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Classical to Quantum Transition of Heat Transfer between Two Silica Clusters

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Heat transfer between two silica clusters is investigated by using the nonequilibrium Green's function method. In the gap range between 4 Å and 3 times the cluster size, the thermal conductance decreases as predicted by the surface charge-charge interaction. Above 5 times the cluster size, the volume dipole-dipole interaction predominates. Finally, when the distance becomes smaller than 4 Å, a quantum interaction where the electrons of both clusters are shared takes place. This quantum interaction leads to the dramatic increase of the thermal coupling between neighbor clusters due to strong interactions. This study finally provides a description of the transition between radiation and heat conduction in gaps smaller than a few nanometers.

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With the recent developments of nanotechnology, electronic devices continue to scale down in dimension and scale up in power density [1]. As a result, near-field radiation starts to play a notable role in the thermal design at nanoscales. Recently, it has been demonstrated both theoretically [2–7] and experimentally [8–10] that heat transfer through near-field radiation between two parallel plates or between a sphere and a plane can be several orders of magnitude larger than the blackbody limit over a limited range of frequency. This clearly corroborates the fact that when the gap between two objects is smaller than the characteristic photon wavelength, a different physical behavior emerges in which near-field radiation and acoustic phonon tunneling significantly contribute to heat transfer [11,12].

The first measurement of the radiative heat flux between two dielectric materials separated by a nanoscale gap distance has recently been performed by Narayanaswamy, Shen, and Chen [8,9]. Their results led them to conclude that the proximity-force approximation is not valid for near-field radiation heat transfer. Shortly after, Rousseau *et al.* [10] also measured the heat transfer in the near-field regime. Interestingly, and in contrast with the conclusions of Narayanaswamy, Shen, and Chen, these later results confirmed the proximity approximation. The difficulty in performing such experiments makes it probable that heat transfer at the nanoscale will continue to be debated, as commented by Kittel [13]. Near-field radiation under the dipole or multipole approximation has been extensively

investigated on a theoretical basis. Nonetheless, mechanisms taking place for separation distances shorter than 10 nm remain unclear. This range of separation distances may not be directly accessible by experiments due to the difficulty in fabricating well-defined planes and spheres at those scales. At the same time, as modern nanostructures might be smaller than 10 nm and are separated in some cases by only a few fractions of a nanometer, this range of lengths is of great interest to those who design nanoscale devices [13,14]. From a fundamental point of view, this domain also involves the less understood transition from a classical charge-charge interaction, logically described as a radiation in the near field, to a chemical bond interaction, yielding pure heat conduction.

By means of molecular dynamics simulations, Domingues *et al.* [15] found a transition regime characterized by a thermal conductance larger than the contact conductance. But the largest value exceeded the upper physical limit. Using ultrahigh vacuum inelastic scanning tunneling microscopy, a previously unknown mechanism of thermal transport—a field-induced phonon tunneling—has been reported by Altfeder, Voevodin, and Roy [16]. The thermal energy transmitted through an atomically narrow vacuum gap exceeds, by 10 orders of magnitude, the one of blackbody thermal radiation. In fact, before these experimental findings, Kosevich [11] and Prunnila and Meltaus [12] modeled how acoustic phonons can directly tunnel through vacuum by introducing coupling mechanisms, and both of them have shown that acoustic phonons can travel

through the vacuum gap with unitary transmission and thus can lead to significant thermal conductance and heat flux.

In this Letter, we estimate the heat transfer through a chain composed of identical noncontacting silica clusters by means of the phonon nonequilibrium Green's functions. We show that there are two critical vacuum gaps of about 4 Å and 3 to 5 times the cluster size. The first critical gap of 4 Å corresponds to a transition between the classical and the quantum regimes with strong interaction. Above this critical gap, the conductance decreases first according to a d^{-3} power law, d being the distance between the center of mass, and then gradually follows a d^{-6} power law, when the gap is larger than 5 times the cluster size. These power laws can be explained by classical surface charge-charge and volume dipole-dipole interactions, respectively. Below 4 Å, the conductance shows a much stronger dependence on gap thickness. The first critical gap is confirmed by *ab initio* calculations showing that the electronic wave functions indeed merge when the gap becomes shorter than 4 Å.

