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# Erodibility characterisation for suffusion process in cohesive soil by two types of hydraulic loading

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**ABSTRACT.** – An experimental program was set up to study the suffusion process by using a triaxial erodimeter developed in our laboratory. This device is equipped with a multichannel optical sensor in order to characterize precisely the initiation and development of suffusion process. With the objective to characterize the erodibility of clayey sand, tests were performed under either flow-rate-controlled or hydraulic-gradient-controlled conditions. The test analysis allows distinguishing three steps. First, suffusion of a small quantity of clay is detected on downstream. In flow-rate-controlled conditions, this suffusion is immediately followed by a high increase of the hydraulic gradient which continues during the second step. The second step is characterized by very low amount of particles in the effluent. During the third step, high suffusion of clay appears and induces erosion of clay and sand. The results reveal the necessity to take into account the evolutions of hydraulic gradient (or pressure gradient) and also the evolutions of velocity (or flow rate) to represent the hydraulic loading. The analysis based on energy expended by fluid flow and eroded mass permits to characterize the soil sensitivity to clay suffusion and clayey sand erosion for tests under the two types of hydraulic loading.

Key words : Geotechnical engineering, erosion sensitivity, laboratory experiments, suffusion, energy, clayey sand.

## Caractérisation de la sensibilité à la suffusion d'un sol cohésif avec deux types de chargement hydraulique

**RÉSUMÉ.** – Un programme expérimental est réalisé afin d'étudier le processus de suffusion en utilisant un érodimètre triaxial développé au sein de notre laboratoire. Cet appareillage est équipé d'un capteur optique polychromatique afin de caractériser précisément l'initiation et le développement du processus de suffusion. Avec l'objectif de déterminer la sensibilité à l'érosion d'un sable argileux, des essais sont menés à débits imposés ou à gradients hydrauliques imposés. L'analyse des essais permet de distinguer trois étapes. Tout d'abord la suffusion d'une faible quantité d'argile est détectée à l'aval. A débit imposé, cette suffusion est immédiatement suivie par une forte augmentation du gradient hydraulique qui se poursuit au cours de la deuxième étape. La deuxième étape est également caractérisée par la présence d'une très faible quantité de particules dans l'effluent. Pendant la troisième étape, une importante suffusion d'argile apparaît et elle précède une érosion de sable argileux. Les résultats soulignent la nécessité de prendre en compte les évolutions du gradient hydraulique (ou du gradient de pression) et également celles de la vitesse (ou du débit) pour représenter le chargement hydraulique. L'analyse basée sur la détermination de l'énergie dissipée par le fluide interstitiel et la masse érodée permet de caractériser la sensibilité du sol à la suffusion d'argile et à l'érosion de sable argileux pour les essais menés suivant les deux types de chargement hydraulique.

Mots clés : Ingénierie géotechnique, sensibilité à l'érosion, essais de laboratoire, suffusion, énergie, sable argileux.

## I. INTRODUCTION

Suffusion describes the process of detachment and migration of finer particles of soil in the pore space between the larger soil particles. With the objective to evaluate the likelihood of suffusion initiation, several criteria based on the study of grain size distribution have been proposed in literature by [Kenney, 1985], [Li, 2008] among others. [Wan, 2008] concluded that the most widely used methods based on particle size distribution are conservative and they proposed a method for assessing internal instability of broadly graded silt-sand-gravel soils. This method is based on two ratios:  $d_{90}/d_{60}$  and  $d_{20}/d_5$  (where  $d_{90}$ ,  $d_{60}$ ,  $d_{20}$  and  $d_5$  are the sieve size for which 90%, 60%, 20% and 5% respectively of the weighed soil is finer).

[Kovacs, 1981] recognized that even if the geometrical conditions allow particle movements, the hydraulic conditions have to be studied. To take into account the hydraulic loading, [Skempton, 1994] proposed to relate the onset of suffusion with a critical value of hydraulic gradient. [Perzlsmaier, 2007] observed that the use of local hydraulic gradient improves the precision of onset of instability detection and [Moffat, 2011] defined the occurrence of internal instability by the decrease with time in local hydraulic gradient. It is worth stressing that variations of local hydraulic gradient can be very different by several orders of magnitude according to the specimen part considered [Sail, 2011]. Thus the detection of onset of instability based on local hydraulic gradient measurements may depend on the localization of pressure transducers. Some detached particles can

be filtrated and this filtration can induce a clogging process within the soil accompanied with the decrease of the hydraulic conductivity [Reddi, 2000; Bendahmane, 2008; Marot, 2011a]. Therefore, variations of both seepage velocity and hydraulic gradient (or pressure gradient) have to be taken into account to evaluate the hydraulic loading.

