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MODELING RAPID FLOOD PROPAGATION OVER NATURAL TERRAINS USING A WELL-BALANCED SCHEME

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ABSTRACT

The consequences of rapid and extreme flooding events, such as tsunamis, riverine flooding and dam breaks show the necessity of developing efficient and accurate tools for studying these flow fields, and devise appropriate mitigation plans for threatened sites. Two-dimensional simulations of these flows can provide information about the temporal evolution of water depth and velocities, but the accurate prediction of the arrival time of the flood and the extent of the inundated areas still pose a significant challenge for numerical models of rapid flows over rough and variable topographies. Careful numerical treatments are required to reproduce the sudden changes in velocities and water depths, evolving under strong nonlinear conditions that often lead to breaking waves or bores. In addition, new controlled experiments of flood propagation in complex geometries are also needed to provide data for testing the models and evaluate their performance in more realistic conditions. In this work we implement a robust well-balanced numerical model to solve the nonlin-

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ear shallow water equations (NSWE) in a non-orthogonal boundary-fitted curvilinear coordinate system. We show that the model is capable of computing flows over highly variable topographies, preserving the positivity of the water depth, and providing accurate predictions for wetting and drying processes. The model is validated against benchmark cases that consider the use of boundary-fitted discretizations of the computational domain. In addition, we perform a laboratory experiment of a rapid flood over a complex topography, measuring the propagation of a dam-break wave on a scaled physical model, registering time series of water depth in 19 cross-sections along the flow direction. We use the data from this experiment to test our numerical model, and compare our model performance with the numerical results of two other recognized NSWE models, showing that ours is a reliable tool for predicting efficiently and accurately extreme inundation events and long-wave propagation over complex topographies.

Keywords: Shallow water equations, shock capturing methods, well-balanced schemes, boundary-fitted curvilinear coordinates

INTRODUCTION

In recent years, a number of catastrophic events have involved rapid flooding over complex topography, such as tsunamis and river floods. In Chile, for example, several Glacial-lake outburst floods (GLOF) have occurred in the Colonia river, a tributary of the Baker river ($47^{\circ}10' \text{ S}$; $73^{\circ}20' \text{ W}$), as a consequence of the Cachet-II lake outburst. In fact, two major events in 2008 generated an increase of the Baker river free surface elevation of above 4.5 m and a peak discharge over $3,000 \text{ m}^3/\text{s}$ (DGA Satellite monitoring station at Baker River, DGA-MOP, Chile), flooding large parts of the Colonia and Baker river valleys and putting at risk the town of Caleta Tortel, located at the mouth of the Baker river (Dussailant et al. 2009). This event has repeated two times a year since 2008, which is likely linked to significant increments of temperature that have been registered on the entire watershed in the last years.

Recently, on February 27th 2010, an 8.8 Mw earthquake occurred off the coast of south-central Chile (Fritz et al. 2011; Lay et al. 2010), generating a destructive tsunami that affected a significant portion of the coast, the Juan Fernández Archipiélago, and Easter Island, taking the lives of 124

43 people. As a consequence of these events, local authorities and the central government are cur-
44 rently developing new hazards and risk plans in different coastal communities along Chile, which
45 consider the investigation of the inundation extent and maximum water depth estimations, peak
46 discharge and velocities, among other hydrodynamic variables for riverine floods and tsunamis.

47 In order to study the large and costly consequences of these major rapid flooding events, it is
48 necessary to develop instruments that can be used to predict accurately and efficiently the flow
49 velocities and water depths, and assess their associated hazards and risks. A good estimation
50 of flow features such as run-up, affected areas, and arrival time of the peak flood will lead to
51 define better the mitigation plans, early warning systems, and improve the preparedness of people
52 when facing such catastrophic situations, incorporating the hydrodynamic forces into the design
53 of coastal and riverine infrastructure (Federal Emergency Management Agency 2011; American
54 Society of Civil Engineers 2006; Yeh 2006).

55 The Nonlinear Shallow Water Equations (NSWE) are usually employed in these cases to de-
56 scribe the flow dynamics, and model fairly long-waves in a homogeneous and incompressible fluid.
57 They are obtained by vertically averaging the three-dimensional Navier-Stokes equations assuming
58 a hydrostatic pressure distribution, resulting in a set of horizontal two-dimensional hyperbolic con-
59 servation laws that describe the evolution of the water depth and depth-averaged velocities (Cunge
60 et al. 1980; Stoker 1992).

61 In the last decades, a significant number of numerical models have been developed to simulate
62 these complex flows, employing finite-difference methods (e.g. Molls and Chaudry 1995; Molls
63 and Zhao 2000), finite-element methods (e.g. Berger and Stockstill 1995; Tucciarelli and Termini
64 2000), or finite-volume methods (e.g. Valiani et al. 2002; Zhou et al. 2004; Loose et al. 2005). In
65 the framework of finite volume methods, Godunov-type formulations have become very useful to
66 solve the NSWE, since they can reproduce complex discontinuities such as shock-waves or wet-
67 dry interfaces by solving a Riemann problem at each cell interface of the discretized domain (Toro
68 2001; Leveque 2002).

69 Many environmental flows such as bore propagation (Hibberd and Peregrine 1979), tsunami

70 inundations (Yeh 1991), or glacial lake outburst floods (Cenderelli and Wohl 2001), fall within this
71 category of extreme flood events that can be represented by the NSW. They are characterized by
72 rapid wetting and drying over highly variable topographies, giving rise to complex unsteady free
73 surface dynamics which pose a significant challenge for the numerical models. Numerical strate-
74 gies for integrating the governing equations in these shallow extreme flows must also deal with
75 complicated geometries and the highly complex dynamics of wave breaking and run-up. Simi-
76 larly, the discretization of the boundaries of the physical domain may have a strong influence in
77 the development of the flow dynamics, introducing errors or numerical instabilities if not carefully
78 performed (Baghlani et al. 2008).

79 Motivated by these applications, in this investigation we develop an efficient numerical model
80 to solve the two-dimensional dynamics of extreme flows over natural terrains. We extend the
81 method of Marche et al. (2007), which has shown to resolve complex features of free-surface
82 flows by implementing a well-balanced approach. Well-balanced schemes are specifically con-
83 ceived to preserve local and global mass conservation to machine accuracy, maintaining also the
84 steady and motionless states. To achieve this requirement, it is necessary to discretize carefully
85 the friction and bed-slope source terms (see Greenberg and Leroux 1996; LeVeque 1998; Gallouet
86 et al. 2003; Audusse et al. 2004; Liang and Marche 2009, for more details). We formulate and
87 solve the governing equations in a non-orthogonal generalized curvilinear coordinate framework
88 to model extreme flows propagation over natural terrains. We use a finite volume well-balanced
89 approach based on a robust VFRoe-relaxation Riemann solver (Gallouet et al. 2003; Berthon and
90 Marche 2008), calculating mass and momentum fluxes at cell interfaces and performing the hy-
91 drostatic reconstruction method proposed by Audusse et al. (2004). The source term that accounts
92 for friction effects is treated with the semi-implicit fractional-step approach of Liang and Marche
93 (2009). Validation of the new model is presented through the comparison with benchmark tests,
94 which are specifically chosen to assess its ability to deal with wet-dry interfaces, complex geome-
95 tries, shocks, friction and bathymetric source terms.

96 In addition, the future studies of these flows will require new experiments, representing the

97 complex features of rapid flooding events over realistic arbitrary geometries, to test and improve
98 the numerical models. In this investigation we also perform a dam-break experiment on a scaled
99 physical model, representing the bed and banks of a mountain river. We register time-series of
100 water depth, and then compare the results with simulations carried out with the new well-balanced
101 numerical model, showing that it can capture the most relevant characteristics of the flow. Fur-
102 thermore, in order to compare our model performance with previously validated numerical mod-
103 els, we simulated this experience using two well-known shock-capturing NSW models, AnuGA
104 (Mungkasi and Roberts 2013) and GeoClaw (Berger et al. 2011). From this comparison we can
105 establish the improvement achieved by our numerical approach in terms of the overall agreement
106 of the free surface variations in time, the estimation of the maximum amplitude of the propagated
107 bore and its arrival time to different locations.