We consider a system of identical silica clusters separated by a distance d between the cluster centers and a gap l (Fig. 1, top). Clusters are coupled through the van Beest, Kramer, and van Santen (BKS) potential [17], composed of Coulomb and Buckingham potentials. The BKS potential provides the full physical picture of the long-range electromagnetic and the short-range repulsive-attractive interactions. We consider one cluster as the reference system and the clusters on its left and right sides serve as reservoirs. The system period is illustrated in Fig. 1 (top). The gap conductance σ between two clusters is derived from the energy transmission T_r as follows [18–20]:

$$\sigma = \int_0^{\omega_{\max}} T_r(\omega) \frac{\partial}{\partial T} \left(\frac{1}{e^{\hbar\omega/k_B T} - 1} \right) \hbar\omega \frac{d\omega}{2\pi}, \quad (1)$$

where ω and ω_{\max} are the energy and the Debye frequencies. T refers to the mean temperature of the system, k_B and \hbar

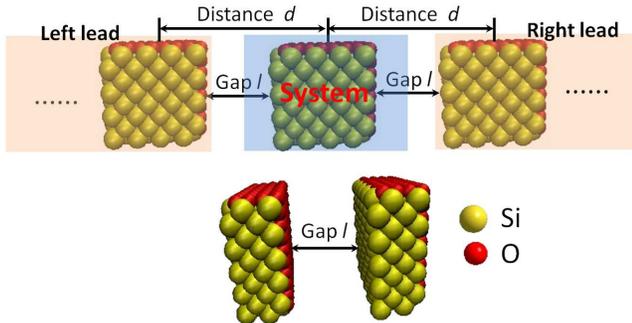


FIG. 1 (color online). Schematics of the silica cluster systems considered in the Green's function calculations (top) and the *ab initio* computations (bottom). For the Green's function calculation, the clusters are $N \times N \times N$ unit cells cubes with SiO_2 lattice constant of 4.52 Å. In the *ab initio* calculations, two parallel silica planes separated with different gap distances are used and electron densities inside the gaps are calculated with this model.

represent the Boltzmann and the reduced Planck's constants, respectively.

The transmission T_r is obtained from a nonequilibrium Green's function approach [18–20] as $T_r(\omega) = Tr[\Gamma_L G_s \Gamma_R G_s^+]$. The advanced and retarded Green functions G_s^+ and G_s^- can be deduced from

$$G_s = [(\omega + i\Delta)^2 I - K_{ss} - \Sigma_L - \Sigma_R]^{-1}, \quad (2)$$

where Δ is an infinitesimal imaginary part that maintains the causality of the Green's function and $\Sigma_L = K_{ab} g_L K_{ab}^+$, $\Sigma_R = K_{ab} g_R K_{ab}^+$ are the self-energies of the left and right leads, the “+” exponent indicating the Hermitian conjugation. Finally, g_L and g_R refer to the surface Green's functions of the left and the right leads, while K_{ss} and K_{ab} are the force constant matrices derived from the BKS potential, for one cluster and between neighboring clusters, respectively. The expression of the transmission also includes $\Gamma_L = i(\Sigma_L - \Sigma_L^+)$ and $\Gamma_R = i(\Sigma_R - \Sigma_R^+)$.

The thermal conductance between clusters obtained from Eq. (1) is reported in Fig. 2. The conductance decreases very quickly with distance in the short gap range. The power law in this range is estimated to be about d^{-12} and the absolute value of the power slightly increases with the increase of the particle size. The thermal conductance per unit cross section indeed increases with cross section as the number of interacting pairs per atom increases. This latter

