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Chaotic vortex induced vibrations

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This study investigates the nature of the dynamic response of an elastically mounted cylinder immersed in a free stream. A novel method is utilized, where the motion of the body during a free vibration experiment is accurately recorded, and then a second experiment is conducted where the cylinder is externally forced to follow this recorded trajectory. Generally, the flow response during both experiments is identical. However, particular regimes exist where the flow response is significantly different. This is taken as evidence of chaos in these regimes.

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This letter presents the results of an investigation of the dynamic response of an elastically mounted cylinder immersed in a free stream. In particular, the focus is on the identification of low-dimensional chaos in the upper branch flow regime^{1,2} of vortex-induced vibration (VIV). For the dynamically more complicated case of a flexible cylinder, chaos has been identified as a generic feature of the response,³ Hover, Techet, and Triantafyllou⁴ and Hover⁵ show experimental evidence of low spanwise correlation and high levels of disorder in the upper branch, and three-dimensional simulations from Lucor, Foo, and Karniadakis⁶ show a variation in the organization of the vortices along the span.

Morse and Williamson⁷ used data from experiments on an externally controlled sinusoidally oscillating cylinder to construct a low-order model of the interaction between the body and flow in the upper branch. It was concluded that the upper branch could consist of slow variation between the 2S and $2P_o$ vortex shedding modes or intermittent switching between the $2P_o$ and 2P modes. The mode naming follows the convention outlined in Williamson and Roshko.⁸ The 2S mode consists of two single vortices shed per oscillation cycle, the 2P mode consists of two pairs of vortices shed per oscillation cycle, and the $2P_o$ mode consists of two pairs of vortices per oscillation cycle where the second vortex of each pair is much weaker than the first. A map of the occurrence of these modes produced by Morse and Williamson,⁷ along with results from fully coupled experiments, is shown in Figure 1. The results of the current study augment and extend the conclusions of Morse and Williamson⁷ regarding the interaction of these modes in the upper branch.

A defining feature of low-dimensional chaos is the rapid divergence of trajectories in phase space that initially start close together. For an elastically mounted circular cylinder, it is often useful to consider the system as two coupled oscillators; one is the elastically mounted body, the other is the wake. The body motion is one phase space parameter, and a scalar representing the wake (often the lift force) can be used as another. If low-dimensional chaos is present, small perturbations to one parameter (the body motion) should result in large deviations of the other (the lift force).

In this system, the fluid and the structure are coupled by the fact that the fluid velocity must be equal to the velocity of the cylinder at its surface. The cylinder motion is driven by the fluid forcing on the body, which comes from integrating the pressure and shear stresses of the fluid on the cylinder surface.

The dependence of the lift force on the cylinder velocity \dot{y} , and therefore the cylinder displacement y, means that whether y follows a trajectory governed by the coupled system or is somehow

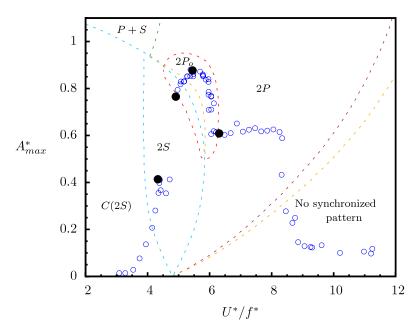


FIG. 1. Plot of the amplitude response of a freely vibrating circular cylinder with $m^* = 2.66$, with an overlay of the map of the wake regimes by Morse and Williamson.⁷ The open circles represent the maximum amplitude at each normalized wavelength value of $\lambda^* = U^*/f^*$, where f^* is the normalized frequency close to the natural frequency of the system. The black solid symbols represent the locations where controlled motion experiments are conducted for comparison. The boundaries between the wake modes of Morse and Williamson⁷ are indicated by the dashed lines.

externally controlled, is unimportant. A particular trajectory y will result in a particular flow and lift force history. However if the flow is chaotic, even infinitesimally small perturbations to this trajectory y will result in large changes in the lift force history.