108 The paper is organized as follows: In section 2 we present the non-dimensional governing
109 equations and the partial transformation to generalized non-orthogonal curvilinear coordinates that
110 are employed in the model. The numerical scheme and the different algorithms used to integrate
111 the NSW are briefly described in section 3. Validation tests and comparisons of numerical simu-
112 lations with benchmark cases and previously published experimental data are presented in section
113 4. In section 5 we describe new dam-break experiments conducted in the Hydraulic Laboratory of
114 the Pontificia Universidad Católica de Chile, intended to further validate the model over a realistic
115 and highly variable topographic configuration. Conclusions and future perspectives of this work
116 are discussed in section 6.

117 **GOVERNING EQUATIONS**

118 The two-dimensional NSW are a system of nonlinear partial differential equations represent-
119 ing the mass and momentum conservation laws, which were originally derived by Saint-Venant
120 (1871). The fluid is assumed as incompressible and homogeneous, with hydrostatic pressure dis-
121 tribution. The shallow water or long-wave hypothesis considers negligible vertical velocities and
122 depth-uniform horizontal velocities. Hence, the NSW are often applied to river or nearshore
123 flows where the characteristic horizontal wave-length is much longer than the characteristic water

124 depth (see Cunge et al. 1980, for more details).

125 In what follows, we will work with a non-dimensionalized set of NSWE by choosing charac-
126 teristic horizontal and vertical length-scales and a velocity scale (\mathcal{L} , \mathcal{H} , and \mathcal{U} respectively). By
127 defining the length and velocity scales of the flow, the time-scale is represented by $T = \mathcal{L}/\mathcal{U}$,
128 and the dimensionless Froude number by $Fr = \mathcal{U}/\sqrt{g\mathcal{H}}$, which quantifies the relative importance
129 of inertial effects over gravity (g). The dimensional variables, noted with a hat ($\hat{\cdot}$), are hereafter
130 defined as $\hat{x} = \mathcal{L}x$, $\hat{y} = \mathcal{L}y$, $\hat{z} = \mathcal{H}z$, $\hat{h} = \mathcal{H}h$, $\hat{u} = \mathcal{U}u$, $\hat{v} = \mathcal{U}v$, and $\hat{t} = Tt$, where \hat{x} and \hat{y}
131 represent the Cartesian directions, \hat{z} defines the bed elevation, \hat{h} is the water depth, \hat{u} and \hat{v} are the
132 depth-averaged flow velocities in each Cartesian direction, and \hat{t} is the time. In order to reproduce
133 better complex arbitrary geometries, we introduce a boundary-fitted curvilinear coordinate system
134 in two dimensions denoted by the system (ξ, η) . Generalized curvilinear coordinates are chosen to
135 follow the boundaries of the physical domain, adapting the grid to the geometrical details of the
136 terrain. With this transformation we can have a better resolution in zones of interest and an ac-
137 curate representation of the boundaries, resulting in an efficient discretization of the flow domain
138 (Lackey and Sotiropoulos 2005; Liang et al. 2007; Baghlani et al. 2008).

139 The Cartesian NSWE can be partially transformed to this new coordinate system maintaining
140 the hydrodynamic variables referenced to the Cartesian frame. This procedure is known as partial
141 transformation and only modifies the mass and momentum fluxes of the governing equations. The
142 full transformation would change the hydrodynamic variables vector, $Q = [h, hu, hv]^T$, to the ve-
143 locity components in the ξ and η directions, using the so-called contravariant velocity components,
144 and the derivatives in the convective terms would yield the well-known Christoffel symbols of the
145 second kind (Ahn and Hosoda 2007). Therefore, considering only bed-slope and friction source
146 terms, the non-dimensional NSWE can be written in curvilinear coordinates in the following form
147 (Lackey and Sotiropoulos 2005),

$$148 \quad \frac{\partial Q}{\partial t} + J \frac{\partial F}{\partial \xi} + J \frac{\partial G}{\partial \eta} = S_b(Q) + S_f(Q) \quad (1)$$

149 where Q is the vector of hydrodynamic variables, F and G are the flux vectors expressed in terms

150 of the new spatial coordinate system ξ and η , respectively, and $S_b(Q)$ and $S_f(Q)$ are the source
 151 terms vectors. These vectors are given by the following expressions:

$$\begin{aligned}
 152 \quad Q &= \begin{pmatrix} h \\ hu \\ hv \end{pmatrix}, F = \frac{1}{J} \begin{pmatrix} hU^1 \\ uhU^1 + \frac{1}{2Fr^2}h^2\xi_x \\ vhU^1 + \frac{1}{2Fr^2}h^2\xi_y \end{pmatrix}, G = \frac{1}{J} \begin{pmatrix} hU^2 \\ uhU^2 + \frac{1}{2Fr^2}h^2\eta_x \\ vhU^2 + \frac{1}{2Fr^2}h^2\eta_y \end{pmatrix}, \quad (2) \\
 153 \quad S_b(Q) &= \begin{pmatrix} 0 \\ -\frac{h}{Fr^2}(z_\xi\xi_x + z_\eta\eta_x) \\ -\frac{h}{Fr^2}(z_\xi\xi_y + z_\eta\eta_y) \end{pmatrix}, S_f(Q) = \begin{pmatrix} 0 \\ -S_{fx} \\ -S_{fy} \end{pmatrix}
 \end{aligned}$$

154 where h represents the water depth, u and v are the non-dimensional depth-averaged flow velocities
 155 in each Cartesian directions; z defines the bed elevation, z_ξ and z_η define the local bed slope with
 156 respect to the transformed coordinate system (ξ, η) and S_f represents the friction source term.

157 The additional terms that appear in the fluxes, ξ_x , ξ_y , η_x , and η_y are the resulting metrics
 158 associated to the coordinate change, and $J = \xi_x\eta_y - \xi_y\eta_x$ is the Jacobian of the transformation,
 159 which will remain constant for a fixed grid. U^1 and U^2 are the contravariant velocity components,
 160 expressed as $U^j = u\epsilon_x + v\epsilon_y$ with $(j, \epsilon) \in \{(1, \xi), (2, \eta)\}$. The transformed system of equations
 161 is discretized on a rectangular and uniform grid in the transformed space (ξ, η) using the finite
 162 volume method that is described in the next section.

163 NUMERICAL SCHEME

164 The curvilinear NSWE system given in Eq. (1) is integrated using a finite volume well-balanced
 165 scheme, coupled with a splitting strategy for the treatment of source terms (Liang and Marche
 166 2009). We decompose the solution associated to the system of equations (1) at each time step
 167 by solving two systems, one associated to the NSWE with topography source terms and a second
 168 associated to the remaining friction terms. In the following subsections we describe the different
 169 steps of the algorithm, including the implementation of the boundary conditions, and the stability
 170 criterion of the numerical solution.

Solution of the NSWE with Topography Source Terms

In this step we solve the following system associated to NSWE with topography source terms,

$$\frac{\partial Q}{\partial t} + J \frac{\partial F}{\partial \xi} + J \frac{\partial G}{\partial \eta} = S_b(Q) \quad (3)$$

We seek a numerical strategy that provides stable shock-capturing integration of system (3) with a precise control of the spurious oscillations induced by numerical dispersion. In addition, the scheme should be able to handle the complex interactions between flow and topography, including the preservation of motionless and steady states. We choose to adapt the robust second-order finite volume scheme introduced by Marche et al. 2007 to the non-orthogonal boundary-fitted coordinate framework.

