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Leading order determination of the gluon polarisation from DIS events with high- p_T hadron pairs

C. Adolph^h, M.G. Alekseev^{ab,x}, V.Yu. Alexakhin^g, Yu. Alexandrov^{o,15}, G.D. Alexeev^g, A. Amoroso^{aa}, A.A. Antonov^g, A. Austregesilo^{j,q}, B. Badełek^{ad}, F. Balestra^{aa}, J. Barth^d, G. Baum^a, Y. Bedfer^v, J. Bernhard^m, R. Bertini^{aa}, M. Bettinelli^p, K. Bicker^{j,q}, J. Bieling^d, R. Birsa^x, J. Bisplinghoff^c, P. Bordalo^{l,1}, F. Bradamante^y, C. Braun^h, A. Bravar^x, A. Bressan^{y,*}, E. Burtin^v, D. Chaberny^m, M. Chiosso^{aa}, S.U. Chung^q, A. Cicuttin^z, M.L. Crespo^z, S. Dalla Torre^x, S. Das^f, S.S. Dasgupta^f, O.Yu. Denisov^{j,ab}, L. Dhara^f, S.V. Donskov^u, N. Doshita^{b,af}, V. Duic^y, W. Dünnweber^p, M. Dzierwiecki^{ae}, A. Efremov^g, C. Elia^y, P.D. Eversheim^c, W. Eyrych^h, M. Faessler^p, A. Ferrero^v, A. Filin^u, M. Finger^s, M. Finger jr.^g, H. Fischerⁱ, C. Franco^l, N. du Fresne von Hohenesche^{m,j}, J.M. Friedrich^q, R. Garfagnini^{aa}, F. Gautheron^b, O.P. Gavriltchouk^g, R. Gazda^{ad}, S. Gerassimov^{o,q}, R. Geyer^p, M. Giorgi^y, I. Gnesi^{aa}, B. Gobbo^x, S. Goertz^{b,d}, S. Grabmüller^q, A. Grasso^{aa}, B. Grube^q, R. Gushterski^g, A. Guskov^g, T. Guthörlⁱ, F. Haas^q, D. von Harrach^m, S. Hedickeⁱ, F.H. Heinsiusⁱ, F. Herrmannⁱ, C. Heß^b, F. Hinterberger^c, N. Horikawa^{r,2}, Ch. Höppner^q, N. d'Hose^v, S. Huber^q, S. Ishimoto^{r,3}, O. Ivanov^g, Yu. Ivanshin^g, T. Iwata^{af}, R. Jahn^c, P. Jasinski^m, R. Joosten^c, E. Kabuß^m, D. Kang^m, B. Ketzer^q, G.V. Khaustov^u, Yu.A. Khokhlov^u, Yu. Kisselev^b, F. Klein^d, K. Klimaszewski^{ad}, S. Koblitz^m, J.H. Koivuniemi^b, V.N. Kolosov^u, K. Kondo^{b,af}, K. Königsmannⁱ, I. Konorov^{o,q}, V.F. Konstantinov^u, A. Korzenev^{v,4}, A.M. Kotzinian^{aa}, O. Kouznetsov^{g,v}, M. Krämer^q, Z.V. Kroumchtein^g, F. Kunne^{v,*}, K. Kurek^{ad}, L. Lauserⁱ, J.-M. Le Goff^v, A.A. Lednev^u, A. Lehmann^h, S. Levorato^y, J. Lichtenstadt^w, A. Maggiora^{ab}, A. Magnon^v, N. Makke^{v,y}, G.K. Mallot^j, A. Mann^q, C. Marchand^v, A. Martin^y, J. Marzec^{ae}, T. Matsudaⁿ, W. Meyer^b, T. Michigami^{af}, Yu.V. Mikhailov^u, M.A. Moinester^w, A. Morreale^v, A. Mutter^{i,m}, A. Nagaytsev^g, T. Nagel^q, J.P. Nassalski^{ad,15}, F. Nerlingⁱ, S. Neubert^q, D. Neyret^v, V.I. Nikolaenko^u, W.D. Nowakⁱ, A.S. Nunes^l, A.G. Olshevsky^g, M. Ostrick^m, A. Padee^{ae}, R. Panknin^d, D. Panziereni^{ac}, B. Parsamyan^{aa}, S. Paul^q, E. Perevalova^g, G. Pesaro^y, D.V. Peshekhonov^g, G. Piragino^{aa}, S. Platchkov^v, J. Pochodzalla^m, J. Polak^{k,y}, V.A. Polyakov^u, G. Pontecorvo^g, J. Pretz^d, S.L. Procureur^v, M. Quaresima^l, C. Quintans^l, J.-F. Rajotte^p, S. Ramos^{l,1}, V. Rapatsky^g, G. Reicherz^b, A. Richter^h, E. Rocco^j, E. Rondio^{ad}, N.S. Rossiyskaya^g, D.I. Ryabchikov^u, V.D. Samoylenko^u, A. Sandacz^{ad}, M.G. Sapozhnikov^g, S. Sarkar^f, I.A. Savin^g, G. Sbrizzai^y, P. Schiavon^y, C. Schillⁱ, T. Schlüter^p, K. Schmidtⁱ, L. Schmitt^{q,5}, K. Schönning^j, S. Schopfererⁱ, M. Schott^j, O.Yu. Shevchenko^g, L. Silva^l, L. Sinha^f, A.N. Sissakian^{g,15}, M. Slunecka^g, G.I. Smirnov^g, S. Sosio^{aa}, F. Sozzi^x, A. Srnka^e, M. Stolarski^l, M. Sulc^k, R. Sulej^{ad}, P. Sznajder^{ad}, S. Takekawa^y, J. Ter Wolbeekⁱ, S. Tessaro^x, F. Tessarotto^x, L.G. Tkatchev^g, S. Uhl^q, I. Uman^p, M. Vandenbroucke^v, M. Virius^t, N.V. Vlassov^g, L. Wang^b, R. Windmolders^d, W. Wiślicki^{ad}, H. Wollny^{i,v}, K. Zaremba^{ae}, M. Zavertyaev^o, E. Zemlyanichkina^g, M. Ziembicki^{ae}, N. Zhuravlev^g, A. Zvyagin^p

^a Universität Bielefeld, Fakultät für Physik, 33501 Bielefeld, Germany⁶

^b Universität Bochum, Institut für Experimentalphysik, 44780 Bochum, Germany⁶

^c Universität Bonn, Helmholtz-Institut für Strahlen- und Kernphysik, 53115 Bonn, Germany⁶

^d Universität Bonn, Physikalisches Institut, 53115 Bonn, Germany⁶

^e Institute of Scientific Instruments, AS CR, 61264 Brno, Czech Republic⁷

^f Matrivani Institute of Experimental Research & Education, Calcutta 700 030, India⁸

* Corresponding authors.

