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Epitaxial undoped indium oxide thin films: Structural and physical properties

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ABSTRACT

Indium oxide thin films were grown by the pulsed electron beam deposition method on c-cut sapphire substrates at 10^{-2} mbar oxygen pressure and temperature up to 500 °C. Such conditions lead to the formation of dense, smooth and stoichiometric In_2O_3 films, with the cubic bixbyite structure. Epitaxial thin films were obtained at substrate temperatures as low as 200 °C. Pole figure measurements indicate the existence of (111) oriented In_2O_3 crystallites with different in-plane symmetry, i.e. three-fold and six-fold symmetry. The origin of this effect may be related to the specificities of the growth method which can induce a large disorder in the oxygen network of In_2O_3 , leading then to a six-fold symmetry in the (111) plane of the bixbyite structure. This temperature resistivity behaviour shows metallic conductivity at room temperature and a metal–semiconductor transition at low temperature for In_2O_3 films grown at 200 °C, while the classical semiconductor behaviour was observed for the films grown at 400 and 500 °C. A maximum mobility of $24.7 \text{ cm}^2/\text{V s}$ was measured at 200 °C, and then it falls off with improving the crystalline quality of films. The optical transparency is high ($> 80\%$) in a spectral range from 500 nm to 900 nm.

Keywords:

Indium oxide

Thin films

Optical and electrical properties

1. Introduction

Indium oxide (In_2O_3) is a transparent conducting oxide which presents a high conductivity (free carriers up to 10^{17} – 10^{19} cm^{-3} range) without intentional doping [1], the origin of which is still under debate [2]. Moreover, undoped In_2O_3 thin films exhibit conductivities with 4–5 orders of magnitude higher than that of the bulk [3], and recently explained by the presence of surface donors instead of bulk defects. When doped with typically 9 at% tin oxide, indium-tin oxide (ITO) is one of the most popular transparent conducting electrode used in thin-film photovoltaics, flat-panel display devices, due to the highest transparency for visible light ($> 85\%$ at wavelengths from 340 to 780 nm) combined with the lowest electrical resistivity ($7.7 \times 10^{-5} \Omega \text{ cm}$) [4]. The recent trend towards higher quality and tailoring transparent conducting electrodes to constraints of specific electronic and solar cell technologies demands the continuous optimisation of In_2O_3 thin film properties and processing conditions [1,2].

The formation of In_2O_3 thin films has been studied by various methods such as molecular organic chemical vapour deposition [5–8], plasma assisted molecular beam epitaxy [9,10], sputtering [11], atomic layer deposition [12] or pulsed laser deposition [13]. The epitaxial growth of In_2O_3 on Y-stabilized ZrO_2 , c-cut sapphire,

InAs or MgO single crystal substrates has been already reported [4,5,13]. Whatever the growth methods, the epitaxial film formation was generally carried out at relatively high substrate temperature, i.e. $T > 500$ °C. However, the crystallisation of In_2O_3 can occur at temperatures as low as 150 °C, following previous reports [14] and studies on indium based oxide materials have indicated that optimum materials properties are obtained for substrate temperature in the 200–400 °C range [15,16]. Low growth temperatures are typically required for transparent conducting layers to avoid the degradation of the solar cell junctions. The possibility to obtain In_2O_3 films with good structural characteristics, low electrical resistivity (about $10^{-4} \Omega \text{ cm}$) and high optical transparency ($> 85\%$) on c-cut substrates in the 200–400 °C range, would open the way to new applications in thin film photovoltaics.

Our first aim in this work was thus to study the growth and properties of indium oxide films in a relatively low temperature domain ($T \leq 500$ °C), i.e. to determine the nature of the crystalline phase, its texture and eventual epitaxial relationships with single crystal substrate, and to correlate these structural characteristics with the optical and electrical properties of the films. Pulsed-electron beam deposition method (PED) which was already used to grow high quality ITO films [17] has been used for the growth of the indium oxide films. Epitaxial In_2O_3 films were thus grown on c-cut sapphire substrates in the 200–500 °C range, with various epitaxial relationships. The physical (optical and electrical) properties of these films were not related to the crystalline quality of the films, but certainly to the oxygen composition.

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2. Experimental

The In_2O_3 thin films were grown by pulsed electron beam deposition method (PED) in the experimental setup previously described [17]. The following parameters were used: an external capacitor of 16 nF, a high voltage of 14 kV, repetition rate 1–2 Hz, 100 ns full width at half maximum (FWHM) pulse width of the electron beam, fluence of about 2 J/cm^2 and an oxygen pressure of 2×10^{-2} mbar. Films with about 50–300 nm in thickness were grown on c-cut single crystal sapphire substrates under controlled substrate temperature in the room temperature to 500 °C range. After deposition the films were cooled down at the oxygen pressure used for the growth, or at atmospheric oxygen pressure.

The structural characterizations were carried out by X-ray diffraction (XRD) analyses using a four circle diffractometer (Philips Xpert MRD) with the $\text{Cu K}\alpha$ radiation ($\lambda=0.154 \text{ nm}$) from the PIMM–Arts et Metiers ParisTech in Paris. The nature of the crystalline phases, their axes parameters and their eventual crystallographic textures were investigated in the symmetric Bragg–Brentano geometry. The in-plane epitaxial relationships between the film and the single crystal substrate were studied by asymmetric X-ray diffraction through pole figures measurements.

The resistivity of the In_2O_3 films was measured as a function of temperature from room temperature to liquid helium, by the classical four probe method, with *ex-situ* deposited gold electrodes and wire-bonded contacts. The resistivity and the nature, concentration and mobility of the carriers were determined with a MMR Hall measurement system (in the van der Pauw geometry) at room temperature under a magnetic field of 0.3 T. The transmittance of the films was measured with a spectrophotometer Cary 100 in the wavelength range 190–900 nm.

3. Results

The oxygen composition in oxide films plays so far a major role not only on their structural and physical properties [18–20], but also on their nature, i.e. homogeneous or heterogeneous [17,21]. Indeed, recent studies have shown that a large oxygen deficiency in indium tin oxide films can lead to the formation of a nanocomposite system with metallic clusters embedded in a stoichiometric matrix [22]. To avoid the formation of such heterogeneous nanocomposite systems, the films were grown by PED under oxygen gas which precludes large oxygen deficiencies. However oxygen vacancies could be present in the films and could play a major role on the electrical conductivity of the In_2O_3 films [23].

