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# An Approach to the Health Monitoring of the Fuel System of a Turbofan

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Abstract— This paper focuses on the monitoring of the fuel system of a turbofan which is the core organ of an aircraft engine control system. The paper provides a method for real time onboard monitoring and on-ground diagnosis of one of its subsystems: the hydromechanical actuation loop. First, a system analysis is performed to highlight the main degradation modes and potential failures. Then, an approach for a real-time extraction of salient features named indicators is addressed. Onground diagnosis is performed through a learning algorithm and a classification method. Parameterization of the on-ground part needs a reference healthy state of the indicators and the signatures of the degradations. The healthy distribution of the indicators is measured on field data whereas a physical model of the system is utilized to simulate degradations, quantify indicators sensibility and construct the signatures. Eventually, algorithms are deployed and statistical validation is performed by the computation of key performance indicators (KPI).

Keywords— Health Monitoring, Diagnosis, Hydromechanical Systems, Actuation Loop, Servovalve, Cylinder, Classification

## I. INTRODUCTION

In aeronautics, the severity of operational availability requirements combined with the increasing complexity of systems gives interest to prognostics and health management (PHM). Standards for PHM according to IEEE are presented in [1]. For aircraft engine manufacturers, PHM is an opportunity to monitor the state of health of the turbofan, to provide a diagnosis support in maintenance and to limit delays and cancellations.

A good state-of-the-art of the main axes of research in PHM can be found in [2] and some of the methods have already been applied in particular in the field of electronics, for example to monitor the remaining useful lifetime of batteries [3]. In France, some PhD works such as [4] or [5] have addressed the issue of modelling a multi-levels architecture for a complex system's monitoring process or formalizing the prognostics process [6].

In the field of predictive monitoring applied to aeronautics, research is mainly focused on the development of algorithmic methods for diagnosis and prognostics. Some good reviews on

the subject can be found in [7] for the diagnosis and [8] for prognostics.

However, academic research is often detached from the industrial needs on the following points: (1) health monitoring is currently restricted to captor faults, vibration analysis and structural surveillance but health assessment of control systems is rarely addressed; (2) papers commonly make the hypothesis that every variable is measured so indicators are easily constructible but actually, the position and the number of sensors are defined and cannot be changed; (3) the extraction of indicators must be performed on-board and the issues related to the real time in-situ computation is almost never addressed and (4) physical models are necessary to quantify the impacts of degradation and their probable evolution.

This paper is part of a larger project which aims at providing an integrated method for developing a PHM system with emphasis on the indicators construction adapted to inflight computation requirements and the use of physical models to simulate the degradation impacts. The targeted system for the application is the fuel system of a turbofan, the main organ of the engine control system. This paper focuses on the diagnosis of the following subsystem: an actuation loop dedicated to the position control of a variable geometry. The study will be articulated around five points: System Analysis, Indicators, Degradations Modelling, Indicator Transformation Laws Computation and Statistical Validation of Performances.

#### II. SYSTEM ANALYSIS

In order to monitor a system, the first step is to determine its degradation modes and it can be achieved through expertise, experience feedback or FMEMA. This study will focus on the mechanical degradations of the system and electrical ones will not be treated.

The system is a closed loop composed of three main components: A controller, a servovalve and a cylinder. The position of the cylinder is measured by a linear variable differential transformer (**LVDT**), as shown in Fig. 1.

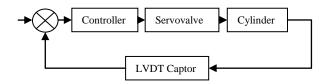


Fig. 1: Schematic of the hydromechanical actuation loop

In this application, the studied servovalve type is two-stage flapper-nozzle. In this type of servovalve, the power transmission chain is the following one:

1. A control current is send to a torque motor

A.

- 2. The current is converted to a displacement of the flapper through an electromagnetic effect
- 3. The displacement of the flapper changes the position of the second stage spool via a hydraulic control
- 4. The position of the spool changes the distribution of the flows. A flapper-nozzle servovalve configuration is shown in Fig. 2.

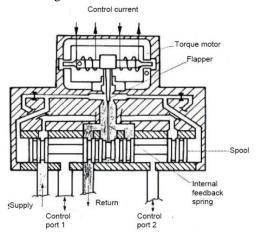


Fig. 2: Electrohydraulic flapper-nozzle servovalve configuration

The following list of the degradation modes selected for the servovalve is inspired by [9]:

- 1) Increased contamination of the filters: As dust and debris accumulate in the servovalve, filters gradually lose their efficiency and the hydraulic resistance increases. The result is a slower response of the servovalve.
- 2) Drift of the null bias current: As the torque motor ages and loses his magnetic properties, the null bias current of the servovalve, namely the current for which the flows are equal in control ports 1 and 2, can drift from its nominal value.
- 3) Increased backlash: With the progressive wear of the internal feedback spring, the hysteresis of the servovalve increases.
- 4) Increase of the friction force between spool and sleeve: This phenomenon is due to the cumulative effects of continuous movement of the spool and contamination of the hydraulic fluid because the debris induces a silting effect.