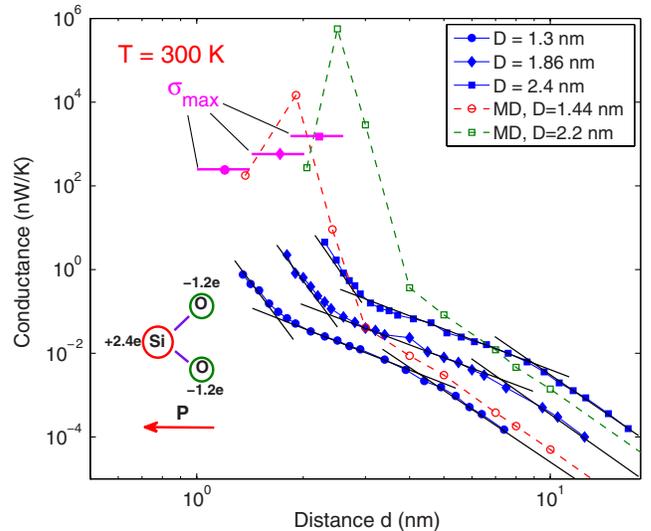


FIG. 2 (color online). Thermal conductance between two neighboring clusters at 300 K for different cluster sizes versus the distance d indicated in Fig. 1. In our calculations, the cluster is a cube $N \times N \times N$ unit cells in volume. The diameter D is set in such a way that the sphere volume is equivalent to that of the simulated cube. The distance d was used as the abscissa instead of the gap distance l in order to discriminate the curves otherwise superimposed. The MD results are taken from Ref. [14], where the same BKS potential parameters as those adopted in this work were used.

number becomes larger at short distances and leads to a slight growth of the absolute exchanged power. This growth should, however, saturate to a maximum value as the number of interacting pairs per atom also saturates, but this limit remains beyond the maximum size under consideration here.

In the intermediate distance range, the conductance decrease with distance turns to be smoother and follows the power law d^{-3} , which is expected in the framework of the nonpiezoelectric interactions [11]. Silicon and oxygen atoms form a dipole as shown in the inset of Fig. 2 and each particle can be regarded as one macroscopic dipole, with bound charges of opposite sign at the front and rear surfaces. When the distance between two clusters is comparable with the cluster size, the force per unit surface area of cluster 1 between surface charges is proportional to S_2/d^2 , where S_2 is the surface area of cluster 2. According to our model, the transmission of acoustic phonons through the vacuum gap can be written as [11]

$$|T_{aph}|^2 = \frac{1}{1 + (\omega/\omega_0)^2}, \quad (3)$$

where ω_0 represents the effective width of the acoustic phonon pass band through the gap; ω_0 is proportional to the modulus of the derivative of the force per unit surface area with respect to the gap width, and as a result, $\omega_0 \propto S_2/d^3$. The total thermal conductance is given by the integral of transmission (3) over all frequencies times the surface area of cluster 1 S_1 and is proportional to $S_1\omega_0$, and, hence, is characterized by the scaling S_1S_2/d^3 [11]. This means that the conductance in this range of distance d is performed mainly by acoustic phonons, which is in agreement with our analysis of transmission function obtained from the Green's function. Interestingly, the slope transition in the log scale occurs at the same gap distance $l = 4 \text{ \AA}$ whatever the cluster diameter D . When the gap increases further, i.e., the distance between two neighboring clusters becomes much larger than the particle size, the energy transfer between two clusters is performed by optical phonon exchange through dipole-dipole interaction [15], following the Förster energy transfer with a $1/d^6$ decay law [21]. The transition from the charge-charge to dipole-dipole interaction occurs smoothly when d is around 3 to 5 times the cluster size. Furthermore, in the charge-charge interaction region, the conductance at a given gap width l follows a $D^{3.85}$ scaling law, while in the dipole-dipole interaction range, the conductance varies with diameter according to $D^{6.5}$ for a given center of mass distance d . These findings further confirm our proposed mechanism of surface charge-charge and volume dipole-dipole heat transfer, since the total conductance is proportional to the product of clusters surface areas S_1S_2 , that is, to $D_1^2D_2^2/d^3$ for surface charge-charge interaction, while the conductance is proportional to the product of clusters volumes V_1V_2 , that is, to $D_1^3D_2^3/d^6$, for volume dipole-dipole interaction.

