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▶ To cite this version:

Alain Audouard, Fabienne Duc, Loïc Drigo, Pierre Toulemonde, Sandra Karlsson, et al.. Quantum oscillations and upper critical magnetic field of the iron-based superconductor FeSe. EPL - Europhysics Letters, 2015, 102 (2), pp.27003. 10.1209/0295-5075/109/27003 . hal-01066343v2

HAL Id: hal-01066343 https://hal.science/hal-01066343v2

Submitted on 8 Jan 2015

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Quantum oscillations and upper critical magnetic field of the ironbased superconductor FeSe

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PACS $74.70.\,\ensuremath{\texttt{Xa}}$ – Pnictides and chalcogenides.

PACS 71.18.+y – Fermi surface: calculations and measurements; effective mass, g factor.

PACS 74.25.Dw - Superconductivity phase diagrams.

Abstract – Shubnikov-de Haas (SdH) oscillations and upper critical magnetic field (H_{c2}) of the iron-based superconductor FeSe $(T_c = 8.6 \text{ K})$ have been studied by tunnel diode oscillatorbased measurements in magnetic fields of up to 55 T and temperatures down to 1.6 K. Several Fourier components enter the SdH oscillations spectrum with frequencies definitely smaller than predicted by band structure calculations indicating band renormalization and reconstruction of the Fermi surface at low temperature, in line with previous ARPES data. The Werthamer-Helfand-Hohenberg model accounts for the temperature dependence of H_{c2} for magnetic field applied both parallel ($\mathbf{H} \parallel ab$) and perpendicular ($\mathbf{H} \parallel c$) to the iron conducting plane, suggesting that one band mainly controls the superconducting properties in magnetic fields despite the multiband nature of the Fermi surface. Whereas Pauli pair breaking is negligible for $\mathbf{H} \parallel c$, a Pauli paramagnetic contribution is evidenced for $\mathbf{H} \parallel ab$ with Maki parameter $\alpha = 2.1$, corresponding to Pauli field $H_P = 36.5 \text{ T}$.

Introduction. – The discovery of iron-based superconductors [1–4] has reactivated the questioning about the interplay, either competition or cooperation, between magnetism and superconductivity in correlated electron systems. Indeed, as the temperature decreases, parent phases of iron-pnictide superconductors, such as $BaFe_2As_2$, undergo a tetragonal-orthorhombic transition closely linked to the condensation of a spin-density wave (SDW), i.e. to the development of an antiferromagnetic long range order. In contrast, concomitant decrease of the Néel temperature and superconducting critical temperature rise is observed on doping in both $Ba(Fe_{1-x}Co_x)_2As_2$ (electron doped) or $Ba_{1-x}K_xFe_2As_2$ (hole doped) [5, 6], suggesting competition between SDW and superconductivity [7].

Even though no clear quantitative consensus has been reached yet for the iron-chalcogenide $\text{FeTe}_{1-x}\text{Se}_x$ phase diagram, it can be stated that superconductivity emerges as x increases (from x in the range $0 \sim 0.3$) from a SDW state, similarly to the case of pnictide compounds [8] even though Te and Se are isovalent. However, at variance with parent phases of iron pnictide superconductors, no long range magnetic order has been detected in the FeSe superconductor although the tetragonal-orthorhombic phase transition is observed at ~ 90 K. Nevertheless, according to NMR data, antiferromagnetic spin fluctuations are strongly enhanced at temperatures close to T_c [9] which suggests that spin fluctuations may nonetheless play an important role in superconductivity. In line with this statement, itinerant SDW instability have been proposed [10].

Within this picture, nesting properties, hence Fermi surface (FS) topology, may play a major role for superconductivity of iron-based superconductors [11]. According to band structure calculations based on density functional theory, the FS of FeSe is composed of 2 concentric quasitwo dimensional electron and 3 hole tubes, located at the corner and center of the first Brillouin zone, respectively, with their axis parallel to the c^* direction [10, 12–14]. Although these tubes are significantly corrugated, imperfect nesting can be considered [10], as in the case of iron-pnictide superconductors. However, strong discrepancy between band structure calculations and ARPES data has been reported [13]. Namely, much smaller tube areas have been observed and interpreted on the basis of a strong band renormalization and Fermi energy shift. In that respect, the tetragonal-orthorhombic transition at 90 K, connected to a nematic state with an orbital character, plays a significant role [15, 16]. Nevertheless, it can be remarked that SDW with imperfect nesting would also lead to small tube area due to FS reconstruction.

