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Multiclass feature learning for hyperspectral image classification: sparse and hierarchical solutions.

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Abstract

In this paper, we tackle the question of discovering an effective set of spatial filters to solve hyperspectral classification problems. Instead of fixing *a priori* the filters and their parameters using expert knowledge, we let the model find them within random draws in the (possibly infinite) space of possible filters. We define an active set feature learner that includes in the model only features that improve the classifier. To this end, we consider a fast and linear classifier, multiclass logistic classification, and show that with a good representation (the filters discovered), such a simple classifier can reach at least state of the art performances. We apply the proposed active set learner in four hyperspectral image classification problems, including agricultural and urban classification at different resolutions, as well as multimodal data. We also propose a hierarchical setting, which allows to generate more complex banks of features that can better describe the nonlinearities present in the data.

Keywords: Hyperspectral imaging, active set, feature selection, multimodal, hierarchical feature extraction, deep learning.

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2014).

1. Introduction

Hyperspectral remote sensing allows to obtain a fine de- 30 scription of the materials observed by the sensor: with arrays 31 of sensors focusing on 5-10 nm sections of the electromag-32 netic spectrum, hyperspectral images (HSI) return a complete 33 description of the response of the surfaces, generally in the visible and infrared range. The use of such data, generally acquired 35 by sensors onboard satellites or aircrafts, allows to monitor the 36 8 processes occurring at the surface in a non-intrusive way, both 37 9 at the local and global scale (Lillesand et al., 2008; Richards 38 10 and Jia, 2005). The reduced revisit time of satellites, in con- $_{39}$ 11 junction with the potential for quick deployment of aerial and 40 12 unmanned systems, makes the usage of hyperspectral systems 41 13 quite appealing. As a consequence, hyperspectral data is be-14 coming more and more prominent for researchers and public 43 15 bodies. 16 44

Even if the technology is at hand and images can be ac-45 17 quired by different platforms in a very efficient way, HSI alone 46 18 are of little use for end-users and decision makers: in order to 47 19 be usable, remote sensing pixel information must be processed 48 20 and converted into maps representing a particular facet of the 21 processes occurring at the surface. Among the different prod-22 ucts traditionally available, land cover maps issued from image 51 23 classification are the most common (and probably also the most 52 24 used). In this paper, we refer to land cover/use classification as 53 25 the process of attributing a land cover (respectively land use) 54 26 class to every pixel in the image. These maps can then be used 27 55 for urban planning (Taubenböck et al., 2012, 2013), agricul-

ture surveys (Alcantara et al., 2012) or surveying of deforesta-

tion (Asner et al., 2005; Naidoo et al., 2012; Vaglio Laurin et al.,

et al., 2009; Camps-Valls et al., 2011; Mountrakis et al., 2011; Camps-Valls et al., 2014). Improving the quality of maps issued from HSI is not trivial, as hyperspectral systems are often high dimensional (number of spectral bands acquired), spatially and spectrally correlated and affected by noise (Camps-Valls et al., 2014).

Among these peculiarities of remote sensing data, spatial relations among pixels have received particular attention (Fauvel et al., 2013): the land cover maps are generally smooth, in the sense that neighboring pixels tend to belong to the same type of land cover (Schindler, 2012). On the contrary, the spectral signatures of pixels of a same type of cover tend to become more and more variable, especially with the increase of spatial resolution. Therefore, HSI classification systems have the delicate task of describing a smooth land cover using spectral information with a high within-class variability. Solutions to this problem have been proposed in the community and mostly recur to spatial filtering that work at the level of the input vector (Benediktsson et al., 2005; Vaiphasa, 2006; Fauvel et al., 2013) or to structured models that work by optimization of a context-aware energy function (Tarabalka et al., 2010; Schindler, 2012; Moser et al., 2013).

In this paper, we start from the first family of methods, those based on the extraction of spatial filters prior to classi-

The quality of land cover maps is of prime importance. Therefore, a wide panel of research works consider image classification algorithms and their impact on the final maps (Plaza

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fication. Methods proposed in remote sensing image classification tend to pre-compute a large quantity of spatial filters re-60 lated to the user's preference and knowledge of the problem: 61 texture (Pacifici et al., 2009), Gabor (Li and Du, in press), mor-62 phological (Benediktsson et al., 2005; Dalla Mura et al., 2010) 63 or bilateral filters (Schindler, 2012) are among those used in re-64 cent literature and we will use them as building blocks for our 65 system. With this static and overcomplete set of filters (or fil-66 terbank), a classifier is generally trained. 67

Even if successful, these studies still rely on the defini-68 tion *a*-priori of a filterbank. This filterbank depends on the 69 knowledge of the analyst and on the specificities of the im-70 age at hand: a pre-defined filterbank may or may not contain 71 the filters leading to the best performances. A filterbank con-72 structed *a*-priori is also often redundant: as shown in Fig. 1, 73 the filter bank is generally applied to each band of the im-74 age, resulting into a $(f \times B)$ -dimensional filter bank, where f 75 is the number of filters and B the number of bands. Proceed-76 ing this way proved in the past to be unfeasible for high di-77 mensional datasets, such as hyperspectral data, for which the 78 traditional way to deal with the problem is to perform a prin-79 cipal components analysis (PCA) and then extract the filters 80 from the $p \ll B$ principal components related to maximal vari-81 ance (Benediktsson et al., 2005). In that case, the final input 82 space becomes $(f \times p)$ -dimensional. A first problem is related 83 during this dimension reduction phase, for which the choice of $\frac{1}{121}$ 84 the feature extractor and of the number of features p remains 85 arbitrary and may lead to discarding information that is dis-86 criminative, but not related to large variance. Therefore, a first 87 objective of our method is to avoid this first data reduction step. 88 But independently to the reduction phase, this goes against the 89 desirable property of a model to be compact, i.e., to depend on 90 as few input variables as possible. Therefore, in most works 91 cited above an additional feature selection step is run to select 92 the most effective subset for classification. This additional step $_{_{130}}$ 93 can be a recursive selection (Tuia et al., 2009) or be based on $\frac{1}{131}$ 94 kernel combination (Tuia et al., 2010), on the pruning of a neu-95 ral network (Pacifici et al., 2009) or on discriminative feature 96 extraction (Benediktsson et al., 2005). 97