In_2O_3 crystallises in two distinct structures, the body-centred cubic bixbyite ($a=1.0118 \text{ nm}$) and the rhombohedral ($a=0.5478 \text{ nm}$ and $c=1.451 \text{ nm}$) structure. In our work, all the PED In_2O_3 films grown at $T \leq 500 \text{ °C}$ were found to crystallise in the pure bixbyite structure. As a matter of fact, Fig. 1 represents typical diffraction patterns for In_2O_3 films grown on c-cut sapphire between 200 and 500 °C. Two peaks located at 30.475° and 35.455° can be observed in the diagrams recorded on the film grown at 200 °C. These peaks can be identified with the (222) and (004) family planes of the In_2O_3 bixbyite indicating preferential (111) and (001) textures. For increasing growth temperatures up to 500 °C, the (004) peak is no longer observed, the films being highly (111) textured, and the intensity of the (222) peak is an increasing function of the growth temperature.

Considering the surface free energy of formation of the main planes of the In_2O_3 bixbyite phase, the (111) texture is expected since the high atomic density (111) plane of the bixbyite presents a lower surface free energy than the polar (001) plane, as it has been previously discussed [24]. The presence of the (001) texture

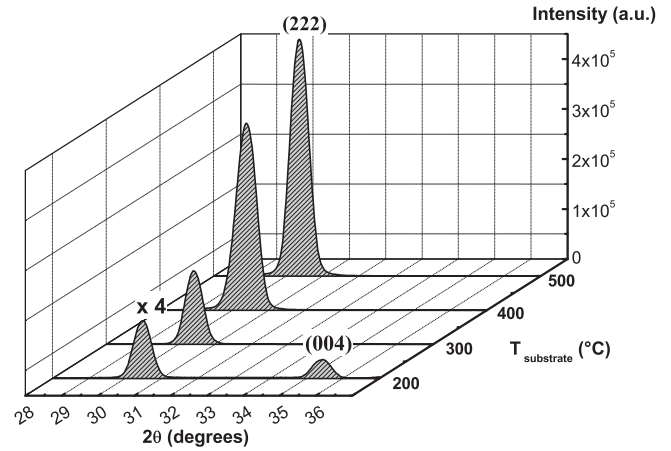


Fig. 1. θ – 2θ X-ray diffraction patterns recorded for In_2O_3 films grown on c-cut sapphire substrates at 200, 300, 400 and 500 °C. The intensity of the patterns of the film grown at 200 °C is multiplied by a factor of 4.

Table 1

Temperature (°C)	200	300	400	500
(222) peak	30.475°	30.415°	30.385°	30.355°
FWHM peaksize	0.58°	0.57°	0.65°	0.60°
FWHM rocking curve	7.5°	5°	2.3°	1.6°
Crystallite size (nm)	14.2	14.4	12.6	13.7

is *a priori* unexpected from surface energy considerations, but other parameters like the fact that the c-cut sapphire plane is a polar plane and/or possible epitaxy of the (001) oriented In_2O_3 on the c-cut sapphire may play a role (see below).

Table 1 summarises the main insights drawn from these XRD patterns. The 2θ values of the (222) plane were found lower than the bulk value (30.581°), even more and more lower for increasing growth temperature. The corresponding increase in axis parameter could be due to a slight oxygen deficiency and/or the existence of stresses in the grown films. The crystallite size (coherence length) was estimated from the (222) line width using the Debye–Scherrer formulae, and was found roughly constant as a function of the growth temperature. The FWHM of rocking curves are presented in Table 1 and show decreasing values with increasing growth temperature, which means an increase in the crystalline quality of the In_2O_3 films, as it is generally observed.

Despite the high values of the film mosaicity (see Table 1), the possible epitaxy of the films was checked. Poles figures for the (044) planes of In_2O_3 ($2\theta=51.04^\circ$) were recorded on films grown between 200 and 500 °C, and are presented in Fig. 2. On these figures three poles located at a declination angle ψ equal to 57.6° are observed (assigned with the * symbol). They represent the poles of the (02–24) planes of the sapphire substrate, which are observed owing to their diffracting angle 2θ (52.56°). Such poles allow us to determine the epitaxial relationships between film and substrate. For the film grown at 200 °C, two series of poles are present. Twelve poles are located at a ψ value equal to 45° (assigned with the @ symbol), i.e. the value expected for the (044) poles of the (001) oriented In_2O_3 crystallites. These 12 poles are related to the respective symmetry of the film and substrate (4×3), i.e. four from cubic film and three from the rhombohedral sapphire substrate. In addition, six poles are observed at a ψ value equal to 35.3° (assigned with the # symbol), corresponding to the (111) oriented In_2O_3 crystallites. This figure also shows that three of these six poles due to (111) oriented crystallites are more intense than the others.

