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## Exciton Condensation Driving the Periodic Lattice Distortion of 1T-TiSe<sub>2</sub>

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We address the lattice deformation of 1T-TiSe<sub>2</sub> within the exciton condensate phase. We show that, at low temperature, condensed excitons influence the lattice through electron-phonon interaction. It is found that at zero temperature, in the exciton condensate phase of 1T-TiSe<sub>2</sub>, this exciton condensate exerts a force on the lattice generating ionic displacements comparable in amplitude to what is measured in experiment. This is thus the first quantitative estimation of the amplitude of the periodic lattice distortion observed in 1T-TiSe<sub>2</sub> as a consequence of the exciton condensate phase.

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In a semimetallic or semiconducting system exhibiting a small electronic band overlap or gap, the Coulomb interaction, when poorly screened, leads to the formation of bound states of holes and electrons, called excitons. If their binding energy  $E_B$  is larger than the gap, they may *spontaneously* condense at low temperature and drive the system into a new ground state with exotic properties. This new ground state, called the excitonic insulator phase, has been theoretically predicted in the 1960s [1]. Recently, we investigated the charge density wave (CDW) system 1T-TiSe<sub>2</sub> with angle-resolved photoemission spectroscopy (ARPES), favoring the excitonic insulator phase scenario as the origin of the CDW phase [2,3], as suggested earlier [4,5]. Furthermore, a superconducting phase has been discovered in this material upon copper intercalation [6] and pressure [7]. This produces a very interesting phase diagram reminiscent of the one of the iron pnictides, in the sense that a density wave phase gives way to a superconducting dome upon chemical intercalation. The nature of the competition between the ordered (CDW) phase and the superconducting dome is of central interest.

The quasi two-dimensional material 1T-TiSe<sub>2</sub> undergoes a phase transition towards a commensurate  $2 \times 2 \times 2$  CDW phase below the critical temperature  $T_c \approx 200$  K. A weak periodic lattice distortion (PLD) accompanying the CDW (which requires only electronic degrees of freedom) has been measured, involving small ionic displacements  $< 0.1$  Å [8]. The occurrence of this PLD lead Hughes to suggest a band Jahn-Teller effect as the driving force of the CDW in 1T-TiSe<sub>2</sub> [9]. In this respect, Motizuki and coworkers, based on a tight-binding (TB) fit to the band structure calculated by Zunger and Freeman [10] found that, by optimizing electronic vs elastic energy, the observed CDW is realized for an ionic displacement very close to the measured one [11]. However, the small

ionic displacements in comparison with the high spectral weight carried by the backfolded bands as observed by ARPES supports rather an electronic origin of the CDW [2].

In this perspective, it is crucial to know whether ionic displacements of a reasonable amplitude may appear at all as a consequence of exciton condensation in the low temperature phase. Here, we address this question and study the influence of an exciton condensate on the lattice.

First, we derive the electron-phonon coupling in the framework of the TB formalism. We derive a formula relating the ionic displacements to the presence of an exciton condensate, the amplitude of which is directly related to the order parameter characterizing the low temperature phase. Applying this formula to the case of 1T-TiSe<sub>2</sub>, we calculate the amplitude of ionic displacements. We find values similar to those obtained from experiment. This demonstrates that the exciton condensate phase, as a possible origin of the CDW phase of 1T-TiSe<sub>2</sub>, can also account for the PLD.

The TB formalism for the electronic band structure and the coupling to the lattice described below is similar to that developed by Yoshida and Motizuki [11,12]. It is applied to the structure of 1T-TiSe<sub>2</sub>, which consists of planes of Ti atoms forming a triangular lattice. Each of these Ti atoms is in octahedral coordination with its six neighboring Se atoms. Then the crystal consists of a regular stacking of such Se-Ti-Se layers along the  $c$  direction. For the TB calculations of the present study, a cluster of atoms centered around one Ti atom will be considered, similar to the cluster of Ref. [13]. In our calculations, for the Ti atoms, we include the five  $3d$ -orbitals of  $xy$ ,  $yz$ ,  $xz$ ,  $x^2 - y^2$  and  $3z^2 - r^2$  symmetry and the three  $4p$  orbitals for each of the two Se atoms (Se1 and Se2), of  $x$ ,  $y$  and  $z$  symmetry. In total we have 11 orbitals. The TB electronic Hamiltonian then reads

$$\begin{aligned}
H_{\text{el}} = & \sum_{l'l'} \sum_{\mu\nu} \sum_{\alpha\beta} J_{\alpha\beta}(\vec{R}_l - \vec{R}_{l'} + \vec{\tau}_\mu - \vec{\tau}_\nu) \\
& \times \sum_{\vec{k}\vec{k}'nn'} e^{-i\vec{k}\cdot\vec{R}_l} T_{\alpha\mu,n}^*(\vec{k}) e^{i\vec{k}'\cdot\vec{R}_{l'}} T_{\beta\nu,n'}(\vec{k}') c_n^\dagger(\vec{k}) c_{n'}(\vec{k}').
\end{aligned} \quad (1)$$

Here,  $\vec{R}_l, \vec{R}_{l'}$  are vectors of the Bravais lattice and  $\vec{\tau}_\mu, \vec{\tau}_\nu$  are the positions of the ions (Ti, Se1, or Se2) labeled  $\mu, \nu$  inside the unit cell. The indices  $\alpha, \beta$  label the 11 orbitals and  $n$  is the index of the bands in which the operators  $c_n^\dagger$  create electrons. The transfer matrix  $J$ , with the eigenvectors  $T$ , consists here only of two-center integrals for simplicity.