Taking into account the new system of coordinates, the spatial discretization of Equation (3) can be recast under the following semi-discrete finite-volume formalism,

$$\frac{d}{dt} Q_{i,j} + \frac{J_{i,j}}{\Delta \xi} (F_{i+\frac{1}{2},j}^* - F_{i-\frac{1}{2},j}^*) + \frac{J_{i,j}}{\Delta \eta} (G_{i,j+\frac{1}{2}}^* - G_{i,j-\frac{1}{2}}^*) = S_{b(i,j)} \quad (4)$$

where $Q_{i,j}$ is the vector of cell-centered hydrodynamic variables, $J_{i,j}$ is the cell-centered Jacobian of the coordinate transformation, $F_{i\pm\frac{1}{2},j}^*$ and $G_{i,j\pm\frac{1}{2}}^*$ correspond to the numerical flux functions through the (i,j) cell interfaces, and $S_{b(i,j)}$ to the centered discretization of the bed-slope source term. We denote by $\Delta \xi$ and $\Delta \eta$ the cell sizes, and the interface between the $(i,j)^{th}$ cell and the $(i+1,j)^{th}$ by $(i+\frac{1}{2},j)$, as depicted in Fig. 1.

The computation of the numerical fluxes $F_{i\pm\frac{1}{2},j}^*$ and $G_{i,j\pm\frac{1}{2}}^*$ is achieved using a robust VFRoe-relaxation scheme proposed by Gallouet et al. (2003). To achieve a second order accurate scheme, we straightforwardly apply the MUSCL extrapolation proposed by Van Leer (1979). This technique considers that numerical fluxes are computed by linearly reconstructing the hydrodynamic variables, leading to more accurate reconstructed states at each side of the interface of every cell as shown in Fig. 1 (see Bouchut 2004, for details). In order to handle topographic variations and the requirement for the preservation of static flows, we also adapted the well-balancing discretiza-

195 tion for the bed-slope term proposed by Audusse et al. (2004) to the boundary-fitted curvilinear
 196 coordinate system of equations. In this step of the algorithm we built a linear reconstruction of the
 197 topography considering the MUSCL reconstructed hydrodynamic variables as shown in Marche
 198 et al. (2007). Finally, the source term $S_b(Q)$ is estimated through the new reconstructed values of
 199 the fluxes. For a detailed description of the computation of the fluxes and the hydrodynamic vari-
 200 ables the reader is referred to the work of Marche et al. (2007) and Berthon and Marche (2008).

201 **Solution of the Friction Source Terms**

202 The friction source term is incorporated using the splitting semi-implicit method proposed
 203 by Liang and Marche (2009). The corresponding ordinary differential equation of the splitting
 204 operation is defined as follows,

$$205 \quad \frac{dQ}{dt} = S_f \quad (5)$$

206 where

$$207 \quad S_f = (0, -\tau_{fx}, -\tau_{fy})^T \quad (6)$$

208 In this equation, the terms τ_{fx} and τ_{fy} are the non-dimensionalized bed shear-stresses for each
 209 cartesian direction. The magnitude of the bed shear stresses in each direction can be calculated as
 210 follows:

$$211 \quad \tau_{fx} = C_f u \sqrt{u^2 + v^2} \quad (7)$$

$$212 \quad \tau_{fy} = C_f v \sqrt{u^2 + v^2} \quad (8)$$

213 where C_f is a non-dimensionalized bed friction coefficient, which can be expressed using one of
 214 the standard existing approaches developed for uniform flows such as Manning or Chézy.

215 Following the algorithm developed by Liang and Marche (2009), equation (5) is integrated
 216 using an implicit scheme and a second-order Taylor series expansion. Note that an additional
 217 friction limitation may be locally added to prevent from unphysical flow reversing, due to large

218 drag forces in vanishing depth areas, as mentioned by Burguete et al. (2008).

219 As far as time-discretization is concerned, we use a classical second-order Runge-Kutta scheme
220 for each time-step in this splitting approach. In order to solve system shown in Eq. (1) at the
221 boundaries of the computational domain, we have implemented and tested in the model three types
222 of boundary conditions: i.) Transmissive or open boundary, allowing the information to freely
223 leave the domain without propagating spurious information back to the domain; ii.) Solid wall or
224 close boundary, that imposes no discharge through the boundary of the domain; and iii.) Absorb-
225 ing/Generating boundary condition, which relies on the work of Sanders (2002) and Cienfuegos
226 et al. (2007), which allow to prescribe inflow discharge or free surface information at the bound-
227 ary, such as incoming waves or stage-discharge relationships, and freely evacuate back-traveling
228 waves. Finally, the stability of the numerical model is controlled by the Courant-Friedrich-Lewy
229 criterion (CFL) (Toro 2001).

230 **VALIDATION**

231 As previously explained, the numerical model in non-orthogonal generalized coordinates is
232 based on the method of Marche et al. (2007), incorporating bed-friction with the splitting semi-
233 implicit method of Liang and Marche (2009). Initially, we validated the model using various
234 benchmark cases that are not shown herein, for rectangular domains employing discretizations in
235 Cartesian coordinates. These first tests involved shock-capturing and moving shoreline problems,
236 obtaining quantitatively accurate results in comparison with analytical solutions and laboratory
237 data, which are the same cases previously studied by Marche et al. (2007). The following series of
238 benchmark tests are intended to illustrate the improvements obtained when a boundary-fitted curvi-
239 linear discretization is used, and to prove the ability of the model to deal with complex geometries,
240 bed-slope, and friction source terms.

241 **Dam-Break in a Convergent-Divergent Flume**

242 We test the numerical model with a dam-break induced flow in a convergent-divergent channel,
243 performing simulations of two-dimensional flood waves studied experimentally by Bellos et al.
244 (1992). The channel is 21.2 m long and has a rectangular cross-section of variable width. At a

245 distance of 5 m downstream from the beginning of the flume, there is a smooth curved contraction
246 and expansion of 0.6 m of minimum width, the flume has a constant bed-slope that can be changed
247 and ranges between $\pm 1\%$. For a detailed description of the domain the reader is referred to the
248 work of Bellos et al. (1992).

249 The simulation of the experiment was carried out using a non-uniform boundary-fitted mesh of
250 241×41 cells and the channel was assumed to have a mild bed-slope, $S_0 = 0.002$, and a Manning
251 friction coefficient $n = 0.012$ consistent with the recommendations of Bellos et al. (1992). The
252 dam is located at the end of the contraction, at a distance of 8.5 m from the upstream boundary
253 of the flume. Initial conditions consist of a water depth upstream of the dam of 0.30 m, null flow
254 velocities, and dry terrain downstream of the dam. A no-flow boundary condition was imposed at
255 the sidewalls and at the upstream boundary of the flume. At the downstream end of the channel
256 an open boundary condition is applied to allow all the information to exit the domain without
257 propagating back and perturbing the numerical solution. The simulations were carried out for 70
258 s using a CFL number equal to 0.9 in order to ensure numerical stability during the computations.
259 The geometry of the channel, dimensions and location of measurement points studied by Bellos
260 et al. (1992) along with the computational mesh are shown in Fig. 2.

261 The results show that dam-break phenomena is correctly captured by the numerical model as
262 observed in Fig. 3. At the breaking, the shock wave spreads through the expansion and propagates
263 downstream inundating the dry bottom. A rarefaction wave propagates upstream decreasing the
264 water depth, which is then reflected at the upstream closed boundary of the flume. Then, the water
265 depth in the flume starts decreasing, reaching a minimum of 0.014 m after 70 s. From the images
266 depicted in Fig. 3, it can be seen that computed water depths and arrival times of the front are
267 in excellent agreement with experimental data for all the studied measurement points, confirming
268 the abilities of the model to capture shocks and deal with wet-dry cells and source terms over a
269 curvilinear geometry.

270 **Dam-Break over a closed basin with steep topography and friction**

271 An important characteristic of the model is its capability of handling frictional source terms in
272 the numerical solution of the NSWE, especially in situations where the flow is shallow or when
273 the process of wave run-up/run-down is important. Here we test the numerical model with the
274 flood produced by a dam-break over a closed channel with three conical obstacles. This test was
275 first proposed by Kawahara and Umetsu (1986) and subsequently used by many researchers (e.g.
276 Brufau et al. 2002; Brufau and García-Navarro 2003; Gallardo et al. 2007; Nikolos and Delis 2009)
277 to assess the ability of numerical models to deal with steep bed-slopes and friction source terms,
278 wetting/drying proceses, and test local and global mass conservation.