E-mail addresses: Andrea.Bressan@cern.ch (A. Bressan), Fabienne.Kunne@cern.ch (F. Kunne).

- ^g Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia⁹
^h Universität Erlangen–Nürnberg, Physikalisches Institut, 91054 Erlangen, Germany⁶
ⁱ Universität Freiburg, Physikalisches Institut, 79104 Freiburg, Germany⁶
^j CERN, 1211 Geneva 23, Switzerland
^k Technical University in Liberec, 46117 Liberec, Czech Republic⁷
^l LIP, 1000-149 Lisbon, Portugal¹⁰
^m Universität Mainz, Institut für Kernphysik, 55099 Mainz, Germany⁶
ⁿ University of Miyazaki, Miyazaki 889-2192, Japan¹¹
^o Lebedev Physical Institute, 119991 Moscow, Russia
^p Ludwig-Maximilians-Universität München, Department für Physik, 80799 Munich, Germany^{6,12}
^q Technische Universität München, Physik Department, 85748 Garching, Germany^{6,12}
^r Nagoya University, 464 Nagoya, Japan¹¹
^s Charles University in Prague, Faculty of Mathematics and Physics, 18000 Prague, Czech Republic⁷
^t Czech Technical University in Prague, 16636 Prague, Czech Republic⁷
^u State Research Center of the Russian Federation, Institute for High Energy Physics, 142281 Protvino, Russia
^v CEA IRFU/SPhN Saclay, 91191 Gif-sur-Yvette, France
^w Tel Aviv University, School of Physics and Astronomy, 69978 Tel Aviv, Israel¹³
^x Trieste Section of INFN, 34127 Trieste, Italy
^y University of Trieste, Department of Physics and Trieste Section of INFN, 34127 Trieste, Italy
^z Abdus Salam ICTP and Trieste Section of INFN, 34127 Trieste, Italy
^{aa} University of Turin, Department of Physics and Torino Section of INFN, 10125 Turin, Italy
^{ab} Torino Section of INFN, 10125 Turin, Italy
^{ac} University of Eastern Piedmont, 1500 Alessandria, and Torino Section of INFN, 10125 Turin, Italy
^{ad} National Center for Nuclear Research and University of Warsaw, 00-681 Warsaw, Poland¹⁴
^{ae} Warsaw University of Technology, Institute of Radioelectronics, 00-665 Warsaw, Poland¹⁴
^{af} Yamagata University, Yamagata 992-8510, Japan¹¹

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ABSTRACT

We present a determination of the gluon polarisation $\Delta g/g$ in the nucleon, based on the longitudinal double-spin asymmetry of DIS events with $Q^2 > 1$ (GeV/c)² including a pair of large transverse-momentum hadrons in the final state. The data were obtained by the COMPASS experiment at CERN using a 160 GeV/c polarised muon beam scattering off a polarised ⁶LiD target. The gluon polarisation is evaluated by a Neural Network approach for three intervals of the gluon momentum fraction x_g covering the range $0.04 < x_g < 0.27$. The values obtained at leading order in QCD do not show any significant dependence on x_g . Their average is $\Delta g/g = 0.125 \pm 0.060$ (stat.) ± 0.063 (syst.) at average $x_g = 0.09$ and a scale of $\mu^2 = 3$ (GeV/c)².

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1. Introduction

The spin structure of the nucleon has been studied in polarised Deep Inelastic lepton–nucleon Scattering (DIS) for many years. The experimental observation by EMC [1] that only a small fraction of the nucleon spin is carried by quark spins has strongly influenced more recent developments of spin physics. Several experiments were performed to confirm this result [2–9]. A number of theoret-

ical ideas were proposed [10] to explain this observation. In order to investigate the origin of the nucleon spin, it is essential to determine the spin fraction carried by gluons. Information about this quantity can be obtained indirectly from scaling violations in the structure function g_1 (see Refs. [8,11,12] and references therein) or from a direct measurement of the gluon polarisation in polarised lepton–nucleon or proton–proton interactions (see Refs. [13–21]).

The leading order virtual photon absorption process (LP) does not provide direct access to the gluon distribution since the virtual photon does not couple directly to the gluon. However, the observation of higher order processes opens a way to determine the gluon helicity distribution. The Photon–Gluon Fusion (PGF) and the QCD Compton scattering processes (QCDC) are shown together with virtual photon absorption in Fig. 1. These two processes are of first order in the strong coupling constant α_S , so their contributions to the DIS cross-section are comparable, but smaller than the virtual photon absorption contribution. Leading order (LO) refers here to all the tree level subprocesses at $\mathcal{O}(\alpha_S^1)$ contributing to hadron production with non-zero p_T , also including the $\mathcal{O}(\alpha_S^0)$ LP, where the hadrons may acquire a non-zero p_T from soft initial or final state radiation.

The cleanest way to tag the PGF process is via open charm production, *i.e.* by selecting charmed mesons in the final state [18]. For this process the contribution from the LP is small because, in the COMPASS kinematic domain, the charm quark content in the nucleon is negligible. Due to the large mass of the charm quark, the contribution from fragmentation processes is also small. However, for the same reason, charm pair production in PGF is suppressed,

¹ Also at IST, Universidade Técnica de Lisboa, Lisbon, Portugal.

² Also at Chubu University, Kasugai, Aichi 487-8501, Japan.

³ Also at KEK, 1-1 Oho, Tsukuba, Ibaraki 305-0801, Japan.

⁴ On leave of absence from JINR Dubna.

⁵ Also at GSI mbH, Planckstr. 1, D-64291 Darmstadt, Germany.

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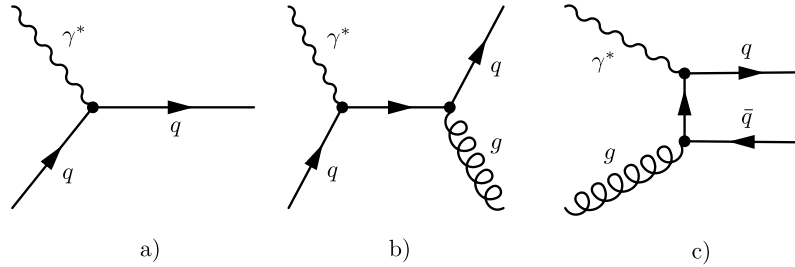


Fig. 1. Feynman diagrams considered for γ^*N scattering: a) Leading order process (LP), b) gluon radiation (QCD Compton scattering), c) photon–gluon fusion (PGF).

so that the statistical precision on the gluon polarisation obtained in this way is limited. A way to overcome this limitation is to tag the PGF process leading to light quark pair production by detecting final state hadrons with large transverse momentum, p_T , with respect to the virtual photon direction.