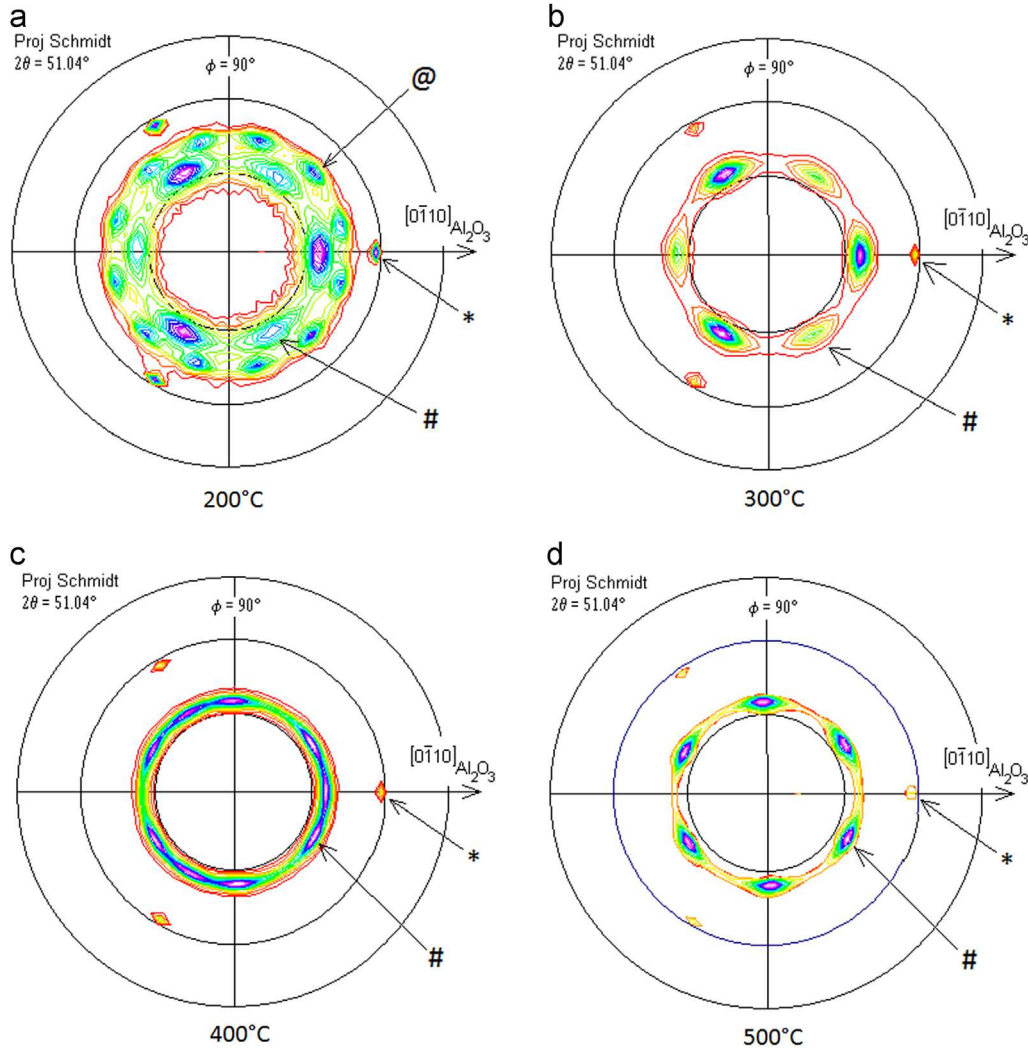


Fig. 2. Pole figures of the (044) planes of In_2O_3 ($\theta=51.04^\circ$) for the films grown at 200, 300, 400 and 500 °C. The symbol * is assigned to 3 poles at every 120° from the (02–24) reflection of the Al_2O_3 sapphire substrate. The symbol @ is assigned to 12 poles at every 30° from the (044) reflection of the In_2O_3 (001) oriented crystallites. The symbol # is assigned to the poles from the (044) reflection of the In_2O_3 (111) oriented crystallites.

The respective azimuthal positions of the poles of the (044) In_2O_3 and three (02–24) sapphire poles lead to the following in-plane epitaxial relationships:

$$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3} \text{ and } [1-10]_{\text{In}_2\text{O}_3} \parallel [0-110]_{\text{Al}_2\text{O}_3}$$

for the (001) In_2O_3 crystallites

$$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3} \text{ for the (111) } \text{In}_2\text{O}_3 \text{ crystallites}$$

With the respective in-plane parameters of hexagon and square unit of the two lattices (0.476 nm for the sapphire and 1.0118 nm for In_2O_3), a very significant lattice mismatch is deduced. However, the specific orientations of the films, can be explained in the frame of the domain matching epitaxy or extended atomic distance mismatch approach [5,25], in which “m” lattice units of the film match with “p” lattice units of the substrate. The values of m and p are defined as the minimum integers which satisfy the following relation:

$$md_f \approx pd_s \text{ or } [d_f/d_s] \approx [p/m]$$

d_f and d_s being the respective atomic distances in the film and substrate parallel directions. The corresponding lattice mismatch δ can thus be defined by [26]:

$$\delta = 2[md_f - pd_s]/[md_f + pd_s]$$

Table 2 summarises the results of this analysis through the matching relationship and lattice mismatch. This table shows that

the $[1-10]$ In_2O_3 direction plays a major role in the epitaxial growth as this direction is present in the epitaxial relationships for both (001) and (111) In_2O_3 epitaxy. As a result the matching relationships and lattice mismatch (Table 2) are the same for (001) and (111) epitaxy. This could at least partly, at the origin of the presence of the (001) In_2O_3 texture in the film grown at 200 °C. At higher temperature the surface mobility of the atoms increases and can lead to the formation of the most energetically favourable texture, i.e. the (111) In_2O_3 texture.

For the pole figures recorded on films grown at $T > 200^\circ\text{C}$, the poles due to the (001) oriented In_2O_3 crystallites are no longer present, in agreement with the XRD diagrams (Fig. 1). Six poles due to (111) oriented In_2O_3 crystallites are observed at 300 and 500 °C growth temperature. The azimuthal positions of the six poles observed at 300 °C are identical to those observed at 200 °C, while the six poles observed at 500 °C are rotated by 30° . The following epitaxial relationships are therefore deduced:

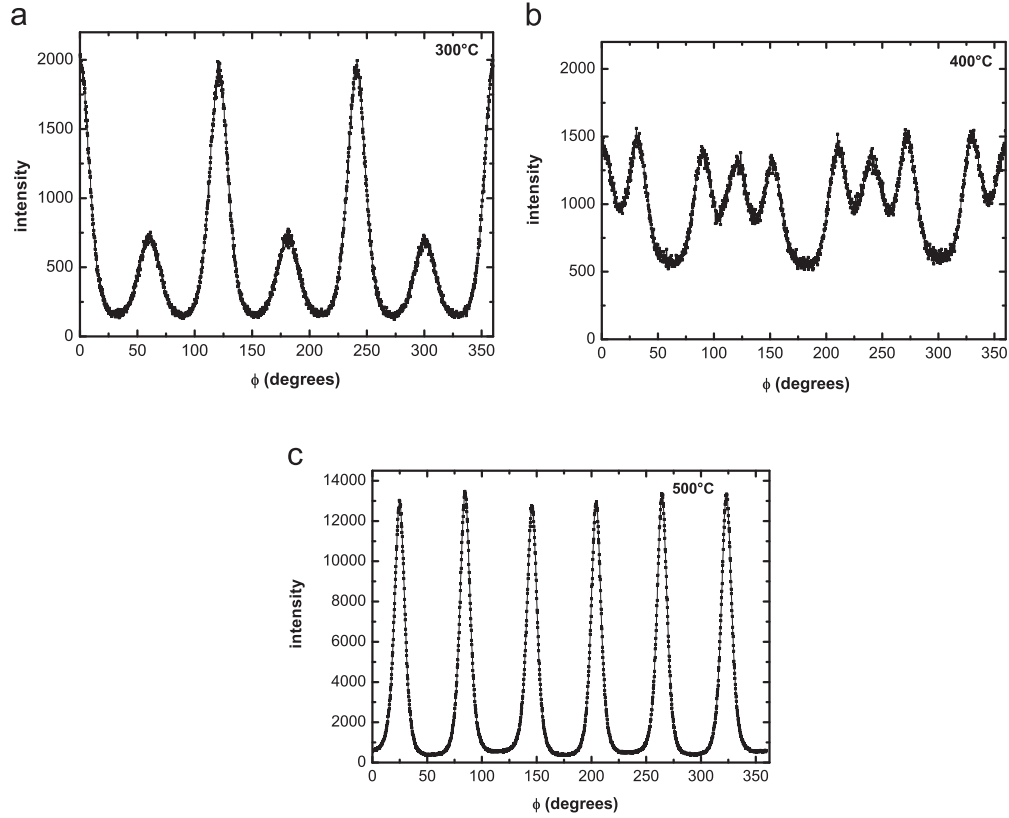
$$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3} \text{ for the (111) } \text{In}_2\text{O}_3 \text{ crystallites at } 300^\circ\text{C}$$

