , **T**:**Theory**, and Φ_1 to n :**Proposition** \langle σ \rangle , then $(\Phi_1, \dots, \Phi_k \mid_{\text{T}}^{\text{D}} \Phi_{k+1}, \dots, \Phi_n)$:**Proposition** \langle σ \rangle .⁴⁵
 - If s :**Sentence** \langle σ \rangle with no free variables, then $\lfloor s \rfloor$:**Proposition** \langle σ \rangle .

ⁱ **Type**² \langle σ $\rangle \equiv \text{Type}\langle \text{Type}\langle \sigma \rangle \rangle$

τ :**Type** \langle σ $\rangle \Leftrightarrow \tau \sqsubseteq \sigma$

ⁱⁱ For $i=1,2$

• If x : σ_i , then $((\sigma_1 \oplus \sigma_2)[x])$: $(\sigma_1 \oplus \sigma_2)$ and $x = ((\sigma_1 \oplus \sigma_2)[x]) \downarrow \sigma_i$.

• $\forall [z:\tau] \rightarrow z ? \sigma_1 \oplus \sigma_2 \Leftrightarrow \exists [x:\sigma_i] \rightarrow z = (\sigma_1 \oplus \sigma_2)[x]$

ⁱⁱⁱ Type of computable procedures from σ_1 into σ_2 .

If f : $([\sigma_1] \mapsto \sigma_2)$ and x : σ_1 , then $f[x]$: σ_2 .

^{iv} The type of $[\sigma_1] \mapsto \sigma_2$ means that “self-referential” types for procedures cannot be constructed in Direct Logic.

^v If f : $\sigma_2^{\sigma_1}$ and x : σ_1 , then $f[x]$: σ_2 .

^{vi} The type of $\sigma_2^{\sigma_1}$ means that “self-referential” types for functions cannot be constructed in Direct Logic.

^{vii} **Proposition**² \langle σ_2 $\rangle \equiv \text{Proposition}\langle \text{Proposition}\langle \sigma_2 \rangle \rangle$

The type of $p[x]$ means that “self-referential” propositions cannot be constructed in Direct Logic.

Grammar trees (*i.e.* expressions and sentences) are defined as follows :