In the LP, the hadron transverse momentum p_T is due to the intrinsic transverse momentum k_T of quarks in the nucleon [22] and to the fragmentation process, both resulting in small transverse momenta. A different situation occurs for QCDC and PGF processes, in which hadrons mainly acquire transverse momentum from the partons produced in the hard process. For this reason the requirement of observing two hadrons with large transverse momentum enhances the contribution of the PGF process in the selected sample [23]. We present hereafter an analysis using this approach for the enhancement of PGF events in light quark production [24,25].

2. Experimental set-up and data sample

The experiment uses the naturally polarised muon beam at CERN. The experimental set-up consists of two major components: a polarised target and a magnetic spectrometer. A detailed description of the experiment can be found elsewhere [26]. A major upgrade of the COMPASS spectrometer was performed in 2005. For this analysis the most relevant improvement was a new target magnet which extended the angular acceptance.

The average beam muon momentum is 160 GeV/c and the average beam polarisation is $P_b = -0.80 \pm 0.04$. The target consists of two cells in 2002–2004 and of three cells in 2006, located along the beam one after the other and filled with ${}^6\text{LiD}$. Lithium-6 can be regarded as a quasi-free deuteron and a helium-4 core. The average deuteron polarisation $|P_t|$ is about 0.5 and the average dilution factor of the target f is 0.36. The latter is the ratio of the cross-section for all polarisable nucleons in the target material (deuterons) to that for all nucleons and includes radiative corrections. The relative uncertainties of $|P_t|$ and f are 5% and 2%, respectively.

The data were collected during four years: 2002 to 2004 and in 2006. Selected events have an interaction vertex located in the target fiducial volume and contain both a beam muon and a scattered muon. The DIS region is selected by the requirement $Q^2 > 1$ (GeV/c) 2 and by a selection depending on the energy fraction y carried by the exchanged virtual photon, which leads to an invariant mass squared of the hadron system of $W^2 > 5$ (GeV/c) 2 . Events with $y < 0.1$ and with $y > 0.9$ are rejected. The cut at low y rejects events where the spectrometer resolution is worsening, and that may be more sensitive to time instabilities. The events at high y are affected by radiative corrections in the dilution factor, especially in the inclusive asymmetries due to the nuclear composition of the target material, and contain a contribution of decay muons. The above requirements define the inclusive sample. At least two additional charged hadrons associated with the vertex are required for the high- p_T sample. In the analysis the two hadrons with the highest p_T are selected and the following

requirements are applied: $p_{T_1} > 0.7$ GeV/c for the leading hadron, $p_{T_2} > 0.4$ GeV/c for the sub-leading hadron, $x_F > 0$ for the Feynman variables of both hadrons and $z_1 + z_2 < 0.95$, where $z_{1,2}$ is the ratio of the hadron energy to the virtual photon energy. The cut on z removes events originating from exclusive processes. After all cuts, a sample of about 7.3 million events is used in the present analysis.

3. Determination of $\Delta g/g$ from measured asymmetries

The longitudinal double-spin asymmetry for the production of two high- p_T hadrons in the DIS regime can be expressed as a function of the Bjorken scaling variable x_{Bj} :

$$A_{LL}^{2h}(x_{Bj}) = R_{PGF} a_{LL}^{PGF} \frac{\Delta g}{g}(x_g) + R_{LP} D A_1^{LP}(x_{Bj}) + R_{QCDC} a_{LL}^{QCDC} A_1^{LP}(x_C), \quad (1)$$

and all other variables are integrated over the experimental kinematic domain. The leading order inclusive asymmetry A_1^{LP} is given by the ratio of spin-dependent and spin-averaged quark distribution functions (PDFs), weighted by the squared quark electric charges; R_i is the fraction of process i and a_{LL}^i the corresponding analysing power (*i.e.* the asymmetry of the partonic cross-section) [27]. The labels LP, QCDC and PGF refer to the processes presented in Fig. 1. The depolarisation factor D is the fraction of the muon beam polarisation transferred to the virtual photon and depends mainly on y . The variables x_{Bj} , x_g and x_C are the quark momentum fraction, the gluon momentum fraction in the PGF process and the quark momentum fraction in the QCDC process, respectively. Eq. (1) is valid at LO in QCD assuming spin independent fragmentation. A possible spin dependence of fragmentation discussed in Ref. [28] can be neglected in the COMPASS kinematic region.

The evaluation of $\Delta g/g$ from the experimental asymmetry A_{LL}^{2h} using Eq. (1) is possible only when the contributions from background processes (LP, QCDC) can be computed and subtracted. In this analysis, the fractions R_i and the analysing powers a_{LL}^i are extracted from Monte Carlo (MC). Therefore, the analysis requires a precise MC description of the data, so that R_i and a_{LL}^i can be calculated reliably. The asymmetry A_1^{LP} is evaluated from the inclusive lepton–nucleon asymmetry A_{LL}^{incl} . As there are two unknowns in Eq. (1), $A_1^{LP}(x_{Bj})$ and $A_1^{LP}(x_C)$, the asymmetry A_{LL}^{incl} has to be known for these two values of x and can be decomposed in a similar way as A_{LL}^{2h} :

$$A_{LL}^{incl}(x_{Bj}) = R_{PGF}^{incl} a_{LL}^{incl,PGF} \frac{\Delta g}{g}(x_g) + R_{LP}^{incl} D A_1^{LP}(x_{Bj}) + R_{QCDC}^{incl} a_{LL}^{incl,QCDC} A_1^{LP}(x_C). \quad (2)$$

Combining Eqs. (1) and (2) and neglecting small terms (note that the fractions R_{PGF} and R_{QCDC} are much smaller for the inclusive sample than for the high- p_T sample), one obtains the following expression, which allows us to extract $\Delta g/g$:

$$\begin{aligned}
A_{LL}^{2h}(x_{Bj}) &= R_{PGF} a_{LL}^{PGF} \frac{\Delta g}{g}(x_g) \\
&+ \frac{R_{LP}}{R_{LP}^{incl}} \left[A_{LL}^{incl}(x_{Bj}) - A_{LL}^{incl}(x_C) \frac{a_{LL}^{incl, QCDC}}{D} \frac{R_{QCDC}^{incl}}{R_{LP}^{incl}} \right. \\
&- R_{PGF} a_{LL}^{incl, PGF} \frac{\Delta g}{g}(x_g) \left. \right] + \frac{R_{QCDC}}{R_{LP}^{incl}} \frac{a_{LL}^{QCDC}}{D} \left[A_{LL}^{incl}(x_C) \right. \\
&- A_{LL}^{incl}(x'_C) \frac{a_{LL}^{incl, QCDC}}{D} \frac{R_{QCDC}^{incl}}{R_{LP}^{incl}} - R_{PGF} a_{LL}^{incl, PGF} \frac{\Delta g}{g}(x'_g) \left. \right]. \quad (3)
\end{aligned}$$

Here Eq. (2) was used twice, once as given and once with the replacements $x_g \rightarrow x'_g$, $x_C \rightarrow x'_C$ and $x_{Bj} \rightarrow x_C$.