279 The basin is 70 m long in the streamwise x direction and 30 m wide in the cross-stream or y
280 direction. The bed topography is defined by the following equation,

$$z(x, y) = \max \begin{bmatrix} 0 \\ 1 - 0.1 \cdot \sqrt{(x - 30)^2 + (y - 22.5)^2} \\ 1 - 0.1 \cdot \sqrt{(x - 30)^2 + (y - 7.5)^2} \\ 2.8 - 0.28 \cdot \sqrt{(x - 47.5)^2 + (y - 15)^2} \end{bmatrix} \quad (9)$$

282 Initial conditions consist of a motionless free surface elevation upstream of the dam location
283 (at $x = 16$ m) equal to 1.85 m, and a dry bottom bed downstream. The simulation was performed
284 employing a 101×101 uniform mesh using the suggested Manning coefficient of $n = 0.018$, and
285 no-flow boundary conditions were applied to all the sidewalls of the basin. Computations were
286 carried out for 400 s in order to achieve steady state as shown in previous investigations (Nikolos
287 and Delis 2009), using a CFL number equal to 0.9 to ensure the stability of the model during the
288 computations.

289 Evolution of the free surface is shown in Fig. 4. After the dam-break, the flood wave wets the
290 small obstacles and a reflected wave is propagated back to the upstream boundary. At the same
291 time, the front passes through the small obstacles and runs up and down over the larger obstacle,

292 which is partially dry. Later, the wetting front separates and symmetrically goes around the larger
293 mound as it crosses back at the middle of the channel downstream from the larger conical obstacle.
294 Finally, the wave hits the downstream solid boundary and is reflected back to the obstacles. The
295 motion decays in time as a consequence of the friction force and after approximately 400 s, the
296 steady state is reached leaving the three obstacles partially dry. These results agree well with those
297 obtained by Gallardo et al. (2007) and Nikolos and Delis (2009), and illustrate the ability of the
298 model to represent the interaction between dry and wet cells with high accuracy over a steep and
299 frictional topography. Results also demonstrate that global mass conservation was achieved during
300 the entire computation. Therefore, the robustness and stability of the friction scheme in conjunction
301 with the well-balancing properties of the solution of the hyperbolic system are validated.

302 **EXPERIMENTAL DAM-BREAK OVER COMPLEX TERRAIN AND NUMERICAL** 303 **SIMULATION**

304 With the purpose of testing the numerical model, we carry out an experiment for the propaga-
305 tion of a dam-break wave generated by the rapid emptying of a reservoir over a scaled physical
306 model of a river. The experiments were conducted in the Hydraulic Laboratory of the *Pontificia*
307 *Universidad Católica de Chile*. In this section we present the details of the experiment, and the
308 comparison between experimental results and numerical solutions obtained with our model and
309 with two recognized NSWE models: AnuGA (Roberts et al. 2010; Mungkasi and Roberts 2013)
310 and GeoClaw (Clawpack Development Team 2013; Berger et al. 2011), showing the capacity of the
311 models to handle highly demanding natural conditions analogous to the propagation of a tsunami
312 wave over varying topography.

313 **Experimental Set-up**

314 Dam-break experiments were conducted in a physical model of a river consisting of a narrow
315 and steep valley with complex topography presented in Fig. 5(a). The model was built using a
316 geometrical scale equal to 1:60 and Froude similarity. The entire river reach is 14.6 m long and
317 has a maximum width of 4.5 m. It starts with a narrow and curved zone with an average adverse
318 bed-slope of nearly -4.5% , then it becomes wider towards its downstream end. The average bed-

319 slope over the river reach considered in the experiments is -1.5% . A longitudinal profile of the
320 river reach along with the location of the measurements points is shown in Fig. 5(b). The river bed
321 was built with a uniform concrete mix with fine gravel, which yields a roughness characterized by
322 a Manning coefficient of $n = 0.014$.

323 Upstream of the river reach, there is a reservoir and a wooden gate that holds a fixed volume
324 of water equal to 2.17 m^3 . The experiment we carry out consists of a sudden lift of the reservoir
325 gate to release the water into a quiescent free surface downstream. A bore wave is then produced
326 and propagated to the end of the river reach. The free surface evolution within the scaled-model is
327 recorded during 60 s. At the reservoir, free surface elevation is set at 0.85 m, while at the river it is
328 set at 0.56 m as shown in Fig. 5(b). Free surface variations are recorded at nineteen points in the
329 river reach and at the reservoir as depicted in Fig. 5(b).

330 At the reservoir, free surface variations were measured using a KPSI brand pressure transducer
331 recording voltage at 100 Hz. The accuracy of this instrument is $\pm 1\%$. It was calibrated such
332 that 1 V equals 1 m of water column. At downstream cross-sections, free surface variations over
333 the mean water level were measured using wave DHI resistive gauges, which were located at the
334 thalweg of the studied cross sections. Each gauge records voltage data at 100 Hz, the accuracy of
335 these gauges is $\pm 1.5 \text{ mm}$ and the zero drift is $\pm 5\%$, depending on the water temperature.

336 For the experiments, we use four resistive gauges, i.e. only four points could be measured
337 at each run. Thus, five set of experiments with different gauge positions, are performed in order
338 to cover the nineteen considered sections. As a verification of the repetability of the data, three
339 repetitions were performed at each gauge location, maintaining the position of the pressure sensor
340 in the reservoir in order to use it as a reference to synchronize the time series.

341 Numerical Simulation

342 The digitized bathymetry of the physical model is constructed from 39 measured cross sec-
343 tions within the river reach. Then, the bathymetric data together with the reservoir geometry is
344 interpolated using a cubic spline method to create a boundary-fitted computational domain, which
345 correctly represents the bathymetric features of the river reach and its geometry. The physical

346 model is discretized into 130×30 cells of variable size, covering an area of $16 \times 4.5 \text{ m}^2$. The mesh
347 used in the simulations and the digitized bathymetry are shown in Fig. 6. As initial conditions, free
348 surface elevations at the reservoir and the river are set to 0.85 m, and 0.56 m, respectively. Zero
349 velocities over the entire domain are considered at $t=0$. The open boundary condition is used at
350 the downstream end of the river reach and close boundary conditions are applied to the sides of the
351 computational domain. CFL condition is set to 0.9 in order to ensure the numerical stability of the
352 simulations. The gate is instantly removed at $t = 0$ and the wave propagates downstream as seen in
353 the experiments.

354 **Results**

355 The numerical model is able to simulate the dam-break event and the propagation of the bore
356 wave over the river reach. Fig. 7 illustrates the propagation process showing 4 snapshots of the
357 numerical computation, where the blue color represents the wet surface. As depicted in these
358 figures, the bore propagates downstream of the river reach through the narrow and steep valley.
359 It takes approximately 10 seconds to the bore wave to reach the end of the river reach ($\approx 14 \text{ m}$).
360 The entire flood wave propagates downstream along the complex geometry of the physical model,
361 flooding and drying cells, and reaches a steady state after nearly 60 seconds. Fig. 8 shows the
362 velocity vectors field 10 seconds after the gate opening; flow features observed in the laboratory
363 experiments, such as recirculation and reflection due to topographical obstacles are observed in
364 these numerical results. The main aspects of the rapidly varying flow measured in the experiments
365 are thus reproduced by the numerical model.

366 Evolution of the bore wave is studied and compared to experimental data through time series
367 of the computed free surface dynamics at the same locations measured in the experiments. Ad-
368 ditionally, we have carried out numerical simulations using similar NSWE numerical models in
369 order to assess and compare our model accuracy for similar discretization settings. The chosen
370 numerical models are AnuGA (Roberts et al. 2010; Mungkasi and Roberts 2013) and GeoClaw
371 (Clawpack Development Team 2013; Berger et al. 2011). Both models solve the NSWE using a
372 well-balanced shock-capturing finite volume method, mainly differing in the discretization of the

373 domain; AnuGA model uses non-structured meshes, while GeoClaw uses an adaptive meshing
 374 approach. In order to define comparable grids for both simulations, we prepared meshes with a
 375 similar discretization sizes. For the AnuGA model, we defined a mesh of 4026 triangular elements.
 376 GeoClaw model uses an adaptive mesh configuration that varies the distribution of element size
 377 with time, defining areas of refinement when needed. For this particular case, the refinement zone
 378 was controlled in order to maintain a number of grid nodes similar to our model and to AnuGA.
 379 Figures showing the defined grids for AnuGA and GeoClaw along with the configuration for both
 380 simulations are presented in Appendix I.