- **Expressions**, *i.e.*, an **Expression** $\langle\sigma\rangle$ is a *discrimination* of the following:
 - **(Boolean):Constant** \langle Type \langle Boolean $\rangle\rangle$, **(N):Constant** \langle Type \langle N $\rangle\rangle$ and **(Theory):Constant** \langle Type \langle Theory $\rangle\rangle$
 - **(True),(False):Constant** \langle Boolean \rangle and **(0),(1):Constant** \langle N \rangle
 - If **x:Constant** $\langle\sigma\rangle$, then **x:Expression** $\langle\sigma\rangle$.
 - If **e:Expression** $\langle\sigma\rangle$, then **(Sentence** \langle e \rangle), **(Proposition** \langle e \rangle), **(Proof** \langle e \rangle), **(Sets** \langle e \rangle):**Expression** \langle Type $\langle\sigma\rangle\rangle$.
 - If **x:Variable** $\langle\sigma\rangle$, then **x:Expression** $\langle\sigma\rangle$.
 - If **x_{1 to n}:Expression** $\langle\sigma_{1 to n}\rangle$, **y:Expression** $\langle\sigma\rangle$ and **v_{1 to n}:Variable** $\langle\sigma_{1 to n}\rangle$ in **y** and in each **x_{1 to n}**⁴⁶, then **(Let v₁ $\langle\tau_1\rangle \equiv x_1, \dots, v_n\langle\tau_n\rangle \equiv x_n$ ⁴⁷. y):Expression** $\langle\sigma\rangle$.
 - If **e₁:Expression** $\langle\sigma_1\rangle$ and **e₂:Expression** $\langle\sigma_1\rangle$, then **(e₁ \oplus e₂),([e₁, e₂]):Expression** \langle e₁ \oplus e₂ \rangle
 - If **e₁:Expression** \langle Type $\langle\sigma_1\rangle\rangle$ and **e₂:Expression** \langle Type $\langle\sigma_2\rangle\rangle$, then **([e₁] \mapsto e₂):Expression** \langle Type \langle [σ_1] \mapsto $\sigma_2\rangle\rangle$ and **(e₂^{e₁}):Expression** \langle Type $\langle\sigma_2^{\sigma_1}\rangle\rangle$.
 - If **t₁:Expression** \langle Boolean \rangle , **t₂, t₃:Expression** $\langle\sigma\rangle$, then **(t₁ \diamond True⁸ t₂ \square False⁸ t₃):Expression** $\langle\sigma\rangle$.⁴⁸
 - If **t:Expression** $\langle\sigma_2\rangle$ and **x:Variable** $\langle\sigma_1\rangle$ in **t**⁴⁹, then **([x: σ_1]: $\sigma_2 \rightarrow t$):Expression** $\langle\sigma_2^{\sigma_1}\rangle$.
 - If **e:Expression** $\langle\sigma_2^{\sigma_1}\rangle$ and **x:Expression** $\langle\sigma_1\rangle$, then **(e[x]):Expression** $\langle\sigma_2\rangle$.
 - If **e:Expression** \langle [σ_1] \mapsto $\sigma_2\rangle$ and **x:Expression** $\langle\sigma_1\rangle$, then **(e.[x]):Expression** $\langle\sigma_2\rangle$.
 - If **e:Expression** $\langle\sigma_2^{\sigma_1}\rangle$ and **x:Expression** $\langle\sigma_1\rangle$, then **(e[x]):Expression** $\langle\sigma_2\rangle$.

- *Sentences*, i.e., a **Sentence** is a *discrimination* of the following:
 - If $s_1:\mathbf{Sentence}\langle\sigma\rangle$ then, $(\neg s_1):\mathbf{Sentence}\langle\sigma\rangle$.
 - If $s_1:\mathbf{Sentence}\langle\sigma\rangle$ and $s_2:\mathbf{Sentence}\langle\sigma\rangle$ then $(s_1\wedge s_2), (s_1\vee s_2), (s_1\Rightarrow s_2), (s_1\Leftrightarrow s_2):\mathbf{Sentence}\langle\sigma\rangle$.
 - If $t:\mathbf{Expression}\langle\mathbf{Boolean}\rangle$, $s_1, s_2:\mathbf{Sentence}\langle\sigma\rangle$, then $(t \diamond \text{True} \circ s_1 \boxtimes \text{False} \circ s_2):\mathbf{Sentence}\langle\sigma\rangle$.⁵⁰
 - If $t_1:\mathbf{Expression}\langle\sigma\rangle$ and $t_2:\mathbf{Expression}\langle\sigma\rangle$, then $(t_1=t_2), (t_1\sqsubseteq t_2), (t_1\subseteq t_2):\mathbf{Sentence}\langle\sigma\rangle$.
 - If $t_1:\mathbf{Expression}\langle\sigma_1\rangle$ and $t_2:\mathbf{Expression}\langle\sigma_2\rangle$, then $(t_1\in t_2), (t_1: ?t_2):\mathbf{Sentence}\langle\sigma_1\oplus\sigma_2\rangle$.
 - If $x:\mathbf{Variable}\langle\sigma_1\rangle$ in s^{51} and $s:\mathbf{Sentence}\langle\sigma_2\rangle$, then $(\forall[x:\sigma_1]\rightarrow s), (\exists[x:\sigma_1]\rightarrow s):\mathbf{Sentence}\langle\sigma_1\oplus\sigma_2\rangle$.
 - If $x:\mathbf{Expression}\langle\sigma_1\rangle$, and $p:\mathbf{Sentence}\langle\sigma_2\rangle^{\sigma_1}$, then $(p[x]):\mathbf{Sentence}^2\langle\sigma_2\rangle$.ⁱ
 - If $T:\mathbf{Expression}\langle\mathbf{Theory}\rangle$, s_1 to $s_n:\mathbf{Sentence}\langle\sigma\rangle$ and $p:\mathbf{Expression}\langle\mathbf{Proof}\langle\sigma\rangle\rangle$, then $(s_1, \dots, s_k \vdash_T^p s_{k+1}, \dots, s_n):\mathbf{Sentence}\langle\sigma\rangle$.