5) Increase in the radial clearance between spool and sleeve: Because of the contamination, abrasion of the corners of the spool lands resulting in an increase of internal leakage.

## B. Degradation modes of a cylinder

The cylinder considered in this application is a doubleacting hydraulic cylinder with a cooling diaphragm between the two sides. The hydraulic fluid used is fuel.

The following list of the degradation modes selected for the hydraulic cylinder is inspired by [10]:

- 1) Internal leakage between the two sides: As the seal ages, dust and debris accumulate between the seal and the sleeve resulting in an abrasive effect degrading the cylinder body.
- 2) Clogging of the cooling diaphragm: With the increase of the temperature, a coking of the fuel can occur, resulting in the clogging of the diaphragm.

### C. Other potential degradation modes

The list of degradation modes presented above is not exhaustive and many other phenomenons can occur such as a damage of the kinematic chain downstream of the cylinder or the burst of a pipe but the choice was made to focus only on the servovalve and cylinder's degradations.

#### III. INDICATORS

#### A. Flow Gain curve of a Servovalve

Among the different measures characterizing a servovalve, the flow gain curve is one of the most significative because it displays both static and dynamic features as shown in Fig. 3.

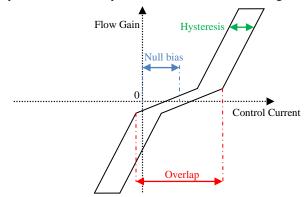


Fig. 3: Flow Gain curve and main features

The extraction of this curve requires that the servovalve is equipped with flowmeters but in our application, only the position of the cylinder is measured. However, the cylinder's velocity  $V_{cyl}$  and the servovalve output flows in each control port  $Q_{SV\_head}$  and  $Q_{SV\_rod}$  can be linked via the simplified equation:

$$V_{cyl} = \begin{cases} (Q_{SV\_head} - Q_{cooling}) / S_{head} \text{ during shaft outlet} \\ -(Q_{SV\_rod} - Q_{cooling}) / S_{rod} \text{ during shaft inlet} \end{cases}$$
 (1)

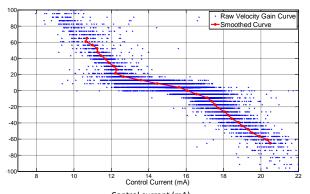
Where  $Q_{cooling}$  is the cooling flow between the two sides of the cylinder and  $S_{head}$  and  $S_{rod}$  are respectively the cross-sectional area of the head and the rod sides.

# B. Velocity Gain of a hydromechanical loop

In order to get around the lack of flowmeters to monitor the servovalve only, the idea is to monitor the whole loop by following salient features on the Velocity Gain curve.

This curve can be obtained only with the measures of both the control current  $I_{control}$  and the cylinder's velocity  $V_{cyl}$ . The value of  $V_{cyl}$  is computed by derivation of the cylinder's position  $X_{cyl}$ .

Blue points in Fig. 4 are the result of an extraction of the velocity gain curve performed during an entire flight. Because of the hysteresis of the servovalve, the dispersion of the points is substantial and therefore a smoothing algorithm based on local means is applied to the data.



Control current (mA)
Fig. 4: In-Flight extracted curve before and after smoothing

# C. Indicators Construction

From the extracted curve, we define many indicators related to the targeted degradation. Those indicators are listed in Table I and their graphical equivalent is shown in Fig. 5.