Quantum oscillations study is a powerful tool to obtain information on the FS [11, 17]. As an example, the de Haas-van Alphen oscillations spectrum of LaFe₂P₂, which is a non-superconducting parent of iron-pnictide superconductors, is in agreement with band structure calculations [18]. This feature, which demonstrates the absence of any nesting of the FS at low temperature, is in conflict with the above mentioned picture of competition between SDW and superconductivity. Oppositely, Shubnikov-de Haas oscillations with frequencies in the range 60 T to 670 T, corresponding to orbits area from 0.2 to 2.3 % of the first Brillouin zone (FBZ) area, much smaller than predicted by band structure calculations, have been very recently observed in FeSe [14]. Even lower frequencies, in the range 45-230 T had been previously reported for thin non-superconducting $FeTe_{1-x}Se_x$ crystals [19], this latter compound having similar FS topology.

Besides quantum oscillations, temperature dependence of the upper critical magnetic field H_{c2} may provide information regarding both the superconducting gap topology and the either single or multiband nature of the superconductivity which are both related to the FS topology [7,17]. As it is the case for e.g. FeTe_{0.5}Se_{0.5}, discrepancies can be observed within the few H_{c2} measurements reported for FeSe [14, 20, 21].

The aim of this article is to report on Shubnikov-de Haas oscillations to get more insight on the Fourier spectrum, hence the FS topology and band renormalization, and upper critical magnetic field measured by contactless tunnel diode oscillator technique (TDO) on high quality FeSe single crystals.

Experimental. – Studied single crystals have been grown using the chemical vapor transport method in sealed quartz tube, starting from Fe and Se powders (with a 1.1:1 molar ratio) in an eutectic KCl+AlCl₃ chlorides mixture as detailed in Ref. [22]. The temperature profile used was inspired from the previous work of Chareev et al. [23] and Böhmer et al. [24] with a gradient temperature of 120°C maintained during 6 weeks between the hot zone (440°C) and the cold zone (320°C) of the furnace. The average composition of the obtained crystals was de-



Fig. 1: (Color online) Temperature dependence of the zero-field TDO frequency and zero-field cooled magnetization. Construction lines for the determination of T_c are displayed.

termined to be $Fe_{1.02(1)}$ Se by EDX micro-analysis of the surface of different crystals in a SEM.

As reported in Ref. [25], the device for radio frequency measurements is a LC-tank circuit powered by a TDO biased in the negative resistance region of the currentvoltage characteristic. This device is connected to a pair of compensated coils made with copper wire (40 μ m in diameter). Each of these coils is wound around a Kapton tube of 2 mm in diameter. The studied crystal, which is a platelet with dimensions of roughly $1.4 \times 1.4 \times 0.04$ mm^3 , is placed at the center of one of them. The fundamental resonant frequency f_0 of the whole set is ~ 24 MHz. This signal is amplified, mixed with a frequency fabout 1 MHz below the fundamental frequency and demodulated. Resultant frequency $\Delta f = f - f_0$ has been measured in zero-field and in pulsed magnetic fields of up to 55 T with a pulse decay duration of 0.32 s in the temperature range 1.5 K to 9 K. It has been checked that the data collected during the raising and the falling part of the pulse coincide, indicating that no discernible temperature change occurred during the field sweep. It must be kept in mind that the TDO frequency is sensitive to the resistivity, yielding Shubnikov-de Haas oscillations [25], and the London penetration depth [26], in the normal and superconducting states, respectively.

Results and discussion. – As previously reported for other iron-based superconductors [27,28], the zero-field TDO frequency displayed in Fig. 1 evidences a large increase as the temperature decreases linked to the decrease of the London penetration depth [26]. The onset of this frequency rise coincides with the onset of the zero-field cooled magnetization decrease and is therefore regarded as the superconducting transition temperature ($T_c = 8.6 \pm 0.1$ K).