Proceeding this way is suboptimal in two senses: first, one 98 35 forces to restrict the number and parameters of filters to be used 99 to a subset, whose appropriateness only depends on the prior 100 knowledge of the user. In other words, the features that are 101 relevant to solve the classification problem might not be in the 102 original filterbank. Second, generating thousands of spatial fil-103 ters and use them all together in a classifier, that also might 104 operate with a feature selection strategy, increases the compu-105 tational cost significantly, and might even deteriorate the classi-106 fication accuracy because of the curse of dimensionality. Note 107 that, if the spatial filters considered bear continuous parameters 108 (e.g. Gabor or angular features), there is theoretically an infinite $_{146}$ 109 number of feature candidates. 110

This paper tackles these two problems simultaneously: instead of pre-computing a specific set of filters, we propose to interact with the current model and retrieve only new filters that will make it better. These candidate filters can be of any nature and with parameters unrestricted, thus allowing to explore



Figure 1: Traditional spatio-spectral classification with contextual filters: using pre-defined filterbanks, applied on the first principal component.

the (potentially infinite) space of spatial filters. This leads to an integrated approach, where we incrementally build the set of filters from an empty subset and add only the filters improving class discrimination. This way of proceeding is of great interest for automatic HSI classification, since the filters are selected automatically among a very large set of possible ones, and are those that best fit the problem at hand.

Two approaches explored similar concepts in the past: Grafting (Perkins et al., 2003) and Group Feature Learning (Rakotomamonjy et al., 2013), which incrementally select the most promising feature among a batch of features extracted from the universe of all possible features admitted. Since this selection is based on a heuristic criterion ranking the features by their informativeness when added to the model, it may be seen as performing active learning (Crawford et al., 2013) in the space of possible features (in this case, the active learning oracle is replaced by the optimality condition, for which only the features improving the current classifier are selected).

In this paper, we propose a new Group Feature Learning model based on multiclass logistic regression (also known as multinomial regression). The use of a group-lasso regularization (Yuan and Lin, 2007) allows to jointly select the relevant features and also to derive efficient conditions for evaluating the discriminative power of a new feature. In Rakotomamonjy et al. (2013), authors propose to use group-lasso for multitask learning by allowing to use an additional sparse average classifier common to all tasks. Adapting their model in a multiclass classification setting leads to the use of the sole group-lasso regularization. Note that one could use a ℓ_1 support vector machine as in Tuia et al. (2014) to select the relevant feature in a One-VS-All setting, but this approach is particularly computationally intensive, as the incremental problem is solved for each class separately. This implies the generation of millions of features, that may be useful for more than one class at a time. To achieve an efficient multiclass strategy, we propose the following three original contributions:



Figure 2: Spatio-spectral classification with the proposed active set models. (a) With only the original HSI image as bands input (shallow model, AS-BANDS); (b) with the hierarchical feature extraction (deep model, ASH-BANDS).

1521. We use here a multiclass logistic classifier (MLC) with
189153a softmax loss. MLC allows to natively handle several
190154classes without using the One-VS-All approach and has
191155the advantage of providing probabilistic prediction scores
192156that can more easily be used in structured models (such
193
as Markov random fields).

 We employ a group lasso regularization, which allows¹⁹⁵ to select features useful for many classes simultaneously, even if they do not show the highest score for a single class. This means sharing information among the classes, similarly to what would happen in a multitask setting (Leiya-Murillo et al., 2013). This model, called AS-BANDS, is₁₉₈ detailed in Fig. 2(a).

3. We investigate the automatic selection of complex hi-165 erarchical spatial filters built as modifications of previ-200 166 ously selected filters. This leads to a tree- (or graph-)₂₀₁ 167 based feature extraction that can encode complex non-168 linear relationship for each class. Such a hierarchical 169 re-processing of features has connections with deep neu-170 ral networks (LeCun et al., 1989, 1998), which have re-171 cently proven to be able to improve significantly the per-formance of existing classification methods in computer 200 172 173 vision (Chatfield et al., 2014; Girshick et al., 2014). This 174 model, called ASH-BANDS, is detailed in Fig. 2(b). 175 209

We test the proposed method on two landcover classifica-210 176 tion tasks with hyperspectral images of agricultural areas and²¹¹ 177 on one landuse classification example over an urban area ex-212 178 ploiting jointly hyperspectral and LiDAR images. In all cases,213 179 the proposed feature learning method solves the classification214 180 tasks with at least state of the art numerical performances and 181 returns compact models including only features that are dis-182 criminative for more than one class. Among the two method 183 proposed, the hierarchical feature learning tends to outperform 184 the shallow feature extractor for traditional classification prob-185 lems. However, when confronted to shifting distributions be-186 tween train and test (i.e. a domain adaptation problem), it pro-187 vides slightly worse performances, probably due to the com-188

plexification of the selected features, that overfit the training examples.

The remainder of this paper is as follows: Section 2 details the proposed method, as well as the multiclass feature selection using group-lasso. In Section 3 we present the datasets and the experimental setup. In Section 4 we present and discuss the experimental results. Section 5 concludes the paper.

2. Multiclass active set feature discovery

In this section, we first present the multiclass logistic classification and then derive its optimality conditions, which are used in the active set algorithm¹.

2.1. Multiclass logistic classifier with group-lasso regularization

Consider an image composed of pixels $\mathbf{x}_i \in \mathbb{R}^B$. A subset of l_c pixels is labeled into one of *C* classes: $\{\mathbf{x}_i, y_i\}_{i=1}^{l_c}$, where y_i are integer values $\in \{1, \ldots, C\}$. We consider a (possibly infinite) set of θ -parametrized functions $\phi_{\theta}(\cdot)$ mapping each pixel in the image into the feature space of the filter defined by θ . As in Tuia et al. (2014), we define as \mathcal{F} the set of all possible finite subsets of features and φ as an element of \mathcal{F} composed of *d* features $\varphi = \{\phi_{\theta_i}\}_{j=1}^d$. We also define $\Phi_{\varphi}(\mathbf{x}_i)$ as the stacked vector of all the values obtained by applying the filters φ to pixel \mathbf{x}_i and $\mathbf{\Phi}_{\varphi} \in \mathbb{R}^{l_c \times d}$ the matrix containing the *d* features in φ computed for all the *l*_c labeled pixels. Note that in this work, we suppose that all the features have been normalized with each column in matrix $\mathbf{\Phi}_{\varphi}$ having a unit norm.