ⁱ $\mathbf{Sentence}^2\langle\sigma_2\rangle \equiv \mathbf{Sentence}\langle\mathbf{Sentence}\langle\sigma_2\rangle\rangle$

The type of $(p[x])$ means that “self-referential” sentences cannot be constructed in Direct Logic.

Forward Chaining

Forward chaining is performed using \vdash

$((\vdash_{Theory} PropositionExpression) : Expression)$
Assert *PropositionExpression* for *Theory*.

$((\text{“When” } \vdash_{Theory} PropositionPattern \text{ “}\rightarrow\text{” } Expression) : Continuation)$
When *PropositionPatterns* holds for *Theory*, evaluate *Expression*.

Illustration of forward chaining:

$\vdash_t Human[Socrates] \blacksquare$

When $\vdash_t Human[x] \rightarrow \vdash_t Mortal[x] \blacksquare$

will result in asserting *Mortal[Socrates]* for theory *t*

Backward Chaining

Backward chaining is performed using \Vdash

$((\Vdash_{Theory} GoalPatterns \text{ “}\rightarrow\text{” } Expression) : Continuation)$
Set *GoalPatterns* for *Theory* and when established evaluate *Expression*

$((\Vdash_{Theory} GoalPattern) : Expression)$
Set *GoalPattern* for *Theory* and return a list of assertions that satisfy the goal.

$((\text{“When” } \Vdash_{Theory} GoalPattern \text{ “}\rightarrow\text{” } Expression) : Continuation)$
When there are goals that matches *GoalPatterns* for *Theory*, evaluate *Expression*.

Illustration of backward chaining:

$\vdash_t Human[Socrates] \blacksquare$

When $\Vdash_t Mortal[x] \rightarrow (\Vdash_t Human[x] \rightarrow \vdash_t Mortal[x]) \blacksquare$

$\Vdash_t Mortal[Socrates] \blacksquare$

will result in asserting *Mortal[Socrates]* for theory *t*.

SubArguments

This section explains how subarguments can be implemented in natural deduction.

When $\Vdash_s(\Psi \vdash_t \Phi) \rightarrow$
Let $t' = \text{Extension}.[t]$,
Do $\vdash_{t'} \Psi$,
 $\Vdash_{t'} \Phi \rightarrow \Vdash_s(\Psi \vdash_t \Phi) \blacksquare$

Note that the following hold for t' because it is an extension of t :

- **When** $\vdash_t \Theta \rightarrow \vdash_{t'} \Theta \blacksquare$
- **When** $\Vdash_{t'} \Theta \rightarrow \Vdash_t \Theta \blacksquare$