Upper critical magnetic field. Field-dependent TDO frequency is displayed in Fig. 2 for magnetic field applied perpendicular ($\mathbf{H} \parallel c$) and parallel ($\mathbf{H} \parallel ab$) to the conduct-



Fig. 2: (Color online) Field dependence of the TDO frequency for **H** perpendicular (a) and parallel (b) to the iron conducting plane, respectively.

ing *ab* plane, at various temperatures. Marked transitions are observed for the two considered field directions. These data allow to reliably determine the temperature dependence of the upper critical magnetic field H_{c2} , reported in Fig. 3, in a similar way to the T_c determination (see Fig. 1 and Ref. [28]). These data yield $dH_{c2}^{ab}/dT \mid_{T=T_c} =$ -9.2 T/K and $dH_{c2}^c/dT \mid_{T=T_c} = -2.3$ T/K. Despite these values are by a factor of 1.4 higher than those deduced from resistivity data of Terashima et al. [14], they yield an anisotropy parameter $\gamma = 4.0$ at $T = T_c$, in agreement with the data of Ref. [14]. This value is higher than the reported value of Braithwaite et al. ($\gamma = 1.4$) [29] and Vedeneev et al. $(\gamma \sim 1.5-2)$ [21]. This discrepancy could be attributed to better crystal quality in the two former cases. In that respect, it has been evidenced that e.g. columnar defects induced by heavy ion irradiation decrease γ [30]. Otherwise, the measured γ value is also higher than the anisotropy parameter of FeTe_{0.5}Se_{0.5} crystals, determined with the same measurement technique ($\gamma = 1.6$) [28], suggesting a stronger two-dimensional character in the former



Fig. 3: (Color online) Temperature dependence of the upper critical magnetic field for $\mathbf{H} \parallel c$ (black symbols) and $\mathbf{H} \parallel ab$ (blue symbols). Dashed lines are the best fits of the WHH model to the data in the whole temperature range and the high temperature range for $\mathbf{H} \parallel c$ and $\mathbf{H} \parallel ab$, respectively. Solid line is the best fit to the data for $\mathbf{H} \parallel ab$ including a Pauli contribution ($\mu_0 H_P = 36.5$ T).

case.

Dashed lines in Fig. 3 are the best fits of the Werthamer, Helfand, and Hohenberg (WHH) model [31] to the data, assuming weak coupling [7]. In this framework, the temperature-dependent upper critical field is given by $\ln(1/t) = \psi(1/2 + h/2t) - \psi(1/2)$ where ψ is the digamma function, $t = T/T_c$ and $h = 4\mu_0 H_{c2}/[\pi^2(-dH_{c2}/dt)|_{t=1}]$. Orbital fields deduced within this framework $(\mu_0 H_{c2}^c(0))$ $= -0.693T_c dH_{c2}/dT |_{T=T_c}$ are $\mu_0 H_{c2}^c(0) = 14$ T and $\mu_0 H_{c2}^{ab}(0) = 55$ T. These values are lower than those deduced from TDO data of $FeTe_{0.5}Se_{0.5}$ ($\mu_0 H_{c2}^c(0) = 49$ T and $\mu_0 H_{c2}^{ab}(0) = 78$ T) [28]. Hence, the deduced coherence lengths $(\xi_c = \sqrt{(\phi_0 H_{c2}^c(0))/(2\pi)}/H_{c2}^{ab}(0) = 1.2$ nm and ξ_{ab} $=\sqrt{\phi_0/2\pi H_{c2}^c(0)}$ = 4.9 nm), which are close to the values deduced from resistivity measurements [14], are larger to that deduced from TDO data for $FeTe_{0.5}Se_{0.5}$. Even smaller coherence lengths are deduced from specific heat data of $FeTe_{0.5}Se_{0.5}$ [32] suggesting larger effective mass, hence stronger renormalization for $FeTe_{0.5}Se_{0.5}$. The orbital field for $\mathbf{H} \parallel c$ yields, according to the Clogston formula [33], a superconducting gap $\Delta = 1.1 \text{ meV}$, i. e. $2\Delta = 3.1 k_B T_c$ which is very close to the weak coupling BCS value $(2\Delta = 3.5k_BT_c)$. This gap value is in agreement with muon-spin rotation [34] and specific heat data [35]. However, larger gaps are deduced from ARPES data [13] which suggests strong coupling instead.

While orbital effects account alone for the temperature dependence of H_{c2} for $\mathbf{H} \parallel c$, Pauli pair breaking contribution must be included for $\mathbf{H} \parallel ab$. In this case, the orbital

Table 1: Frequency (F_i) , effective mass (m_i^*) and Fermi energy (E_F) , calculated assuming parabolic dispersion, of the Fourier components with index *i* observed in the data of Fig. 4.