In this paper we consider the classification problem as a multiclass logistic regression problem with group-lasso regularization. Learning such a classifier for a fixed amount of features

¹A MATLAB toolbox can be downloaded at the address http://remi. flamary.com/soft/soft-fl-rs-svm.html. It contains both the models presented in this paper (AS-Bands, Section 2.2 and ASH-Bands, Section 2.3), as well as the method of Tuia et al. (2014)

 φ corresponds to learning a weight matrix $\mathbf{W} \in \mathbb{R}^{d \times C}$ and the bias vector $\mathbf{b} \in \mathbb{R}^{1 \times C}$ using the softmax loss. In the following, we refer to \mathbf{w}_c as the weights corresponding to class c, which corresponds to the *c*-th column of matrix \mathbf{W} . The *k*-th line of matrix \mathbf{W} is denoted as $W_{k,..}$ The optimization problem for a fixed feature set φ is defined as:

$$\min_{\mathbf{W},\mathbf{b}} \quad \mathcal{L}(\mathbf{W},\mathbf{b}) = \left\{ \frac{1}{l_c} \sum_{i=1}^{l_c} H(y_i, \mathbf{x}_i, \mathbf{W}, \mathbf{b}) + \lambda \Omega(\mathbf{W}) \right\}$$
(1)

where the first term corresponds to the soft-max loss with $H(\cdots)$ defined as

$$H(\cdots) = \log\left(\sum_{c=1}^{C} \exp\left((\mathbf{w}_{c} - \mathbf{w}_{y_{i}})^{\mathsf{T}} \Phi_{\varphi}(\mathbf{x}_{i}) + (b_{c} - b_{y_{i}})\right)\right)$$

and the second term is a group-lasso regularizer. In this paper,²³³ we use the weighted $\ell_1 \ell_2$ mixed norm : ²³⁴

$$\Omega(\mathbf{W}) = \sum_{j=1}^{d} \gamma_j ||W_{j,\cdot}||_2 \qquad (2)_{237}^{236}$$

where the coefficients $\gamma_j > 0$ correspond to the weights used²³⁹ for regularizing the *j*th feature. Typically one want all features²⁴⁰ to be regularized similarly by choosing $\gamma_j = 1$, $\forall j$. However, in the hierarchical feature extraction proposed in Section 2.3²⁴¹ we will use different weights in order to limit over-fitting when using complex hierarchical features.

This regularization term promotes group sparsity, due to its 221 non differentiability at the null vector of each group. In this 222 case we grouped the coefficients of W by lines, meaning that 223 the regularization will promote joint feature selection for all 224 classes. Note that this approach can be seen as multi-task learn-225 ing where the tasks corresponds to the classifier weights of each 226 class (Obozinski et al., 2006; Rakotomamonjy et al., 2011). As 227 a result, if a variable (filter) is active, it will be active for all²⁴² 228 classes. This is particularly interesting in in a multiclass set-243 229 ting, since a feature that helps in detecting a given class also²⁴⁴ 230 helps in "not detecting" the others C - 1 classes: for this reason²⁴⁵ 231 246 a selected feature should be active for all the classifiers. 232

The algorithm proposed to solve both the learning problem²⁴⁷ and feature selection is derived from the optimality conditions²⁴⁸ of the optimization problem of Eq. (1). Since the problem²⁴⁹ defined in Eq. (1) is non-differentiable, we compute the sub-²⁵⁰ differential of its cost function:

$$\partial_{\mathbf{W}} \mathcal{L}(\mathbf{W}, \mathbf{b}) = \mathbf{\Phi}_{\omega}^{\top} \mathbf{R} + \lambda \partial \Omega(\mathbf{W})$$
(3)₂₅₃

where the first term corresponds to the gradient of the softmax²⁵⁴ data fitting and the second term is the sub-differential of the²⁵⁶ weighted group lasso defined in Eq. (2). **R** is a $l_c \times C$ matrix²⁵⁴ that, for a given sample $i \in \{1, .., l_c\}$ and a class $c \in \{1, .., C\}$ ²⁵⁷₂₅₈ equals:

$$R_{i,c} = \frac{\exp(M_{i,c} - M_{i,y_i}) - \delta_{\{y_i - c\}} \sum_{k=1}^{C} \exp(M_{i,k} - M_{i,y_i})}{l_c \sum_{k=1}^{C} \exp(M_{i,k} - M_{i,y_i})} \quad (4)_{260}^{256}$$

where $\mathbf{M} = \mathbf{\Phi}_{\varphi} \mathbf{W} + \mathbf{1}_{l_c} \mathbf{b}$ and $\delta_{\{y_i - c\}} = 1$ if $c = y_i$ and 0 other-262 wise. In the following, we define $\mathbf{G} = \mathbf{\Phi}_{\varphi}^{\mathsf{T}} \mathbf{R}$ as a $d \times C$ matrix.263 corresponding to the gradient of the data fitting term *w.r.t* **W**. Note that this gradient can be computed efficiently with multiple scalar product between the features Φ_{φ} and the multiclass residual **R**. The optimality conditions can be obtained separately for each $W_{j,\cdot}$, *i.e.* for each line *j* of the **W** matrix. $\Omega(\mathbf{W})$ consists in a weighted sum of non differentiable norm-based regularization (Bach et al., 2011). The optimality condition for the ℓ_2 norm consists in a constraint with its dual norm (namely itself):

$$\|G_{j,\cdot}\|_2 \le \lambda \gamma_j \qquad \forall j \in \varphi \tag{5}$$

which in turn breaks down to:

$$\begin{cases} ||G_{j,\cdot}||_2 = \lambda \gamma_j & \text{if } W_{j,\cdot} \neq \mathbf{0} \\ ||G_{j,\cdot}||_2 \le \lambda \gamma_j & \text{if } W_{j,\cdot} = \mathbf{0} \end{cases}$$
(6)

These optimality conditions show that the selection of one variable, *i.e.* one group, can be easily tested with the second condition of equation (6). This suggests the use of an active set algorithm. Indeed, if the norm of correlation of a feature with the residual matrix is below $\lambda \gamma_j$, it means that this feature is not useful for classification and its weight will be set to 0 for all the classes. On the contrary, if not, then the group can be defined as "active" and its weights have to be estimated.

