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Infrared dichroism of gold nanorods controlled using a magnetically addressable mesophase

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Gold nanorods have unique optical properties, which make them promising candidates for building nano-structured materials using a “bottom-up” strategy. We formulate stable bulk materials with anisotropic optical properties by inserting gold and iron oxide nanorods within a lamellar mesophase. Quantitative measurements of the order parameter by modelling the absorbance spectra show that the medium is macroscopically aligned in a direction defined by an external magnetic field. Under field, the system exhibits significant absorption dichroism in the infrared range, at the position of the longitudinal plasmon peak of the gold nanorods (about 1200 nm), indicating strong confinement of these particles within the water layers of the lamellar phase. This approach can yield soft and addressable optical elements.

1 Introduction

Orienting anisotropic nanoparticles at the bulk level is a current challenge in nanotechnology, being a necessary step to exploit the anisotropic physical properties of individual nanoparticle into devices. This is particularly relevant for noble metal particles, actively used due to their particular optical properties. The absorption spectrum of such particles is dominated by peaks corresponding to the surface plasmon modes. For gold in water, a first peak occurs at a wavelength of $\lambda \simeq 520\text{nm}$ for spheres and for the transverse mode of nanorods, while the longitudinal plasmon peak (LPP) of the latter shifts as a function of particle size and geometry¹. At high aspect ratio (AR), the LPP wavelength λ_{max} increases nearly linearly with the particle length.

Among the host materials used for nanoparticle self-assembly, surfactant mesophases doped with inorganic nanoparticles² are easily produced in bulk, and thus especially adapted to the formulation of nano-structured materials via bottom-up techniques. Moreover, their orientational order allows us to take advantage of the anisotropic properties of asymmetric particles, by propagating this anisotropy up to the macroscopic level of the bulk material (*e.g.* optical birefringence and dichroism.) In recent years, gold nanoparticles (both spheres and rods) were inserted within nematic or lamellar mesophases and their optical response was thoroughly studied.

However, bulk self-assembled systems based on gold

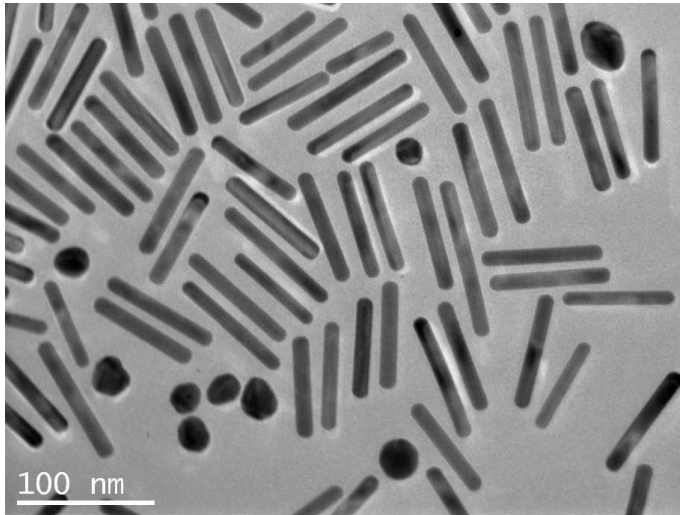
nanorods so far had their LPP in the visible^{3,4} or near-infrared range (below about 900 nm)^{5,6}; to the best of our knowledge, there is no study yet reporting the macroscopic orientation of gold nanorods having their LPP in the infrared domain. In the present study we focus on wavelengths around 1200 nm. This spectral range is particularly interesting for applications in two different domains:

- Human skin and subcutaneous tissue exhibit here the highest penetration depth within the visible and infrared spectrum⁷, facilitating both imaging and photothermal treatment using metal nanoparticles⁸.
- Several popular types of laser (Nd:YAG, HeNe and Yb-doped fibers⁹) operate in this range. It is therefore essential to develop suitable optical elements (such as polarizers).