i	F_i (T)	m_i^*/m_e	$E_F \ (meV)$
1	~ 50		
2	96 ± 6	0.75 ± 0.20	15 ± 5
3	200 ± 10	2.0 ± 0.4	12 ± 3
4	~ 580		
5	660 ± 5	3.2 ± 0.6	24 ± 5

critical field is reduced as $\mu_0 H_P = \mu_0 H_{c2}^{orb} / \sqrt{1 + \alpha^2}$ where the Maki parameter is given by $\alpha = \sqrt{2H_{c2}^{orb}}/H_P$. A very good agreement with experimental data is obtained with a Pauli field $\mu_0 H_P = 37$ T, *i.e.* $\alpha = 2.1$ (see solid line in Fig. 3) yielding $\mu_0 H_{c2}(0) = 23$ T. Due to the contribution of the Pauli effect for \mathbf{H} parallel to the abplane, the anisotropy parameter decreases down to $\gamma =$ 1.7 as the temperature goes to zero. Nevertheless, the still unexplained anisotropy inversion (in which H_{c2}^{ab} is lower than H_{c2}^c below ~ 4 K), reported for FeTe_{0.5}Se_{0.5} [28,36,37] is not observed for FeSe. Noticeably, multiband superconductivity observed in muon-spin rotation data [34] and inferred from the almost linear temperature dependence of H_{c2}^c and H_{c2}^{ab} upturn at low temperature reported by Terashima et al. [14] is not detected in the temperature dependence of H_{c2} . This result suggests that despite the reported multiband nature of the Fermi surface, superconducting properties are dominated by one band, possibly due to strongly different diffusivities of the various bands [38] as discussed for 1111 and 122 arsenides by Lei et al. [39]. The different behaviour reported in Ref. [14] could be ascribed to the influence of vortices dynamics on conductivity data below T_c .

Shubnikov-de Haas oscillations. Field dependence of the oscillatory part of the TDO frequency, obtained by removing a monotonically field-dependent background (i.e. a polynomial with a constantly positive second derivative in the studied field range), and corresponding Fourier analysis are displayed in Fig. 4 for two directions of the magnetic field with respect of the conducting plane ($\theta = 0$ and 11°, where θ is the angle between the field direction and the normal to the conducting *ab* plane). Five frequencies are observed as reported in Table 1.

These frequencies correspond to orbits area in the range 0.2-2.3 % of the first Brillouin zone area. Similar and slightly smaller frequencies are observed in magnetoresistance data of FeSe [14] and FeTe_{0.65}Se_{0.35} [19], respectively. It should be noticed that less than 3 oscillations with the frequency F_1 are involved in the window field considered in Fig. 4 preventing any reliable data analysis, such as effective mass determination, for this Fourier component. This statement also holds for the data of



Fig. 4: (Color online) (a) Field-dependent oscillatory part of TDO signal at various temperatures. (b) corresponding Fourier analysis in the field range 15-55 T and 25-55 T below and above 0.4 kT, respectively. Salient frequency peaks are marked as thin lines (see text). The temperature and angle θ between the field direction and the normal to the conducting plane is indicated in (b).

Ref. [14]. Nevertheless, F_1 is close to the frequency labeled F_{γ} , observed for FeTe_{0.65}Se_{0.35} in the field range $\sim 4-7$ T (which involves about 4 oscillations) [19]. Therefore this very small frequency might be actually present in the oscillatory spectrum. Assuming circular orbits, band structure calculations predict electron and hole tubes with Fermi wave vector values corresponding to Shubnikov-de Haas frequencies of few thousands of Tesla [10, 12, 13]. In contrast, ARPES data at low temperature [13] evidence only one electron and one hole orbit with Fermi wave vectors $k_F = 0.18 \text{ } \text{\AA}^{-1}$ and $k_F = 0.05 \text{ } \text{\AA}^{-1}$, respectively. Still assuming circular cross sections, these latter values correspond to frequencies of 1000 T and 80 T, respectively, which is roughly within the range of the frequency values observed in Fig. 4. Low temperature ARPES data of Refs. [15,16] yield additional orbits, due to the orthorhombic distortion, with Fermi energies of few tens of a meV, in agreement with the data in Table 1 as well. Taking FS warping into account, the number of frequencies observed should be twice the number of orbits due to necks and



Fig. 5: (Color online) (a) Temperature dependence of the Fourier amplitude of components with frequency F_2 , F_3 and F_5 . (b) Field dependence of the Fourier amplitude A_5 at various temperatures. Solid lines are best fits of the Lifshitz-Kosevich model yielding effective masses ($m_2 = 0.75$, $m_3 = 2.0$ and $m_5 = 3.2$, in m_e units) and Dingle temperature ($T_{D5} = 3.7$ K) in (a) and (b), respectively.