2.2. Proposed active set criterion (AS-BANDS)

We want to learn jointly the best set of filters $\varphi^* \in \mathcal{F}$ and the corresponding MLC classifier. This is achieved by minimizing Eq. (1) jointly on φ and **W**, **b**. As in Rakotomamonjy et al. (2013), we can extend the optimality conditions in (6) to all filters with zero weights that are *not* included in the current active set φ :

$$\|G_{\phi_{\theta}}\|_{2} \leq \lambda \gamma_{\phi_{\theta}} \qquad \forall \phi_{\theta} \notin \varphi \tag{7}$$

Indeed, if this constraint holds for a given feature not in the current active set, then adding this feature to the optimization problem will lead to a row of zero weights $W_{(d+1),.}$ for this feature. But this also means that if we find a feature that violates Eq. (7), its inclusion in φ will (after re-optimization) make the global MLC cost decrease and provide a feature with non-zero coefficients for all classes.

The pseudocode of the proposed algorithm is given in Algorithm 1: we initialize the active set φ_0 with the spectral bands and run a first MLC minimizing Eq. (1). Then we generate a random minibatch of candidate features, Φ_{θ_j} , involving spatial filters with random types and parameters. We then assess the optimality conditions with (7): if the feature $\phi_{\theta_j}^*$ with maximal $||G_{\theta_j,\cdot}||_2$ is greater than $\lambda \gamma_j + \epsilon$, it is selected and added to the current active set $[\phi_{\theta_j}^* \cup \varphi]$. After one feature is added the MLC classifier is retrained and the process is iterated using the new active set.

2.3. Hierarchical feature learning (ASH-BANDS)

Algorithm 1 searches randomly in a possibly infinite dimensional space corresponding to all the possible spatial filters computed on the input bands. But despite all their differences, the spatial filters proposed in the remote sensing community

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Algorithm	1	Multiclass	active	set	selection	for	MLC	(AS
Bands)								

Inputs

- Bands to extract the filters from (B)

- Initial active set $\varphi_0 = B$

1: repeat

Solve a MLC with current active set φ 2:

- Generate a minibatch $\{\phi_{\theta_j}\}_{j=1}^p \notin \varphi$ 3:
- Compute G as in (7) $\forall j = 1 \dots p$ 4:
- Find feature $\phi_{\theta_i}^*$ maximizing $\|G_{\theta_j,\cdot}\|_2$ 5:

if $||G_{\theta_{j}^{*},\cdot}||_{2} > \lambda \gamma_{i} + \epsilon$ then 6:

- 7: $\varphi = \phi_{\theta_i}^* \cup \varphi$
- end if 8:
- 9: **until** stopping criterion is met

(see, as an example, those in Tab. 4) can yield only a limited 264 complexity and non-linearity. When the classes are not linearly 265 separable, learning a linear classifier may require a large num-266 ber of these relatively simple features. In this section we inves-267 tigate the use of hierarchical feature generation that can yield 268 much more complex data representation and therefore hope-269 fully decrease the number of features necessary for a good clas-303 270 sification. 271

Hierarchical feature extraction is obtained by adding the al-304 272 ready selected features in the pool of images that can be used₃₀₅ 273 for filtering at the next feature generation step. Using a retained 274 filter as a new possible input band leads to more complex fil-306 275 ters with higher nonlinearity. This is somehow related to the₂₀₇ 276 methods of deep learning, where deep features are generally₃₀₈ 277 obtained by aggregation of convolution operators. In our case, 309 278 those operators are substituted by spatial filters with known 279 properties, which adds up to our approach the appealing prop-310 280 erty of direct interpretability of the discovered features. In deep₃₁₁ 281 learning models, interpretation of the features learned is becom-312 282 ing possible, but at the price of series of deconvolutions (Zeiler₃₁₃ 283 and Fergus, 2014). 284 314

Let $h_j \in \mathbb{N}$ be the depth of a given feature ϕ_{θ_i} , with 0 be-315 285 ing the depth of original features: this is the number of filtering₃₁₆ 286 steps the original bands has undergone to generate filter $\phi_{\theta_i,317}$ 287 For example, the band 5 has depth $h_5 = 0$, while the filters that₃₁₈ 288 are issued from this band, for example a filter k issued from an₃₁₉ 289 opening computed on band 5, will have depth $h_k = 1$. If the₃₂₀ 290 opening band is then re-filtered by a texture filter into a new₃₂₁ 291 filter l, its depth will be $h_l = 2$. This leads to a much more com-₃₂₂ 292 plex feature extraction that builds upon an hierarchical, tree-323 293 shaped, suite of filters. The depth of the feature in the feature 294 generation tree is of importance in our case since it is a good³²⁴ 295 proxy of the complexity of the features. In order to avoid over-325 296 fitting, we propose to regularize the features using their depth³²⁶ 297 in the hierarchy. As a criterion, we use a regularization weight³²⁷ 298 of the form $\gamma_j = \gamma_0^{h_j}$, with $\gamma_0 \ge 1$ being a term penalizing depth³²⁸ 299 in the graph. 300

The proposed hierarchical feature learning is summarized³³⁰ 301 in Algorithm 2. 302

Algorithm 2 Multiclass active set selection for MLC, hierarchical deep setting (ASH-BANDS)

Inputs

- Bands to extract the filters from (*B*) with depth h = 1

Initial active set
$$\varphi_0 = B$$

- 1: repeat
- 2: Solve a MLC with current active set φ
- Generate a minibatch $\{\phi_{\theta_i}, h_j\}_{i=1}^p \notin \varphi$ using *B* as input for 3: filters
- Compute depth-dependent regularizations as 4: $\gamma_j = \gamma_0^{h_j}$
- 5: Compute G as in (7) $\forall j = [1 \dots p]$
- Compute optimality conditions violations as 6: $\Lambda_{i} = \|G_{\theta_{i},\cdot}\|_{2} - \lambda \gamma_{i} - \epsilon, \forall j = [1 \dots p]$
- Find feature $\phi_{\theta_i}^*$ maximizing Λ_j 7:
- if $\Lambda_{\theta_j^*} > 0$ then 8:
- $\varphi = \phi_{\theta_j}^* \cup \varphi$ $B = \phi_{\theta_j}^* \cup B$ 9:
- 10:
- end if 11:
- 12: until stopping criterion is met

3. Data and setup of experiments

In this section, we present the three datasets used, as well as the setup of the four experiments considered.