In the case of cohesive soils, [Reddi, 2000] proposed to represent the porous medium by a system of parallel capillary tubes each of a constant radius  $r$ , which can be estimated by:

$$r = \sqrt{\frac{8K}{n}} \quad (1)$$

where  $n$  is the porosity,  $K$  is the intrinsic permeability ( $K = k \eta / \gamma_w$ , where  $k$  is the hydraulic conductivity,  $\eta$  is the dynamic viscosity and  $\gamma_w$  is the volumic weight of water).

Thus by this approach, the hydraulic shear stress along a horizontal capillary tubes system can be expressed by:

$$\tau = \left( \frac{\Delta P}{\Delta L} \right) \frac{r}{2} = \left( \frac{\Delta P}{\Delta L} \right) \sqrt{\frac{2K}{n}} \quad (2)$$

where  $\Delta P = P_A - P_B$  is the pressure drop between upstream section A and downstream section B of the specimen;  $\Delta L$  is the distance between sections A and B. It is worth noting that in eq. (2), pressure gradient and permeability are both considered.

From results of interface erosion tests, [Marot, 2011b] proposed a new analysis based on the energy expended by seepage flow which is a function of flow rate and pressure gradient. Three assumptions were used: the fluid temperature is assumed constant, the system is considered as adiabatic and only a steady state is considered. The Reynolds number can be defined by:

$$R_e = \frac{\rho \bar{U} d_0}{\mu}$$

where  $\rho$  is the unit mass of water,  $\bar{U}$  the mean velocity in the pore,  $d_0$  the average capillary tube diameter of the coarser fraction defined by Kovacs's approach [Kovacs, 1981] and  $\mu$  the dynamic viscosity. In the case of the suffusion process, the value of the Reynolds number is relatively low (with a high value of hydraulic gradient  $i=150$ , on clayey sand specimen with initial value of hydraulic conductivity  $k = 10^{-5}$  m/s,  $R_e = 0.25$  [Marot, 2012]). As the value of Reynolds number is indicating laminar flow, it is assumed that energy is mainly dissipated in the erosion process. Finally, the power dissipated by suffusion process,  $P_{erosion}$  is expressed by:

$$P_{erosion} = (\gamma_w \Delta z + \Delta P) Q \quad (3)$$

where  $\Delta z = z_A - z_B$ ,  $z_A$  and  $z_B$  are vertical coordinates of section A and B respectively,  $Q$  is fluid flow rate.  $\Delta z > 0$  if the flow is in downward direction,  $\Delta z < 0$  if the flow is upward and the erosion power is equal to  $Q \Delta P$  if the flow is horizontal. The energy dissipation  $E_{erosion}$  is the temporal integration of the instantaneous erosion power for the test duration.

Concerning erosion sensibility classification, different methods were proposed in the case of interface erosion. The method proposed by [Wan, 2004] assumed a linear expression between the rate of erosion and the hydraulic shear stress. The gradient of this correlation was named erosion

rate coefficient  $k_d$ . According to value of the erosion rate index  $I_{kd} = -\log(k_d)$ , [Wan, 2004] proposed six categories varying from extremely slow to extremely rapid. Another method [Marot, 2011b] was based on an erosion resistance index as:

$$I_\alpha = -\log_{10} \left( \frac{\text{Eroded dry mass}}{E_{erosion}} \right) \quad (4)$$

Depending on the values of  $I_\alpha$  index, six categories of soil erodibility were proposed from highly erodible to highly resistant. However, suffusion erodibility classification is not yet well established,

This paper describes triaxial erodimeter tests which were performed on clayey sand with seepage flow under either constant hydraulic gradient or constant injected flow rate. The characterization of soil sensibility to suffusion under the two types of hydraulic loading is evaluated by different methods including energy analysis.