Due to the fact that $\Delta g/g$ is present in Eq. (3) at two different x_g values (denoted x_g and x'_g), the extraction of $\Delta g/g$ requires a new definition of the averaged x_g at which the result is obtained:

$$x_g^{av} = \frac{\lambda_1 x_g - \lambda_2 x'_g}{\lambda_1 - \lambda_2}, \quad \text{where} \quad (4)$$

$$\lambda_1 = a_{LL}^{PGF} R_{PGF} - a_{LL}^{incl, PGF} R_{LP} \frac{R_{PGF}^{incl}}{R_{LP}^{incl}} \quad \text{and}$$

$$\lambda_2 = a_{LL}^{incl, PGF} R_{QCDC} \frac{R_{PGF}^{incl} a_{LL}^{QCDC}}{R_{LP}^{incl} D}. \quad (5)$$

Eq. (4) relies on the assumption of a linear dependence of $\Delta g/g$ upon x_g . The impact of the possible differences between x_g and x'_g as well as between x_C and x'_C on the final $\Delta g/g$ result is taken into account in the systematic uncertainty.

The final relation between the gluon polarisation and A_{LL}^{2h} can be written as:

$$\begin{aligned}
\Delta g/g(x_g^{av}) &= \frac{A_{LL}^{2h}(x_{Bj}) - a^{corr}}{\lambda_1 - \lambda_2}, \quad \text{with} \\
a^{corr} &= A_{LL}^{incl}(x_{Bj}) \frac{R_{LP}}{R_{LP}^{incl}} + A_{LL}^{incl}(x_C) \frac{1}{R_{LP}^{incl}} \left(\frac{a_{LL}^{QCDC}}{D} R_{QCDC} \right. \\
&- \left. \frac{a_{LL}^{incl, QCDC}}{D} R_{QCDC} \frac{R_{LP}}{R_{LP}^{incl}} \right) \\
&- A_{LL}^{incl}(x'_C) \frac{a_{LL}^{incl, QCDC}}{D} \frac{R_{QCDC}^{incl}}{R_{LP}^{incl}} \frac{R_{QCDC}}{R_{LP}^{incl}} \frac{a_{LL}^{QCDC}}{D}. \quad (6)
\end{aligned}$$

In the extraction of $\Delta g/g$ we use a method similar to the one used in Ref. [29]. The target cells are labelled u , d for upstream and downstream. For 2006 the label u refers to the two outer cells and d to the central cell. The material in u and d cells is polarised in opposite directions. Spin orientations are reversed three times per day in 2002–2004 and once per day in 2006 by rotation of the target magnetic field by 180° . Data from before (u , d) and after such a rotation (u' , d') are combined in a so-called spin configuration, where nucleon spins in u and d' (d and u') have the same orientation.

Data from different cells $j = u, d, u', d'$ are combined so that beam flux, apparatus acceptance and spin-averaged cross-section cancel. The gluon polarisation is measured by solving the second order equation:

$$\begin{aligned}
\frac{p_u p_{d'}}{p_{u'} p_d} &= \left[(1 + \langle A_u^{corr} \rangle_w + \langle A_u \rangle_w \Delta g/g(x_g^{av})) \right. \\
&\times (1 + \langle A_{d'}^{corr} \rangle_w + \langle A_{d'} \rangle_w \Delta g/g(x_g^{av})) \left. \right] \\
&\times \left[(1 + \langle A_{u'}^{corr} \rangle_w + \langle A_{u'} \rangle_w \Delta g/g(x_g^{av})) \right.
\end{aligned}$$

$$\times (1 + \langle A_d^{corr} \rangle_w + \langle A_d \rangle_w \Delta g/g(x_g^{av})) \left. \right]^{-1}, \quad (7)$$

where p_j is the sum of event weights w in sample j and $\langle A_j^{corr} \rangle_w$ and $\langle A_j \rangle_w$ are weighted means of $f P_b P_t a^{corr}$ and $f P_b P_t (\lambda_1 - \lambda_2)$, respectively. The weight w in the current analysis is defined as $w = f P_b (\lambda_1 - \lambda_2)$. In this way, $\Delta g/g(x_g^{av})$ is directly obtained, without going through the intermediate step of evaluating the $A_{LL}^{2h}(x_{Bj})$ asymmetry.

In previous analyses of high- p_T events [13,17] only mean values of R_i and a_{LL}^i/D for the three processes were used and the contribution of the leading process was suppressed by requiring the presence of two hadrons with high transverse momenta. Unfortunately, these requirements lead to a severe loss of statistics. In the present analysis, a Bayesian driven Neural Network (NN) approach for the extraction of $\Delta g/g$ is used. It allows the use of loose p_T cuts by dealing simultaneously with the three processes. The NN, trained on a MC sample, assigns to each event a probability to originate from one of these processes, which is then included in the weight w . Events more likely originating from processes other than PGF are kept with a small weight. For a given event, different NNs provide not only the probabilities to originate from a particular process but also the corresponding analysing powers and the momentum fractions x_C and x_g . This approach makes optimal use of the data and avoids biases which may arise from correlations between analysing power and kinematic quantities used to evaluate the asymmetries. The statistical uncertainty of $\Delta g/g$ is reduced by a factor of three comparing with the method used in [13].

4. Monte Carlo optimisation and Neural Network training

In the present analysis the NN package from Ref. [30] is used. Many results derived from a Neural Network approach strongly depend on the Monte Carlo sample on which the NN is trained. Thus, a good description of the experimental data by MC simulations is essential for the analysis.