3.1. Datasets

We studied the proposed active set method on four hyperspectral classification tasks, involving two crops identification datasets and one urban land use dataset (considered in two ways):

- a) Indian Pines 1992 (AVIRIS spectrometer, HS): the first dataset is a 20-m resolution image taken over the Indian Pines (IN) test site in June 1992 (see Fig. 3). The image is 145×145 pixels and contains 220 spectral bands. A ground survey of 10366 pixels, distributed in 16 crop types classes, is available (see Table 1). This dataset is a classical benchmark to validate model accuracy. Its challenge resides in the strong mixture of the classes' signatures, since the image has been acquired shortly after the crops were planted. As a consequence, all signatures are contaminated by soil signature, making thus a spectralspatial processing compulsory to solve the classification problem. As preprocessing, 20 noisy bands covering the region of water absorption have been removed.
- b) Indian Pines 2010 (ProSpecTIR spectrometer, VHR HS): the second dataset considers multiple flightlines acquired near Purdue University, Indiana, on May 24-25, 2010 by the ProSpecTIR system (Fig. 4). The image subset analyzed in this study contains 445×750 pixels at 2m spatial resolution, with 360 spectral bands of 5nm width. Sixteen land cover classes were identified by field surveys, which included fields of different crop residue, vegetated

Table 1: Classes and samples (n_l^c) of the ground truth of the Indian Pines 1992 dataset (cf. Fig. 3).

Class	n_l^c	Class	n_l^c
Alfalfa	54	Oats	20
Corn-notill	1434	Soybeans-notill	968
Corn-min	834	Soybeans-min	2468
Corn	234	Soybeans-clean	614
Grass/Pasture	497	Wheat	212
Grass/Trees	747	Woods	1294
Grass/Pastmowed	26	Towers	95
Hay-windrowed	489	Other	380
L		Total	10366



Figure 3: Indian Pines 1992 AVIRIS data.(a) False color composition and (b)₃₅₀ ground truth (for color legend, see Tab. 1). Unlabeled samples are in black.



Figure 4: Indian Pines 2010 SpecTIR data.(a) RGB composition and (b) ground₃₇₀ truth (for color legend, see Tab. 2). Unlabeled samples are in black.

332areas, and man-made structures. Many classes have reg-373333ular geometry associated with fields, while others are re-374334lated with roads and isolated man-made structures. Ta-375335ble 2 shows class labels and number of training samples376336per class.

c) Houston 2013 (CASI spectrometer VHR HS + LiDAR₃₇₉ data). The third dataset depicts an urban area nearby the₃₈₀

Table 2: Classes and samples (n_l^c) of the ground truth of the Indian Pines 2010 dataset (cf. Fig. 4).

Class	n_l^c	ĺ	Class	n_l^c
Corn-high	3387		Нау	50045
Corn-mid	1740		Grass/Pasture	5544
Corn-low	356		Cover crop 1	2746
Soy-bean-high	1365		Cover crop 2	2164
Soy-bean-mid	37865		Woodlands	48559
Soy-bean-low	29210		Highway	4863
Residues	5795		Local road	502
Wheat	3387		Buildings	546
Total 19807				

campus of the University of Houston (see Fig. 5). The dataset was proposed as the challenge of the IEEE IADF Data Fusion Contest 2013 (Pacifici et al., 2013). The hyperspectral image was acquired by the CASI sensor (144 spectral bands at 2.5m resolution). An aerial LiDAR scan was also available: a digital surface model (DSM) at the same resolution as the hyperspectral image was extracted, coregistered and used as an additional band in the input space. Fifteen urban land-use classes are to be classified (Tab. 3). Two preprocessing steps have been performed: 1) histogram matching has been applied to the large shadowed area in the right part of the image (cf. Fig 5), in order to reduce domain adaptation problems (Camps-Valls et al., 2014), which are not the topic of this study: the shadowed area has been extracted by segmenting a near-infrared band and the matching with the rest of the image has been applied; 2) A height trend has been removed from the DSM, by applying a linear detrending of 3m from the West along the x-axis. Two classification experiments were performed with this data:

- Houston 2013A: we consider the left part of the image, which is unaffected by the cloud shadow. This corresponds to an image of size (349×1100) pixels. The same subsampling was applied to the LiDAR DSM. The whole ground truth within the red box in Figure 5c was used to extract the train and test samples.
- Houston 2013B: the whole image was considered. Separate training and test set (in green and red in Fig. 5d, respectively), are considered instead of a random extraction. In this case, even though the projected shadow has been partially corrected by the local histogram matching, some spectral drift remains between the test samples (some of which are under the shadow) and the training ones (which are only in the illuminated areas). This was the setting of the IEEE IADF Data Fusion Contest 2013 and aimed at classification under dataset shift (Camps-Valls et al., 2014). This problem is much more challenging than HOUSTON 2013A and we use it as a benchmark against the state of the art, i.e. the results of the contest. However, remind that our

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Table 3: Classes and samples (n_l^c) of the ground truth of the Houston 2013 dataset (cf. Fig. 5).

Class	n_l^c	Class	n_l^c
Healthy grass	1231	Road	1219
Stressed grass	1196	Highway	1224
Synthetic grass	697	Railway	1162
Trees	1239	Parking Lot 1	1233
Soil	1152	Parking Lot 2	458
Water	325	Tennis Court	428
Residential	1260	Running Track	660
Commercial	1219	Total	14703

³⁸¹ 382

method is not designed to solve domain adaptation problems explicitly.

383 3.2. Setup of experiments

For every dataset, all the features have been mean-centered and normalized to unit norm. This normalization is mandatory due to the optimality conditions, which is based on a scalar product (thus depending linearly on the norm of the feature).

In all the experiments, we use the multiclass logistic classifier (MLC) with $\ell_1 \ell_2$ norm implemented in the SPAMS package². We start by training a model with all available bands (plus the DSM in the HOUSTON2013A/B case) and use its result as the first active set. Therefore, we do not reduce the dimensionality of the data prior to the feature generation. Regarding the active set itself, we used the following parameters:

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395	- The stopping criterion is a number of iterations: 150 in_{419}
396	the PINES 1992, 2010 and HOUSTON 2013 B and 100 in the $_{app}$
397	HOUSTON 2013A case (the difference explained by faster ₄₂₁
398	convergence in the last dataset).