381 Comparisons between measured and computed time series of the free surface evolution for the
 382 three models are presented in Fig. 9. Our analysis shows that the main features of the process,
 383 i.e. the arrival times, peak amplitudes and recession curves, are well reproduced by our numerical
 384 model and by GeoClaw. AnuGA results seem to be accurate in representing maximum amplitude,
 385 but for this particular case, the model overestimates the final free surface elevation.

386 Based on the results obtained in the simulations, we establish three quantities related to the
 387 inundation and propagation process that are studied, namely the overall agreement of the free sur-
 388 face elevation on time, the maximum amplitude of the bore at each measurement location and the
 389 arrival time of the wave front. For each of these variables, mean relative errors to the measurements
 390 were calculated at gauge locations; these relative errors are defined as follows:

391 **Relative root mean square error (RRMSE)**

392 A root mean square error is used to compare the experimental and numerical free surface
 393 elevation at each location and at the same time to highlight the locations where the larger differences
 394 were found. The relative root mean square error for a location k , and the average relative root mean
 395 square error considering all locations are defined respectively as:

$$396 \quad RRMSE_k^2 = \frac{1}{T} \int_0^T \left(\frac{\eta_m^k(t) - \eta_n^k(t)}{\eta_m^k(t)} \right)^2 dt \quad (10)$$

$$RRMSE = \left(\frac{1}{M} \sum_{k=1}^n RRMSE_k^2 \right)^{1/2} \quad (11)$$

where T is the period of time considered in measurements and in simulations (60 s); M is the number of measurement points, and η_m^k and η_n^k are the measured and numerical free surface elevation at each k location respectively.

Maximum amplitude of the wave

The maximum amplitude of the bore is an important flood variable since it is related with the destructive potential of the wave. This variable is defined as the difference between the maximum and the initial free surface elevation at the river reach. The mean relative error between experimental data and numerical results is estimated as follows:

$$\Delta H_r = \frac{1}{M} \sum_{k=1}^M \left| \frac{H(\eta_m^k) - H(\eta_n^k)}{H(\eta_m^k)} \right| \quad (12)$$

Arrival time

The arrival time of the wave is an interesting parameter for defining evacuation plans as it indicates the available time to leave flood-prone areas and it is also a proxy for the celerity of the bore. The arrival time of at a location k is defined as the first instant where the signal surpasses the initial value by a certain threshold, which is defined here as 1 mm. The mean relative error of this variable over all the measuring sections is defined as:

$$\Delta T^a = \frac{1}{M} \sum_{k=1}^M \left| \frac{T^a(\eta_m^k) - T^a(\eta_n^k)}{T^a(\eta_m^k)} \right| \quad (13)$$

The calculated mean relative errors for each model are summarized in Fig. 10. The RRMSE for the three models shows a very good overall agreement between measurements and numerical predictions, with a 1.7% relative error for our model and a 2.1% relative error for AnuGA and GeoClaw, which is an acceptable error considering how demanding the experiment is. For our model, the highest relative errors are found in the gauges located upstream, near the gate.

419 It is found that in average, the maximum amplitude is underestimated by all models, being
420 the variable with the higher relative error. However, in terms of arrival times of the wave front,
421 predicted results are in excellent agreement with observations (less than 5% mean relative error for
422 our model). Main differences were found in the first gauges closer to the reservoir with maximum
423 local errors reaching 10%. These differences might be explained by the opening mechanism of the
424 gate, which is frictionless and instantaneous in the simulation, but performed in a finite time in the
425 experiments, where vertical velocities might also be generated and interfere with the dynamics of
426 the wave downstream, thus increasing the maximum amplitude of the wave.

427 Summarizing, the results from our model show that it can correctly capture the time evolution
428 of the free surface elevation, the arrival time of the bore and its maximum amplitude. For this
429 singular case, our simulations show a decrease in the studied relative errors when comparing to
430 the results of previously validated numerical models when a similar discretization setting of the
431 domain is used.

432 **CONCLUSIONS**

433 In this investigation we have developed and validated a finite-volume numerical model to simu-
434 late extreme flows and rapid flooding over natural terrains and complex geometries. The numerical
435 scheme successfully reproduces the flow hydrodynamics over rough and highly variable topogra-
436 phies, incorporating an accurate and robust treatment of bore dissipation and wet and dry process.
437 The method is based on algorithms proposed by Marche et al. (2007), and adapted here to solve
438 the bed-slope source term and to incorporate friction by using the splitting semi-implicit scheme
439 developed by Liang and Marche (2009). An important advantage of this model is the simplicity
440 and low cost of its implementation, yielding accurate results using coarse computational grids.

441 Two benchmark test cases are considered to illustrate the capabilities of our new model. Test
442 cases involve the use of boundary-fitted grids, with frictional and varying bathymetry, and dam-
443 break floods. The use of boundary fitted grids is shown for the case of the dam-break in a
444 converging-diverging flume (Bellos et al. 1992). Numerical results are in excellent agreement with
445 experimental data obtained by Bellos et al. (1992), showing the ability of the model to deal with

446 a complex geometry and a rapidly varying flow. The process of run-up and run-down, and wet-
447 ting and drying of the terrain as the wave propagates are reproduced in the numerical simulations
448 of the benchmark cases analyzed in this investigation. This case also illustrates the stability and
449 the well-balanced property of our model, since steady state is correctly reached due to frictional
450 effects.

451 We report new experimental data for a dam-break wave propagating over the scaled physical
452 model of a river reach with narrow and steep valleys. This experiment was specially designed to
453 test the numerical model and to evaluate its ability for representing extreme and rapid flooding
454 over natural conditions. For this case, we have also compared our results with those from two
455 other NSW numerical models, showing a better relative performance by our model in terms of
456 the studied hydrodynamic variables when similar computational discretizations are employed.

457 The results reported in this research confirm that our numerical model is a robust and powerful
458 tool that can be used to simulate high-volume flash-floods and significant inundation over dry ter-
459 rain under realistic conditions, giving accurate results in terms of water depth evolution, discharge
460 and inundated area. The model performance shows that it can become a useful tool for evaluating
461 extreme and rapid flood events over complex bathymetries, and to assess their hazards in terms
462 of inundation extent and depth, depth-averaged velocities, arrival time of peak discharge, etc. We
463 expect that the model will be used as an instrument to develop new inundation hazard maps in
464 coastal and riverine areas.

465 Future research using the model developed in this investigation will focus on the study of com-
466 plex engineering and geophysical flows. Large-scale coastal flows, such as tsunami propagations
467 (Yamazaki and Cheung 2011), will also be studied by incorporating the Coriolis effect into the
468 model. Also, advanced sediment transport and morphodynamic models (Cao et al. 2004; Vasquez
469 et al. 2008) will be added to the basic equations of the flow to study erosion and sedimentation
470 processes in fluvial and coastal environments. Finally, this model will be employed to investigate
471 density-coupled flows, incorporating the transport of active and passive contaminants in rivers and
472 estuaries (Loose et al. 2005).

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480 In this section we present additional information about the configuration used for the numer-
481 ical simulations of the Dam-break over a physical model using AnuGA and GeoClaw numerical
482 models. Fig. 11 present the mesh configuration for each model; Fig. 11(a) presents the triangular
483 mesh of 4026 required by the AnuGA model and Fig. 11(b) presents the initial adaptive mesh used
484 for the simulation with GeoClaw. The element size distribution of the AnuGa and of our model
485 considered approximately a 60% of the elements under 100 cm^2 in size, being both distributions
486 comparable. For the simulation using GeoClaw, the time evolution of the distribution of elements
487 was controled in order to maintain the number of the finer elements aroud 4000, which are 69.4
488 cm^2 in size. For both models, CFL number was set equal to 0.95 in order to achieve numerical
489 stability.