Here, this relationship is tested explicitly. Free vibration experiments have been conducted and the trajectory y accurately recorded at a sampling frequency of 1000 Hz. Following these, a second set of experiments has been conducted, where the motion recorded during the free vibration experiments has been fed back to a highly accurate motion control system, forcing the cylinder to follow the same trajectory as during the free vibration experiments. The results show that generally, the forces recorded during the free vibration and controlled motion experiments are very similar. However, for a case where the cylinder response is in the upper branch, a major deviation is recorded. This deviation is indicative of the presence of chaos, as any error in the y trajectory from the free vibration experiment results in diverging trajectories.

The experiments were conducted in a free-surface recirculating water channel with a test section of 4000 mm in length, 600 mm in width and, 800 mm in depth.

For the free vibration experiments, a test rigid circular cylinder was vertically mounted on a low-friction air bearing system which was placed on top of the water channel, allowing linear oscillatory movement of the cylinder transverse to the free-stream. Full details of this air bearing setup, control of end conditions, and the facility in general can be found in Nemes *et al.*⁹ and Zhao *et al.*¹⁰

The test cylinder used was a carbon fibre tube having an outside diameter of D = 25 mm and a wall thickness of 1.5 mm. The immersed length of the body was L = 620 mm, giving an aspect ratio of L/D = 24.8 and a displaced water mass of $m_d = \pi D^2 L/4 = 306.2$ g. The total mass of the oscillating system was m = 813.2 g, resulting in a mass ratio of $m^* = m/m_d = 2.66$. Such a low mass ratio is required for the upper branch to occur.¹¹

Free decay tests were conducted individually in air and quiescent water to measure the natural frequencies of the system, $f_{na} = 0.874$ Hz in air and $f_{nw} = 0.740$ Hz in quiescent water. The structural damping ratio with consideration of the added mass effect was found to be $\zeta = c/$

 $(2\sqrt{k(m+m_A)}) = 2.74 \times 10^{-3}$, where *c* is the structural damping coefficient, resulting in a low massdamping ratio of $m^{*}\zeta = 7.28 \times 10^{-3}$, where $m_A = m_d$. The independent parameter of the reduced velocity was defined as $U^{*} = U/(f_{nw}D)$, where *U* is the freestream velocity. The dynamic response of free VIV was investigated over a range of $2.5 < U^{*} < 15$ (1450 < Re < 7500).

Shown in Figure 1 is the amplitude response of the free vibration tests plotted in an amplitudewavelength plane overlaid on the map of wake regimes from Morse and Williamson⁷ for a cylinder undergoing sinusoidal forced oscillations. For comparison, the wavelength of free vibration is given by $\lambda^* = U^*/f^*$, where f^* is the normalized predominant oscillation frequency. The classic feature delimiting the upper and lower branches is the high and (relatively) low amplitudes of the oscillation in each branch, and this difference is clearly shown in Figure 1.

Four cases were selected for comparison with controlled motion experiments, and they are marked by the black solid symbols on Figure 1. These cases were selected to test the response in each of the major response regimes of VIV. One case is on the initial branch ($U^* = 4.09$), one at the very beginning of the upper branch ($U^* = 4.93$), one in the middle of the upper branch close to where the maximum amplitude is recorded ($U^* = 5.91$), and one at the beginning of the lower branch ($U^* = 6.10$).

In the controlled motion experiments, a real-time feedback closed-loop motion control system was employed to drive the test cylinder. This control system consisted of a hardware-in-theloop (HIL) control board (model: Q4, Quanser, Inc., Canada) embedded in a personal computer (PC) desktop, running on a combined software platform of MATLAB R2010a & Simulink and Real-Time Windows Target (MathWorks), and QUARC 2.1 (Quanser, Inc., Canada). The motion plant consisted of a digital servo drive (model: DPRANIE-015A400, Advanced Motion Controls, USA), a brushless DC rotary motor (model: SM231AL-NMSN, Parker Hannifin, USA) with high resolution incremental encoder feedback device (5000 pulses per revolution or 20000 counts per revolution post quadrature) attached to a linear ball-screw actuator (12.7 mm in lead and 150 mm in stroke, model: ERS50-B02LA20-FSR150-A, Parker Hannifin, USA). The feedback control algorithm used was a Proportional-Integral-Derivative (PID) method,¹² which resulted in motion tracking errors within $\pm 5 \ \mu m \ (0.0002D)$. Errors in the velocity and acceleration could be momentarily large (around 30% of the intended instantaneous value), particularly when the actuator changed direction. However, the error in the velocity was typically less than 5% of the intended instantaneous value, while the error in the acceleration was typically less than 10% of the intended instantaneous value.