The unpolarised LEPTO event generator [31] (version 6.5) is used to generate both an inclusive DIS sample and a sample which already contains at least two high- p_T hadrons. The generated events were processed by the detector simulation program COMGEANT and reconstructed in the same way as real events by the reconstruction program CORAL. Finally, the same requirements are used in the analysis of real and MC events.

Prior to the MC generator studies, an extensive effort was made to improve the detector simulation in COMGEANT. The MSTW08LO PDF parametrisation [32] is used in the analysis as it gives reasonable agreement with F_2 measured in the COMPASS kinematic range [33] and is valid down to $Q^2 = 1$ (GeV/c) 2 . Also the F_L function option from LEPTO is used, which improves data-to-MC agreement in the high- y region. Finally, a correction for radiative effects as described in Ref. [34] was introduced.

The description of lepton variables was found to be satisfactory at this stage. For the hadron variables, the Parton Shower (PS) option in LEPTO had to be enabled to improve their description. However, this procedure introduces some inconsistency, since PS simulates higher order effects while the expression of $\Delta g/g$ is derived at LO. The impact of this discordance will be taken into account in the evaluation of systematic uncertainties. In order to further improve the agreement with data for the hadron variables, some parameters describing the fragmentation process in LEPTO were tuned (high- p_T tuning in Table 1). They correspond to the width of the Gaussian p_T distribution (PARJ 21), the shape of the non-Gaussian tail (PARJ 23, PARJ 24) and the symmetric Lund fragmentation function (PARJ 41, PARJ 42). In the optimisation process the parameter PARJ(42), related to the transverse mass dependence

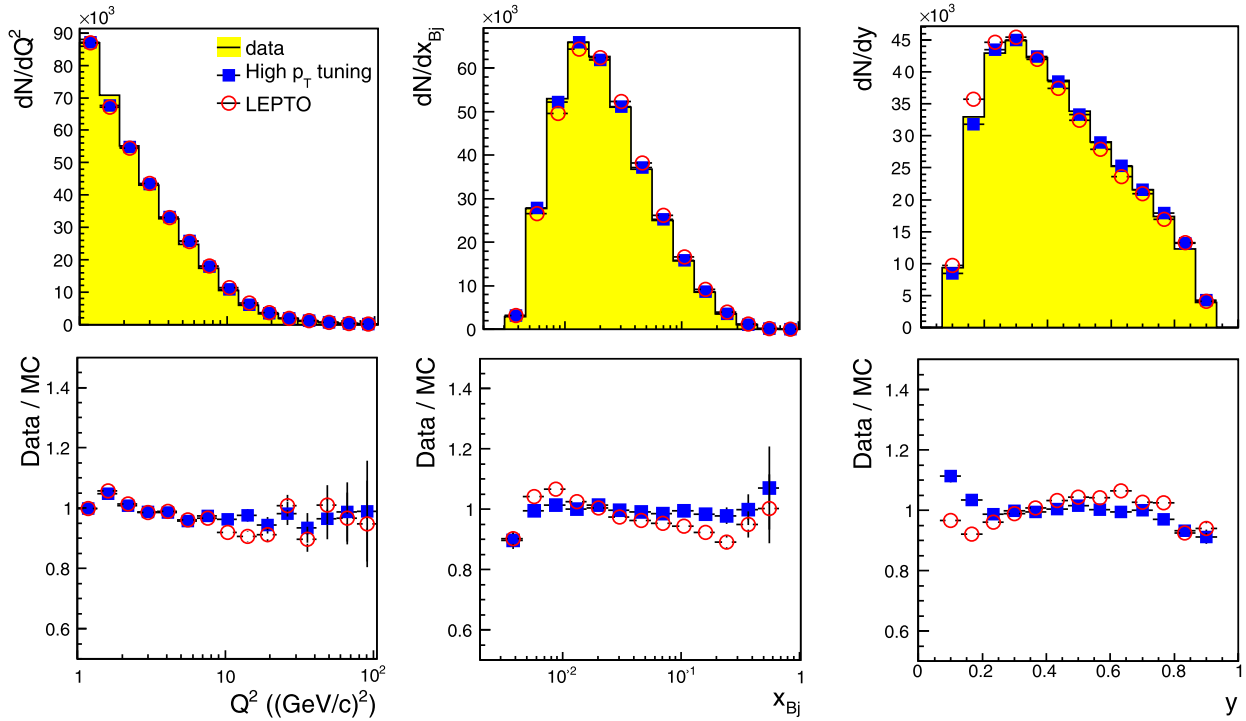


Fig. 2. Comparison between data (histogram) and MC simulations using high- p_T tuning (full squares) and default LEPTO tuning (open circles): distributions and Data/MC ratios for the lepton variables, Q^2 , x_{Bj} and y , normalised to the number of events.

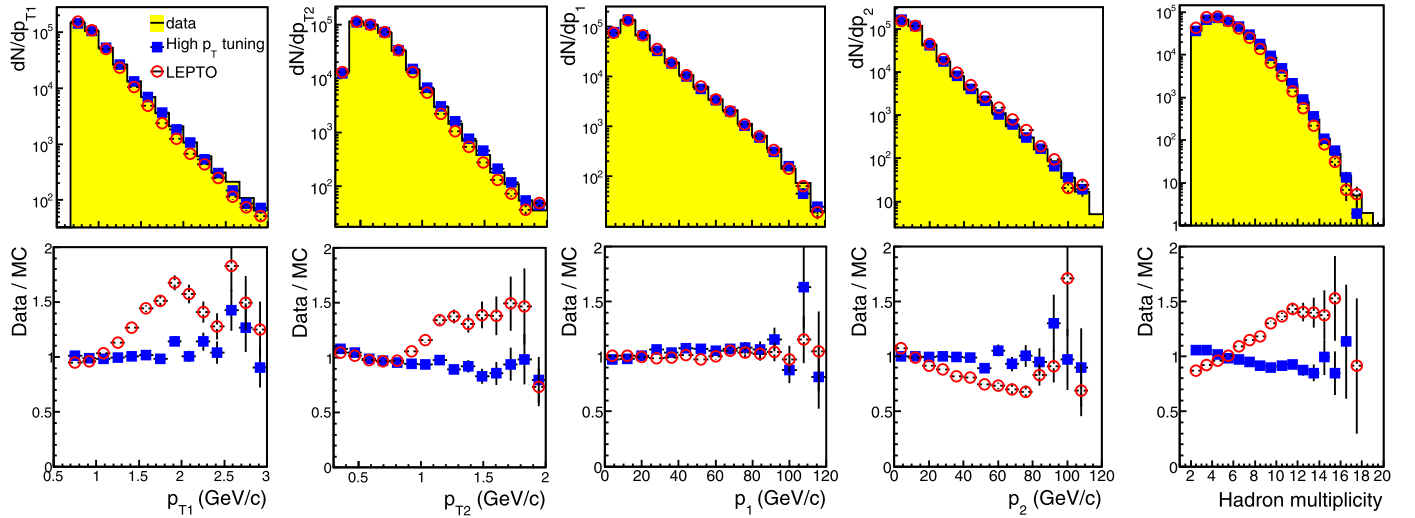


Fig. 3. Comparison between data (histogram) and MC simulations using high- p_T tuning (full squares) and default LEPTO tuning (open circles): distributions and Data/MC ratios for the hadron variables, p_{T1} , p_{T2} , p_1 , p_2 and the hadron multiplicity, normalised to the number of events.