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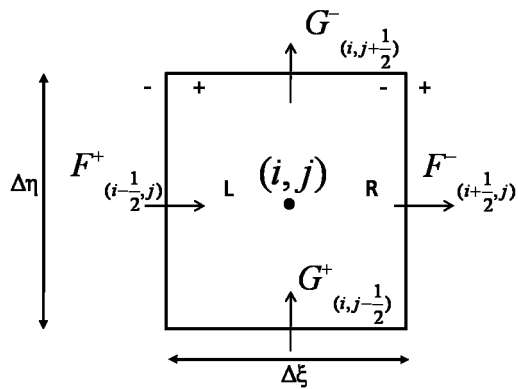


FIG. 1. Discretization cell and numerical fluxes. L and R denote the left and right boundaries of the cell, - and + signs are the left and right sides of the cell interface.

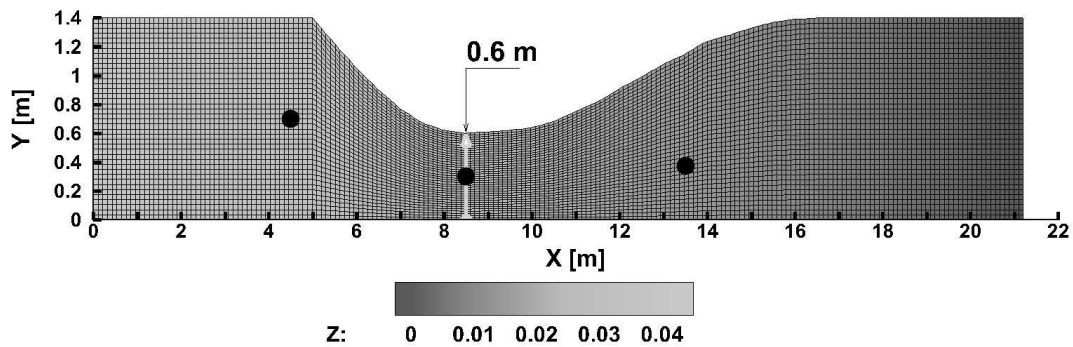


FIG. 2. Dam-Break in a convergent-divergent flume: Geometry of the channel, boundary-fitted grid, bathymetry and measurement points (black dots)

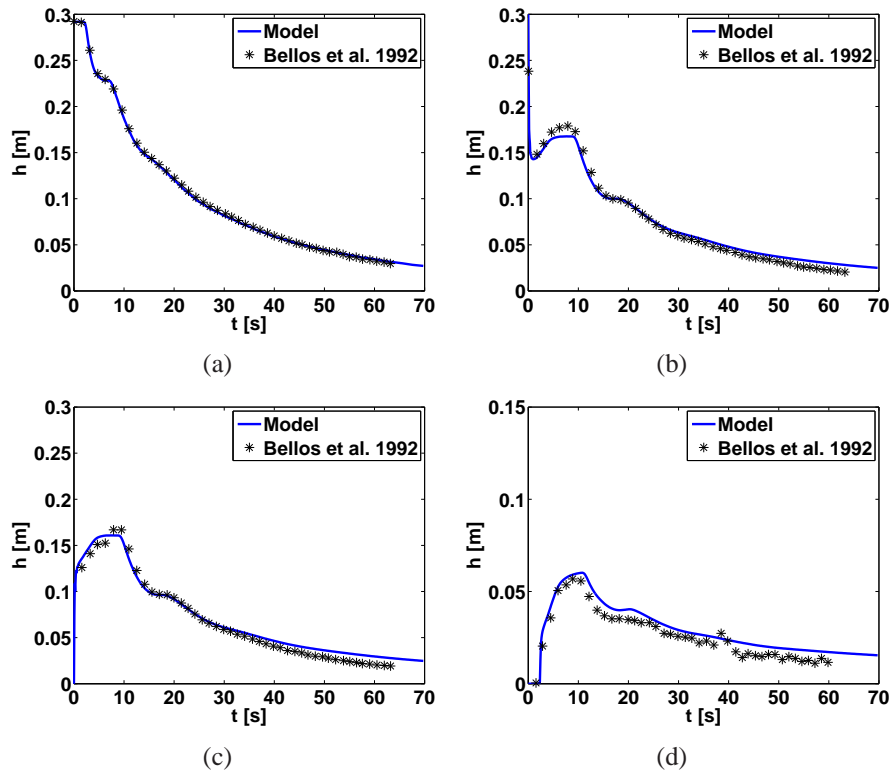


FIG. 3. Dam-Break in a convergent-divergent flume: Water depth time series at measurement points. (a) $x = 4.0$ m, (b) $x = 8.5^-$ m, (c) $x = 8.5^+$ m, (d) $x = 13.5$ m

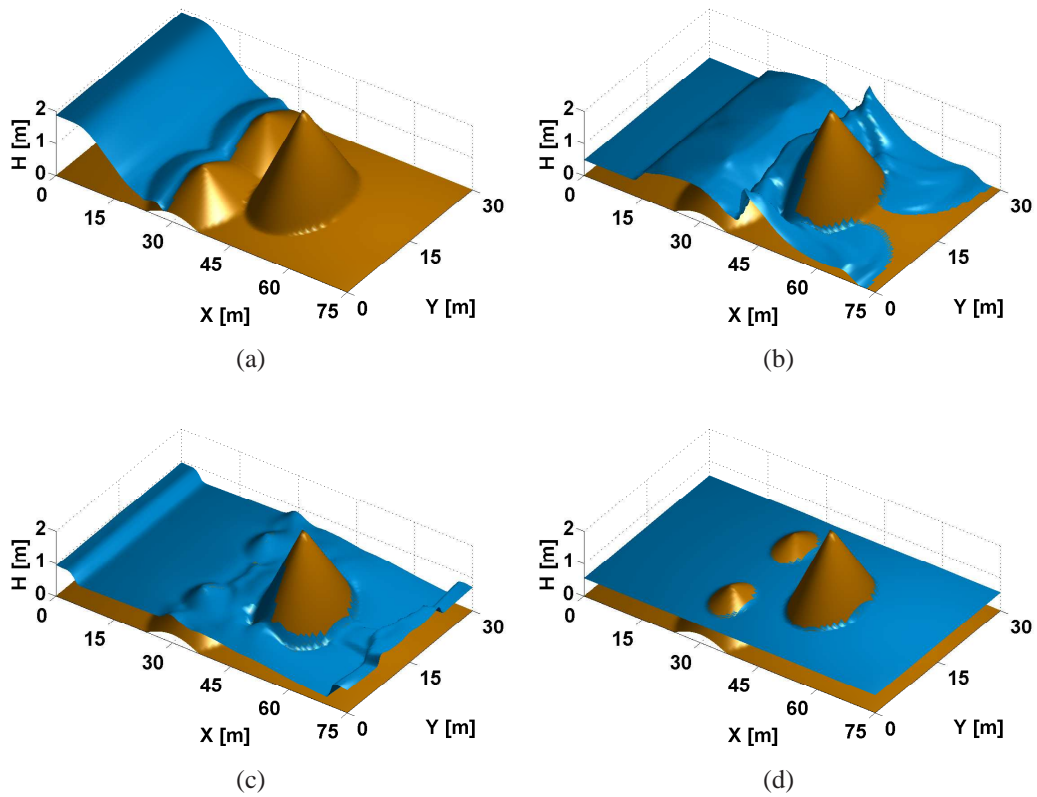
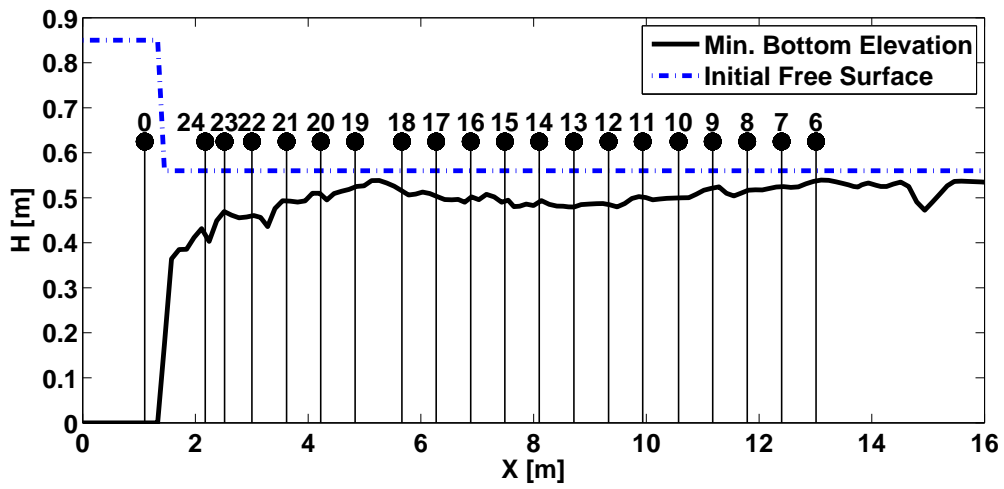