$$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-110]_{\text{Al}_2\text{O}_3} \text{ for the (111) } \text{In}_2\text{O}_3 \text{ crystallites at } 500^\circ\text{C}$$

The corresponding matching relationships and lattice mismatch are given in Table 2. In the case of the film grown at 400 °C, the pole figure shows nine poles, i.e. three series of three

Table 2

Texture	In-plane orientation	Matching relationships	Lattice mismatch (%)
(001)	$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3}$	$d_f \approx 3d_s$ ($d_f = 1.4308$ nm; $d_s = 0.4759$ nm)	$\delta = 0.217$
	$[1-10]_{\text{In}_2\text{O}_3} \parallel [0-110]_{\text{Al}_2\text{O}_3}$	$4d_f \approx 7d_s$ ($d_f = 1.4308$ nm; $d_s = 0.8242$ nm)	$\delta = 0.803$
(111)	$[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3}$	$d_f \approx 3d_s$ ($d_f = 1.4308$ nm; $d_s = 0.4759$ nm)	$\delta = 0.217$
	$[1-10]_{\text{In}_2\text{O}_3} \parallel [0-110]_{\text{Al}_2\text{O}_3}$	$4d_f \approx 7d_s$ ($d_f = 1.4308$ nm; $d_s = 0.8242$ nm)	$\delta = 0.803$

Fig. 3. (044) Φ -scan profile for the In_2O_3 films grown at (a) 300 °C, (b) 400 °C and (c) 500 °C.

poles. Such a pole figure seems schematically to correspond to the superposition of the pole figures observed at 300 and 500 °C.

The fact that the 6 poles corresponding to the (111) oriented crystallites observed at 200 and 300 °C are not equivalent (three of them present a higher intensity) has to be commented. Indeed, taking into account the 3-fold symmetry of the (0001) plane of the sapphire substrate, and the 3-fold symmetry of the (111) planes of the cubic bixbyite structure, only 3 poles should be present, while 6 are observed in Fig. 2. The presence of six poles has been previously observed in various oxide films grown on c-cut sapphire substrate and has been explained by the real surface of the c-cut sapphire which is usually stepped, leading to unconventional number of variants in epitaxial films [27]. Moreover, previous studies of the epitaxial growth of cubic In_2O_3 (111) on c-cut sapphire substrates reported poles figures or phi scans showing a six-fold symmetry and discrete peaks [8,9,11]. These results were interpreted by the existence of two different symmetry-equivalent twinned crystal orientations shifted by 60°. High resolution TEM images on indium based oxide films grown on c-cut sapphire substrates were recorded showing the domain boundary of such twin crystals [9,12].

In these preceding cases, the intensity of the poles or peaks in phi scans was similar, while in our work a drastic difference is observed. Indeed, three poles in Fig. 2a, show a larger intensity, and this was checked by the measurement of a phi scan at a 35.3°

declination angle which is presented in Fig. 3a. Three of the peaks present a larger intensity and a slightly lower width. On the contrary the phi scan corresponding to the 500 °C growth temperature (Fig. 3c) shows 6 peaks with the same intensity, shifted by a 30° angle with respect to Fig. 3a. Fig. 3b which corresponds to the film grown at 400 °C seems to be roughly the sum of the two phi scans presented in Fig. 3a and c.

Such results cannot be explained by defects on the sapphire substrates or presence of twin crystal in the films, which would lead to equivalent intensity and FWHM for the poles or peaks. The origin of these differences has been related to the presence of two kinds of (111) In_2O_3 oriented crystallites in the films, i.e. crystallites with different in-plane symmetry: three-fold and six-fold symmetry.

Let us recall that in the bixbyite structure, indium atoms are located on two non-equivalent sites and that 25% of the oxygen sites are not occupied. This leads to a specific arrangement of “constitutional” oxygen vacancies network, along the body diagonal and face diagonal of the cubic cell [28]. In this bixbyite structure, this arrangement leads to a three-fold symmetry in the (111) plane. However, if some disorder is introduced in the network of “constitutional” oxygen vacancies (random distribution of the vacancies in the plane), the three-fold symmetry is no longer preserved, and a six-fold symmetry will appear in the (111) plane as it is the case in the fluorite structure [28]. We can thus

assume that in the low temperature range, the film growth leads to the formation of both ordered bixbyite crystallites with a three-fold symmetry, and disordered bixbyite crystallites with a six-fold symmetry. Such an assumption can explain the pole figure presented in Fig. 2a. For $T=500^\circ\text{C}$, the six poles present in the pole figure show the same intensity (as it can be checked on the phi scan presented in Fig. 3c), meaning that a sole phase is present, i.e. the disordered bixbyite phase with a six-fold symmetry in the (111) plane. In this frame, the pole figure recorded on the film grown at 400°C corresponds to the transition from the low temperature (both ordered and disordered bixbyite) to high temperature (only disordered bixbyite) behaviour.