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End Notes

- ¹ Church's system was quickly shown to be inconsistent because it allowed Gödelian “self-referential” propositions, which lead to inconsistency in Mathematics [Hewitt 2011].
- ² [Kowalski1988]
- ³ According to [Kowalski 1979]:
“an inconsistent system can ... organize useful information... Thus [finding a] contradiction, far from harming an information system, helps to indicate areas in which it can be improved. It facilitates the development of systems by successive approximation – daring conjectures followed by refutation and reconciliation. It favours bold, easily falsified beliefs, which can be weakened if need should arrive, over save, timid beliefs, which are difficult to strengthen later on. Better to make mistakes and to correct them than to make no progress at al.”
- ⁴ Raising issues of Inconsistency Robustness, The Obama administration deleted the following statement from its 2008 campaign website:
“Protect Whistleblowers: Often the best source of information about waste, fraud, and abuse in government is an existing government employee committed to public integrity and willing to speak out. Such acts of courage and patriotism, which can sometimes save lives and often save taxpayer dollars, should be encouraged rather than stifled. We need to empower federal employees as watchdogs of wrongdoing and partners in performance. Barack Obama will strengthen whistleblower laws to protect federal workers who expose waste, fraud, and abuse of authority in government. Obama will ensure that federal agencies expedite the process for reviewing whistleblower claims and whistleblowers have full access to courts and due process.”
It may be that Obama's Administration's statement on the importance of protecting whistleblowers went from being a promise for his administration to a political liability. There are manifest contradictions in what Obama said then and what he is doing now.
- ⁵ In 1666, England's House of Commons introduced a bill against atheism and blasphemy, singling out Hobbes' Leviathan. Oxford university condemned and burnt Leviathan four years after the death of Hobbes in 1679.
- ⁶ In Latin, the principle is called *ex falso quodlibet* which means that from falsity anything follows.
- ⁷ [Nekham 1200, pp. 288-289]; later rediscovered and published in [Lewis and Langford 1932]

⁸ [Pospeseł 2000] has discussed extraneous \vee introduction on in terms of the following principle: $\Psi, (\Psi \vee \Phi \vdash \Theta) \vdash \Theta$ However, the above principle immediately derives extraneous \vee introduction when Θ is $\Psi \vee \Phi$. In Direct Logic, argumentation of the above form would often be reformulated as follows to eliminate the spurious Φ middle proposition: $\Psi, (\Psi \vdash \Theta) \vdash \Theta$

⁹ using \vee -*Elimination*, i.e., $\neg\Phi, (\Phi \vee \Psi) \vdash_T \Psi$

¹⁰ Turing noted that classical logic can be used to make invalid inferences using inconsistent information “*without actually going through* [an explicit] *contradiction*.” [Diamond 1976] Furthermore, [Church 1935, Turing 1936] proved that it is computationally undecidable whether a mathematical theory of practice is inconsistent.

¹¹ [Green 1969].

¹² [Kowalski 1988]

¹³ Resolution Theorem Proving is not Inconsistency Robust because it can be used to prove that there are no contradictions as follows:

Using Resolution Theorem Proving, $\neg(\Psi \wedge \neg\Psi)$ can be proved because

$\Psi, \neg\Psi \vdash_{\text{ClassicalResolution}} \text{False}$

It is possible to use *Inconsistency-Robust Resolution* as follows:

$\Psi \vee \neg\Psi, \neg\Psi \vee \Phi, \Psi \vee \Omega \vdash_T \Phi \vee \Omega$ that requires the additional assumption $\Psi \vee \neg\Psi$ in order to make the inference.

Of course, it is possible to add the classical resolution rule to a theory \mathcal{T}

by adding the following: $\Psi \vee \Phi, \neg\Phi \vee \Theta \vdash_T \Psi \vee \Theta$

¹⁴ The argument below originated in [Nekham 1200, pp. 288-289] (later rediscovered and published in [Lewis and Langford 1932]) is an argument that an inconsistency $\mathfrak{A} \wedge \neg\mathfrak{A}$ can be used to infer every proposition X . The Nekham argument is not valid in Inconsistency Robust Direct Logic because it make use of the rule of Extraneous \vee -Introduction, i.e., $\Psi \vdash (\Psi \vee \Phi)$. The Nekham argument can be formalized is as follows: $\mathfrak{A} \vdash (\mathfrak{A} \vee X)$ and therefore $\mathfrak{A}, \neg\mathfrak{A} \vdash X$ because $\neg\mathfrak{A}, (\mathfrak{A} \vee X) \vdash X$

¹⁵ [Wos et. al., 1965]

¹⁶ I am grateful to Kowalski for clarifying his position. [Personal communication March 8, 2014].