FIG. 4. Dam-Break over a closed basin: Free surface elevation. (a) $t = 2$ s, (b) $t = 12$ s, (c) $t = 20$ s, (d) $t = 300$ s



(a)



(b)

FIG. 5. Dam break Experience: (a) Physical model and measurement instruments, upstream view, (b) Longitudinal profile of the river reach bottom elevation, initial conditions and measurement points

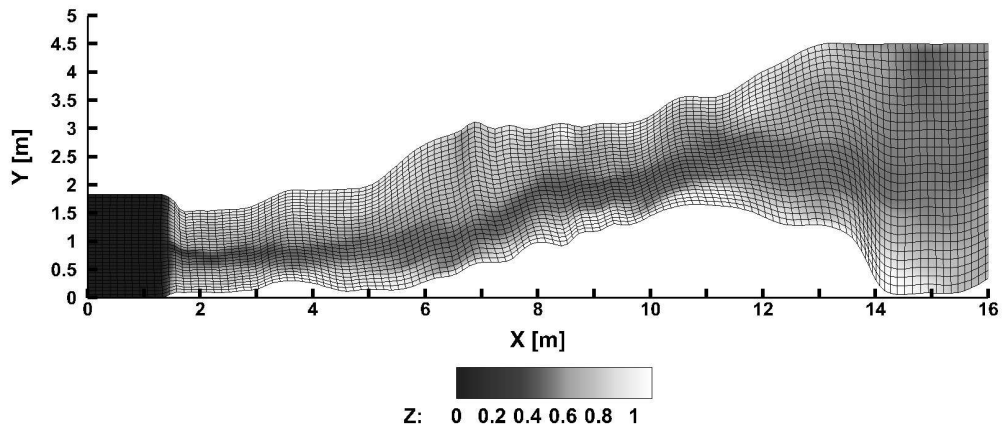


FIG. 6. Numerical Model of dam break experience: Digital bathymetry of the physical domain and curvilinear mesh of the physical model of 130×30 cells

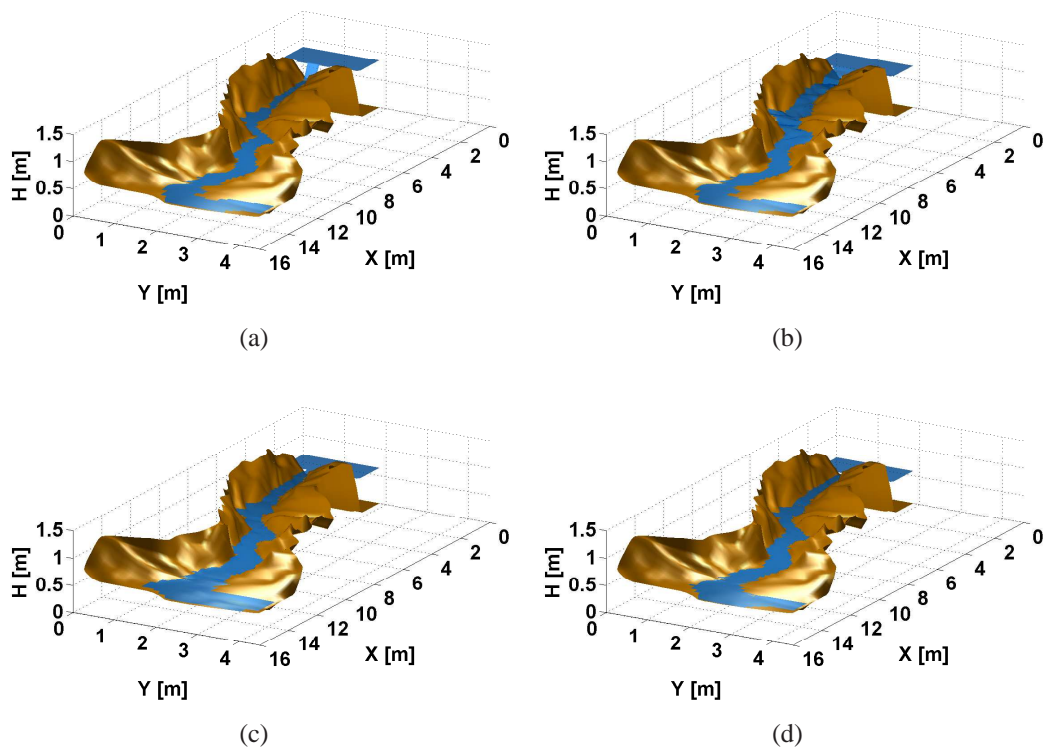


FIG. 7. Numerical model of dam-break experience: Flood extension at different times (a) Initial condition, (b) $t = 4.4$ s, (c) $t = 20$ s, (d) $t = 60$ s

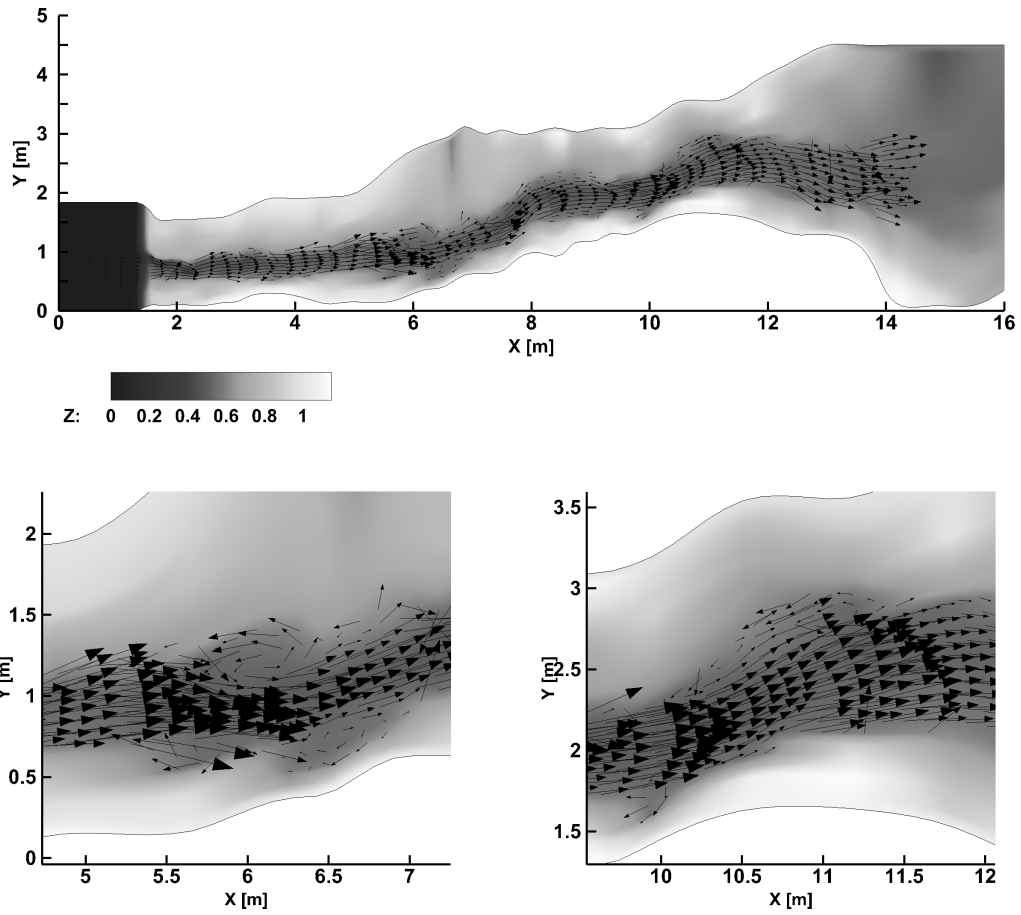


FIG. 8. Numerical model of dam-break experience: Velocity vectors for the propagation of the flooding wave over the river at $t=10$ s