The transition temperature from ordered to disordered bixbyite structure depends upon the film growth rate. Indeed, growth rates as high as 1 nm per pulse can be obtained by PED, thanks to the high efficiency of energy transfer from incident polyenergetic (up to 15 keV) electrons to the target. In the case of a very high deposition rate, the pole figure recorded on a film grown at 500°C with such a high growth rate (Fig. 4a) is similar to that presented in Fig. 2c, with three series of three poles. This point can be checked on the corresponding phi scan presented in Fig. 4b. It follows that at least two experimental parameters play a role on the nature (ordered or disordered) of bixbyite phase which can be grown: the substrate temperature and the deposition rate which is related to the flux of incident species coming from the target.

The physical properties of the films grown between 200 and 500°C were studied and Fig. 5 shows their transmittance in the 300–900 nm range. All the films are transparent, with values of the transmittance between 80% and 85% over 500 nm, including that of the double polished c-cut sapphire substrate. The absorption coefficient (α) was calculated using the relation $\alpha = (1/d) \ln [(1 - R)/T]$, where T is the transmittance, R is the reflectance (neglected here) and d is the film thickness. The values of the direct optical band gap (E_g) were determined from absorption coefficient data by the extrapolating the linear part of the fundamental absorption edge to the energy axis (Tauc's plot, i.e. $(\alpha E)^2$ vs. E , where E is the photon energy) and are presented in the Table 3, together with the results of the Hall effect measurements at room temperature. As example, in the inset of Fig. 5, is shown the Tauc plot for film grown at 500°C . The direct optical band gap values are varying slightly with substrate temperature, being lower than value of 3.75 eV, typically reported in previous studies [1,2,5,8]. The value of In_2O_3 direct electronic band gap was recently revised to be

≤ 3 eV [29] and the low-energy tail which is seen below the absorption edge (Fig. 5) and which was previously attributed to indirect optical transitions, was found to be due to dipole forbidden transitions [29–31].

In Table 3 the values of carrier mobility are similar in the In_2O_3 films grown at 200 and 300°C , while the crystalline quality of the films (estimated through the FWHM rocking curves) increases with temperature. A further increase in growth temperature leads to a large decrease in mobility while at the same time the XRD results indicate a further increase in crystalline quality. This demonstrates that the mobility in these In_2O_3 films is not dominated by the scattering at grain boundaries or on structural defects as it has been concluded for films grown on YSZ [32]. Indeed, indium oxide is known to exhibit high mobility in the amorphous state which contrasts with the classical observation on Si or other semiconductors [33], i.e. its mobility does not depend on its structure [3,34].

In order to try to correlate the electrical and structural properties of films, the fraction of ordered bixbyite phase in In_2O_3 epitaxial films was estimated from the phi scans presented in Fig. 3. Actually, Fig. 6 shows the variation of the electrical resistivity (ρ), carrier density (n) and fraction of ordered to disordered bixbyite phase (f) as a function of growth temperature. Electrical properties of In_2O_3 films grown at room temperature and 120°C were added to data already presented in Table 3. In the

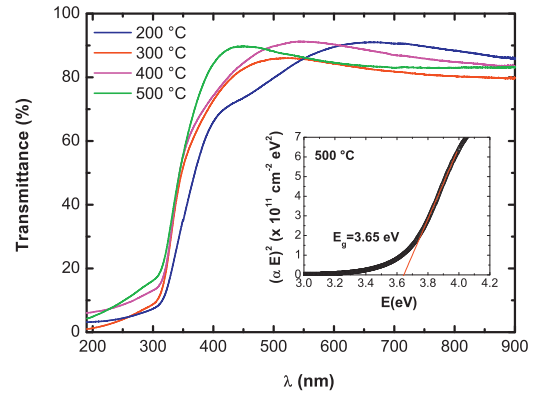


Fig. 5. Optical transmittance of the In_2O_3 films grown on transparent c-cut sapphire single crystal substrates at 200, 300, 400 and 500°C .

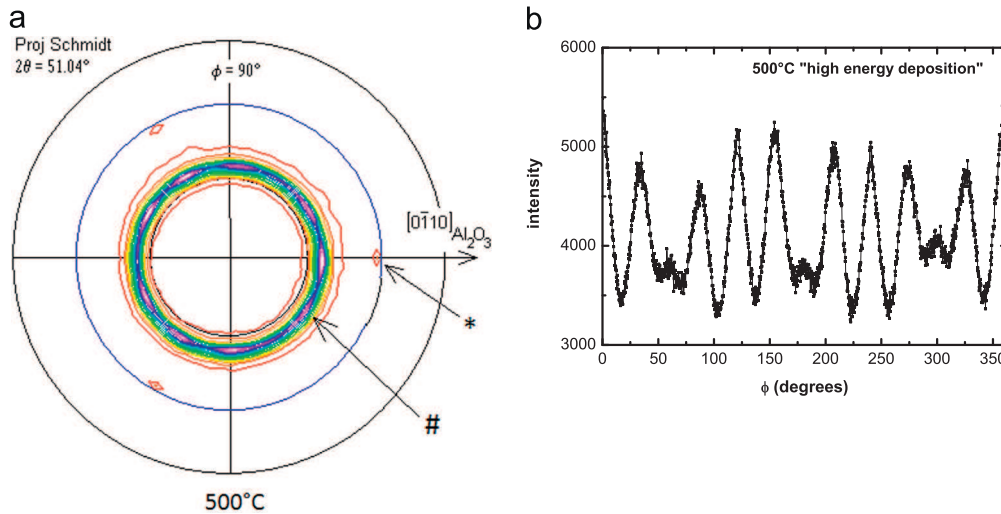


Fig. 4. Pole figure of the (044) planes of In_2O_3 ($\theta=51.04^\circ$) for the film grown at 500°C with a high deposition rate (a) and corresponding Φ -scan profile (b). The symbol * is assigned to 3 poles at every 120° from the (02-24) reflection of the Al_2O_3 sapphire substrate. The symbol # is assigned to the poles from the (044) reflection of the In_2O_3 (111) oriented crystallites.

200–300 °C range the resistivity shows a shallow minimum, while in the same temperature range the estimated fraction of ordered bixbyite phase is roughly constant and maximum. Moreover, the comparison of the variation of the carrier density and fraction of ordered bixbyite phase shows behaviour roughly similar in the 200–300 °C range. This fact would mean that the ordered bixbyite phase favours a high carrier density and accordingly a lower resistivity. The reason why the ordered bixbyite phase would play this role on the transport properties is not yet clear, but the Fig. 6 indicates a correlation (in the 200–300 °C range) between the structural characteristics of the In_2O_3 films and their transport properties.