- A minibatch is composed of filters extracted from 20 bands³, randomly selected. In the Houston 2013A/B case, the
 DSM is added to each minibatch.
- The possible filters are listed in Tab. 4. Structuring ele-427 402 ments (SE) can be disks, diamonds, squares or lines. If₄₂₈ 403 a linear structuring elements is selected, an additional ori-429 404 entation parameter is also generated ($\alpha \in [-\pi/2, \dots, \pi/2]$).⁴³⁰ 405 These filters are among those generally used in remote⁴³¹ 406 sensing hyperspectral classification literature (see Fauvel432 407 et al. (2013)), but any type of spatial or frequency filter,433 408 descriptor or convolution can be used in the process. 434 409
- A single minibatch can be used twice (i.e. once a first⁴³⁵/₄₃₆
 filter has been selected, it is removed and Eq. (7) is re-⁴³⁷/₄₃₇
 evaluated on the remaining filters after re-optimization⁴³⁸/₄₃₈
 of the MLC classifier). 439

In each experiment, we start by selecting an equal number to f labeled pixels per class l_c : we extracted 30 random pixels per class in the INDIAN PINES 1992 case, 60 in the INDIAN PINES

Table 4: Filters considered in the experiments (B_i, B_j) : input bands indices $(i, j \in [1, ..., b])$; s: size of moving window, SE: type of structuring element; α : angle).

Fil	lter	θ					
M	Morphological						
-	Opening / closing	B_i, s, α					
-	Top-hat opening / closing	B_i, s, SE, α					
-	Opening / closing by re-	B_i, s, SE, α					
	construction						
-	Opening / closing by re-	B_i, s, SE, α					
	construction top-hat						
Te	xture						
-	Average	B_i, s					
-	Entropy	B_i, s					
-	Standard deviation	B_i, s					
-	Range	B_i , s					
At	tribute						
-	Area	B_i , Area threshold					
-	Bounding box diagonal	B_i , Diagonal thresh-					
		old					
Band combinations							
-	Simple ratio	B_i/B_j					
-	Normalized ratio	$(B_i - B_j)/(B_i + B_j)$					
-	Sum	$B_i + B_j$					
-	Product	$B_i * B_j$					

2010 and in the Houston 2013A/B case³. The difference in the amount of labeled pixels per class is related to i) the amount of labeled pixels available per task and ii) the complexity of the problem at hand. As test set, we considered all remaining labeled pixels, but disregard those in the spatial vicinity of the pixels used for training. In the INDIAN PINES 1992 case, we consider all labeled pixels out of a 3×3 window around the training pixels, in the INDIAN PINES 2010 case a 7×7 window and in the HOUSTON 2013A case a 5×5 window. The difference is basically related to the images spatial resolution. In the HOUSTON 2013B case, a spatially disjoint test set was provided in a separate file and was therefore used for testing purposes without spatial windowing.

When considering the hierarchical model ASH-BANDS, every feature that is added to the active set is also added to the input bands *B* (see line 10 of Algorithm 2). In order to penalize overcomplex deep features, we considered $\gamma = 1.1^h$, where *h* is the depth of the feature defined in Section 2.3. When adding filters issued from two inputs (as, for example, band ratios) $h = max(h_{B_i}, h_{B_i}) + 1$.

Each experiment was repeated 5 times, by random sampling of the initial training set (the test set also varies in the INDIAN PINES 1992/2010 and HOUSTON 2013A datasets, since it depends on the specific location of the training samples). Average performances, along with their standard deviations, are reported.

²http://spams-devel.gforge.inria.fr/

³When the number of pixels available was smaller than l_c , we extracted 80% for training and left the rest for testing

(a) CASI image after local histogram matching



Figure 5: Houston 2013.(a) RGB composition of the CASI data, (b) DSM issued from the LiDAR point cloud and (c) train and test ground truths. (for color legend, see Tab. 2). The area in the red box of the (c) panel has been used in the Houston2013A experiment, while the whole area has been used in the Houston2013B experiment, with (d) a training/test separation shown in the last panel (green: training, red: test). Unlabeled samples are in black.

42 4. Results and discussion

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In this section, we present and discuss both the numerical₄₅₇ results obtained and the feature selected in the AS-BANDS (shal-₄₅₈ low) and ASH-BANDS (deep) algorithms.

446 4.1. Performances along the iterations

AS-BANDS: Numerical results for the three datasets in the AS-462 447 BANDS (shallow) setting are provided in Fig. 6: the left column463 448 illustrates the evolution of the Kappa statistic (Foody, 2004)464 449 along the iterations and for three levels of $\ell_1 \ell_2$ regularization₄₆₅ 450 λ : the higher the λ parameter, the sparser the model (and the 466 451 harder to violate the optimality conditions). The right column₄₆₇ 452 of Fig. 6 shows the evolution of the number of features in the468 453 active set. 469 454

For all the datasets, the iterative feature learning corresponds to a continuous, almost monotonic, increase of the performance. This is related to the optimality conditions of Eq. (1): each time the model adds one filter $\phi_{\theta_j^*}$ to φ , the MLC cost function decreases while the classifier performances raises. Overfitting is prevented by the group-lasso regularization: on the one hand this regularizer promotes sparsity through the ℓ_1 norm, while on the other hand it limits the magnitude of the weight coefficients **W** and promotes smoothness of the decision function by the use of the ℓ_2 norm. Note that for the Houston 2013B dataset, the final classification performance is at the same level as the one of the winners of the contest, thus showing the ability of our approach to compete with state of the art methods.