To validate our predictions, molecular dynamics (MD) simulation results as taken from Ref. [14] are plotted in Fig. 2 for comparison. A clear agreement between MD and Green's function predictions appears in the long distance range. But there is no intermediate region in MD predictions and the conductance from the Green's function is several orders of magnitude smaller than the one yielded from MD in the small gap range. Also, in contrast to MD simulations, no conductance decrease is found right before the contact in our Green's function calculations. Instead, the conductance increases monotonically while the gap decreases. In fact, the maximum conductance before contact predicted by MD simulations exceeds the physical upper limit σ_{\max} as shown in Fig. 2. This limit is calculated from the maximum energy $3Nk_B(T_1 - T_2)$ possibly transferred between two neighbor clusters of N atoms each, set to temperatures T_1 and T_2 . Considering the fastest transfer characterized by the highest mode frequency f_{\max} , the maximum conductance is obtained as $\sigma_{\max} = 3Nk_Bf_{\max}$. The MD predicted conductance just before the contact is 1 or 2 orders of magnitude larger than the maximum value while the nonequilibrium Green's function predictions give estimations below this limit.

To understand the origin of the change in the dependence of the conductance to the distance d , we performed *ab initio* calculations (ABINIT code [22]) of the electron densities for two silica planes schematically shown in Fig. 1, and separated by vacuum gaps ranging from 0 to 6 \AA . As each plane consists of a $1 \times 1 \times 2$ supercell, the two cells' axes are perpendicular to the interacting surfaces. Each unit cell contains twelve atoms and the simulation box includes four cells and 48 atoms. Experimental data for the atomic positions are used and the exchange-correlation Hamiltonian is treated within the generalized gradient approximation with the Perdew-Burke-Ernzerhof functional [23]. Fritz-Haber Institute pseudopotentials [24] are adopted for Si and O atoms. The cutoff energy is set to 820 eV and the k -grid size to $4 \times 4 \times 1$.

As revealed by Fig. 3, the electron density is nonzero in the middle of the gap, when the gap is smaller than 4 \AA but decreases rapidly as the gap widens from 0 to 4 \AA . The electron density reaches zero in the middle of the gap when l increases beyond 4 \AA and the zero electron density domain extends when further increasing the gap. This indicates that the electron wave functions of both sides actually overlap in the short gap range when $l < 4 \text{ \AA}$ to form a bond. In this region, the atoms of both sides are connected through a single electronic wave function instead of interacting through electromagnetic forces relating two separated wave functions. Beyond 4 \AA , near-field radiative heat transfer can be described by Maxwell equations while the quantum Schrödinger equation has to be considered when $l < 4 \text{ \AA}$. Since the bonds between atoms in silica are covalent, we may call the bond before the contact "pseudocovalent." With the formation of those latter bonds, the force between two neighbors dramatically increases

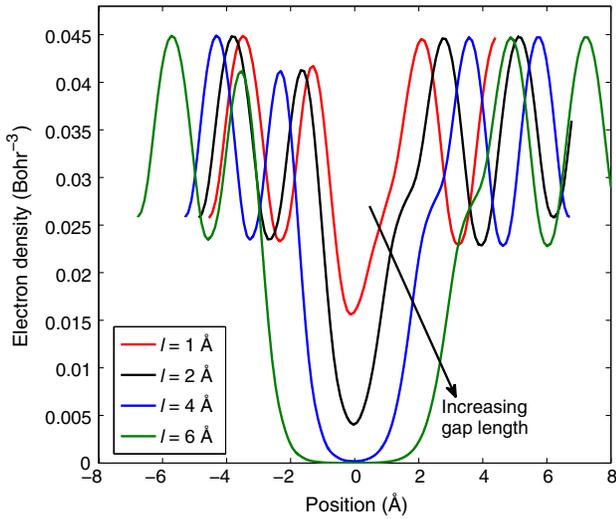


FIG. 3 (color online). *Ab initio* computation of the electron density generated by two parallel silica films separated by different gap widths.

beyond the force produced by electromagnetic waves. As a result, heat transfer shifts from radiative to conductive, also leading to a slope change of the thermal conductance in the small gap range.

To check the relative contribution of acoustic and optical phonons to heat conduction, we now turn to our previous modeling of the transmission of acoustic phonon modes through a vacuum gap as shown in Eq. (3). Since ω_0 represents the effective width of the acoustic phonon passband through the gap and it is proportional to the derivative of the force between clusters with respect to the gap width, it decreases with the increase of the gap width. Consequently, the acoustic phonon cutoff frequency decreases when the gap widens and the frequency range of allowed transmission converges to zero.