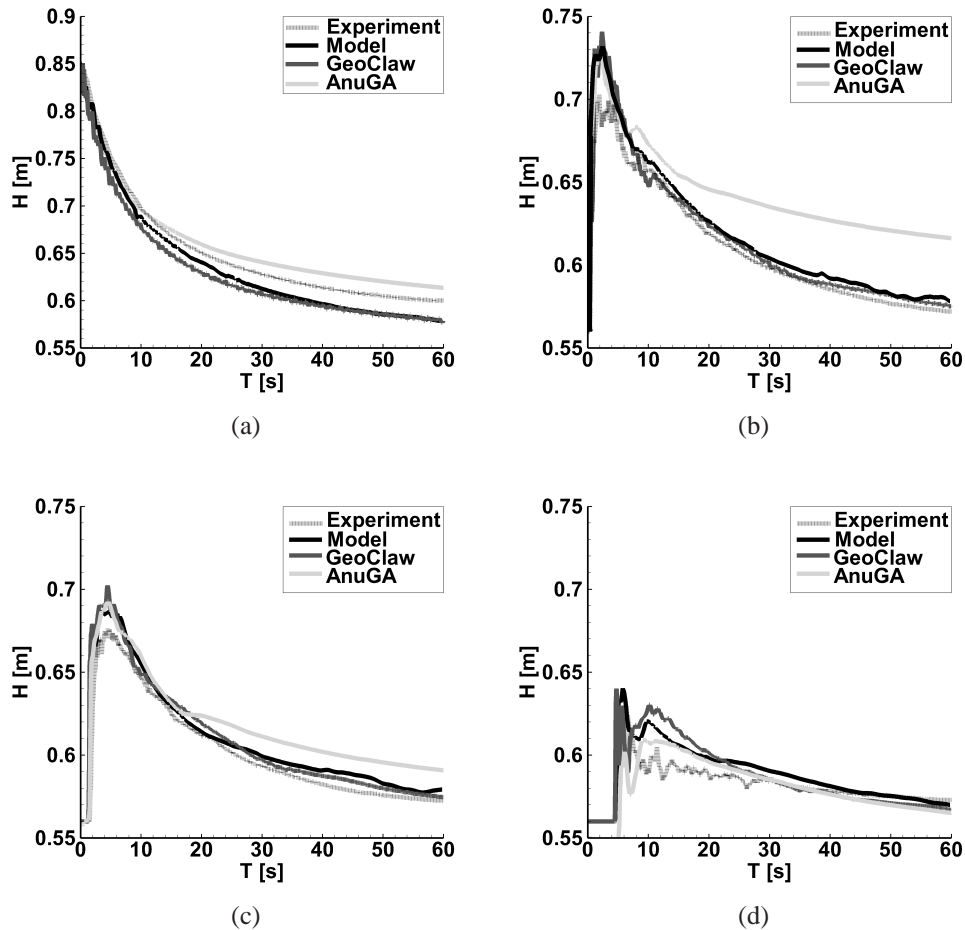


FIG. 9. Numerical model of dam-break experience: Comparison between measured and predicted free surface elevation at different locations, (a) Reservoir, (b) Gauge location 24, (c) Gauge location 20, (d) Gauge location 12. In all figures, the dotted black line represents the experiments and the solid lines represent the numerical results of our model, GeoClaw, AnuGA.

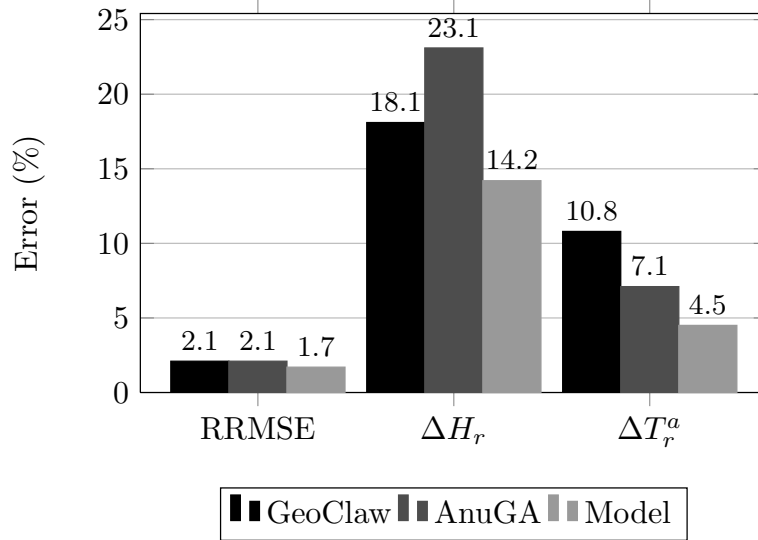


FIG. 10. Summary of mean relative errors between experiments and numerical results for each NSW model. RRMSE: Relative root mean square error between experimental and numerical free surface elevation. ΔH_r : Mean relative error in the maximum amplitude of the bore. ΔT_r^a : Mean relative error in the arrival time of the bore.

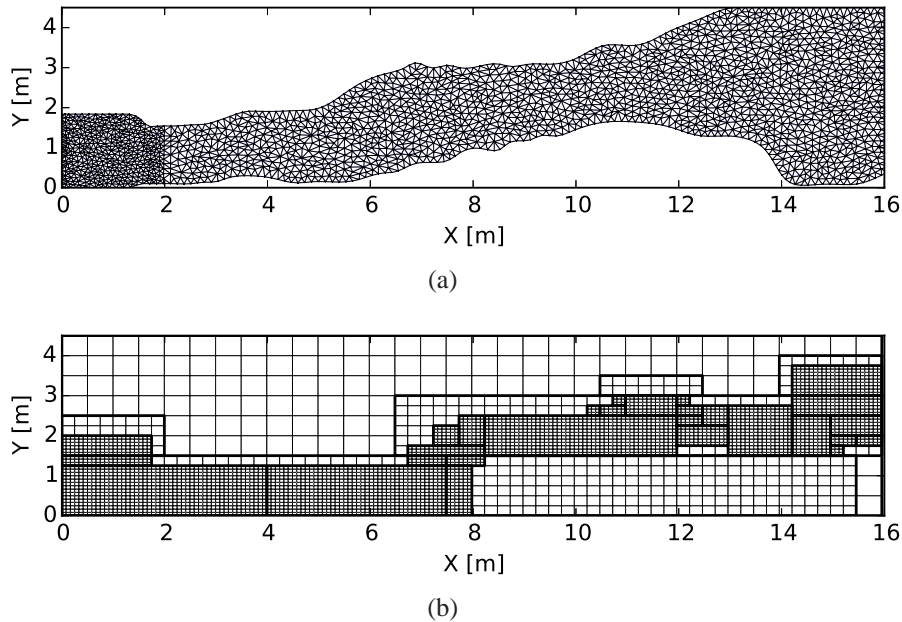


FIG. 11. Physical model discretization grids: (a) Triangular mesh of 4060 elements for AnuGA model, (b) Initial adaptive mesh with three levels of refinement for GeoClaw model