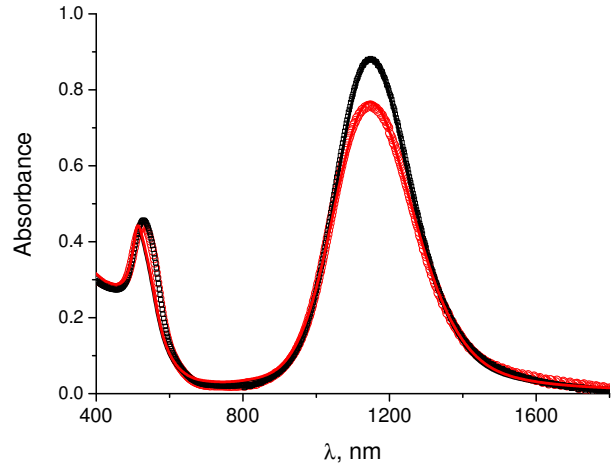
We synthesized, functionalized and guided the self-organization of the nanorods by a soft matter template (a lamellar mesophase of nonionic surfactant). In this type of phase, layers of water separated by surfactant bilayers can be aligned over millimeter ranges. Furthermore, the water layer thickness can be finely tuned by the composition of the phase, between about 1 and 100 nm. We demonstrated by infrared dichroism that the gold nanorods are strongly confined within the lamellar matrix. Adding iron oxide nanorods with magnetic properties renders the phase sensitive to an applied magnetic field, so that its orientation (and thus its optical anisotropy) can be controlled at will.

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a)



b)

Fig. 1 a) Transmission electron microscopy (TEM) image of the gold nanorods. b) Absorbance of the gold nanorods dispersed in water (red dots) and confined in the lamellar matrix (black squares). The symbols are the experimental values and the curves are fits with Equation (6). We fix $S = 0$ for the aqueous solution.

2 Experimental

2.1 Gold nanorod synthesis

All reagents were from Sigma Aldrich, used as received.

A stock suspension of gold nanoparticles was synthesized by a modified seed-growth method¹⁰. The seed solution was prepared by mixing NaAuCl_4 solution (5 ml, 0.5 mM) with hexadecyltrimethylammonium bromide (CTAB) solution (5 ml, 0.2 M). 0.6 ml of fresh 0.01 M NaBH_4 solution were injected into the Au-CTAB solution under stirring at 1200 rpm for 2 min at 30°C, which resulted in the formation of a brownish-yellow solution. The solution was kept undisturbed at 30°C for 30 min before use.

The growth solution was prepared by dissolving 9 g of CTAB with 1.23 g of sodium oleate in 250 ml of water at 30 °C. Then 30 ml of 4 mM of AgNO_3 solution were added. The mixture was kept undisturbed for 15 min, after which 250 ml of 1 mM HAuCl_4 solution were added and when the solution became colorless 62 ml of HCl (37 w.% in water) were injected to lower the pH. After 15 min of slowly stirring at 400 rpm, 1.25 ml of 64 mM ascorbic acid were added to the solution which was vigorously stirred for 30 sec.

In the final step, 0.8 ml of seed solution was added to the growth solution. The resulting solution was stirred at 600 rpm for 30 s and left at 30 °C for 12 h. The color of the solution changes with time depending on the aspect ratio of the gold nanorods. The suspension also contains a significant amount

of spheres and cubes (volume fraction comparable to that of the nanorods), but their contribution to the infrared absorbance is negligible.

Pure water was added to the final solution to stop the synthesis and to reach a CTAB concentration of 50 mM. The stock suspension of gold nanoparticles was concentrated by centrifuging at 6000 g for 30 min and removing the supernatant.

Due to the presence of CTAB in the initial suspension of gold nanorods, the latter aggregate upon mixing with the lamellar phase. We stabilized the system by exchanging the CTAB with the nonionic surfactant (1-mercaptopundec-11-yl)hexa(ethylene glycol) (MUDOL). First, the gold suspension was diluted 100 times, to a CTAB concentration of 0.5 mM and $\phi_{\text{Au}} = 0.01$ vol%. Then, 10 μl of 5 mM MUDOL were added to 0.5 ml of the dilute suspension. The mixture was vigorously stirred for 1 min and left for 24 h at 30 °C. This waiting time is sufficient to complete the CTAB to MUDOL exchange at the surface of the nanorods¹¹.