Another important point is the large difference in the mobility and carrier concentration of films grown at 300 °C but with different cooling process (at growth pressure or at atmospheric oxygen pressure). In fact, the cooling down under atmospheric oxygen pressure leads to a large decrease in the carrier concentration and mobility with respect to the measured values in the film cooled down under 2×10^{-2} mbar (Table 3). This is certainly in relation with the oxygen uptake during this cooling down and a slight difference in the oxygen vacancies density in these two films. As a result large changes in the carrier density could occur due to the cooling down process.

The temperature dependent resistivity curves $R(T)$ were measured for In_2O_3 thin films grown by PED in oxygen at various temperatures. Fig. 7 summarises the results through the resistivity curves for films grown in the range 200–400 °C. Depending on the growth temperature and cooling process, these curves show either a semiconducting (400 °C and 300 °C cooled under atmospheric oxygen pressure) or a metallic (200 °C and 300 °C cooled at 2×10^{-2} mbar) behaviour, in relation with the carrier densities given in Table 3. Actually, the critical carrier density for the onset of metallic conductivity as given by the Mott criterion [35] is estimated to be $7.21 \times 10^{18} \text{ cm}^{-3}$ for In_2O_3 [10]. Above this value the In_2O_3 degenerates, as observed for the In_2O_3 films grown at 200 and 300 °C, in correlation with the resistivity–temperature curves (Fig. 7), while films grown at 400 and 500 °C have values below this limit.

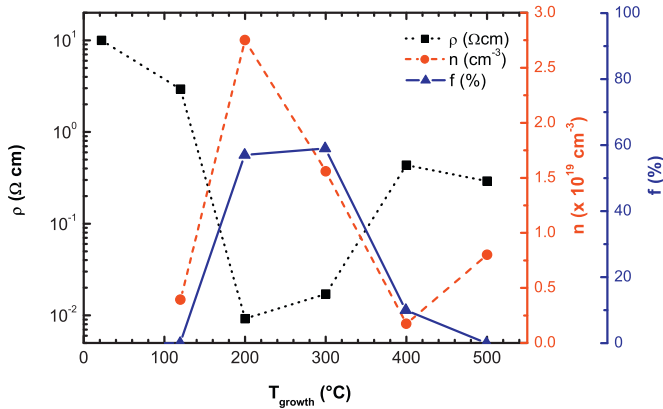


Fig. 6. Electrical resistivity (ρ), carrier density (n) and fraction of ordered to disordered bixbyite phase (f) as a function of growth temperature.

The resistivity curve for the films grown at 400 °C shows a semiconductor behaviour (Fig. 7) in the whole temperature range, with a negative temperature coefficient resistance (TCR). A thermally activated transport mechanism can be deduced from the Arrhenius plot (Fig. 8d), with the linear variation of $\ln \rho$ with T^{-1} in the 295–213 K range. The activation energy estimated from the slope is about 31 meV. For lower temperatures, an increase of the resistivity and a curvature in the Arrhenius plot are observed. This feature is frequently observed for semiconductor oxides [20], and is generally interpreted by the localisation of carriers which can be described by the variable range hopping (VRH) mechanism [35]. The resistivity can be described by the following relationships:

$$\rho(T) = \rho_0 \exp(T_0/kT)^{1/4} \quad (1)$$

In that case, $\ln \rho(T)$ follows a linear dependence in $T^{-1/4}$ for a three dimensional hopping. Such behaviour which can be observed in the inset of Fig. 8d, was systematically observed in the In_2O_3 films grown at $T > 400$ °C.

For the films grown at 300 °C, although a negative TCR is observed in Fig. 8b and c, an important difference in the $R(T)$ curves was observed depending upon the cooling process. Indeed, for the film cooled down under atmospheric oxygen pressure (Fig. 8c) the ratio of resistivity between 4 K and 300 K is equal to 44, i.e. a value of the order of those observed in oxide semiconductors (> 20), while a value equal to 1.15 is deduced from the Fig. 8b for the film cooled down under growth oxygen pressure (2×10^{-2} mbar).

The Arrhenius plot shown in the inset of Fig. 8c for the films cooled under atmospheric oxygen pressure shows a linear variation of $\ln \rho(T)$, characteristic of a thermally assisted transport mechanism from 293 to 192 K, with activation energy equal to 49 meV. On the contrary such an analysis for the curve of Fig. 8b (In_2O_3 films cooled down under growth oxygen pressure) does not show a linear behaviour on a noticeable temperature range. Thus change in the oxygen pressure during the cooling process which could lead to a change in the oxygen composition, i.e. in the oxygen vacancies concentration, leads to a drastic change in the transport phenomena of indium oxide films.

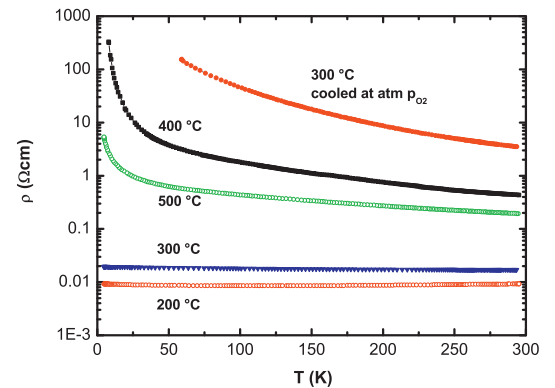


Fig. 7. Electrical resistivity curves as a function of temperature for the In_2O_3 films grown at 200, 300, 400, 500 °C and 300 °C under cooling at atmospheric pO_2 .