bellies. Besides, eventual presence of harmonics should be taken into account. Therefore, the oscillation spectrum should be more complex than reported in Table 1. Nevertheless, additional frequencies such as those labeled F'and F" in Fig. 4 cannot be excluded. As for harmonics, F_2 and F_3 could be the second harmonics of F_1 and F_2 , respectively. This hypothesis can be checked through the effective mass determination. Indeed, in the framework of the Lifshitz-Kosevich and Falicov-Stachowiak models [40,41], the effective mass m_{pi}^{\ast} of the p^{th} harmonics of the frequency F_i is given by $m_{pi}^* = p \times m_i^*$ where m_i^* is the effective mass of the *i* orbit. Temperature dependence of the oscillation amplitude is displayed in Fig. 5a for the frequencies F_2 , F_3 and F_5 , yielding, in m_e units, $m_2^* = 0.75$ \pm 0.20, $m_3^* = 2.0 \pm 0.4$ and $m_5^* = 3.2 \pm 0.6$. Owing to the error bars, it cannot be excluded that F_3 is the second harmonics of F_2 . It should be noticed that such statement is at variance with previous data [14] for which it is reported that F_2 is the second harmonics of F_1 , instead,

even though the effective mass relevant to F_1 cannot be reliably, determined as above discussed.

Otherwise, effective mass values m_2^* and m_3^* are significantly smaller than those, corresponding to frequencies $F_{2\alpha}$ and F_{β} , respectively in Ref. [14], measured in a lower temperature range which remains to be understood. Nevertheless, the measured values are close or even slightly larger than those deduced from quantum oscillations of underdoped cuprates with similar frequency. For example, the effective mass linked to $F_5 = 660 \pm 5 \text{ T} (m_5^*)$ $= 3.2 \pm 0.6$) can be compared to the effective mass of $YBa_2Cu_3O_{6.5}$ ($m^* = 1.9 \pm 0.1$ for $F = 530 \pm 20$ T) and $YBa_2Cu_4O_8 \ (m^* = 2.7 \pm 0.3 \text{ for } F = 660 \pm 30 \text{ T}), \text{ respec-}$ tively [42]. This result is in line with the strong renormalization of the effective mass of FeSe observed by ARPES measurements [13, 15, 16]. Finally, the Dingle temperature deduced from the field dependence of the amplitude relevant to the frequency F_5 (see Fig. 5b) is $T_{D5} = 3.7 \pm 0.8$ K, yielding mean free path $\lambda_5 = 17 \pm 4$ nm.

Summary and conclusion. – Shubnikov-de Haas oscillations and magnetic field- and temperature-dependent superconducting transition of single crystalline FeSe have been studied by contactless tunnel diode oscillator-based measurements. In zero-field, the temperature dependence of the TDO frequency yields a superconducting transition temperature $T_c = 8.6 \pm 0.1$ K in agreement with magnetization data.

The WHH model accounts for the temperature dependence of the upper critical magnetic field for magnetic field applied both parallel ($\mathbf{H} \parallel ab$) and perpendicular to the conducting ab plane ($\mathbf{H} \parallel c$). While the orbital contribution accounts for the data with $\mathbf{H} \parallel c$, a Pauli limiting contribution is evidenced for $\mathbf{H} \parallel ab$. The good agreement of the data with the WHH model suggests that superconducting properties of FeSe in magnetic field are mainly controlled by one band, only, despite the multiband nature of the Fermi surface. Finally, the anisotropy of the critical magnetic field close to T_c ($\gamma = 4$) is higher than for FeTe_{0.5}Se_{0.5}. Besides, γ stays above 1 as the temperature goes to zero, in contrast to FeTe_{0.5}Se_{0.5}. The larger anisotropy of FeSe suggests stronger two-dimensionality.

Shubnikov-de Haas oscillations with frequencies in the range 50 T to 660 T, corresponding to orbits area from 0.2 to 2.3 % of the first Brillouin zone area have been observed in agreement with ARPES data at low temperature. Some of the effective masses, measured in the temperature range 1.5 - 4.2 K, are significantly smaller than the recently reported values measured in a lower temperature range which remains to be understood [14]. Nevertheless, they are at least as large as in the case of underdoped cuprates. Owing to the small frequency values, these data account for the strong band renormalization deduced from ARPES data [13, 15, 16].

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The authors acknowledge the support of the European Magnetic Field Laboratory (EMFL) and the financial support of UJF and Grenoble INP through the AGIR-2013 contract of S.Karlsson.

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