## II. TRIAXIAL ERODIMETER

A triaxial erodimeter was designed to apply downward seepage flow on intact soil sample or on reconstituted soil specimen (see Figure 1). A detailed description of the device was reported by [Bendahmane, 2008] and a brief summary is provided hereafter.

The testing device comprises a modified triaxial cell which was designed to saturate the sample in upward direction, to consolidate it under isotropic confinement and finally to force fluid through the sample in downward direction. The system to generate seepage flow under constant hydraulic gradient comprises a pressure sensor and an injection cell connected to air/water interface cylinder. Injection cell is continuously weighed in order to determine injected flow rate. The system to generate seepage flow in flow-rate-controlled conditions comprises a gear pump connected to a pressure sensor.

The sample is supported by a lower mesh screen of 4 mm opening size. The funnel-shaped draining system is connected to effluent tank by a glass pipe. Effluent tank is placed on a mass balance in order to continuously measure the effluent mass.

In the case of clay suffusion, the detection of suffusion is not accurate enough by weighing measurement or by visual observation. Thus a multichannel optical sensor was placed at the end of the draining pipe. Thanks to a previous calibration, the optical sensor allows measuring the clay concentration,  $C$ , within the fluid which is expressed by the ratio of clay mass particles and water mass within the fluid. By neglecting the water mass change inside the sample, the eroded clay mass  $m_{clay}$  can be computed [Marot, 2011a]. For a high value of clay concentration within effluent or when effluent contents sand grains, the mass solid measurement can be performed by continuous weighing as mass accuracy of a few milligrams is sufficient. The comparison of the voltages of each optical sensor LED makes it possible to detect the presence of sand grains in the effluent [Marot, 2011a].

A confining pressure cell connected to an air / water interface cylinder is used to generate isotropic confinement. Sample volume change is measured by automatic volume change transducer connected between confining pressure cell and the inlet of triaxial cell.

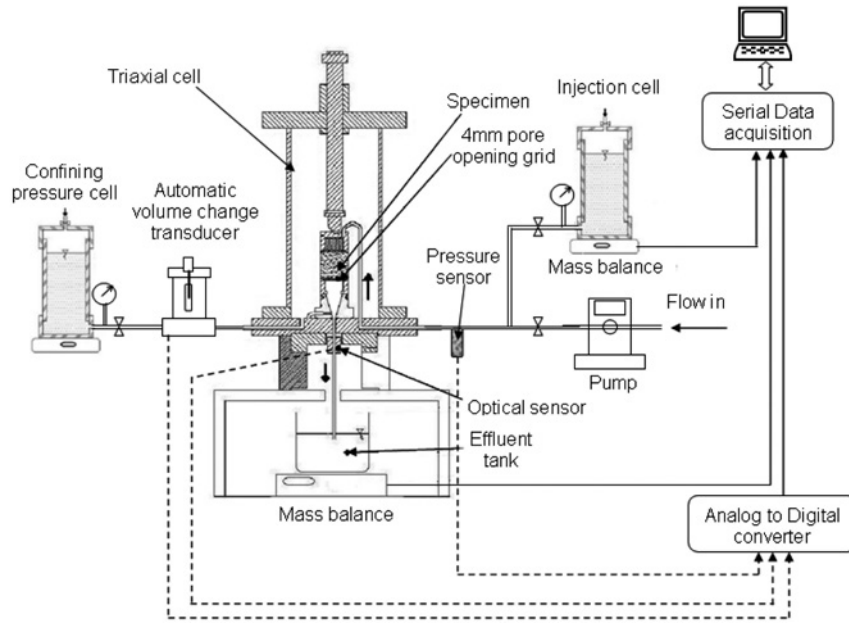


figure 1: Schematic diagram of the triaxial erodimeter.

### III. PROPERTIES OF SPECIMENS AND TEST PROCEDURE

#### III.1. material properties

The tested material is a mixture of 75% Fontainebleau sand (percentage by weight) and 25% Kaolinite Proclay. A laser diffraction particle-size analyzer was used to measure the grain size distribution of sand, clay and mixture. These measurements were performed with demineralised water and without deflocculation agent. As shown by Figure 2, the grain size distribution of such clayey sand is gap graded, the coarse fraction is composed of sand grains and the fine fraction corresponds to the clay fraction. By using the method proposed by [Wan, 2008] for assessing the potential of suffusion, tested clayey sand would be placed in transition zone ( $15/\text{Log}(D_{20}/D_5)=16$  and  $30/\text{Log}(D_{90}/D_{60})=137$ ).

