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# BLOCKS OF THE GROTHENDIECK RING OF EQUIVARIANT BUNDLES ON A FINITE GROUP

by

CÉDRIC BONNAFÉ

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*Abstract.* — If  $G$  is a finite group, the Grothendieck group  $\mathbf{K}_G(G)$  of the category of  $G$ -equivariant  $\mathbb{C}$ -vector bundles on  $G$  (for the action of  $G$  on itself by conjugation) is endowed with a structure of (commutative) ring. If  $K$  is a sufficiently large extension of  $\mathbb{Q}_p$  and  $\mathcal{O}$  denotes the integral closure of  $\mathbb{Z}_p$  in  $K$ , the  $K$ -algebra  $K\mathbf{K}_G(G) = K \otimes_{\mathbb{Z}} \mathbf{K}_G(G)$  is split semisimple. The aim of this paper is to describe the  $\mathcal{O}$ -blocks of the  $\mathcal{O}$ -algebra  $\mathcal{O}\mathbf{K}_G(G)$ .

## 1. Notation, introduction

**1.A. Groups.** — We fix in this paper a finite group  $G$ , a prime number  $p$  and a finite extension  $K$  of the  $p$ -adic field  $\mathbb{Q}_p$  such that  $KH$  is split for all subgroups  $H$  of  $G$ . We denote by  $\mathcal{O}$  the integral closure of  $\mathbb{Z}_p$  in  $K$ , by  $\mathfrak{p}$  the maximal ideal of  $\mathcal{O}$ , by  $k$  the residue field of  $\mathcal{O}$  (i.e.  $k = \mathcal{O}/\mathfrak{p}$ ) We denote by  $\text{Irr}(KG)$  the set of irreducible characters of  $G$  (over  $K$ ).

A  $p$ -element (respectively  $p'$ -element) of  $G$  is an element whose order is a power of  $p$  (respectively prime to  $p$ ). If  $g \in G$ , we denote by  $g_p$  and  $g_{p'}$  the unique elements of  $G$  such that  $g = g_p g_{p'} = g_{p'} g_p$ ,  $g_p$  is a  $p$ -element and  $g_{p'}$  is a  $p'$ -element. The set of  $p$ -elements (respectively  $p'$ -elements) of  $G$  is denoted by  $G_p$  (respectively  $G_{p'}$ ).

If  $X$  is a  $G$ -set (i.e. a set endowed with a left  $G$ -action), we denote by  $[G \backslash X]$  a set of representatives of  $G$ -orbits in  $X$ . The reader can check that we will use formulas like

$$\sum_{x \in [G \backslash X]} f(x)$$

(or families like  $(f(x))_{x \in [G \backslash X]}$ ) only whenever  $f(x)$  does not depend on the choice of the representative  $x$  in its  $G$ -orbit. If  $X$  is a set- $G$  (i.e. a set endowed with a right  $G$ -action), we define similarly  $[X/G]$  and will use it according to the same principles.

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**1.B. Blocks.** — A *block idempotent* of  $kG$  (respectively  $\mathcal{O}G$ ) is a primitive idempotent of the center  $Z(kG)$  (respectively  $Z(\mathcal{O}G)$ ) of  $\mathcal{O}G$ . We denote by  $\text{Blocks}(kG)$  (respectively  $\text{Blocks}(\mathcal{O}G)$ ) the set of block idempotents of  $kG$  (respectively  $\mathcal{O}G$ ). Reduction modulo  $\mathfrak{p}$  induces a bijection  $\text{Blocks}(\mathcal{O}G) \xrightarrow{\sim} \text{Blocks}(kG)$ ,  $e \mapsto \bar{e}$  (and whose inverse is denoted by  $e \mapsto \tilde{e}$ ).

A *p-block* of  $G$  is a subset  $\mathcal{B}$  of  $\text{Irr}(G)$  such that  $\mathcal{B} = \text{Irr}(KGe)$ , for some block idempotent  $e$  of  $\mathcal{O}G$ .