Table 1

Default and tuned values of the LEPTO parameters describing the fragmentation process.

	PARJ 21	PARJ 23	PARJ 24	PARJ 41	PARJ 42
Default tuning	0.36	0.01	2.0	0.3	0.58
High- p_T tuning	0.34	0.04	2.8	0.025	0.075

of the Lund string fragmentation function, is found to be close to 0.10, *i.e.* the value used in the SMC analysis [13]. As a result the fragmentation function peaks at much lower z values than for the default value. In contrast the impact of PARJ(41), which governs the behaviour of the fragmentation function at high z , turned out to be small.

For the lepton variables the comparison of the high- p_T data sample to the MC sample is shown in Fig. 2 both for default LEPTO tuning and high- p_T tuning. Fig. 3 displays the corresponding comparison for the hadron variables; total and transverse momenta p_1 , p_{T1} of the leading and the sub-leading hadron p_2 , p_{T2} and the hadron multiplicity. The normalisation of data and MC in Figs. 2 and 3 is done to the number of events. One observes that MC with high- p_T tuning yields a satisfactory description of all distributions justifying its use to parametrise process fractions and analysing powers.

Several NNs are used to parametrise all needed quantities. For a set of input parameters, the NN is trained to output the corresponding expectation value for a given quantity X . For the inclusive sample the input parameter space is spanned by x_{Bj} and Q^2 ,

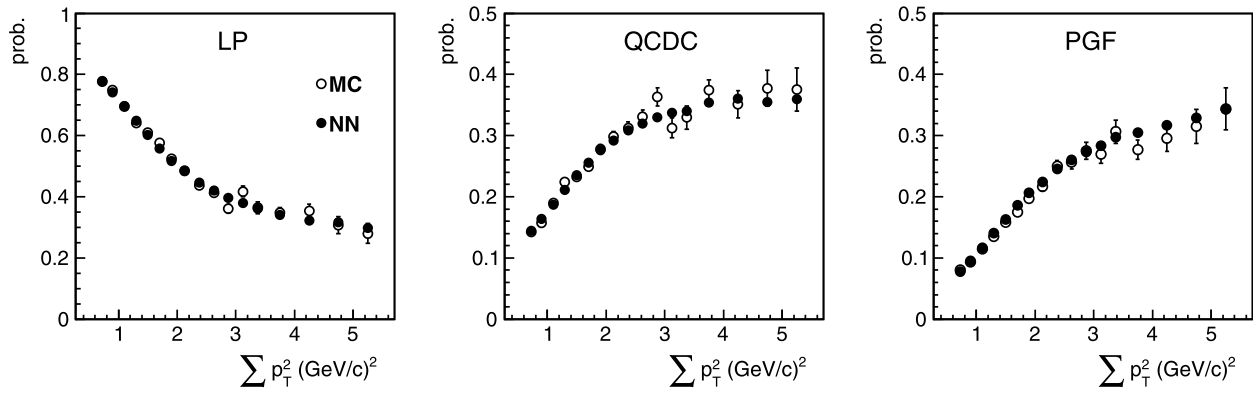


Fig. 4. Values of R_{LP} , R_{QCDC} , R_{PGF} obtained from MC and from NN as functions of $\sum p_T^2$.

while for the high- p_T sample the transverse and longitudinal momenta of the leading and sub-leading hadrons with respect to the virtual photon direction p_{T1} , p_{T2} , p_{L1} , and p_{L2} are used in addition.

An example of the quality of the NN parametrisation is given in Fig. 4. For the same MC sample it shows the probability for LP, QCDC and PGF events as a function of $\sum p_T^2$ ($= p_{T1}^2 + p_{T2}^2$) once as generated and once as obtained from the NN. The NN training was performed on a statistically independent MC sample. A good agreement is observed. While the LP probability reduces with increasing p_T (p_{T1} , p_{T2} and $\sum p_T^2$), QCDC and PGF become the dominant contributions rising with similar strength.

5. Systematic studies

The main contribution to the systematic uncertainty comes from the dependence of the analysis on the MC. In total seven MC samples were prepared with different combinations of fragmentation parameters tuning (default LEPTO or high- p_T), ‘PS on’ or ‘PS off’, different choices of the PDFs (MSTW08LO or CTEQ5L [35]) and F_L from LEPTO or from the $R = \sigma_L/\sigma_T$ parametrisation of Ref. [36]. These MC samples predict fractions of the PGF process in the high- p_T data sample differing by up to 50%. As a result both the value of $\Delta g/g$ and its statistical uncertainty differ for different MC samples. In addition to what was already discussed, it is worth mentioning that for ‘PS on’ and ‘PS off’ different so-called cut-off schemes were used to prevent divergences in the cross-section calculations in LEPTO (see Ref. [31]). These schemes and their parameters are quite important since their choice does not affect the data-to-MC comparison but changes the fraction of, e.g. PGF events. So, while keeping the default cut-off parameters proposed by the authors of Ref. [31], we tested various cut-off schemes.

A small RMS value of 0.020 was found for the $\Delta g/g$ values obtained from these seven MC samples. However, it turned out that the asymmetry obtained from Eq. (7) under the assumption that $A_i^{\text{corr}} = 0$, is within less than a half of the statistical uncertainty consistent with zero, and so the above RMS may underestimate the systematic uncertainty related to MC. In order to avoid this, we consider in addition how the statistical uncertainty of $\Delta g/g$ changes for various MC tunings. This leads to $\delta(\Delta g/g)_{\text{MC}} = 0.045$.