¹⁷ such as the one immediately above

¹⁸ (later generalized, e.g., ActorScript [Hewitt 2013])

¹⁹ A ground-complete predicate is one for which all instances in which the predicate holds are explicitly manifest, i.e. instances can be generated using patterns. See [Ross and Sagiv 1992, Eisner and Filardo 2011].

²⁰ Execution can proceed differently depending on how sets fit into computer storage units.

²¹ Sussman and Steele [1975] mistakenly concluded

“we discovered that the 'Actors' and the lambda expressions were identical in implementation.”

The actual situation is that the lambda calculus is capable of expressing some kinds of sequential and parallel control structures but, in general, not the concurrency expressed in the Actor model. On the other hand, the Actor model is capable of expressing everything in the lambda calculus and more.

Sussman and Steele noticed some similarities between Actor customers and continuations introduced by [Reynolds 1972] using a construct called escape that was a further development of hairy control structure. In their program language Scheme, they called their variant of escape by the name *“call with current continuation.”* Unfortunately, general use of escape is not compatible with usual hardware stack discipline introducing considerable operational inefficiency. Also, using escape can leave customers stranded. Consequently, use of escape is generally avoided these days and exceptions are used instead so that clean up can be performed. [Hewitt 2009]

²² and unlike Prolog (see below)

²³ There was somewhat similar work that Hayes had discussed with the researchers at Aberdeen on ABSYS/ABSET [Foster and Elcock 1969].

²⁴ According to [Colmerauer and Roussel 1996]:

While attending an IJCAI convention in September '71 with Jean Trudel, we met Robert Kowalski again and heard a lecture by Terry Winograd on natural language processing. The fact that he did not use a unified formalism left us puzzled. It was at this time that we learned of the existence of Carl Hewitt's programming language, Planner [Hewitt, 1969]. The lack of formalization of this language, our ignorance of Lisp and, above all, the fact that we were absolutely devoted to logic meant that this work had little influence on our later research.

However, according to [Kowalski 2008]:

During the next couple of years, I tried to reimplement Winograd's system in resolution logic and collaborated on this with Alain Colmerauer in Marseille. This led to the procedural interpretation of Horn clauses (Kowalski 1973/1974) and to Colmerauer's development of the programming language Prolog.

²⁵ [Horn 1951]

-
- ²⁶ In practice, Prolog implemented a number of non-logical computational primitives for input-output, *etc.* Like Planner, for the sake of efficiency, it used backtracking. Prolog also had a non-logical computational primitive like the one of Planner to control backtracking by conditionally testing for the exhaustive failure to achieve a goal by backward chaining. However, Prolog was incapable of expressing strong “Negation as Failure” because it lacked both the assertions and true negation of Planner and thus it was impossible in Prolog to say “if attempting to achieve the goal G exhaustively fails then assert (*not* G).” Prolog extended Planner by using unification (but not necessarily soundly because for efficiency reasons it can omit use of the “occurs” check).
- ²⁷ Prolog required a top-level goal $\Phi_1 \wedge \dots \wedge \Phi_n$ to be stated as follows: **False** $\Leftarrow(\Phi_1 \wedge \dots \wedge \Phi_n)$ [logically equivalent to the disjunctive clause $\neg\Phi_1 \vee \dots \vee \neg\Phi_n$], which requires that in order to find solutions to the goal, the disjunctive clause must be refuted by deriving a contradiction, which is not Inconsistency Robust.
- ²⁸ some of material below was contributed by the author for publication in Wikipedia on “The Actor Model.”
- ²⁹ [Kowalski 1988a] On the other hand since the fall of 1972 with the invention of the Actor Model, Logic Programs can be rigorously defined very general terms (starting with the McCarthy’s Advice Taker proposal [McCarthy 1958]) as “*what can be programmed in mathematical logic.*” Of course, what can be programmed in mathematical logic is exactly “*each computational step (e.g. as defined in the Actor model) can be logically deduced.*” Even allowing the full power of Direct Logic, computation is not reducible to Logic Programs [Hewitt 2011].
- ³⁰ *cf.* Plotkin [1976]
- ³¹ When asserted that `aResult` is sent in `aResponse`
- ³² Assert in `Unbounded1[aRequest]` that **Counter** is sent `[]`
- ³³ e.g. [Kowalski and Sadri 2015]
- ³⁴ ICOT used monotonic *mutable* lists instead of events in its Prolog-style clause programs.
- ³⁵ later adapted for concurrency, e.g., Java, etc.
- ³⁶ Use of multiple ports is an awkward programming idiom that introduces many difficulties, *e.g.*, starvation due not properly servicing a port. For a contrary view, see [Kahn and Saraswat 1990].
- ³⁷ [Kowalski 2014]