**1.C. Fourier coefficients.** — Let

$$\text{IrrPairs}(G) = \{(g, \gamma) \mid g \in G \text{ and } \gamma \in \text{Irr}(KC_G(g))\}$$

and

$$\text{BlPairs}_p(G) = \{(s, e) \mid s \in G_{p'} \text{ and } e \in \text{Blocks}(\mathcal{O}C_G(s))\}.$$

The group  $G$  acts (on the left) on these two sets by conjugation. We set

$$\mathcal{M}(G) = [G \backslash \text{IrrPairs}(G)] \quad \text{and} \quad \mathcal{M}^p(G) = [G \backslash \text{BlPairs}_p(G)].$$

If  $(g, \gamma), (h, \eta) \in \text{IrrPairs}(G)$ , we define, following Lusztig [Lu, 2.5(a)],

$$\{(g, \gamma), (h, \eta)\} = \frac{1}{|C_G(g)| \cdot |C_G(h)|} \sum_{\substack{x \in G \\ xhx^{-1} \in C_G(g)}} \gamma(xhx^{-1})\eta(x^{-1}g^{-1}x).$$

Note that  $\{(g, \gamma), (h, \eta)\}$  depends only on the  $G$ -orbit of  $(g, \gamma)$  and on the  $G$ -orbit of  $(h, \eta)$ .

**1.D. Vector bundles.** — Except from Proposition 2.3 below, all the definitions, all the results in this subsection can be found in [Lu, §2]. We denote by  $\mathcal{Bun}_G(G)$  the category of  $G$ -equivariant finite dimensional  $K$ -vector bundles on  $G$  (for the action of  $G$  by conjugation). Its Grothendieck group  $\mathbf{K}_G(G)$  is endowed with a ring structure. For each  $(g, \gamma) \in \mathcal{M}(G)$ , let  $V_{g, \gamma}$  be the isomorphism class (in  $\mathbf{K}_G(G)$ ) of the simple object in  $\mathcal{Bun}_G(G)$  associated with  $(g, \gamma)$ , as in [Lu, §2.5] (it is denoted  $U_{g, \gamma}$  there). Then

$$\mathbf{K}_G(G) = \bigoplus_{(g, \gamma) \in \mathcal{M}(G)} \mathbb{Z}V_{g, \gamma}.$$

The  $K$ -algebra  $K\mathbf{K}_G(G) = K \otimes_{\mathbb{Z}} \mathbf{K}_G(G)$  is split semisimple and commutative. Its simple modules (which have dimension one) are also parametrized by  $\mathcal{M}(G)$ : if  $(g, \gamma) \in \mathcal{M}(G)$ , the  $K$ -linear map

$$\Psi_{g, \gamma} : K\mathbf{K}_G(G) \longrightarrow K$$

defined by

$$\Psi_{g, \gamma}(V_{h, \eta}) = \frac{|C_G(g)|}{\gamma(1)} \cdot \{(h^{-1}, \eta), (g, \gamma)\}$$

is a morphism of  $K$ -algebras and all morphisms of  $K$ -algebras  $K\mathbf{K}_G(G) \rightarrow K$  are obtained in this way.

We define similarly block idempotents of  $k\mathbf{K}_G(G)$  and  $\mathcal{O}\mathbf{K}_G(G)$ , as well as  $p$ -blocks of  $\mathcal{M}(G) \xrightarrow{\sim} \text{Irr}(K\mathbf{K}_G(G))$ .

**1.E. Brauer maps.** — Let  $\Lambda$  denote one of the two rings  $\mathcal{O}$  or  $k$ . If  $g \in G$  (and if we set  $s = g_{p'}$ ), we denote by  $\text{Br}_g^\Lambda$  the  $\Lambda$ -linear map

$$\text{Br}_g^\Lambda : \Lambda C_G(s) \rightarrow \Lambda C_G(g)$$

such that

$$\text{Br}_g^\Lambda(h) = \begin{cases} h & \text{if } h \in C_G(g), \\ 0 & \text{if } h \notin C_G(g), \end{cases}$$

for all  $h \in C_G(s)$ . Recall [Is, Lemma 15.32] that

$$(1.1) \quad \text{Br}_g^k \text{ induces a morphism of algebras } Z(kC_G(s)) \rightarrow Z(kC_G(g)).$$

Therefore, if  $e \in \text{Blocks}(\mathcal{O}C_G(s))$ , then  $\text{Br}_g^k(e)$  is an idempotent of  $Z(kC_G(g))$  (possibly equal to zero) and we can write it a sum  $\text{Br}_g^k(e) = e_1 + \cdots + e_n$ , where  $e_1, \dots, e_n$  are pairwise distinct block idempotents of  $kC_G(g)$ . We then set

$$\beta_g^\mathcal{O}(e) = \sum_{i=1}^n \tilde{e}_i.$$

It is an idempotent (possibly equal to zero, possibly non-primitive) of  $Z(\mathcal{O}C_G(g))$ .