The uncertainties of $\Delta g/g$ due to the choice of the A_1^d parametrisation and to the NN stability were found to be small, $\delta(\Delta g/g)_{A_1^d} = 0.015$ and $\delta(\Delta g/g)_{\text{NN}} = 0.010$. The uncertainties of f , P_b , and P_t have an even smaller impact on the final result: $\delta(\Delta g/g)_{f, P_b, P_t} = 0.004$. The HERMES results [37] suggest that for heavier nuclei the dilution factor depends upon the transverse momentum of hadrons. Tests were performed to check the

dN/dp_{T1} dependence for the ${}^6\text{LiD}$ target as compared to helium, the medium in which the target material is immersed. No such dependence is observed. On average COMPASS measures at significant higher photon energies as compared to HERMES, i.e. in a range from 20 to 140 GeV, similar to that of the EMC experiment, where no significant dependences were found.

False asymmetries appear if the acceptance ratio of neighbouring target cells is different for the data taken before and after field reversal. They were searched for in a sample in which the event selection cuts were relaxed to $p_{T1,2} > 0.35$ GeV/c and $Q^2 > 0.7$ (GeV/c) 2 . This leads to a large increase in statistics and allows for more precise studies of the spectrometer stability. No false asymmetries exceeding the statistical uncertainty were found. Taking the statistical uncertainty as limit for the false asymmetries one obtains $\delta(\Delta g/g)_{\text{false}} = 0.019$.

The two different values χ_C and χ'_C appearing in Eq. (3) were assumed to be equal. Two tests were done to check the systematic effect of this assumption. In the first one, $\chi'_C = 1.6 \cdot \chi_C$ was assumed, the value 1.6 being an estimate taken from MC. In the second one, the NN parametrisation of χ_C was used with the previously obtained χ_C as input parameter instead of χ_{Bj} . This leads to an uncertainty in $\Delta g/g$ of 0.035. Similar tests performed for χ_g and χ'_g changed χ_g^{av} by less than 0.01.

The expression used for the calculation of a_{LL} assumes that the quarks are massless. This assumption is not valid for strange quarks. Tests were performed excluding kaons from the data sample, or making a parametrisation of the NN based on events with pions only. The final results are found to be stable within statistical fluctuations. The impact of the non-zero k_T used in the simulation has also a negligible effect on a_{LL} , which are calculated using collinear pQCD. The k_T is only a small addition to the p_T of the parton produced in the PGF or QCDC processes. In addition, while a_{LL} varies from -0.8 to $+0.5$ as a function of Q^2 , the full variation in p_T over the measured range is about 0.1.

The impact of resolved photon processes on the extracted value of $\Delta g/g$ was studied using the RAPGAP generator [38]. It was found that events originating from resolved photons are expected to have very different kinematic distributions with respect to our standard high- p_T sample. It was checked whether adding an admixture of events originating from resolved photon processes would change the MC description of the data. The results show that the contribution from resolved photons in our kinematic range is negligible.

The contributions to the systematic uncertainty and their quadratic sum are presented in Table 2. They were also evaluated separately in the three χ_g bins of Table 3. The total systematic uncertainty of the overall $\Delta g/g$ result is obtained as 0.063, which is slightly larger than the statistical uncertainty.

Table 2
Summary of the contributions to the systematic uncertainty of $\Delta g/g$.

$\delta(\Delta g/g)$	x_g range			
	[0.04, 0.27]	[0.04, 0.12]	[0.06, 0.17]	[0.11, 0.27]
MC simulation	0.045	0.077	0.067	0.129
Inclusive asymmetry A_1^d	0.015	0.021	0.014	0.017
NN parametrisation	0.010	0.010	0.010	0.010
f, P_b, P_t	0.004	0.007	0.007	0.010
False asymmetries	0.019	0.023	0.016	0.012
$x_C = x'_C$ in Eq. (3)	0.035	0.026	0.039	0.057
Total systematic uncertainty	0.063	0.088	0.081	0.143

Table 3
Summary of the $\Delta g/g$ results and their errors.

	x_g range			
	[0.04, 0.27]	[0.04, 0.12]	[0.06, 0.17]	[0.11, 0.27]
x_g^{av}	0.09	0.07	0.10	0.17
$\Delta g/g$	$0.125 \pm 0.060 \pm 0.063$	$0.147 \pm 0.091 \pm 0.088$	$0.079 \pm 0.096 \pm 0.081$	$0.185 \pm 0.165 \pm 0.0143$

6. Results and conclusions

The values of $\Delta g/g$ provided by Eq. (7) were extracted for every spin configuration separately¹⁶ in order to reduce systematic uncertainties. A correction for the probability of the deuteron to be in a D-wave state [39] was applied. The mean values for each year of data taking are shown in Fig. 5. They are compatible within their statistical uncertainties and average to

$$\Delta g/g = 0.125 \pm 0.060 \text{ (stat.)} \pm 0.063 \text{ (syst.)} \quad (8)$$

at $x_g^{\text{av}} = 0.09$ and a scale of $\mu^2 = 3 \text{ (GeV/c)}^2$.

The data cover the range $0.04 < x_g < 0.27$ and were divided into three statistically independent subsamples in x_g as given by the NN. The correlation between the generated x_g and the one obtained from the NN is about 62%. The results do not show any significant dependence of $\Delta g/g$ on x_g (Table 3).

These results are compared with previous LO evaluations of $\Delta g/g$ based on high- p_T hadron events in Fig. 6. The value taken from Ref. [17] is also derived from COMPASS data, however in the quasi-real photoproduction process instead of DIS. The hard scale and the range of gluon momentum are almost the same as in the present analysis and the two values of $\Delta g/g$ are compatible within their statistical uncertainties. The $\Delta g/g$ value obtained in the LO open-charm analysis [40] at a higher scale $\mu^2 = 13 \text{ (GeV/c)}^2$ is also shown. The SMC results from high- p_T hadron pairs with $Q^2 > 1 \text{ (GeV/c)}^2$ [13] and the HERMES results from high- p_T single hadrons using all Q^2 [14] are compatible with the present results.

The $\Delta g/g$ curves shown in Fig. 6 are the results of global fits to spin asymmetries in inclusive and semi-inclusive DIS [41] and also to asymmetries from polarised proton–proton scattering [42]. They were obtained at NLO in QCD and are thus not directly comparable with the LO result of the present analysis. It is however interesting to note that they all point to low values of $\Delta g/g$ for $x_g \leq 0.20$.