³⁸ Computerization of argumentation is still in its infancy, *cf.*, [Toulmin 1959, Woods 2000, Bench-Capon 2012]. Also, there is a great deal of ongoing research in formalizing mathematical proofs [Avigad and Harrison 2014].

³⁹ The *Computational Representation Theorem* [Clinger 1981; Hewitt 2006] characterizes computation for systems which are closed in the sense that they do not receive communications from outside:

The denotation Denote_S of a closed system S represents all the possible behaviors of S as³⁹

$$\text{Denote}_S = \lim_{i \rightarrow \infty} \text{Progressions}_S^i$$

where $\text{Progressions}_S^i \rightarrow \text{Progressions}_S^{i+1}$

In this way, S can be mathematically characterized in terms of all its possible behaviors (including those involving unbounded nondeterminism).

The denotations of the Computational Representation Theorem form the basis of procedurally checking programs against all their possible executions.

⁴⁰ e.g. [Shulman 2012, nLab 2014]

⁴¹ **True** ≠ **False**

$$\forall [x:\mathbf{Boolean}] \rightarrow x = \mathbf{True} \vee x = \mathbf{False}$$

⁴² The natural numbers are axiomatised as follows where *Successor* is the successor function:

- $0:\mathbf{N}$
- $\text{Successor}:\mathbf{N} \rightarrow \mathbf{N}$
- $\forall [i:\mathbf{N}] \rightarrow \text{Successor}[i] \neq 0$
- $\forall [i, j:\mathbf{N}] \rightarrow \text{Successor}[i] = \text{Successor}[j] \Rightarrow i = j$
- $\forall [P:\mathbf{Proposition} \langle \mathbf{N} \rangle^{\mathbf{N}}] \rightarrow \text{Inductive}[P] \Rightarrow \forall [i:\mathbf{N}] \rightarrow P[i]$

where

$$\forall [P:\mathbf{Proposition} \langle \mathbf{N} \rangle^{\mathbf{N}}] \rightarrow$$

$$\text{Inductive}[P:\mathbf{Proposition} \langle \mathbf{N} \rangle^{\mathbf{N}}]:\mathbf{Proposition}^2 \langle \mathbf{N} \rangle \equiv$$

$$P[0] \wedge \forall [i:\mathbf{N}] \rightarrow P[i] \Rightarrow P[\text{Successor}[i]]$$

⁴³ type of 2-element list with first element of type σ_1 and with second element of type σ_2

⁴⁴ *if t then Φ_1 else Φ_2*

⁴⁵ Φ_1, \dots and Φ_k infer Ψ_1, \dots , and Ψ_n

⁴⁶ if present

⁴⁷ parameterized mutually recursive definitions of v_1 to n $\langle t_1$ to $n \rangle$

⁴⁸ *if t_1 then t_2 else t_3*

⁴⁹ if present

⁵⁰ *if t then s_1 else s_1*

⁵¹ if present