TABLE I
INDICATORS EXTRACTED FROM THE CURVE

Names		Targeted degradations	
Long	Short		
Slope change #1 abscissa	$X_1$	Degradations impacting the horizontal position of the curve  → Increase of the radial clearance between spool and sleeve	
Slope change #1 ordinate	<i>Y</i> <sub>1</sub>	Degradations impacting the vertical position of the curve  → Diaphragm clogging, cylinder internal leakage	
Slope change #2 abscissa	$X_2$	Idem X <sub>1</sub>	
Slope change #2 ordinate	<i>Y</i> <sub>2</sub>	Idem Y <sub>1</sub>	
Null Bias Current $I_{nb} = \frac{X_1 + X_2}{2}$	$I_{nb}$	Degradations impacting the value of the Null Bias  → Null Bias current shift	
Idle Current of the Loop (Current for null velocity)	$I_0$	Degradations impacting the static behaviour of the loop  → All the degradations	

Standard Deviation (hysteresis) at idle current	$Hys_0$	Degradations impacting the hysteresis  → Increased Backlash
Velocity Gain for Shaft Inlet	$G_{in}$	Degradations impacting the global dynamic behaviour of the loop  → Increased Backlash, Contamination of the filters, Increased friction force
Velocity Gain for Shaft Outlet	$G_{out}$	Idem $G_{in}$
Velocity Gain for Null Region	$G_{null}$	Idem $G_{in}$

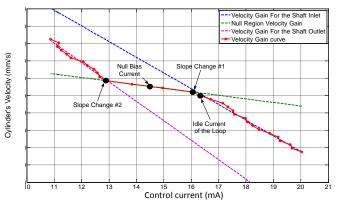


Fig. 5: Graphical representation of the indicators

#### IV. DEGRADATIONS MODELLING

# A. Model and Sub-models Construction

A physical model of the hydromechanical system has been developed in Matlab-Simulink® in order to simulate its behaviour in presence of some degradation and to quantify their impacts. This model is composed of three sub-models: Servovalve, cylinder and controller. The granularity of the sub-models must be important enough to simulate all the degradations discussed in the system analysis. For example, the sub-model of the servovalve, the most complex one, must include the modelling of the two-stages, the filters and the feedback spring. A good method for modelling servovalves is given in [11].

There are two ways degradations can be modelled: additive and multiplicative. The former consists in adding a value to some parameters and the latter consists in a multiplication of some parameters as shown in Fig. 6. In Fig. 6,  $Y_u$  and U are healthy values of variables, f is the degradation intensity and Y is the degraded value of variables.

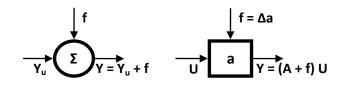


Fig. 6: Additive and Multiplicative modelling of degradations

# TABLE III MODELLING OF DEGRADATIONS

Degradation	Modelling		
Increased contamination of the filters	Multiplicative: To simulate a decrease of the efficiency, the flow is multiplied by a scalar in the range [0,1]		
Drift of the null bias current	Additive: A value corresponding to the opposite of the drift is added to the control current.		
Increased Backlash	Multiplicative:  Modification of the transfer function governing the position of the spool in the second stage.		
Increase of the friction force	Additive: Increase of the coefficient of friction between spool and sleeve.		
Increase in the radial clearance	Additive: Decrease of the restriction coefficient at the corners of the spool lands victims of abrasion.		
Internal leakage between the two sides	Additive: Increase of the restriction coefficient of the cooling flow		
Clogging of the cooling diaphragm	Additive: Decrease of the restriction coefficient of the cooling flow		

#### B. Recalibration of the model

The main hypothesis of this method is that operational data are available. Thus, it is supposed that the distribution of the indicators corresponding to a healthy state is well known.

For each simulation, the goal is to compute the velocity gain of the system by simulating the velocity of the cylinder for a gradually increasing control current from lower saturation boundary to upper saturation boundary.

Before simulating the degraded states, it is necessary to simulate and recalibrate the model parameters against operational data for the reference healthy state. Fig. 7 shows both extracted and estimated velocity gain curves for the healthy state. The estimated one is obtained from a model configured with averaged parameters given by constructors. The result after recalibration on parameters is also given in Fig. 7, and it can be noted that a difference remains between the curves around the idle current of the loop. The model used in this application is not enough accurate to explain this local deviation.

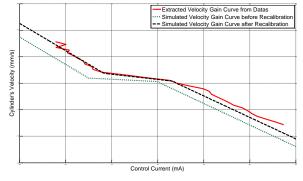


Fig. 7: Extracted against Estimated Velocity Gain of the healthy state

# C. Simulation of the degradations

For this paper, the focus will be on only two degradations namely the drift of the null bias current of the servovalve and the internal leakage between the two sides of the cylinder.

Results of the simulation on the recalibrated model with those two degradations are given in Fig. 8.