We now introduce ionic displacements of the form

$$\begin{aligned}
\vec{u}_{l\mu} = & \frac{1}{\sqrt{M_\mu}} \sum_{\vec{q},\lambda} e^{i\vec{q}\cdot\vec{R}_l} \vec{e}(\mu, \vec{q}, \lambda) Q(\vec{q}, \lambda) \\
= & \sum_{\vec{q},\lambda} e^{i\vec{q}\cdot\vec{R}_l} \vec{u}_\mu(\vec{q}, \lambda),
\end{aligned} \quad (2)$$

where  $M_\mu$  is the mass of the ion labeled  $\mu$ ,  $\vec{e}$  a polarization vector and  $Q$  the normal coordinate of the phonons. Here,  $\vec{u}_\mu(\vec{q}, \lambda)$  is the ionic displacement for the atom labeled  $\mu$  (Ti, Se1, or Se2) and associated to a particular mode  $\vec{q}, \lambda$ . Equation (2) provides us with a direct way to compute the amplitude of the displacement of each ion, once we get a value for  $Q$ . This is our goal in the next paragraphs. After introducing the small ionic displacements  $\vec{u}_{l\mu}$  in the argument of the transfer matrix  $J$  in Eq. (1), we expand  $J$  to first order in  $\vec{u}_{l\mu}$  to deduce the electron-phonon interaction

$$H_{\text{el-ph}} = \sum_{nn'} \sum_{\vec{k}, \vec{q}, \lambda} g_{nn'}(\vec{k}, \vec{q}, \lambda) c_n^\dagger(\vec{k}) c_{n'}(\vec{k} - \vec{q}) Q(\vec{q}, \lambda), \quad (3)$$

where the electron-phonon coupling constant

$$\begin{aligned}
g_{nn'}(\vec{k}, \vec{q}, \lambda) = & \sum_{\vec{\rho}} \sum_{\mu\nu} \sum_{\alpha\beta} T_{\alpha\mu,n}^*(\vec{k}) \frac{dJ_{\alpha\beta}}{d\vec{x}} \Big|_{\vec{x}=\vec{\rho}+\vec{\tau}_\mu-\vec{\tau}_\nu} \\
& \times T_{\beta\nu,n'}(\vec{k} - \vec{q}) e^{-i\vec{k}\cdot\vec{\rho}} \cdot [\vec{e}(\mu, \vec{q}, \lambda) e^{i\vec{q}\cdot\vec{\rho}} \\
& - \vec{e}(\nu, \vec{q}, \lambda)],
\end{aligned} \quad (4)$$

with  $\vec{\rho} = \vec{R}_l - \vec{R}_{l'}$ , involves the derivatives of the transfer matrix  $dJ_{\alpha\beta}/d\vec{x}$ .

In what follows, we focus on the influence of excitons. In our simplified model of the band structure of 1T-TiSe<sub>2</sub>, we essentially consider the topmost valence band having its maximum at the center of the Brillouin zone ( $\Gamma$  point) and the three symmetry equivalent conduction bands having their maximum at the border of the Brillouin zone ( $L$  points), whose extrema are separated from  $\Gamma$  by the wave vectors  $\vec{w}_i$  ( $i = 1, 2, 3$ ) [3]. These excitons are composed of holes created by  $a(\vec{k})$  in the valence band (near its maximum) with a wave vector  $\vec{k}$  and electrons created by  $b_i^\dagger(\vec{k})$  in the conduction band  $i$  (near its minimum) with wave vector  $\vec{k} + \vec{w}_i$ . Thus the sum over the

band indices  $n, n'$  in Eq. (3) is restricted to terms mixing  $a$  and  $b$  operators only, so that

$$\begin{aligned}
H_{\text{el-ph}} = & \sum_i \sum_{\vec{k}, \vec{q}, \lambda} Q(\vec{q}, \lambda) g_{ab_i}(\vec{k}, \vec{q}, \lambda) a^\dagger(\vec{k}) b_i(\vec{k} - \vec{w}_i - \vec{q}) \\
& + Q(\vec{q}, \lambda) g_{b_i a}(\vec{k}, \vec{q}, \lambda) b_i^\dagger(\vec{k} - \vec{w}_i) a(\vec{k} - \vec{q}) \\
= & \sum_i \sum_{\vec{p}, \lambda} Q(-\vec{w}_i, \lambda) g_{ab_i}(\vec{p}, -\vec{w}_i, \lambda) a^\dagger(\vec{p}) b_i(\vec{p}) \\
& + Q(\vec{w}_i, \lambda) g_{b_i a}(\vec{p} + \vec{w}_i, \vec{w}_i, \lambda) b_i^\dagger(\vec{p}) a(\vec{p}).
\end{aligned}$$