**1.F. The main result.** — In order to state more easily our main result, it will be more convenient (though it is not strictly necessary) to fix a particular set of representatives of conjugacy classes of  $G$ .

**Hypothesis and notation.** From now on, and until the end of this paper, we denote by:

- $[G_{p'}/\sim]$  a set of representatives of conjugacy classes of  $p'$ -elements in  $G$ .
- $[G/\sim]$  a set of representatives of conjugacy classes of elements of  $G$  such that, for all  $g \in [G/\sim]$ ,  $g_{p'} \in [G_{p'}/\sim]$ .

We also assume that, if  $(g, \gamma) \in \mathcal{M}(G)$  or  $(s, e) \in \mathcal{M}^p(G)$ , then  $g \in [G/\sim]$  and  $s \in [G_{p'}/\sim]$ .

If  $(s, e) \in \mathcal{M}^p(G)$ , we define  $\mathcal{B}_G(s, e)$  to be the set of pairs  $(g, \gamma) \in \mathcal{M}(G)$  such that:

- (1)  $g_{p'} = s$ .
- (2)  $\gamma \in \text{Irr}(kC_G(g)\beta_g^\mathcal{O}(e))$ .

**Théorème 1.2.** — *The map  $(s, e) \mapsto \mathcal{B}_G(s, e)$  induces a bijection between  $\mathcal{M}^p(G)$  to the set of  $p$ -blocks of  $\mathcal{M}(G)$ .*

## 2. Proof of Theorem 1.2

**2.A. Central characters and congruences.** — If  $(g, \gamma) \in \text{IrrPairs}(G)$ , we denote by  $\omega_{g, \gamma} : Z(KG) \rightarrow K$  the *central character* associated with  $\gamma$  (if  $z \in Z(KG)$ , then  $\omega_{g, \gamma}(z)$  is the scalar through which  $z$  acts on an irreducible  $KG$ -module affording the character  $\gamma$ ). It is a morphism of algebras: when restricted to  $Z(\mathcal{O}G)$ , it has values in  $\mathcal{O}$ .

If  $h \in C_G(g)$ , we denote by  $\Sigma_g(h)$  conjugacy class of  $h$  in  $C_G(g)$  and we set

$$\hat{\Sigma}_g(h) = \sum_{v \in \Sigma_g(h)} v \in Z(\mathcal{O}G).$$

We have

$$(2.1) \quad \omega_{g, \gamma}(\hat{\Sigma}_g(h)) = \frac{|\Sigma_g(h)| \cdot \gamma(h)}{\gamma(1)}.$$

We also recall the following classical results:

**Proposition 2.2.** — *If  $g \in G$  and  $\gamma, \gamma'$  are two irreducible characters of  $C_G(g)$ , then  $\gamma$  and  $\gamma'$  lie in the same  $p$ -block of  $C_G(g)$  if and only if*

$$\omega_{g, \gamma}(\hat{\Sigma}_g(h)) \equiv \omega_{g, \gamma'}(\hat{\Sigma}_g(h)) \pmod{\mathfrak{p}}$$

for all  $h \in C_G(g)$ .

**Proposition 2.3.** — *Let  $(g, \gamma)$  and  $(g', \gamma')$  be two elements of  $\mathcal{M}(G)$ . Then  $(g, \gamma)$  and  $(g', \gamma')$  belong to the same  $p$ -block of  $\mathcal{M}(G)$  if and only if*

$$\Psi_{g, \gamma}(V_{h, \eta}) \equiv \Psi_{g', \gamma'}(V_{h, \eta}) \pmod{\mathfrak{p}}$$

for all  $(h, \eta) \in \mathcal{M}(G)$ .