#### III.2. specimen preparation

The mixture is prepared by mixing sand grains with a moisture content of 9%. Then, while mixing continues during 10 minutes, powder clay is progressively added. The specimens are prepared using a single layer semi-static

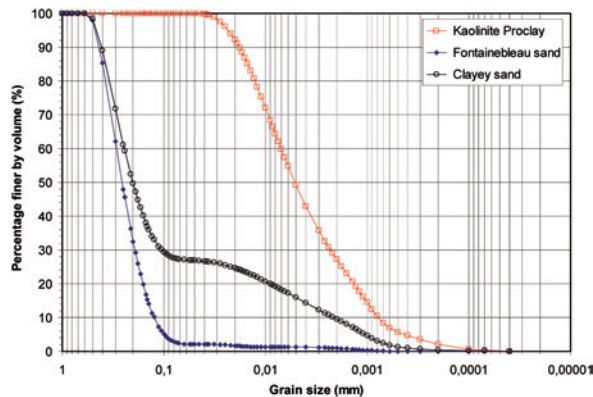


figure 2: Grain size distribution of clay, sand and clayey sand.

compaction technique with a 50 mm diameter and 50 mm high mould. The obtained value of dry unit weight is  $16 \text{ kN/m}^3$ . Specimen is placed in cell and a 15 kPa isotropic confinement pressure is applied. Carbon dioxide is injected followed by the saturation phase which requires approximately 24 h. Specimens were subjected to a seepage flow in downward direction with deaerated and demineralised water. Three tests, named N1, N2 and N3 were performed under controlled-flow-rate (values of flow rate were  $1.2 \text{ cm}^3/\text{min}$ ,  $1.4 \text{ cm}^3/\text{min}$  and  $1.6 \text{ cm}^3/\text{min}$  respectively) and four tests, N4 to N7, under controlled-hydraulic-gradient in the range of 5 to 18.

### IV. TEST RESULTS

The erosion rate of clay is expressed per unit pore area by:

$$\dot{m}_{clay}(t) = \frac{m_{clay}(t)}{N_p S_p t} \quad (5)$$

where  $m_{clay}$ : eroded clay mass,  $S_p$ : average pore area with  $S_p = 2 \pi r \Delta z$ ;  $r$ : radius of average pore determined by eq. (1);  $N_p$ : number of average pore calculated by:

$$N_p = \frac{S n}{\pi r^2} \quad (6)$$

where  $S$  is the cross section of specimen.

#### IV.1. Effluent properties

Figure 3 shows the erosion rate of clay during the time for all performed tests. The optical detection of sand grains in effluent is indicated by the arrows in Fig. 3, at  $t=21 \text{ min}$  for test N7,  $t=54 \text{ min}$  for test N3,  $t=65 \text{ min}$  for test N2 and  $t=64 \text{ min}$  for test N1. When sand grains appear in effluent, concentration of clay cannot be computed.

Test N7, characterized by a high value of hydraulic gradient  $i=18$ , exhibited great variations of erosion rate of clay. After reaching in 40 s a peak of about  $5 \cdot 10^{-9} \text{ kg.s}^{-1}.\text{m}^{-2}$ , erosion rate decreased rapidly toward  $10^{-10} \text{ kg.s}^{-1}.\text{m}^{-2}$ , but at  $t=9 \text{ min}$ , another increase was measured up to  $1.2 \cdot 10^{-9} \text{ kg.s}^{-1}.\text{m}^{-2}$ .

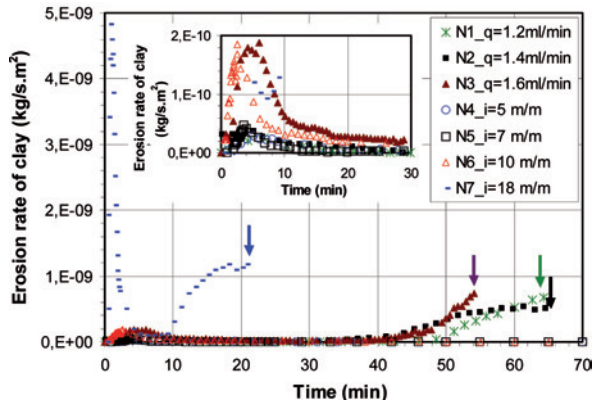


figure 3: Erosion rate of clay vs time (insert: erosion rate of clay below  $2.10^{-10} \text{ kg.s}^{-1}.\text{m}^{-2}$ ).