Full details of the measurement techniques employed for the cylinder displacement, the transverse lift force, and the flow vorticity fields in the near wake of the body can be found in Zhao et al.¹⁰

Figure 2 shows time histories of the cylinder trajectory and the lift force for both the free vibration and controlled motion experiments for each of the four test cases. The most pertinent result shown in Figure 2 is the time history of the lift force for $U^* = 5.91$. While all the other cases show a near-perfect match between the force history of the free vibration and controlled motion experiments, this one shows a significant deviation. The magnitude and frequency are similar, however there is a clear difference in the phase of the two signals. This mismatch leads to the conclusion that the flow is chaotic in the middle of the upper branch.

It should also be noted that the case at the beginning of the upper branch ($U^* = 4.93$) shows no evidence of chaos. In fact, this case oscillates periodically, with a 2S wake mode. This periodic oscillation in the 2S mode in the upper branch is in contrast to the results presented in Govardhan and Williamson² that show a $2P_o$ mode over the entire branch. Morse and Williamson⁷ also concluded from controlled sinusoidal motion experiments that the 2S mode should only occur in competition with the $2P_o$ mode in the upper branch. It is possible that this stable regime of the 2S mode occurs over a very small range of U^* , or that the fully coupled oscillation departs (even very slightly) from purely sinusoidal, allowing the 2S mode to become stable.

To further investigate the apparent chaos in the middle of the upper branch, Figure 3 presents portions of the time histories of the total phase ϕ_{total} and the vortex phase ϕ_{vortex} for the free vibration and controlled motion experiments for the case in the middle of the upper branch ($U^* = 5.93$). The total phase ϕ_{total} is defined as the phase difference between the lift force and the cylinder

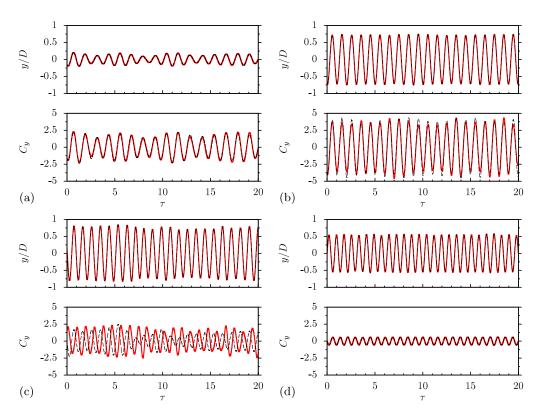


FIG. 2. Time histories in terms of periods of oscillation (τ) of cylinder displacement y/D for free vibration (black dashed line) and controlled motion (red solid line) and the lift coefficient C_y for free vibration (black dashed line) and controlled motion (red solid line), for (a) $U^* = 4.09$ (initial branch), (b) $U^* = 4.93$ (beginning of upper branch), (c) $U^* = 5.91$ (middle of upper branch) and (d) $U^* = 6.10$ (lower branch). Only the case in the middle of the upper branch (figure (c)) shows a discrepancy between the lift force of the free vibration and controlled motion experiments.

displacement, whereas the vortex phase ϕ_{vortex} is defined as the phase between the vortex lift force and the cylinder displacement. The vortex force is defined using the method of Lighthill¹³ and can be thought of as the force due to vortex shedding. The instantaneous values of ϕ_{total} and ϕ_{vortex} were found by finding the instantaneous value of phase of the force and displacement signals using a Hilbert transform and subtracting the phase of the force from the phase of the displacement.