**2.B. Around the Brauer map.** — As Brauer maps are morphisms of algebras, we have

$$\sum_{e \in \text{Blocks}(kC_G(g_{p'}))} \text{Br}_g^p(e) = 1,$$

and so

$$(2.4) \quad \text{The family } (\mathcal{B}_G(g, e))_{(g, e) \in \mathcal{M}^p(G)} \text{ is a partition of } \mathcal{M}(G).$$

Now, let  $(g, \gamma) \in \mathcal{M}(G)$  and let  $s = g_{p'}$ . If  $e \in \text{Blocks}(\mathcal{O}C_G(s))$  is such that  $\gamma \in \text{Irr}(KC_G(g)\beta_g^\theta(e))$ , and if  $\sigma \in \text{Irr}(KC_G(s)e)$ , then [Is, Lemma 15.44]

$$(2.5) \quad \omega_{s,\sigma}(z) \equiv \omega_{g,\gamma}(\text{Br}_g^\theta(z)) \pmod{\mathfrak{p}}$$

for all  $z \in Z(\mathcal{O}C_G(s))$ .

**2.C. Rearranging the formula for  $\Psi_{g,\gamma}$ .** — If  $(g, \gamma), (h, \eta) \in \text{IrrPairs}(g)$  then

$$(2.6) \quad \Psi_{g,\gamma}(V_{h,\eta}) = \sum_{\substack{x \in [C_G(g) \backslash G / C_G(h)] \\ xhx^{-1} \in C_G(g)}} \eta(x^{-1}gx) \omega_{g,\gamma}(\hat{\Sigma}(xhx^{-1})).$$

*Proof.* — By definition,

$$\Psi_{g,\gamma}(V_{h,\eta}) = \frac{1}{\gamma(1) \cdot |C_G(h)|} \sum_{\substack{x \in G \\ xhx^{-1} \in C_G(g)}} \eta(x^{-1}gx) \gamma(xhx^{-1}) = \frac{1}{\gamma(1)} \sum_{\substack{x \in [G/C_G(h)] \\ xhx^{-1} \in C_G(g)}} \eta(x^{-1}gx) \gamma(xhx^{-1}).$$

Now, if  $x \in G$  is such that  $xhx^{-1} \in C_G(g)$  and if  $u \in C_G(g)$ , then

$$\eta((ux)^{-1}g(ux)) \gamma((ux)h(ux)x^{-1}).$$

So we can gather the terms in the last sum according to their  $C_G(g)$ -orbit. We get

$$\Psi_{g,\gamma}(V_{h,\eta}) = \sum_{\substack{x \in [C_G(g) \backslash G / C_G(h)] \\ xhx^{-1} \in C_G(g)}} \eta(x^{-1}gx) \frac{|C_G(g)|}{|C_G(g) \cap xC_G(h)x^{-1}|} \cdot \frac{\gamma(xhx^{-1})}{\gamma(1)}.$$

But, for  $x$  in  $G$  such that  $xhx^{-1} \in C_G(g)$ ,

$$\frac{|C_G(g)|}{|C_G(g) \cap xC_G(h)x^{-1}|} = |\Sigma_g(xhx^{-1})|,$$

so the result follows from 2.1. □

**Corollaire 2.7.** — Let  $g \in [G/\sim]$  and let  $\gamma, \gamma' \in \text{Irr}(KC_G(g))$  lying in the same  $p$ -block of  $C_G(g)$ . Then  $(g, \gamma)$  and  $(g, \gamma')$  lie in the same  $p$ -block of  $\mathcal{M}(G)$ .

*Proof.* — This follows from 2.6 and Proposition 2.3. □

**2.D.  $p'$ -part.** — Fix  $(g, \gamma) \in \mathcal{M}(G)$ . Then it follows from 2.6 that, for all  $\chi \in \text{Irr}(KG)$ ,

$$(2.8) \quad \Psi_{g, \gamma}(V_{1, \chi}) = \chi(g).$$

**Proposition 2.9.** — Let  $(g, \gamma)$  and  $(h, \eta)$  be two elements in  $\mathcal{M}(G)$  which lie in the same  $p$ -block. Then  $g_{p'} = h_{p'}$ .