Table 3

Temperature (°C)	200	300	400	500 °C	300 cooled at atmospheric pO_2
Thickness (nm)	130	105	99.5	85	71
Resistivity ($\Omega \text{ cm}$)	9.198×10^{-3}	1.711×10^{-2}	0.435	0.292	3.501
Mobility ($\text{cm}^2/\text{V s}$)	24.70 ± 0.7	23.37 ± 4	8.27 ± 1.7	2.67 ± 0.6	3.17 ± 2.1
Carrier Density (cm^{-3})	2.75×10^{19}	1.56×10^{19}	1.73×10^{18}	8.00×10^{18}	3.68×10^{18}
E_{gap} (eV)	3.55	3.69	3.66	3.65	3.64

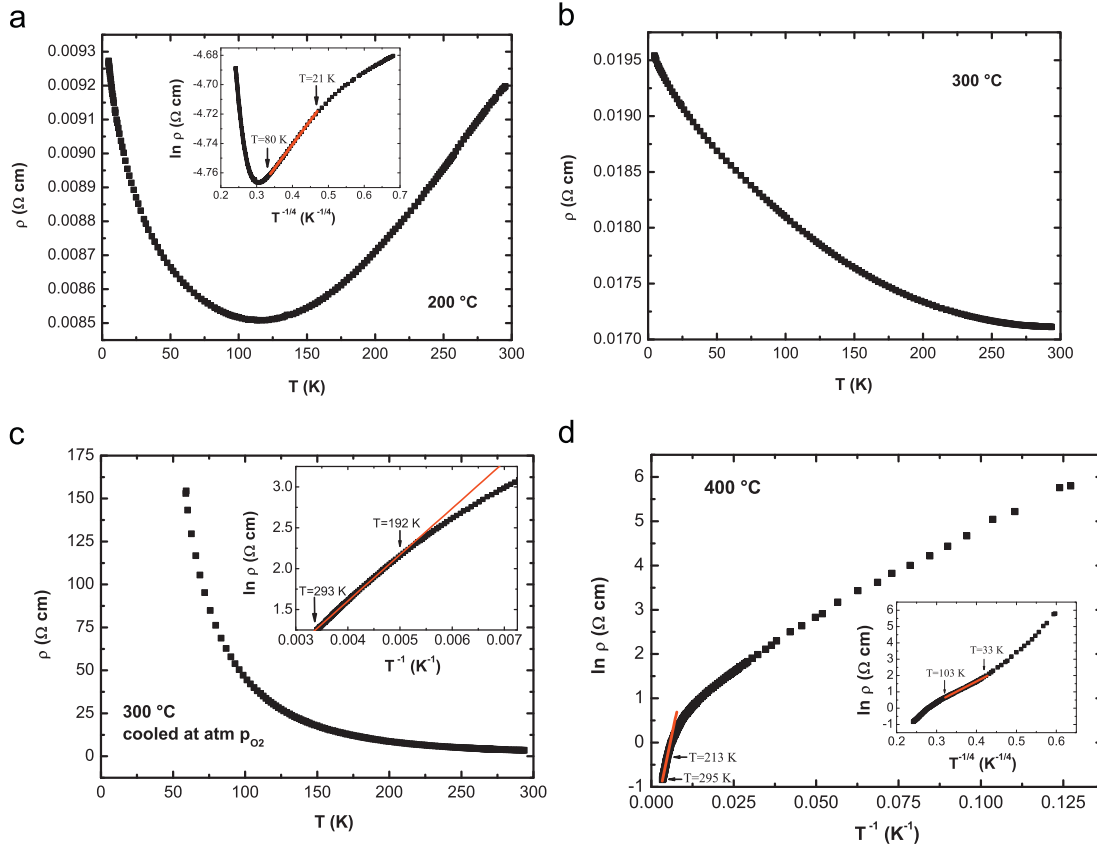


Fig. 8. Resistivity as a function of temperature for the In_2O_3 films on c-cut sapphire substrate grown at (a) 200 °C, (b) 300 °C under cooling at atmospheric PO_2 and (d) 400 °C.

For the films grown at 200 °C (Fig. 8a), the $\rho(T)$ curve shows a change of TCR around 118 K. In fact from room temperature down to 118 K a positive TCR (metallic conductivity) is observed, followed at lower temperatures by a negative TCR, i.e. a metal-semiconductor transition (MST) occurs in the film around 118 K. MST has been already observed in pure [36] or doped In oxide films [37] and in pure [38] or doped Zn oxide films [39]. In these cases the MST was generally analysed in the frame of the quantum corrections to conductivity (QCC) in a disordered conductor [40]. This model used to describe the resistivity curve is considered to be valid provided that the quantum corrections are much smaller than the Boltzmann conductivity at the transition temperature [41]. It must be noticed that the variation of resistivity in Fig. 8a between 118 and 5 K is about 9%, i.e. a variation which seems to be too high to explain this MST via the model of quantum corrections to conductivity which has been used in some cases [38,41]. A more plausible approach would be based on the phenomenon of carrier localisation inducing a metal semiconductor transition at low temperature [35,40]. In that case, the low temperature resistivity is generally interpreted by Eq. (1) as Mott's variable-range hopping (VRH) caused by localised states in a disordered oxide films [35,42].

The inset of the Fig. 8a represents the variation of $\ln \rho$ as a function of $T^{-1/4}$, and a linear variation is observed in the 21–82 K temperature range. This result is very similar to that recently reported in the case of single crystalline In_2O_3 nanowires [42]. In this frame, the carrier localisation at the origin of the MST would be due to the structural disorder in the In_2O_3 films grown at 200 °C. Indeed, as noted above, the crystalline quality of this low temperature grown film is lower than those obtained in the films grown at higher temperatures. Let us notice that recently it has been reported that such a $T^{-1/4}$ variation for $\ln \rho(T)$ could be

interpreted in the frame of a percolation conduction model [43], in the case of studies on carrier transport mechanisms in disordered oxide semiconductors (crystalline and amorphous In–Ga–Zn–oxides). However, the use of such an interpretation for epitaxial films on c-cut sapphire substrates seems questionable.

4. Discussion

Specific structural characteristics of the In_2O_3 films grown on sapphire substrates reported here have to be discussed. Indeed, the preferential formation of the bixbyite In_2O_3 phase (with the three fold symmetry in the (111) plane) is observed for growth T lower than 300 °C, while at higher T , a disordered bixbyite phase (with a six fold symmetry in the (111) plane) is present. Moreover, the epitaxial growth of (111) In_2O_3 on sapphire substrate corresponds to a “hexagon on hexagon” growth for $T \leq 300$ °C, while at higher temperatures, the epitaxial relationship corresponds to a 30° rotation of the In_2O_3 hexagon with respect to the Al_2O_3 hexagon. There is a clear effect of the growth temperature on these facts, but some specificity of the PED growth methods have to be taken into account to explain these results.