Finally at  $t=21$  min, the suffusion of clay was accompanied by erosion of sand grains. For tests N3 and N6, erosion rate increased slightly to reach  $2 \cdot 10^{-10} \text{ kg.s}^{-1}.\text{m}^{-2}$  after 3 min of downward flow. Afterwards, erosion rate decreased slowly over time towards zero.

With a constant flow rate smaller than  $1.6 \text{ cm}^3/\text{min}$  or with a hydraulic gradient smaller than 10 (tests N1, N2, N4, N5) erosion rate of clay stayed near zero during 35 min. After 35 min, a sharp increase of erosion rate was measured during flow-rate-controlled tests. Erosion rate exceeded  $5 \cdot 10^{-10} \text{ kg.s}^{-1}.\text{m}^{-2}$  for time between 51 min (test N3) to 60 min (test N1) and then suffusion clay was accompanied by sand erosion. At the same time, erosion rate of clay was about zero for tests N4, N5 and N6.

When suffusion clay is accompanied by sand erosion, the eroded mass of clay particles and sand grains is determined by continuous weighing. Figure 4 shows the instantaneous values of eroded mass. For flow-rate-controlled tests (N1, N2, N3), the increase of eroded mass was higher with a higher injected flow rate, whereas for test N7, under a high value of constant hydraulic gradient ( $i=18$ ), the eroded mass led to an asymptote. It is worth stressing that for test N6 ( $i=10$ ), finally after 235 min of seepage flow, sand erosion begun.

#### IV.2. specimen properties

Variations of hydraulic conductivity with time of all tests are plotted in Figure 5. The initial value of hydraulic conductivity was ranging from  $1.7 \cdot 10^{-6} \text{ m.s}^{-1}$  (for test N5)

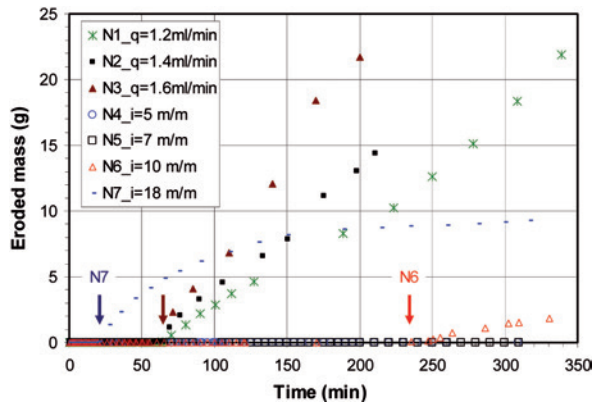


figure 4: Eroded mass vs time. Arrows show time detection of sand grains in effluent.

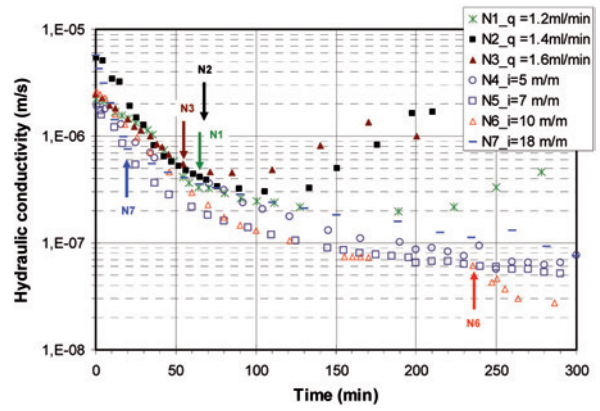


figure 5: Hydraulic conductivity vs time.

to  $5.7 \cdot 10^{-6} \text{ m.s}^{-1}$  (for tests N2 and N7). It can be noted that hydraulic conductivity decreased during the whole duration of hydraulic-gradient-controlled tests. In the case of flow-rate-controlled tests, after the hydraulic conductivity decrease, hydraulic conductivity increased with a final value between  $4.7 \cdot 10^{-7} \text{ m.s}^{-1}$  for test N1 and  $1.7 \cdot 10^{-6} \text{ m.s}^{-1}$  for test N2.