For each case study, the model with the lowest sparsity ($\lambda = 0.0001$) shows the initial best performance (it utilizes more fea-



Figure 6: Left: numerical performance (Kappa statistic) of AS-BANDS for different degrees of regularization λ and filtering the original bands. Right: number of active features during the iterations.

tures, as shown in the right column) and then keeps providing489 470 the best performances. However, the model with $\lambda = 0.001$ has⁴⁹⁰ 471 an initial sparser solution and shows a steeper increase of the491 472 curve in the first iterations. When both models provide similar⁴⁹² 473 performance, they are actually using the same number of fea-493 474 tures in all cases. The sparsest model ($\lambda = 0.01$, black line)⁴⁹⁴ 475 shows the worst results in two out of the three datasets and⁴⁹⁵ 476 in general is related to less features selected: our interpreta-496 477 tion is that the regularization ($\lambda = 0.01$) is too strong, leading⁴⁹⁷ 478 to a model that discards relevant features and is too biased for498 479 a good prediction (even when more features are added). As a⁴⁹⁹ 480 consequence, the learning rate may be steeper than for the other500 481 models, but the model does not converge to an optimal solution.501 482 ASH-BANDS: The performance of ASH-BANDS are compared⁵⁰² 483 to those of AS-BANDS in Fig. 7. The case of $\lambda = 0.001$ is⁵⁰³ 484 shown (the blue curves of Fig. 7 correspond to the blue curves⁵⁰⁴ 485 of Fig. 6). From this comparison, two tendencies can be no-505 486 ticed: on the one hand, ASH-BANDS shows better learning rates⁵⁰⁶ 487 when the classification problem is fixed (i.e., no spectral shifts507 488



Figure 7: Results of the ASH-BANDS method. Left: numerical performance (Kappa statistic) for $\lambda = 0.001$. Right: number of active features during the iterations.

are observed between the training and test data: INDIAN PINES 1992, INDIAN PINES 2010 and HOUSTON 2013A): by constructing more complex features, ASH-BANDS can solve the classification problem in a more accurate way and without increasing substantially the size of the model (both AS-BANDS and ASH-BANDS show similar number of active features during the process). On the other hand, in the HOUSTON 2013B case ASH-BANDS is outperformed by the shallow model AS-BANDS by 0.03 in κ . The variance of the single runs is also significantly higher (see, the ASH-BANDS row for this dataset in Tab. 5). We interpret this slower learning rate by an overfitting of the training data in the presence of dataset shift: since the test distribution is different that the one observed in training (by the projected cloud in the hyperspectral data), the spatial filters learned seem to become too specialized in explaining the training data and are then less accurate in the case of the (shifted) test distribution. Such behavior has been documented before in deep learning literature, especially when little training examples are used to learn the features (Bengio, 2012). Note that the classification perfor-

	Method	Ω	Pines 1992	Pines 2010	HOUSTON 2013A	HOUSTON 2013B
No spatial info	MLC-ω	ℓ_1	0.42 ± 0.02	0.58 ± 0.01	0.90 ± 0.02	0.61 ± 0.01
(baseline)	# fea	atures	60 ± 3	107 ± 9	135 ± 6	54 ± 3
	MLC-ω	ℓ_2	0.59 ± 0.03	0.90 ± 0.01	0.92 ± 0.02	0.80 ± 0.01
	# fea	atures	200	360	145	145
Spatial info	AS-bands	$\ell_1\ell_2$	0.83 ± 0.02	0.98 ± 0.01	$\textbf{0.98} \pm \textbf{0.01}$	0.93 ± 0.01
from bands	# fea	atures	96 ± 5	68 ± 5	46 ± 4	71 ± 3
(proposed)	ASH-bands	$\ell_1\ell_2$	0.85 ± 0.03	$\textbf{0.99} \pm \textbf{0.001}$	0.99 ± 0.01	0.90 ± 0.03
	# fea	atures	86 ± 6	56 ± 3	52 ± 5	75 ± 2
Spatial info from	MLC-s	ℓ_1	0.85 ± 0.02	0.84 ± 0.01	0.97 ± 0.01	0.76 ± 0.01
three top PCs	# features		85 ± 7	64.2 ± 3	122 ± 12	82 ± 5
(baseline)	MLC-s ℓ_2		0.85 ± 0.01	0.96 ± 0.01	0.97 ± 0.01	0.87 ± 0.01
	# features		217	228	269	273
Spatial info from	AS-pcs	$\ell_1\ell_2$	0.89 ± 0.03	$\textbf{0.99} \pm \textbf{0.01}$	0.98 ± 0.01	0.92 ± 0.01
all PCs	# features		82 ± 4	83 ± 8	57 ± 4	64 ± 4
(proposed)	ASH-pcs	$\ell_1\ell_2$	0.88 ± 0.01	0.99 ± 0.01	0.99 ± 0.01	0.92 ± 0.02
	# fea	atures	102 ± 7	68 ± 2	59 ± 3	74 ± 6

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Table 5: Results by MLC classifiers trained with the spectral bands (ω), with spatial features extracted from the three first principal components, PCs (s, including morphological and attribute filters) or with the proposed active set (AS-). In the Houston 2013A/B cases, features extracted from the DSM have been added to the input space of the baselines.

mance is still $\kappa = 0.9$ on average. 508

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4.2. Numerical performances at the end of the feature learning 540509

Comparisons with competing strategies where the MLC class41 510 sifier is learned on pre-defined feature sets are reported in Ta-542 511 ble 5. First, we discuss the performance of our active set ap-543 512 proach when learning the filters applied on the original bands⁵⁴⁴ 513 (AS-BANDS and ASH-BANDS): in the INDIAN PINES 1992 case, the545 514 AS- methods obtain average Kappas of 0.83 using 96 features⁵⁴⁶ 515 and 0.85 using 86 features, respectively. This is a good result⁵⁴⁷ 516 if compared to the upper bound of 0.86 obtained by a classifier⁵⁴⁸ 517 using the complete set of 14'627 morphological and attribute549 518 features extracted from each spectral band (result not reported550 519 in the table)⁴. On both the INDIAN PINES 2010 and HOUSTON⁵⁵¹ 520 2013A datasets, the AS-BANDS method provided average Kappa⁵⁵² 521 of 0.98. ASH-BANDS provided comparable results, on the aver-553 522 age 0.01 more accurate, but still in the standard deviation range 523 of the shallow model. The exception is the last dataset, HOUSTON 554 524 2013B, for which the shallow model provides a Kappa of 0.93,555 525 while the hierarchical model is 0.03 less accurate, as discussed 526

in the previous section. 557 We compared these results to those obtained by classifiers₅₅₈ 528 trained on fixed raw bands (MLC- ω) or on sets of morpholog-559 529 ical and attribute filters extracted form the three first principal₅₆₀ 530 components (MLC-s). We followed the generally admitted hy-561 531 pothesis that the first(s) principal component(s) contain most of $_{562}$ 532 the relevant information in hyperspectral images (Benediktsson₅₆₃ 533 et al., 2005). On all the datasets, the proposed AS-BANDS method₅₆₄ 534 performs remarkably well compared with models using only the565 535 spectral information (MLC- ω) and compares at worse equiv-₅₆₆ 536 alently (and significantly better in the INDIAN PINES 2010 and 567 537

HOUSTON 2013B cases) with models using ℓ_2 classifiers (thus without sparsity) and three to four times more features including spatial information (MLC-s). The good performance of the ℓ_2 method on the Indian Pines 1992 dataset (Kappa observed of (0.85) is probably due to the application of the PCA transform prior to classification, which, besides allowing to decrease the dimensionality of the data, also decorrelates the signals and isolates the bare soil reflectance, which is present for almost all classes (cf. the data description in Section 3). For this reason, we also investigated a variant of our approach where, instead of working on the original spectral space, we used all the principal components extracted from the original data (AS-PCs and ASH-PCs). In the INDIAN PINES 1992 case, the increase in performance is striking, with a final Kappa of 0.89. For the three other datasets, the results remain in the same range as for the **AS-BANDS** results.