A direct measurement of the gluon polarisation, extracted in the leading order approximation, was performed on all COMPASS data taken with a longitudinally polarised ⁶LiD target. The gluon polarisation $\Delta g/g$ is extracted from a large sample of DIS events with $Q^2 > 1 \text{ (GeV/c)}^2$ including a pair of high- p_T hadrons. Although asymmetries A_{LL}^{2h} are not used directly in the $\Delta g/g$ ex-

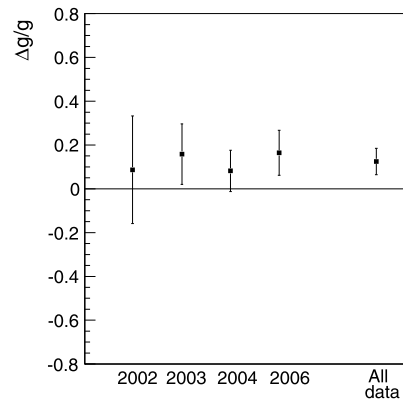


Fig. 5. Year by year $\Delta g/g$ result and final average value.

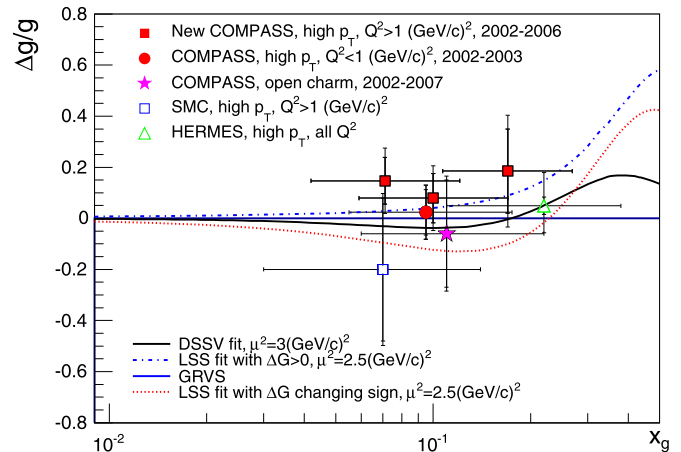


Fig. 6. Comparison of the final $\Delta g/g$ with previous results (see text); the NLO curves are from Refs. [41,42].

¹⁶ One configuration usually corresponds to 16 h (2 days) of data taking in 2002–2004 (2006).

traction method described in this Letter, we present them in Appendix A in a few bins of x_{Bj} and $\sum p_T^2$. A novel method using neural networks reduced the statistical uncertainty of the result and allowed for the first time an evaluation of the gluon polarisation in three bins of the gluon momentum fraction x_g .

Table 4
 A_{LL}^{2h}/D asymmetries as a function of x_{Bj} and $\sum p_T^2$.

x_{Bj}	$p_{T_1}^2 + p_{T_2}^2$ (GeV/c) ²	$\langle x_{Bj} \rangle$	$\langle Q^2 \rangle$ (GeV/c) ²	$\langle p_{T_1}^2 + p_{T_2}^2 \rangle$ (GeV/c) ²	A_{LL}^{2h}/D
0.004–0.01	0.65–1.0	0.007	1.4	0.86	0.002 ± 0.011
0.004–0.01	1.0–2.0	0.007	1.4	1.35	–0.002 ± 0.009
0.004–0.01	2.0–3.0	0.007	1.4	2.39	–0.019 ± 0.020
0.004–0.01	3.0–4.0	0.007	1.4	3.41	–0.075 ± 0.037
0.004–0.01	4.0–	0.007	1.5	5.45	0.001 ± 0.045
0.01–0.02	0.65–1.0	0.014	2.4	0.86	–0.009 ± 0.012
0.01–0.02	1.0–2.0	0.014	2.4	1.35	–0.016 ± 0.010
0.01–0.02	2.0–3.0	0.014	2.5	2.39	0.007 ± 0.024
0.01–0.02	3.0–4.0	0.014	2.6	3.41	0.054 ± 0.045
0.01–0.02	4.0–	0.014	2.7	5.48	–0.033 ± 0.056
0.02–0.05	0.65–1.0	0.030	4.8	0.85	0.015 ± 0.016
0.02–0.05	1.0–2.0	0.030	5.0	1.35	0.018 ± 0.013
0.02–0.05	2.0–3.0	0.030	5.3	2.39	0.056 ± 0.031
0.02–0.05	3.0–4.0	0.030	5.5	3.41	0.054 ± 0.057
0.02–0.05	4.0–	0.031	5.9	5.52	0.066 ± 0.068
0.05–0.10	0.65–1.0	0.069	10.9	0.85	0.074 ± 0.029
0.05–0.10	1.0–2.0	0.068	11.4	1.35	0.038 ± 0.025
0.05–0.10	2.0–3.0	0.069	12.2	2.39	0.051 ± 0.057
0.05–0.10	3.0–4.0	0.068	12.9	3.40	–0.079 ± 0.105
0.05–0.10	4.0–	0.069	13.6	5.67	–0.087 ± 0.123
0.10–1.00	0.65–1.0	0.170	28.2	0.85	0.100 ± 0.043
0.10–1.00	1.0–2.0	0.172	29.9	1.35	0.143 ± 0.036
0.10–1.00	2.0–3.0	0.172	31.7	2.39	–0.037 ± 0.083
0.10–1.00	3.0–4.0	0.158	29.0	3.41	–0.191 ± 0.156
0.10–1.00	4.0–	0.168	32.8	5.67	0.593 ± 0.180

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Appendix A. A_{LL}^{2h} asymmetries

Using the same data sample entering this analysis, *i.e.* with the same event selection used for the $\Delta g/g$ analysis, we have evaluated also the A_{LL}^{2h} asymmetries in a 2-dimensional 5×5 binning in x_{Bj} and $\sum p_T^2$; the results are shown in Table 4. Typically A_{LL}^{2h} is given as a function of $\sum p_T^2$, since, as the transverse momentum p_T of the hadrons grows, an increase of contributions from higher order processes like PGF and QCDC is expected; however for the high- p_T analysis of $Q^2 > 1$ (GeV/c)² the asymmetry A_{LL}^{incl} (needed for the extraction of $\Delta g/g$) strongly depends upon x_{Bj} and, similarly, the analysing power a_{LL}/D has a strong Q^2 dependence, going from -0.8 to $+0.5$ in the range of our measurement (and the average Q^2 is growing with increasing x_{Bj}). As a result without an additional binning in x one can easily bias the $\Delta g/g$ extraction from A_{LL}^{2h} . These asymmetries are extracted with the 2nd order weighted method [24,25], with an event selection optimised for the extraction of $\Delta g/g$ and not for the measurement of the asymmetries. The systematic checks performed have shown no presence of systematic effects within the statistical error. As a result a systematic error smaller than the statistical one can be assumed for this measurement.

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