Figure 6 shows the instantaneous values of the hydraulic gradient which were measured during the flow-rate-controlled tests. Hydraulic gradient stayed constant over a few minutes only, with a value between 2.3 (test N2) and 5.5 (test N3). Then, hydraulic gradient increased continuously to reach about  $i=25$  at  $t=55$  min for test N3 and at  $t=66$  min for tests N1 and N2. Afterwards, for tests N2 and N3, the hydraulic gradient stayed relatively constant for 1 hour followed by a sharp decrease, whereas for test N1, the hydraulic gradient kept on increasing up to 34. However, this second increase was lower than the previous and followed by a decrease towards average value of 18.

It is worth noting that hydraulic gradient  $i=25$  occurred a few minutes after sand grains were detected in effluent. The detection of sand grains in effluent induced a great decrease of specimen volume. Nevertheless, for tests N4, N5 and N6 with  $t < 235$  min, a slight and continuous decrease of specimen volume could be measured during clay suffusion process without sand grain erosion.

Clay suffusion is probably not homogeneous but it seems to occur throughout the sample while clayey sand erosion first appears at the bottom of specimen and progresses in upward direction [Marot, 2009].

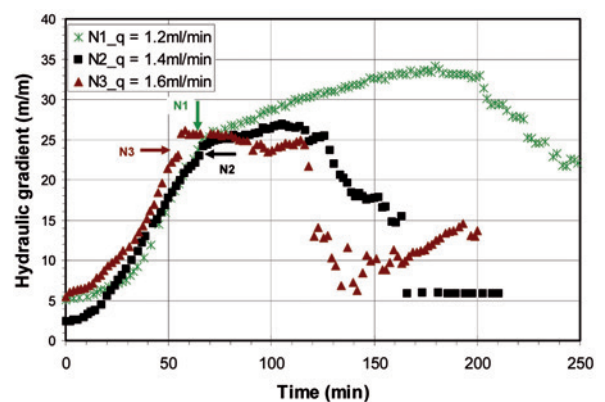


figure 6: Hydraulic gradient vs time (flow-rate-controlled tests).

## V. DISCUSSION

### V.1. Characterization of suffusion sensibility by the mean of erosion rate

By using eq.(2) expressed for a system of horizontal capillary tubes, hydraulic shear stress is reformulated in the case of vertical system by:

$$\tau = \left( \frac{\Delta h \gamma_w}{\Delta L} \right) \sqrt{\frac{2K}{n}} \quad (7)$$

where  $h$  is the hydraulic head.

Figures 7a and 7b show the values of erosion rate of clay versus hydraulic shear stress computed by eq.(7). By selecting some values, a linear correlation between erosion rate of clay and hydraulic shear stress can be built. The slope of this correlation corresponds to the  $k_d$  coefficient. The range of values of the erosion rate index,  $I_{kd}$ , was from 6.9 (test N7, see Fig. 7a) to 9.8 (test N5, see Fig. 7b). However, as shown notably by the curve plotted for test N7, such approach implies to select only some values. Thus the value of  $k_d$  coefficient doesn't characterize the soil erodibility for the whole duration of suffusion process.

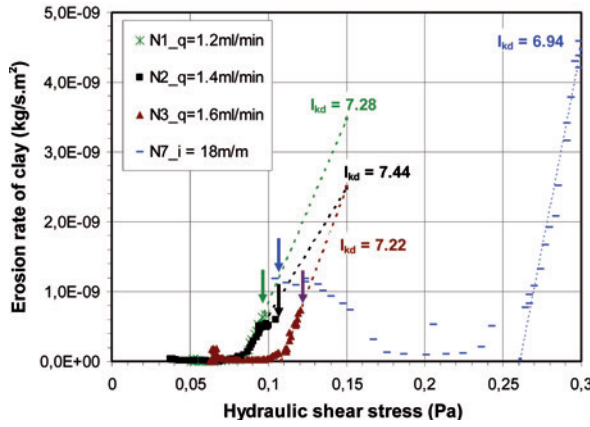
Values of hydraulic shear stress don't permit to estimate sand erosion as the corresponding values vary from 0.02 Pa (test N6, see arrow in Fig. 7b) to 0.12 Pa (test N3, see arrow in Fig. 7a).