2.2 Goethite nanorod synthesis

The goethite (α – FeOOH) nanorods were synthesized according to well-established protocols^{12,13}. They are lath-shaped, with length $L = 350 \pm 120$ nm and width $W = 36 \pm 13$ nm, as determined by TEM. Stable aqueous suspensions of goethite nanorods are obtained by repeated centrifugation

and dispersion in water at pH = 3, where their surface is hydroxylated, with a surface charge of 0.2 C m^{-2} (the isoelectric point corresponds to pH = 9). Although bulk goethite is antiferromagnetic, the nanorods bear along their long axis a permanent magnetic dipole μ of a few thousand μ_B (with $\mu_B = 9.274 \times 10^{-24} \text{ J/T}$ the Bohr magneton), probably due to uncompensated surface spins. Therefore, in suspension, the nanorods are easily aligned parallel to a small magnetic field. Furthermore, the easy magnetisation axis is perpendicular to this direction so that, at high applied fields, the induced magnetic moment overtakes the permanent one and the orientation of the rods switches to perpendicular to the field at a critical value $H \sim 350 \text{ mT}^{14}$.

2.3 Lamellar phase

The matrix is the $\text{C}_{12}\text{EO}_5/\text{hexanol}/\text{H}_2\text{O}$ system, with C_{12}EO_5 the nonionic surfactant penta(ethylene glycol) monododecyl ether. Its lamellar phase can be diluted down to spacings d in the micron range, while the bilayer thickness $\delta \approx 2.9 \text{ nm}^{15,16}$. We used a hexanol/ C_{12}EO_5 ratio of 0.35 by weight, corresponding to a molar ratio of 1.3 (hexanol molecules for each surfactant molecule). The main role of hexanol is to bring the lamellar phase domain down to room temperature. The surfactant was acquired from Nikko and the hexanol from Fluka; they were used without further purification.

2.4 Magnetic field alignment

The magnetic field was applied using a home-made setup based on permanent magnets with a variable gap. One can thus reach field intensities of up to 0.9 T. During field application the samples were observed using an Olympus BX51 microscope (with $5\times\text{--}40\times$ objectives) using linearly polarized light and, when specified, an analyzer perpendicular to the incident polarization.

2.5 Absorbance spectroscopy

We used a Cary 5000 spectrometer (Agilent). The beam was linearly polarized by a rotating UV polarizer (Edmund Optics) and defined by a $1 \times 4 \text{ mm}^2$ slit placed immediately before the sample.

The individual absorbance of a nanorod oriented along \mathbf{u} illuminated by a light beam polarized along \mathbf{p} can be written as:

$$a(\lambda, \mathbf{u}) = a_{\text{long}}(\lambda)(\mathbf{p} \cdot \mathbf{u})^2 + a_{\text{tr}}(\lambda)[1 - (\mathbf{p} \cdot \mathbf{u})^2] \quad (1)$$

If the nematic director \mathbf{n} of the nanorod population is parallel to the direction of the beam (and hence perpendicular to \mathbf{p}) as in Figure 3(a), we can write $\langle (\mathbf{p} \cdot \mathbf{u})^2 \rangle = \left\langle \frac{1 - (\mathbf{u} \cdot \mathbf{n})^2}{2} \right\rangle$. The

macroscopic absorbance, averaged over $f(\mathbf{u})$, is then:

$$\begin{aligned} A(\lambda) &\propto \langle a(\lambda, \mathbf{u}) \rangle = \\ a_{\text{long}}(\lambda) \left\langle \frac{1 - (\mathbf{u} \cdot \mathbf{n})^2}{2} \right\rangle + a_{\text{tr}}(\lambda) \left\langle \frac{1 + (\mathbf{u} \cdot \mathbf{n})^2}{2} \right\rangle &\Rightarrow \quad (2) \\ A(\lambda) &\propto \frac{1 - S}{3} a_{\text{long}}(\lambda) + \frac{2 + S}{3} a_{\text{tr}}(\lambda) \end{aligned}$$

where in the last step we used (5) in order to finally obtain (6). By symmetry, the relation (2) holds for all polarizations \mathbf{p} with $\mathbf{p} \perp \mathbf{n}$ and hence for any polarization state of the beam in Figure 3(a).