Govardhan and Williamson,² Carberry, Sheridan, and Rockwell,¹⁴ and Morse and Williamson⁷ have shown that the values of ϕ_{total} and ϕ_{vortex} are linked to the wake mode present. The 2S mode has $\phi_{total} \simeq \phi_{vortex} \simeq 0^{\circ}$, the 2P_o mode has $\phi_{total} \simeq 0^{\circ}$ and $\phi_{vortex} \simeq 180^{\circ}$, and the 2P mode has $\phi_{total} \simeq \phi_{vortex} \simeq 180^{\circ}$.

Using these definitions, the phase history presented in Figure 3 shows that the free vibration case in the middle of the upper branch switches between the 2S and $2P_o$ wake modes, as suggested by Morse and Williamson.⁷ However during the controlled motion experiment, the flow switches between the 2S, $2P_o$, and 2P wake modes. Phase averaged PIV images of these wake modes are also presented in Figure 3. The PIV images were obtained on a plane z/D = 4.5 from the cylinder free end. Previous results from Hover, Techet, and Triantafyllou⁴ and Hover⁵ have shown that the wake mode can be different at the same instant at different points along the cylinder. It is possible that this occurred during the current experiments. However, sampling at z/D = 4.5 from the cylinder end (where a platform technique was used to mitigate the impact of the channel boundary layer) should provide a clear picture of the modes present and the amount of time the flow spends in each mode. The snapshots used to construct each image were selected based on the phase history, e.g., the images for the 2S mode were selected from instants where $\phi_{total} \simeq \phi_{vortex} \simeq 0$. The similarities between the 2S and $2P_o$ modes from both the free vibration and controlled motion experiments are clear. However, the appearance of the 2P mode in the controlled motion experiments only is also

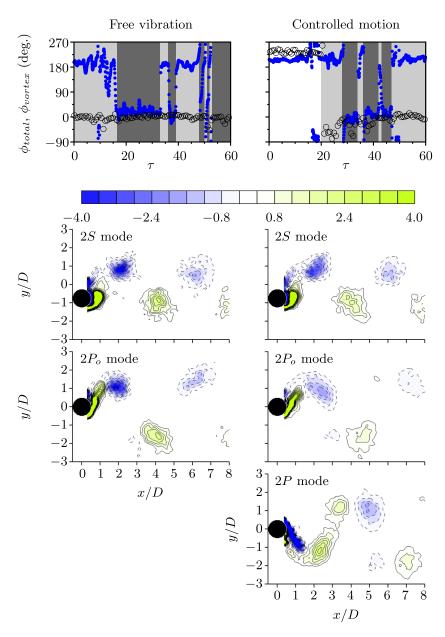


FIG. 3. Upper: total phase ϕ_{total} (black open circles) and vortex phase ϕ_{vortex} (blue solid circles) for the free vibration and controlled motion case in the middle of the upper branch ($U^* = 5.91$). Evidence of switching between two wake modes (2S and $2P_o$ modes) is found during free vibration, while evidence of switching between three wake modes (2S, $2P_o$, and 2P modes) is found in the corresponding controlled motion experiment. The background of segments of each mode are shaded: 2S (dark grey), $2P_o$ (light grey), 2P (white). Lower panes show images of the wake modes constructed via phase averaging. The vorticity contour levels shown are normalized by $\omega_z^* = \omega_z D/U$.

clear. These distinct modes and the apparent sudden switching between them illustrated by the time histories of ϕ_{total} and ϕ_{vortex} are evidence of chaos via mode competition. The competition between these modes for oscillations of the typical amplitude and frequency experienced in the upper branch is consistent with the data from the wake mode map presented by Morse and Williamson⁷ and shown in Figure 1.

Further evidence of chaos via mode competition is found by looking at the time the flow spends in each mode. The presence of each mode at a given instant can be determined using the relationship between the instantaneous total and vortex phases outlined above. To further simplify, the phases