The erosion power is calculated using eq.(3) for all tests and the erosion rate of clay versus erosion power is plotted in Fig. 8. The selection of some values allows defining linear correlation with a slope corresponding to the coefficient  $\alpha$  proposed by [Regazzoni, 2011] as:

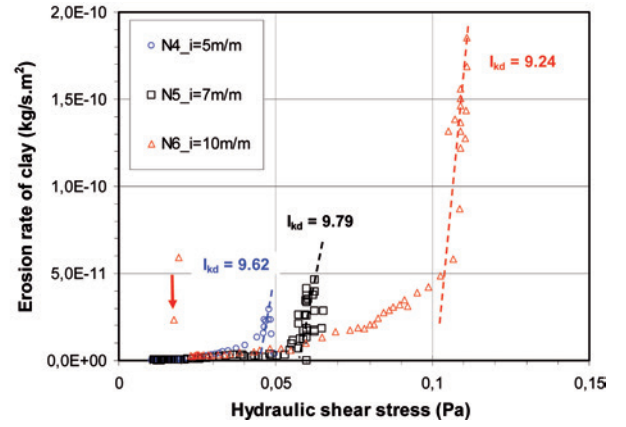
$$\alpha = \left( \frac{\dot{m}}{P_{erosion}} \right) \quad (8)$$

With a similar approach of the erosion coefficient, the parameter  $-\log \alpha$  was computed. For tests characterized by great clay suffusion (tests N1, N2, N3 and N7) the values of  $-\log \alpha$  are within the range: 4.82 to 5, whereas for tests N4, N5 and N6, the values are from 6.58 to 6.81. Thus these values don't lead to a unique erodibility classification.

These results show up the necessity to take into account the history of the hydraulic loading on one hand, and the evolution of the corresponding specimen answer on the other hand. With the objective to characterize independently the hydraulic loading and the induced surface erosion, [Marot, 2011b] proposed to compute by trapezoidal rule the energy dissipated by erosion ( $E_{erosion}$ ) and to measure the cumulative eroded dry mass. The erosion resistance index is calculated by eq.(4) and the obtained values during the whole test duration are plotted in Fig. 9.

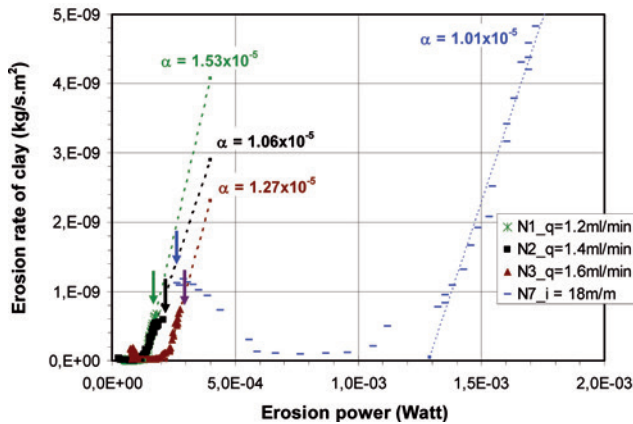


(a) Tests N1, N2, N3, N7

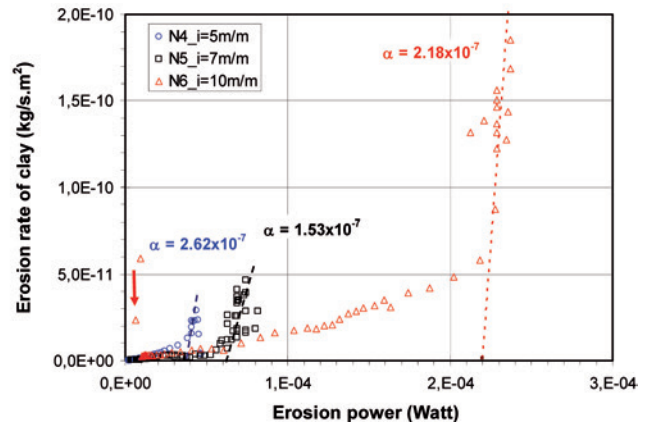


(b) Tests N4, N5, N6

Figure 7: Erosion rate of clay vs hydraulic shear stress. Arrows show time detection of sand grains in effluent.