If, on the other hand, \mathbf{n} is perpendicular to the beam direction (Figure 3(b)) one must consider the two absorbance functions, $A_{\parallel}(\lambda)$ and $A_{\perp}(\lambda)$, for $\mathbf{p} \parallel \mathbf{n}$ and $\mathbf{p} \perp \mathbf{n}$, respectively. In the first case (corresponding to $\beta = 90^\circ$ in Figure 3(b)) we simply have $(\mathbf{p}_{\parallel} \cdot \mathbf{u})^2 = (\mathbf{u} \cdot \mathbf{n})^2$ and

$$A_{\parallel}(\lambda) \propto \frac{1 + 2S}{3} a_{\text{long}}(\lambda) + \frac{2 - 2S}{3} a_{\text{tr}}(\lambda), \quad (3)$$

while in the second one (for $\beta = 0^\circ$) $\langle (\mathbf{p}_{\perp} \cdot \mathbf{u})^2 \rangle = \left\langle \frac{1 - (\mathbf{u} \cdot \mathbf{n})^2}{2} \right\rangle$, yielding:

$$A_{\perp}(\lambda) \propto \frac{1 - S}{3} a_{\text{long}}(\lambda) + \frac{2 + S}{3} a_{\text{tr}}(\lambda). \quad (4)$$

The simplifying assumption $a_{\text{tr}}(\lambda_{\text{max}}) \ll a_{\text{long}}(\lambda_{\text{max}})$ then leads to (7).

3 Results and discussion

3.1 Sample preparation

To reach the infrared domain we used nanorods with an aspect ratio $AR = 7.6 \pm 0.6$, and $\lambda_{\text{max}} \approx 1180 \text{ nm}$, see Figure 1. They were obtained using the classical seed synthesis recently modified by Murray's group¹⁰. For such large and anisotropic particles, the challenge is obtaining both a stable dispersion and a significant confinement so that the particles can achieve a high degree of orientational order. To reach these goals we functionalize the gold nanorods with a nonionic surfactant very similar in structure to the mesophase surfactant.

Afterwards, we prepared lamellar phases of C_{12}EO_5 , hexanol and gold nanorods by mixing appropriate amounts of stock particle solutions with a concentrated lamellar phase and by adding water as necessary (this particular mixing sequence affords good control of the hexanol/ C_{12}EO_5 ratio, which strongly influences the phase diagram of the system). The typical volume fractions are: $\phi_m = (V_{\text{C}_{12}\text{EO}_5} + V_{\text{hexanol}})/V_{\text{total}} = 6.3 \text{ vol}\%$ for the membrane, corresponding to a smectic repeat distance $d \simeq 42 \text{ nm}$, and $\phi_{\text{Au}} = 0.01 \text{ vol}\%$ for the gold nanorods.

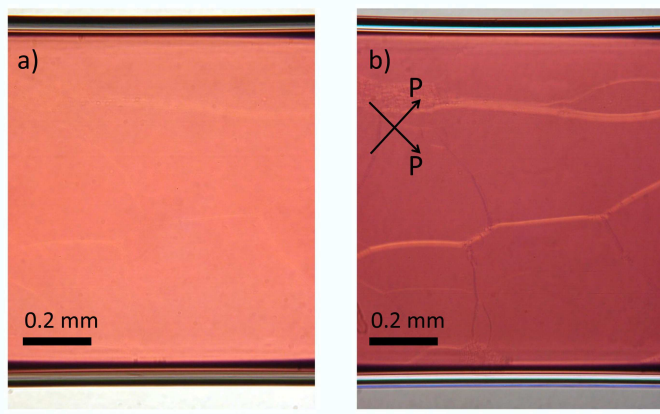


Fig. 2 Microscopy images of the lamellar phase doped with gold nanorods in natural light (a) and between crossed polarizers (b). The double arrows labelled “P” represent the directions of the polarizer and analyzer. The exposure time for image (b) was 250 times longer than for (a).