First in PED, the kinetic energy of the species emitted by the target is high, typically of the order of 50–100 eV. Such high energy species will present a high mobility at the surface of the growing film which could favour the formation of crystalline material at low temperature and the epitaxial growth of In_2O_3 at temperature as low as 200 °C. Such a high kinetic energy could be also the reason of the presence of the disordered In_2O_3 bixbyite for growth $T < 300$ °C. Indeed, the bombardment by the species coming from the target could induce oxygen vacancy creation and migration in the near surface region of the bixbyite film.

This would destroy the organisation of the “constitutional oxygen vacancies” of the bixbyite phase and lead to the formation of the disordered bixbyite phase with the six fold symmetry in the (111) plane of this phase.

For increasing temperatures ($T \geq 300^\circ\text{C}$), the migration of oxygen vacancies at the surface of the bixbyite phase will be easier and accordingly a random distribution of these vacancies in the (111) plane will lead to the increasing formation of the disordered bixbyite phase. As a result, at $T = 500^\circ\text{C}$, this disordered bixbyite phase is solely present in the In_2O_3 films.

The temperature will play an important role on the precise epitaxial relationships between the In_2O_3 film and c-cut sapphire substrate. For $T \leq 300^\circ\text{C}$, the epitaxial relationships correspond to the “hexagon on hexagon” growth, which is not the most likely in terms of energy. Indeed, in this configuration as noted previously the In ions from the films and O ions of the substrate do not coincide optimally [5]. On the contrary, in the case of the other epitaxial relationship (30° rotation of the film hexagon):

$$[1-10]_{\text{In}_2\text{O}_3} \parallel [0-101]_{\text{Al}_2\text{O}_3}$$

The In ions are into a good coincidence with the O ions of the substrates, leading to a lower interfacial energy which would favour this configuration [5]. However, with the first epitaxial relationship (hexagon on hexagon), the minimum size of the epitaxial domain, which is deduced from the lattice matching, is rather limited (1.4038 nm as deduced from Table 2), while the corresponding minimum size of the domain in the other epitaxial relationship is much higher, 5.7232 nm. As a result, for $T \leq 300^\circ\text{C}$, the diffusion of the incident species at the surface of the growing film will be limited and the low size epitaxial domain will be favoured in these conditions, i.e. the $[1-10]_{\text{In}_2\text{O}_3} \parallel [1-210]_{\text{Al}_2\text{O}_3}$ epitaxial relationship will be observed. For increasing temperature, the incident species could diffuse on longer distances and therefore the formation of an extended epitaxial domain will occur, i.e. the $[1-10]_{\text{In}_2\text{O}_3} \parallel [0-110]_{\text{Al}_2\text{O}_3}$ epitaxial relationship will be thus favoured. It is worth noticing that such a situation corresponds to limited deposition rate. Indeed for large value of deposition rate (1 nm per pulse) the high flux of species on the film surface will “quench” at least partly the film structure, as atoms will not have sufficient time to migrate at the film surface. As a result the bixbyite and disordered bixbyite phases would be observed even at $T = 500^\circ\text{C}$, as reported in Fig. 3.

The study of the transport properties of the indium oxide films grown in this work clearly demonstrates that the crystalline quality of the films is not the main parameter governing their physical properties. Actually we only observed a correlation between the presence of the ordered bixbyite phase and the carrier density in the films. Otherwise, the results showed that the highest conductivities are obtained in films grown at the lower temperature (200°C), corresponding to films presenting different textures, i.e. a lower crystalline quality. A maximum mobility of $24.7\text{ cm}^2/\text{Vs}$ was measured at 200°C , and then it falls with improvement in the crystalline quality of films. On the contrary, the main parameter which seems to determine the transport properties of these films is their oxygen composition, i.e. the density of oxygen vacancies in the films. A decrease of the concentration of oxygen vacancies acting as electron donors leads to an increase of the resistivity. The variation of the carrier density changes In_2O_3 from degenerate to non-degenerate films.

As it has been noted, even the simple change in the cooling atmosphere for a film grown at 300°C leads to drastic differences in the carrier density and mobility. The mobility falls rapidly from 23.37 to $3.5\text{ cm}^2/\text{Vs}$ and the carrier density decreases from above to below the onset of metallic conductivity. Taking into account the initial low temperature (300°C), and the limited duration of the cooling process (less than 30 min), the oxygen uptake during

the cooling should be limited. As a result, a slight change of the oxygen composition (and in oxygen vacancy concentration) of the films induces large effects on the transport phenomena of the film. This result can be related to those reported in a recent publication [3]. Indeed, it has been demonstrated by using surface calculations and thickness-dependent Hall measurements that surface donors rather than defects dominate the conductivity of undoped In_2O_3 films [3]. This means that conductivity of In_2O_3 films is very sensitive to the precise oxygen composition, i.e. oxygen vacancies play the role of donors in this material.

5. Conclusion

Epitaxial indium oxide films with the cubic bixbyite structure were obtained by PED method on c-cut sapphire substrates at 10^{-2} mbar oxygen pressure at low growth temperatures from 200 to 500°C . Two distinct structural phases were evidenced in the films: an ordered bixbyite phase with the three-fold symmetry in the (111) plane, and, a disordered bixbyite phase with a six fold symmetry in the (111) plane. This is related to the specificities of the growth conditions which can induce a large disorder in the oxygen network of In_2O_3 . While the optical transparency is high ($> 80\%$) in the visible spectral range for all films, the electrical properties were tailored as a function of growth temperature. For films grown at 200°C a metallic conductivity at room temperature and a metal–semiconductor transition at low temperature were evidenced. For the films grown at 400 and 500°C the classical semiconductor behaviour was observed, the mobility decreasing with improvement in the crystalline quality of films. Moreover, the ordered bixbyite phase was found to favour a high carrier density and accordingly a lower resistivity in the films leading these epitaxial films as potential layers as substrates for the subsequent solar cells growth. Such results open the way to the optimisation of the growth conditions in order to obtain pure ordered bixbyite films with a very high carrier density, while preserving the high optical transparency, in view of their use as transparent conducting electrodes. The fact that such pure ordered bixbyite films could be obtained at low growth temperature ($< 200^\circ\text{C}$) would favour their use as transparent conducting layers to avoid the degradation of the solar cell junctions in photovoltaics.

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