Figure 4 reports the cumulative transmission coefficient from one cluster to its neighbor as a function of frequency and distance l . The cumulative transmission function increases continuously for the smallest gap of 1 Å (black line) reflecting a continuous dependence of the transmission on frequency. The continuous decrease of the transmission as the frequency ω_0 reduces to zero reveals that the modes involved are indeed acoustical ones.

When the gap width is slightly increased from 1 to 4 Å, the cumulative transmission function dramatically decreases and includes both a continuum at low frequencies and a set of jumps due to a discrete transmission at higher frequencies as highlighted by the inset of Fig. 4. In qualitative agreement with the model of Eq. (3), widening the gap indeed results in a decrease of the acoustic frequency pass band, which uncovers the presence of optical contributions appearing as peaks in the transmission spectrum. A careful analysis of our data shows that the frequency range of the acoustic phonons continuum

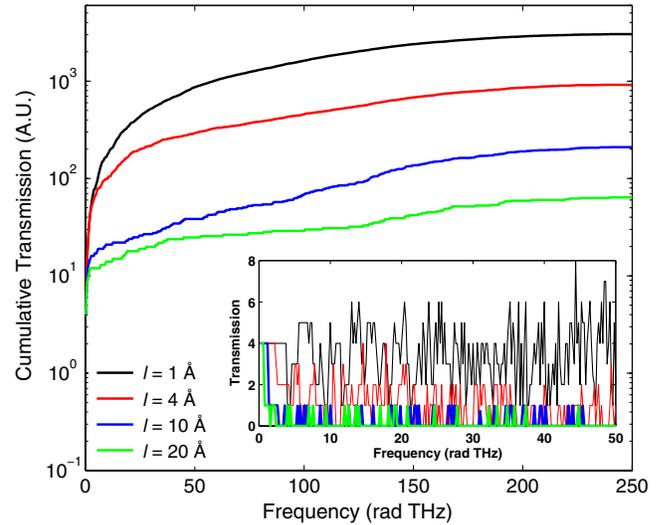


FIG. 4 (color online). Angular frequency dependent cumulative phonon transmission for different gap distance l in the cluster of diameter $D = 1.3$ nm. Inset: phonon transmission function versus angular frequency at low frequencies.

reduces to zero as the gap width reaches 5 times the particle size and accomplishes most of the heat transfer when the gap width is smaller than 3 times the particle size. The discrete set of modes also progressively disappears when the gap width is further increased and only the modes related to force constants of long range interactions remain when the gap is enlarged, and those also gradually disappear as those long range interactions vanish.

By considering the phonon-induced interactions of the gap edges, Kosevich [11] and Prunnila and Meltaus [12] have shown independently that acoustic phonons could transmit energy between separated bodies by tunneling through the vacuum gap, which can lead to a significant thermal conductance enhancement and which is consistent with our findings. Accordingly, Altfeder, Voevodin, and Roy [16] observed phonon tunneling from a sharp STM tip into a gold film at a vacuum gap distance of 3 Å. The authors claim that the tunneling effect is driven by surface electron-acoustic-phonon interaction. This result supports our argument stating that acoustic phonons are predominant in the phonon tunneling through small gaps.

In conclusion, the nonequilibrium Green's function technique has been implemented for calculating the heat transfer between two silica clusters. We found that the studied gap range can be divided into three parts with two critical gaps of 4 Å and 3 to 5 times the cluster size. The heat transfer regimes are characterized by the decay power laws of d^{-12} , d^{-3} , and d^{-6} , successively. The critical gap of 4 Å corresponds to the classical to quantum transition beyond which heat transfer between neighboring clusters follows the classical law prescribed by surface charge-charge (intermediate range) and volume dipole-dipole (long-range) interactions, while the heat flux drastically increases for the gap distance below 4 Å. Near-field

radiation clearly captures the thermal interaction above $l = 4 \text{ \AA}$, but the heat transfer below this distance is dominated by heat conduction as we have shown that electrons are actually forming a chemical bond in the gap. Our results thus provide a deeper insight into understanding the behavior of the transition between radiation and heat conduction in gaps smaller than a few nanometers.

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