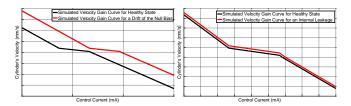


Fig. 8: (a) Left: effect of a null bias drift. (b) Right: effect of an internal leakage in the cylinder

#### V. INDICATORS TRANSFORMATION LAW COMPUTATION

#### A. Construction of the laws

In this part, a design of experiment is generated to organize the simulations of the behaviour of the system in presence of degradations. For each case, simulations are run for gradually increasing intensities of degradation. Eventually, the results are summarized in the form of indicators transformation laws (ITL).

With  $Ind_i$  representing the  $i^{th}$  indicator in a healthy state,  $Ind_i^{deg}$  the  $i^{th}$  indicator in presence of the degradation deg, and  $Int^{deg}$  the intensity of the degradation deg, the ITL named  $F_i^{deg}$  corresponding to the  $i^{th}$  indicator and the degradation deg can be defined as follows:

$$Int^{deg} \xrightarrow{F_i^{deg}} \Delta I_i^{deg} = A_i^{deg} Int^{deg}$$
 (2)

where  $A_i^{deg}$  is the coefficient of the linear regression of  $\Delta I_i^{deg}$  with respect to  $Int^{deg}$ .  $\Delta I_i^{deg}$  is the change in the value of the indicator and can be also expressed this way:

$$\Delta I_i^{deg} = Ind_i^{deg} - Ind_i \tag{3}$$

Thus,  $F_i^{deg}$  provides the change in the indicator's value for a given intensity of degradation.

#### B. Utilization of the laws

Once computed, an ITL makes it possible to generate an estimated value of indicators for a degraded state from a healthy value computed from operational data according to the following equation:

$$I_i^{deg} = I_i^{healthy} + \Delta I_i^{deg} \tag{4}$$

In this application, 7 degradations and 10 indicators are considered, which means that 70 ITL must be computed. For instance, the law giving the value of  $X_1$  for the degradation drift of the null bias current is:

$$I_{\chi_1}^{NB\ drift} = I_{\chi_1}^{healthy} + A_{\chi_1}^{NB\ drift} Int^{NB\ drift}$$
 (5)

Where  $I_{X1}^{healthy}$  is computed by averaging the extracted value of  $X_1$  for a given number of flights for which the system is considered flawless.

#### VI. STATISTICAL VALIDATION OF PERFORMANCES

### A. Key Performance Indicators

For this application, both fault detection and diagnosis are addressed. A presentation and definition of Key Performance Indicators (KPI) is given in Table III.

#### TABLE IIIII KEY PERFORMANCE INDICATORS

KPI	Definition
False Positive Rate	Proportion of False Positive (false alarm) among all the states where a fault is detected (see Fig. 9)
False Negative Rate	Proportion of False Negative (undetected faults) among all the states where no fault is detected (see Fig. 9)
False Classification Rate	Proportion of False Classification among all classifications
Robustness	Capacity of the monitoring system to be still efficient when some parameters drift from their nominal values.

#### **Estimated Condition**

No Fault	Fault
NFD	FP
FN	FD
	NFD

Fig. 9: Condition Assessment Matrix

#### B. Method for fault detection and diagnosis

A more precise presentation of the method presented below can be found in [12].

#### 1) Indicators Model Learning:

The first step is to learn a Gaussian model of the indicators distribution in a reference state, typically a healthy state. The model is learned from extracted indicators on a given number of flights and is presented as follows:

$$Model(i) = \begin{pmatrix} \mu_i^{healthy} \\ \sigma_i^{healthy} \end{pmatrix} \tag{6}$$
 where  $\mu_i^{healthy}$  is the mean of the indicators and  $\sigma_i^{healthy}$  their

standard deviation.

# 2) Fault Detection:

It is based on an abnormality score named  $Z_{score}$ . For the indicator i,  $Z_{score,i}$  is defined as follows:

$$Z_{score,i} = \frac{I_i - \mu_i^{healthy}}{\sigma_i^{healthy}} \tag{7}$$

where  $I_i$  is the currently measured value of indicator.

Then a global abnormality score of the system Global\_Z<sub>score</sub> is computed from  $Z_{score,i}$  with  $i \in [1; 10]$  via the Mahalanobis distance [13].

Indicators are extracted on-board and Global\_Z<sub>score</sub> is computed on-ground at each flight. The parameterization of the fault detection consists in defining a relevant threshold value Thr and if the value of  $Global\_Z_{score}$  crosses Thr, it means that a fault has been detected.

# 3) Diagnosis:

Diagnosis is performed via a classification of signatures. A signature is a vector of indicators. For this application, a signature is a vector appending 10 indicators extracted from flight data:

$$Sign = \left(Z_{score,X_1}, Z_{score,Y_1}, \dots, Z_{score,G_{null}}\right)^T \tag{8}$$

If the system is healthy, Sign is a zero vector of size 10.