The samples were introduced in flat glass capillaries, $50 \mu\text{m}$ thick and 1 mm wide (Vitrocom, NJ, USA) by gentle suction with a hand-operated 1 ml syringe. The aspect of the samples immediately after preparation is shown in Figure 2, in natural light and between crossed polarizers. The uniform red color of the capillary shows that the distribution of the nanorods is homogeneous. Furthermore, the sample has remained stable for months. The as-prepared doped lamellar phase is not birefringent, as illustrated by the very low intensity transmitted between crossed polarizers (see Figure 2b). This indicates that the lamellar phase orients homeotropically, *i.e.* with the director \mathbf{n} perpendicular to the flat faces of the capillary.

In order to determine the degree of orientation of the gold nanorods in a more quantitative manner, we derived a theoretical expression for the absorbance and used it to adjust the experimental spectra. The gold nanorods are symmetrically distributed with respect to \mathbf{n} , forming a uniaxial nematic distribution $f(\mathbf{u})$ (where \mathbf{u} represents the nanorod orientation) with director along \mathbf{n} and with an order parameter S given by

$$S = \left\langle \frac{3(\mathbf{u} \cdot \mathbf{n})^2 - 1}{2} \right\rangle = \int d\mathbf{u} f(\mathbf{u}) \frac{3(\mathbf{u} \cdot \mathbf{n})^2 - 1}{2}. \quad (5)$$

Particles perfectly aligned along one axis (the director \mathbf{n}) have an order parameter $S = 1$, while $S = -0.5$ if they are perpendicular to this axis. If the orientation is completely isotropic (constant $f(\mathbf{u})$) $S = 0$. The absorbance of an electromagnetic beam propagating along \mathbf{n} by a suspension of gold nanorods with order parameter S is (see § 2.5):

$$A(\lambda) \propto (1 - S)a_{\text{long}}(\lambda) + (2 + S)a_{\text{tr}}(\lambda), \quad (6)$$

where a_{tr} and a_{long} are the absorbances of a nanorod due to

the transverse and longitudinal plasmonic resonances (for an electric field perpendicular and parallel to the nanorod, respectively), calculated according to Gans’ formula for the dipole approximation¹⁷. For the sample in Figure 2, the full curve fit¹⁸ of the absorbance by (6) is very good (see Figure 1) and yields an order parameter $S = -0.15 \pm 0.01$.

3.2 Absorbance dichroism

In order to exploit the anisotropy of the lamellar phase to orient the gold nanorods in the desired direction, its texture must be switched to planar orientation (\mathbf{n} parallel to the faces of the capillary, see Figure 3b). To this end, we further add to the lamellar phase goethite nanorods that confer magnetic sensitivity to the system, at a concentration $\phi_g = 1.5 \text{ vol}\%$ (Note that ϕ_g is much higher than ϕ_{Au} !). The goethite nanorods were thoroughly characterized in previous work^{14,19}, and the lamellar phase doped with these nanoparticles (but without gold nanorods) was also investigated^{20,21}. Hence, by doping the gold nanorod mesophase with magnetic nanoparticles, our aim is to couple the orientation of the two populations of nanorods through the surfactant mesophase and provide magnetic addressability to the gold nanorods.

This coupling occurs because both the goethite nanorods¹⁸ and the gold nanorods (see Figure 1b and the discussion below) are confined within the water layers of the lamellar phase. Furthermore, it was shown that the orientation of the lamellar phase could be controlled by the application of a magnetic field, since the magnetic rods impose their orientation to the surfactant mesophase²⁰. Consequently, the magnetic field indirectly controls the orientation of the gold nanorods.