(a) Tests N1, N2, N3, N7



(b) Tests N4, N5, N6

Figure 8: Erosion rate of clay vs erosion power. Arrows show time detection of sand grains in effluent.

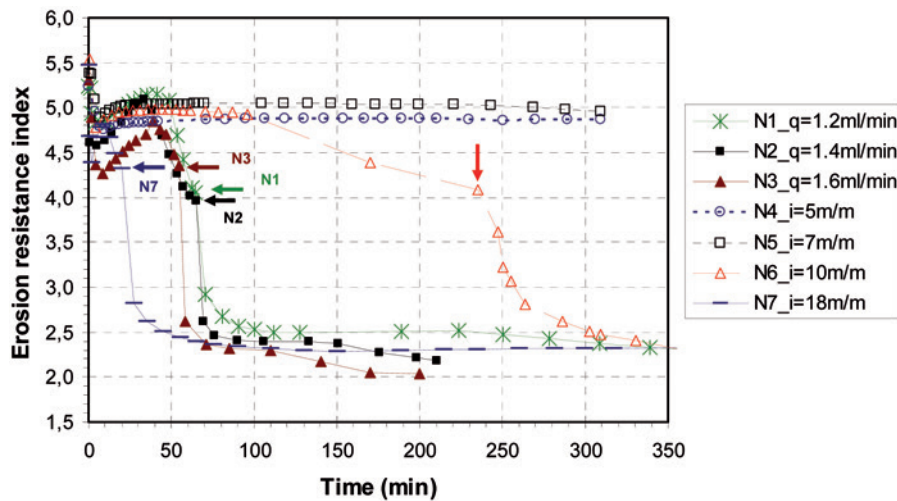


figure 9: Erosion resistance index vs time. Arrows show time detection of sand grains in effluent.

During the development of suffusion process, erosion resistance index reached a maximum value in a few minutes ranging from 4.8 (test N7) to 5.2 (test N1). For tests N4 and N5, erosion resistance index stayed constant during the remaining of test duration at around 4.9 and 5 respectively. For tests N1, N2, N3, N6 and N7, detection of sand grains in effluent was associated with a value of erosion resistant index between 4 (test N2) and 4.3 (test N7). The development of sand erosion induced a decrease of erosion resistance index which led to an asymptote value ranging from 2 (test N3) to 2.3 (tests N1, N6 and N7).

Thus for the tested soil, clay suffusion development was characterized by erosion resistance index about 5, initiation of sand and clay erosion was associated with a average value of erosion resistance index about 4.1, and finally just before the failure of specimen, erosion resistance index was about 2.1. According to the erosion resistance index, the obtained classification of erosion processes was identical for hydraulic-gradient-controlled tests and for flow-rate-controlled tests.

## VI. CONCLUSION

By using a triaxial erodimeter, tests on clayey sand were performed involving seepage flow in downward direction under either hydraulic-gradient-controlled or flow-rate-controlled conditions. Suffusion of clay particles is accompanied by filtration of a part of the detached clay particles. This process induces a decrease of hydraulic conductivity and in the case of flow-rate-controlled tests an increase of hydraulic gradient is also measured. Under a high hydraulic gradient or under flow-rate-controlled conditions, clay suffusion leads to sand and clay erosion which induces a great decrease of specimen volume.

Measurements of instantaneous variations of specimen hydraulic properties together with erosion rate of clay reveal that it is necessary to take into account the variations of hydraulic gradient (or pressure gradient) and the variations of velocity (or water flow rate) to represent hydraulic loading. Methods characterizing the erosion sensibility which are based on rate of erosion cannot allow obtaining a unique characterization of suffusion process for the whole test duration. Thus, such approaches don't permit the estimation

of the development of clay suffusion and the initiation of clayey sand erosion. The proposal erosion resistance index leads to a similar erodibility classification for hydraulic-gradient-controlled tests and flow-rate-controlled tests. These results demonstrate that this approach is efficient to characterize clay suffusion development and also the induced clayey sand erosion.

## VII. ACKNOWLEDGMENTS

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