4.3. Multiclass selection

For the four images, the active set models end up with a maximum of 50 - 100 features, shared by all classes. This model is very compact, since it corresponds to only 30 - 50%of the initial dimensionality of the spectra. Due to the grouplasso regularization employed, the features selected are active for several classes simultaneously, as shown in Fig. 8, which illustrates the \mathbf{W}^{T} matrix for the INDIAN PINES 2010 and HOUSTON 2013B experiments. The matrices correspond to those at the end of the feature learning, for one specific run of AS-BANDS with $\lambda = 0.0001$. In both plots, each column corresponds to a feature selected by the proposed algorithm and each row to one class; the color corresponds to the strength of the weight (positive or negative). One can appreciate that the selected features (columns) have large coefficients - corresponding to strong green or brown tones in the figures - for more than one class (the rows).

⁴Only squared structuring elements were used and the filter size range was⁵⁶⁹ 570 pre-defined by expert knowledge.



Figure 8: Final weight matrix for a run of the INDIAN PINES 2010 (top) and $^{603}_{604}$ HOUSTON 2013B (bottom) experiments.



Figure 10: Analysis of the depth of the features in the final active set of one run of the ASH-BANDS and $\lambda = 0.001$.

571 4.4. Features visualization in AS-BANDS

Figure 9 illustrates some of the features selected by AS-625 572 BANDS in the HOUSTON 2013B case. Each column corresponds⁶²⁶ 573 to a different zoom in the area and highlights a specific class.⁶²⁷ 574 We visualized the features of the same run as the bottom row⁶²⁸ 575 of Fig. 8 and visualized the six features with highest $||W_{i..}||_2$, 576 corresponding to those active for most classes with the highest 577 squared weights. By analysis of the features learned, one can⁶³¹ 578 appreciate that they clearly are discriminative for the specific 632 579 classification problem: this shows that, by decreasing the over-580 634 all loss, adding these features to the active set really improves 581 . 635 class discrimination. 582 636

4.5. Role of the features issued from the hierarchical model ASH-BANDS 638

⁵⁸⁵ Finally, we study in detail the hierarchical features that have⁶⁴⁰ ⁵⁸⁶ been discovered by our method. First, we discuss the distribu-⁶⁴¹ tion of the depth of features in the active set in the ASH-BANDS⁶⁴² ⁵⁸⁸ model. Top row of Fig. 10 shows the distribution of the weights⁶⁴³ ⁶⁴⁹ of the features in both the inputs bank *B* and in the active set φ at the end of the feature learning. Regarding the final bank B, which contains 489 features in the INDIAN PINES 2010 and 244 in the HOUSTON 2013A case, most of the features are of depth 0 (the original features), 1 and 2. But if we consider the final active set φ , of size 67 (INDIAN PINES 2010) and 56 (Houston 2013A), we see that the median depth is of 2 in both cases: this means that no features of depth 0 (no original features) are kept in the final active set. The only exception is provided by the LiDAR data in the Houston 2013A dataset, which is kept in the final active set. These observations are confirmed by the distributions illustrated in the bottom row of Fig. 10: the distribution of depths in the final bank B (blue dashed line) has 60-70% of features of depth 0, while the distribution of the features selected during the iterations (green line with circle markers) shows an average more towards a depth of 2. The features in the final active set φ (red line) show a distribution even more skewed towards higher depth levels, showing that features of low depth (typically depths of 1) are first added to φ and then replaced by features with higher depth issued from them.

To confirm this hypothesis even further, we study some of the features in the final active set, illustrated in Fig. 11: when considering features of higher depth, we can appreciate the strong nonlinearity induced by the hierarchical feature construction, as well as the fact that intermediary features (the original band 105 or the features of depth 2) are discarded from the final model, meaning that they became uninformative during the process, but were used as basis to generate other features that were relevant. Another interesting behavior is the bifurcation observed in these features: the entropy filter on band 105 was re-filtered in two different ways, and ended up providing two very complementary, but informative filters to solve the problem.

5. Conclusions

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In this paper, we proposed an active set algorithm to learn relevant features for spatio-spectral hyperspectral image classification. Confronted to a set of filters randomly generated from the bands of the hyperspectral image, the algorithm selects only those that will improve the classifier if added in the current input space. To do so, we exploit the optimality conditions of the optimization problem with a regularization promoting groupsparsity. We also propose a hierarchical extension, where active features (firstly bands and then also previously selected filters) are used as inputs, thus allowing for the generation of more complex, nonlinear filters. Analysis of four hyperspectral classification scenarios confirmed the efficiency (we use a fast and linear classifier) and effectiveness of the approach. The method is fully automatic, can include the user favorite types of spatial or frequency filters and can accommodate multiple co-registered data modalities.

In the future, we would like to extend the hierarchical algorithm to situations, where a datasets shift has occurred between the training and testing distribution: we observed that the proposed hierarchical algorithm yields lower performances on data with spectral distortion between training and test data, as in the HOUSTON 2013B dataset. Moreover, connections to deep neural



Figure 9: Visualization of the features with highest $||W_{j,\cdot}||_2$ for one run of the HOUSTON 2013B results (cf. bottom matrix of Fig. 8). First row: RGB subsets; second row: ground truth; third row: output of the classification with the proposed approach; fourth row to end: visualization of the six features with highest squared weights.

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nets can be better formalized and lead to more principled way
 of exploring and choosing the features.

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Figure 11: Examples of the bands retrieved by the hierarchical feature learning for one specific run of the experiments on the HOUSTON 2013A dataset. Highlighted are bands that are included in the final active set (after 100 iterations).

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