We measured the birefringence and dichroism of the sample as a function of the strength of the magnetic field, applied perpendicular to the light beam that was parallel to the sample normal, Figure 3a. In the absence of the field, the lack of sample birefringence (Figure 3c) indicates that the lamellar phase orients homeotropically and that the goethite nanorods have a uniaxial nematic distribution along the normal to the sample^{20,21}. For magnetic field intensities below 350 mT , when the lamellar phase remains homeotropic, the dichroism was zero (Figure 3e), *i.e.* the director of the gold nanorods remains parallel to the beam.

Under stronger fields, above 400 mT , the goethite nanorods reorient perpendicular to \mathbf{H} . The lamellar phase follows²⁰, so that \mathbf{n} becomes parallel to \mathbf{H} (and perpendicular to the beam), and the distribution of the gold nanorods tilts by $\pi/2$ with respect to the initial orientation, see Figure 3a. Indeed, the sample showed strong birefringence (Figure 3d) and negative dichroism $A_{\parallel} - A_{\perp} < 0$, where A_{\parallel} and A_{\perp} are the absorbance values (measured at λ_{max}) corresponding to light polarization parallel and perpendicular to \mathbf{n} , respectively (Figure 3f). We checked that the magnetic field has no measurable effect on

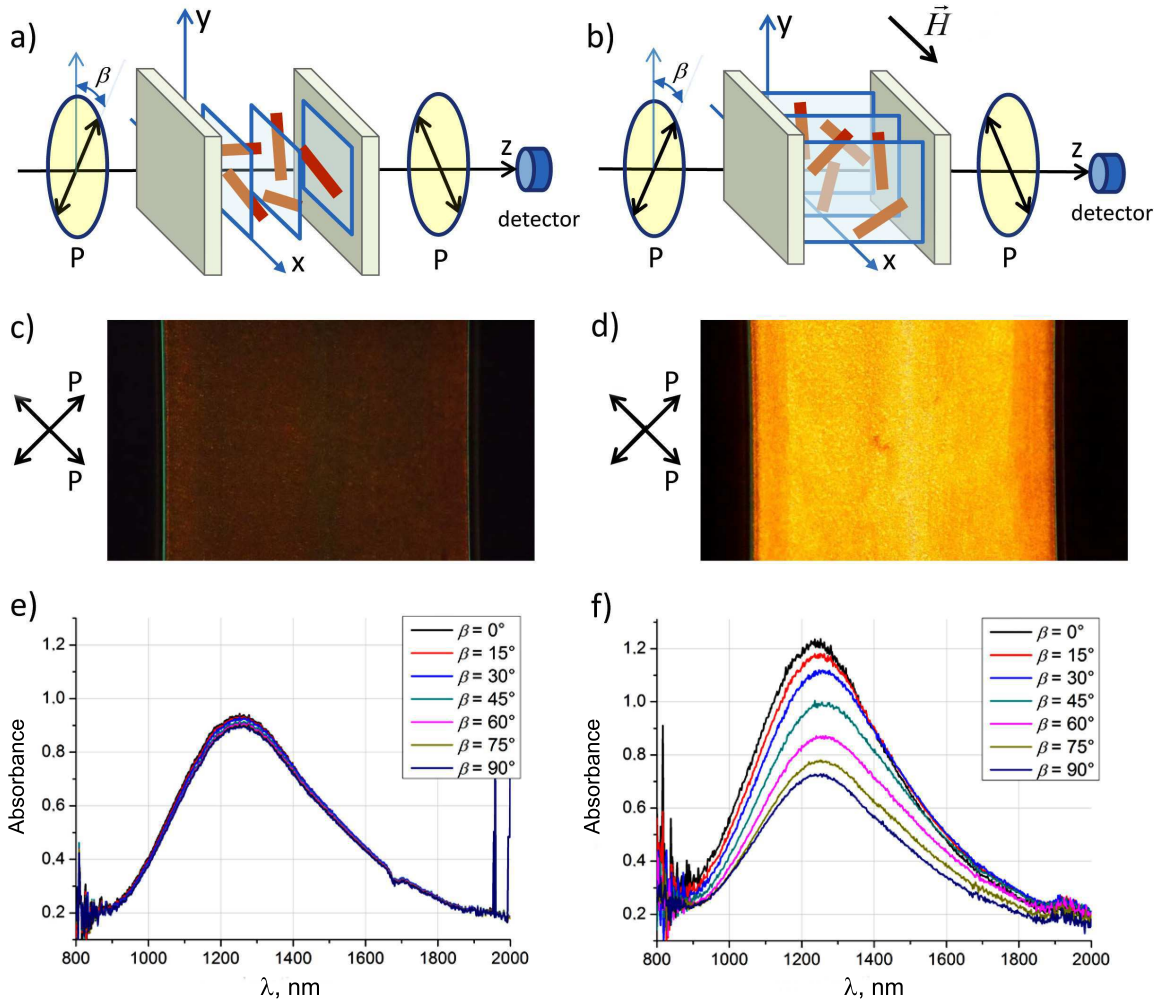


Fig. 3 Diagram of the experimental setup, with the lamellar phase in homeotropic (a) and planar orientation (b). The double arrows labelled “P” represent the directions of the crossed polarizer and analyzer and the angle between polarizer and the vertical axis z is denoted by β . The magnetic field \vec{H} is shown in (b). Polarized optical microscopy images (in the visible range) for situations (a) and (b) are shown in (c) and (d), respectively. The capillary width is 1 mm. Absorbance spectra of the longitudinal plasmon resonance peak in the infrared range for situations (a) and (b) are shown in (e) and (f), respectively. These measurements were made using a dedicated infrared polarizer (see Materials) and no analyzer. The optical path length is $50\ \mu\text{m}$.

the orientation of the gold nanorods by themselves, in water or in the lamellar phase.