*Proof.* — By Proposition 2.3 and Equality 2.8, it follows from the hypothesis that

$$\chi(g) \equiv \chi(h) \pmod{p}$$

for all  $\chi \in \text{Irr}(KG)$ . Hence  $g_{p'}$  and  $h_{p'}$  are conjugate in  $G$  (see [Bo, Proposition 2.14]), so they are equal according to our conventions explained in §1.F.  $\square$

**Proposition 2.10.** — Let  $s \in G_{p'}$  and let  $\sigma, \sigma' \in \text{Irr}(KC_G(s))$ . Then  $(s, \sigma)$  and  $(s, \sigma')$  lie in the same  $p$ -block if and only if  $\sigma$  and  $\sigma'$  lie in the same  $p$ -block of  $C_G(s)$ .

*Proof.* — The if part has been proved in Corollary 2.7. Conversely, assume that  $(s, \sigma)$  and  $(s, \sigma')$  lie in the same  $p$ -block. Fix  $h \in C_G(s)$ . Then  $s \in C_G(h)$ . Let  $\eta_{s, h} : C_G(h) \rightarrow K$  be the class function on  $C_G(h)$  defined by:

$$\eta_{s, h}(g) = \begin{cases} 1 & \text{if } g_{p'} \text{ and } s \text{ are conjugate in } C_G(h), \\ 0 & \text{otherwise.} \end{cases}$$

It follows from [Bo, Proposition 2.20] that  $\eta_{s, h} \in \mathcal{O} \text{Irr}(KC_G(h))$ . Therefore, by 2.6 and Proposition 2.3,

$$(\#) \quad \sum_{\substack{x \in [C_G(s) \backslash G / C_G(h)] \\ xhx^{-1} \in C_G(s)}} \eta_{s, h}(x^{-1}sx) \left( \omega_{s, \sigma}(xhx^{-1}) - \omega_{s, \sigma'}(xhx^{-1}) \right) \equiv 0 \pmod{p}.$$

Now, let  $x \in G$  be such that  $xhx^{-1} \in C_G(s)$ . Since  $x^{-1}sx$  is also a  $p'$ -element,  $\eta_{s, h}(x^{-1}sx) = 1$  if and only if  $s$  and  $x^{-1}sx$  are conjugate in  $C_G(h)$  that is, if and only if  $x \in C_G(s)C_G(h)$ . So it follows from (#) that

$$\omega_{s, \sigma}(h) \equiv \omega_{s, \sigma'}(h) \pmod{p}$$

for all  $h \in C_G(s)$ . This shows that  $\sigma$  and  $\sigma'$  lie in the same  $p$ -block of  $C_G(s)$ .  $\square$

**2.E. Last step.** — We shall prove here the last intermediate result:

**Proposition 2.11.** — *Let  $(s, e) \in \mathcal{M}^p(G)$  and let  $(g, \gamma), (g', \gamma') \in \mathcal{B}_G(s, e)$ . Then  $(g, \gamma)$  and  $(g', \gamma')$  are in the same  $p$ -block of  $\mathcal{M}(G)$ .*

*Proof.* — We fix  $\sigma \in \text{Irr}(KC_G(s)e)$ . It is sufficient to show that  $(g, \gamma)$  and  $(s, \sigma)$  are in the same  $p$ -block of  $\mathcal{M}(G)$ . For this, let  $(h, \eta) \in \mathcal{M}(G)$ . By Proposition 2.9, we have  $g_{p'} = s$ , so  $C_G(g) \subset C_G(s)$ . So 2.6 can be rewritten:

$$\Psi_{g,\gamma}(E_{h,\eta}) = \sum_{x \in [C_G(s) \backslash G / C_G(h)]} \sum_{\substack{y \in [C_G(g) \backslash C_G(s) x C_G(h) / C_G(h)] \\ y h y^{-1} \in C_G(g)}} \eta(y^{-1} g y) \omega_{g,\gamma}(\hat{\Sigma}_g(y h y^{-1})).$$