Assuming that the maximal intensities of the degradations are known, it is possible to determine the signatures of the degradations  $Sign_{ref,deg}$  associated.

$$Sign_{ref,deg} = \left(\frac{I_{X_1}^{deg} - \mu_{X_1}^{healthy}}{\sigma_{X_1}^{healthy}}, \dots, \frac{I_{G_{null}}^{deg} - \mu_{G_{null}}^{healthy}}{\sigma_{G_{null}}^{healthy}}\right)^T \tag{9}$$

When a fault is detected, the classification algorithm is run. This algorithm is based on a pattern recognition method which finds the reference signature that most closely matches the currently measured signature. A guilt probability is assigned to each component of the system.

# C. Statistical Validation

# 1) Matrix of the signatures

To perform fault detection and diagnosis, it is essential to determine the matrix of the signatures. It shows the signature corresponding to the maximal intensity of the degradations. A part of this matrix, taking into account only two degradations is given in Table IV.

TABLE IV MATRIX OF THE SIGNATURES

Degradation	Influences $(Z_{scores})$									
	$X_1$	$Y_1$	$X_2$	$Y_2$	$I_{nb}$	$I_0$	$Hys_0$	$G_{in}$	$G_{out}$	$G_{null}$
Drift of the null bias current	24	0	26	0	28	24	0	0	0	0
Internal leakage between the two sides	0	4	0	11	0	1	0	0	0	0

# 2) Performances of fault detection

Once the matrix of the signatures is available, a detection threshold Thr on the global score Global\_Zscore must be

The value of this threshold must be low enough to ensure detection of all the different degradation, even those not provided by the system analysis and high enough to ensure a low rate of false alarms. To set this value in an optimal way, it is essential to take into account the standard deviation of the *Global\_Z<sub>score</sub>*.

First, the computation of the maximum likelihood function of  $Global\_Z_{score-healthy}$  is performed to set a first value of Thr, as shown in Fig. 10. In this paper, the likelihood function is a Gaussian and its parameters are the mean  $\mu_{healthy}$  and the standard deviation  $\sigma_{healthy}$ . Typically, the chosen value for Thr is:

$$Thr = \mu_{healthy} + A. \, \sigma_{healthy} \tag{10}$$

At first approach, the chosen value for A is A = 2 because it ensures only 5% of false detection. However, this value can potentially limit the false negative rate, so it is necessary to check if the degradations are still detectable.

To ensure the performances, the distributions of  $Global\_Z_{score-healthy}$ ,  $Global\_Z_{score-leak}$  and  $Global\_Z_{score-drift}$  are compared as presented in Fig. 10.

Performances for different values of A are proposed in Table V.

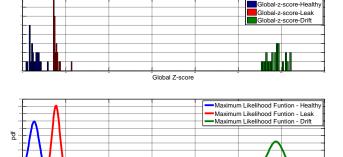


Fig. 10: Distribution of Global\_scores and likelihood functions

### TABLE V FAULT DETECTION PERFORMANCES

	Null B	ias Drift	Internal Leakage		
A	False Positive Rate	False Negative Rate	False Positive Rate	False Negative Rate	
0	0%	0%	50%	0%	
1	0%	0%	16%	0%	
2	0%	0%	3%	0%	
3	0%	0%	0.3%	2%	
5	0%	0%	0%	6%	

#### 3) Performances of diagnosis

The classification algorithm gives, for each component of the system, a probability of guilt proportional to the collinearity between the current signature and the referenced signatures. The diagnosis performances depend on the intensity of the degradations. Results are shown in Table VI.

#### TABLE VI DIAGNOSIS PERFORMANCES

Effective Degradation	Percentage of max intensity (From ITL)	Probability of guilt of Drift	Probability of guilt of Leak
Drift	25%	0.94	0.06
Drift	50%	0.94	0.06
Drift	100%	0.94	0.06
Leak	25%	0.37	0.63
Leak	50%	0.13	0.87
Leak	100%	0.11	0.89

#### VII. CONCLUSIONS

This paper provides a methodology to perform fault detection and diagnosis on a hydromechanical actuation loop. A first part details how to construct relevant indicators to perform on-board extraction of indicators and a second part how to achieve and validate fault detection and diagnosis onground. It must be noted that further works will follow, dealing with the management of uncertainties, the architecture of monitoring for a wider system and also prognostics.

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