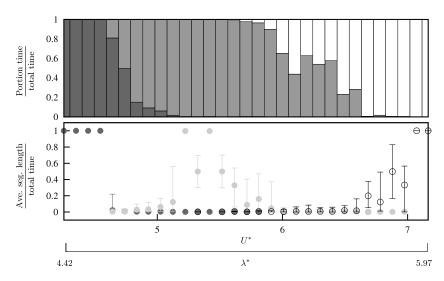


FIG. 4. (a) A histogram of the portion of time spent in each of the modes $2S(\square)$, $2P_o(\square)$, and $2P(\square)$ in the upper branch during free vibration experiments. The flow moves from a 2S mode, to a mix of 2S and $2P_o$, to a mix of $2P_o$ and 2P, to a 2P mode in the lower branch. (b) Mean (marked by points), minimum, and maximum segment lengths (marked by range bars) of the modes $2S(\bullet)$, $2P_o(\bullet)$, and $2P(\circ)$. For cases in the middle of the upper branch that spend almost all of their time in the $2P_o$ mode, the flow does not settle to a stable periodic oscillation.

have been binned into two classes, i.e., a phase in the range $-90^{\circ} < \phi \le 90^{\circ}$ is treated as $\phi = 0^{\circ}$ and a phase in the range $90^{\circ} < \phi \le 270^{\circ}$ is treated as $\phi = 180^{\circ}$. Each instant can then be classified as belonging to the 2*S*, 2*P*_o, or 2*P* mode, as indicated by the shaded regions in the example time series presented in Figure 3.

Figure 4 presents data from 300*s*-long segments of time histories for free vibration cases over a range of U^* in the upper branch. Figure 4(a) presents a stacked histogram of the time spent in each mode as a fraction of the total length of the 300*s* segment as a function of U^* . The plot shows that initially the flow is in the 2*S* mode practically all the time. Increasing U^* sees a regime where the flow switches between the 2*S* and 2*P*_o modes, with the proportion of time in the 2*P*_o mode increasing with increasing U^* . Around the middle of the upper branch, the flow switches between the 2*P*_o mode practically all the time. Further increasing U^* sees a regime where the flow switches between the 2*P*_o mode the middle of the upper branch, the flow switches between the 2*P*_o mode practically all the time. Further increasing U^* sees a regime where the flow switches between the 2*P*_o mode the practically all the time. Further increasing U^* sees a regime where the flow switches between the 2*P*_o mode the practically all the time. Further increasing U^* sees a regime where the flow switches between the 2*P*_o mode increasing with increasing U^* . With the proportion of time in the 2*P* mode increasing U^* . With the transition to the lower branch, the flow remains permanently in the 2*P* mode.

Figure 4(b) shows the mean, minimum, and maximum segment lengths as a proportion of the total time for each mode as a function of U^* . As expected from Figure 4(a), initially the average segment length of the 2S mode is the whole measurement time. At high values of U^* in the lower branch, the average segment length of the 2P mode is practically the whole measurement time. However, in the middle of the upper branch which is dominated by the $2P_o$ mode, the $2P_o$ segment lengths can still be quite variable, indicated by an average segment length of less than 1 and a significant variation between the minimum and maximum segment lengths. This indicates that the $2P_o$ mode is never seen as a completely stable periodic state.

The overall picture presented by Figure 4 is that at the beginning of the upper branch, the dynamics are governed by a competition between the 2S and $2P_o$ modes. At the end of the upper branch, the dynamics are governed by a competition between the $2P_o$ and 2P modes. This may go some way to explaining why all three modes are found in the controlled motion experiment—small deviations from the free vibration trajectory cause the flow to visit some regions of parameter space where there is $2S-2P_o$ competition and others where there is $2P_o-2P$ competition.

To conclude, the argument for the appearance of chaos in the middle of the upper branch is summarized. Experiments were performed where the recreated trajectory matched the free vibration trajectory to within $\pm 5 \ \mu m \ (0.0002D)$. Only for the case in the middle of the upper branch were differences in the force recorded, the large change due to a small perturbation indicative of chaos.

Further evidence for chaos due to mode competition is that in the middle of the upper branch the flow switches between at least two distinct wake modes. Mode competition and switching were implied by Morse and Williamson.⁷ Here, it has been shown there are two competitions in the upper branch $(2S-2P_o \text{ competition at the beginning of the branch and } 2P_o-2P \text{ competition at the end})$ and the statistics of this competition presented. Consistent with this finding, it has also been shown that a stable, periodic 2S wake mode exists at the very beginning of the upper branch, which has not been predicted by any previous analysis.

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