Now, let  $x \in [C_G(s) \backslash G / C_G(h)]$  and  $y \in [C_G(g) \backslash C_G(s) x C_G(h) / C_G(h)]$  be such that  $y h y^{-1} \in C_G(g)$ . Then  $y h y^{-1} \in C_G(s)$  and so  $x h x^{-1} \in C_G(s)$ . Moreover  $y^{-1} s y$  is conjugate to  $x^{-1} s x$  in  $C_G(h)$ . Finally, it is well-known (and easy) that  $\eta(y^{-1} h y) \equiv \eta(y^{-1} s y) \pmod{\mathfrak{p}}$  (see for instance [Bo, Proposition 2.14]). Therefore:

$$(\diamond) \quad \Psi_{g,\gamma}(E_{h,\eta}) \equiv \sum_{\substack{x \in [C_G(s) \backslash G / C_G(h)] \\ x h x^{-1} \in C_G(s)}} \eta(x^{-1} s x) \omega_{g,\gamma} \left( \sum_{\substack{y \in [C_G(g) \backslash C_G(s) x C_G(h) / C_G(h)] \\ y h y^{-1} \in C_G(g)}} \hat{\Sigma}_g(y h y^{-1}) \right) \pmod{\mathfrak{p}}.$$

Now, let  $x \in [C_G(s) \backslash G / C_G(h)]$  be such that  $x h x^{-1} \in C_G(s)$ . Then, by definition of the Brauer map,

$$(\heartsuit) \quad \text{Br}_g^\theta(\hat{\Sigma}_s(x h x^{-1})) = \sum_{\substack{z \in [C_G(g) \backslash C_G(s) / (C_G(s) \cap C_G(x h x^{-1}))] \\ z(x h x^{-1}) z^{-1} \in C_G(g)}} \hat{\Sigma}_g((z x) h (z x)^{-1}).$$

But  $(z x)_{z \in [C_G(g) \backslash C_G(s) / (C_G(s) \cap C_G(x h x^{-1}))]}$  is a set of representatives of double classes in  $C_G(g) \backslash C_G(s) x C_G(h) / C_G(h)$ . So it follows from  $(\diamond)$  and  $(\heartsuit)$  that

$$\Psi_{g,h}(E_{h,\eta}) \equiv \sum_{\substack{x \in [C_G(s) \backslash G / C_G(h)] \\ x h x^{-1} \in C_G(s)}} \eta(x^{-1} s x) \omega_{g,\gamma}(\text{Br}_g^\theta(x h x^{-1})).$$

Using now 2.5 and 2.6, we obtain that

$$\Psi_{g,h}(E_{h,\eta}) \equiv \Psi_{s,\sigma}(E_{h,\eta}) \pmod{\mathfrak{p}},$$

as desired.  $\square$

*Proof of Theorem 1.2.* — Let  $(s, e)$  and  $(s', e')$  be two elements of  $\mathcal{M}^p(G)$  such that  $\mathcal{B}_G(s, e)$  and  $\mathcal{B}_G(s', e')$  are contained in the same  $p$ -block of  $\mathcal{M}(G)$  (see Proposition 2.11). Let  $\sigma \in \text{Irr}(KC_G(s)e)$  and  $\sigma' \in \text{Irr}(KC_G(s')e')$ .

Then  $(s, \sigma)$  and  $(s', \sigma')$  are in the same  $p$ -block, so it follows from Proposition 2.9 that  $s = s'$  and it follows from Proposition 2.10 that  $\gamma$  and  $\gamma'$  are in the same  $p$ -block of  $C_G(s)$ , that is  $e = e'$ . This completes the proof of Theorem 1.2.  $\square$

### References

- [Bo] C. BONNAFÉ, On the character ring of a finite group, *Publ. Math. Univ. Franche-Comté* (2006), 5-23.
- [Is] I. M. ISAACS, *Character theory of finite groups*, Pure and Applied Mathematics **69**, Academic Press, New York-London, 1976. xii+303 pp.
- [Lu] G. LUSZTIG, Leading coefficients of character values of Hecke algebras, in *The Arcata Conference on Representations of Finite Groups* (Arcata, Calif., 1986), Proc. Sympos. Pure Math. **47**, Part 2 (1987), 235-262; Amer. Math. Soc., Providence, RI, 1987.

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