ExBLAS: Reproducible and Accurate BLAS Library
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To cite this version:
Roman Iakymchuk, Stef Graillat, Caroline Collange, David Defour. ExBLAS: Reproducible and Accurate BLAS Library. RAIM: Rencontres Arithmétiques de l’Informatique Mathématique, Apr 2015, Rennes, France. , 7ème Rencontre Arithmétique de l’Informatique Mathématique, 2015. hal-01140280

HAL Id: hal-01140280
https://hal.science/hal-01140280
Submitted on 8 Apr 2015

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Abstract

We aim at providing algorithms and implementations for fundamental linear algebra operations – like the ones included in the Basic Linear Algebra Subprograms (BLAS) library – that would deliver reproducible and accurate results with reasonable performance overhead compared to the standard non-reproducible implementations on modern parallel architectures such as Intel processors, Intel Xeon Phi co-processors, and GPU accelerators.

Introduction

In general, BLAS routines rely on the optimized version of parallel reduction and dot product involving floating-point additions and multiplications operations that are non-associative. Due to non-associativity of these operations and dynamic scheduling on parallel architectures, getting a bitwise reproducible floating-point result for multiple executions of the same code on different or even similar parallel architectures is challenging. These discrepancies worsen on heterogeneous architectures – such as clusters composed of standard CPUs in conjunction with GPU accelerators and/or Intel Xeon Phi co-processors –, which combine together different programming environments that may obey various floating-point models and offer different intermediate precision or different operators. Such non-determinism and non-reproducibility of floating-point computations on parallel machines poses validation and debugging issues, and may even lead to deadlocks.

Existing solutions to enhance reproducibility of BLAS routines are:
- **Fixed reduction scheme** such as Intel’s “Conditional Numerical Reproducibility” (CNR) available as an option in the Math Kernel Library (MKL);
- **Avoid rounding error** by using the Kulisch accumulator [3];
- **Mixed solution** as the one proposed by Demmel and Nguyen for BLAS level-1.

Our Approach

We introduced in [1] an approach to compute deterministic sums of floating-point numbers. This approach is based on a **multi-level algorithm** that combines efficiently floating-point expansion [2], which are placed in registers, and Kulisch accumulator.

Performance Results

We provided implementations of the multi-level summation scheme on a range of parallel platforms: desktop and server CPUs, the Intel Xeon Phi many-core accelerator, and both NVIDIA and AMD GPUs. We relied on the parallel summation algorithm as well as exact multiplication to develop the fast, accurate, and reproducible implementations of fundamental linear algebra operations such as dot product, triangular solver, and matrix-matrix multiplication. We verified the accuracy of our implementations by comparing the computed results with the ones produced by the multiple precision MPFR library.

Conclusions and Future Work

We presented an approach to achieve correct rounding for the floating-point summation problem, along with implementations on multi- and many-core architectures. This yielded results that are both reproducible and accurate to the last bit at no performance lost. We applied this approach to the other BLAS routines. Even though the performance of triangular solver and matrix product can be argued, their output is consistently reproducible and accurate independently of threads scheduling and data partitioning. We plan to extend this approach to the rest of BLAS routines, derive specific implementations for compute-bound algorithms to be within 10 times performance overhead at most, and perform theoretical analysis of their accuracy.

Acknowledgement

This work undertaken (partially) in the framework of CALSIMLAB is supported by the public grant ANR-11-LAHX-0007-01 overseen by the French National Research Agency (ANR) as part of the “Investissements d’Avenir” program (reference: ANR-11-IDEX-0004-02). This work was also granted access to the HPC resources of ICS financed by Region Île-de-France and the project Equip@Meso (reference: ANR-10-EQPX-05-01).

References


Fig. 2: The summation performance results on an 8-core Intel Xeon E5-2690.  
Fig. 3: Performance scaling on the Moro cluster composed of 64 Intel Xeon E5-2690L nodes.  
Fig. 4: The DTRSV and DGEMM performance results on NVIDIA K5000 and Tesla K20c, respectively.