This behavior indicates that, in the lamellar phase, the gold nanorods have a nematic uniaxial distribution with their director along the lamellar phase director. The order parameter can be obtained as (see § 2.5):

$$S_{\text{exp}} = \frac{A_{\parallel} - A_{\perp}}{A_{\parallel} + 2A_{\perp}}. \quad (7)$$

From the experimental data in Figure 3f we obtained $S = -0.17 \pm 0.01$. This is remarkably close to the value of -0.15 ± 0.01 estimated above for the gold nanorods under confinement in the lamellar phase, in homeotropic alignment and without goethite. We conclude that the presence of goethite does not perturb the distribution of the gold nanorods and that the magnetic field induces a complete orientation transition (from homeotropic to planar).

The absorbance spectra in Figure 3e) and f) show a change in the position and shape of the longitudinal peak of the gold nanorods with respect to their spectrum in water (Fig. 1b) We attribute this to changes in dielectric properties of the medium due to the presence of the goethite nanorods but we have not studied this feature quantitatively. Note that the position of the longitudinal peak is exactly the same in water and in the lamellar phase (without goethite), see Figure 1b.

The goethite absorbs very strongly at the position of the transverse peak of the gold nanorods (around 520 nm), so that we cannot measure adequately the transverse peak of the gold nanorods in the presence of goethite. For this reason, in Figure 3 we only show the infrared region of the spectrum, where the goethite absorbance is negligible.

4 Conclusions

We have successfully aligned gold nanorods on macroscopic scales by confining them between the bilayers of a surfactant lamellar phase. Their negative order parameter was measured by fitting the absorbance spectrum. By doping the phase with goethite nanorods, we can tune the orientation of the entire sample using a moderate magnetic field. Both the surfactant mesophase and the gold nanorods are dragged by the magnetic nanoparticles. This results in strong dichroism in the infrared

range, which can be potentially tuned by varying the aspect ratio of the nanorods *via* the synthesis conditions. This property can be of great interest for fabricating new optical elements addressable by an external field.

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