We considered only  $\vec{q} = -\vec{w}_i$  in the term involving  $g_{ab_i}$  and  $\vec{q} = \vec{w}_i$  in that involving  $g_{b_i a}$  (together with the substitution  $\vec{p} = \vec{k} - \vec{w}_i$ ), restricting ourselves to the scattering between the extrema of the bands. Then, averaging  $\langle H_{\text{el-ph}} \rangle_{\text{el}}$  to lowest order over the electronic degrees of freedom yields the contribution of condensed excitons to the phonon Hamiltonian

$$\begin{aligned}
\langle H_{\text{el-ph}} \rangle_{\text{el}} = & \sum_i \sum_{\vec{p}, \lambda} Q(-\vec{w}_i, \lambda) g_{ab_i}(\vec{p}, -\vec{w}_i, \lambda) \langle a^\dagger(\vec{p}) b_i(\vec{p}) \rangle \\
& + Q(\vec{w}_i, \lambda) g_{b_i a}(\vec{p} + \vec{w}_i, \vec{w}_i, \lambda) \langle b_i^\dagger(\vec{p}) a(\vec{p}) \rangle.
\end{aligned}$$

In analogy to the BCS-theory, the averages  $\langle b_i^\dagger a \rangle$  are related to anomalous Green's functions  $F_i(\vec{p}, \tau) = (-i) \times \langle T b_i^\dagger(\vec{p}, \tau) a(\vec{p}) \rangle$  (introduced in Ref. [3]), so that the previous equation becomes

$$\begin{aligned}
\langle H_{\text{el-ph}} \rangle_{\text{el}} = & i \sum_i \sum_{\vec{p}, \lambda} Q(-\vec{w}_i, \lambda) g_{ab_i}(\vec{p}, -\vec{w}_i, \lambda) F_i^\dagger(\vec{p}, 0) \\
& + Q(\vec{w}_i, \lambda) g_{b_i a}(\vec{p} + \vec{w}_i, \vec{w}_i, \lambda) F_i(\vec{p}, 0) \\
= & H_{\text{ph-x}}.
\end{aligned}$$

This exciton-phonon Hamiltonian  $H_{\text{ph-x}}$  can be further simplified using the inversion symmetry of the system to replace  $-\vec{w}_i$  by  $\vec{w}_i$  and using also the property  $F_i(\vec{p}, 0) = F_i^\dagger(\vec{p}, 0)$ , giving

$$\begin{aligned}
H_{\text{ph-x}} = & i \sum_{i,\lambda} Q(\vec{w}_i, \lambda) \sum_{\vec{p}} F_i(\vec{p}, 0) [g_{ab_i}(\vec{p}, \vec{w}_i, \lambda) \\
& + g_{b_i a}(\vec{p} + \vec{w}_i, \vec{w}_i, \lambda)].
\end{aligned}$$

From this last equation, the equilibrium condition for the lattice in the presence of a condensate of excitons,  $\partial(H_{\text{ph},0} + H_{\text{ph-x}})/\partial Q(\vec{w}_i, \lambda) = 0$ , leads to an expression for the normal coordinate of the phonons  $Q$  caused by the exciton condensate

$$Q(\vec{w}_i, \lambda) = \frac{i \sum_{\vec{p}} F_i(\vec{p}, 0) [g_{ab_i} + g_{b_i a}]}{\omega^2(\vec{w}_i, \lambda)}, \quad (5)$$

where  $H_{\text{ph},0} = (1/2) \sum_{i,\lambda} \omega^2(\vec{w}_i, \lambda) Q^*(\vec{w}_i, \lambda) Q(\vec{w}_i, \lambda)$  is the bare Hamiltonian of the lattice (in the absence of the exciton condensate). By using Eq. (2) we can relate  $Q$  to the resulting ionic displacements.

We now look for the necessary numerical parameters for the final computation. We start with the transfer matrix  $J_{\alpha\beta}$ . According to Slater and Koster [14], its elements are

computed as a combination of direction cosines and transfer integrals. In our case, these transfer integrals are determined by fitting a band structure computed with density functional theory (DFT). This first-principles band structure has been calculated using the full potential augmented plane wave plus local orbitals (APW + lo) method with the generalized gradient approximation in the parametrization of Perdew, Burke, and Ernzerhof [15], in the local density approximation [16]. The numerical and unit cell parameters [17,18] are similar to those used in Ref. [19].

The resulting DFT band structure is plotted in Fig. 1. The goal of this DFT calculation (such a DFT band structure is discussed in detail in Refs. [19]) is to offer a basis for the TB fit we perform for determining the transfer integrals. A least-square fit method was used on our DFT band structure along the high symmetry directions  $\Gamma MK\Gamma A$  and the obtained transfer integrals are summarized in Table I [21]. The TB fit of the DFT band structure is good for states below the Fermi energy  $E_F$  but becomes poor for states above  $E_F$ . This TB parametrization allows us to build an effective Hamiltonian which can be diagonalized (at each  $\vec{k}$  point) to provide the eigenvectors  $T_{\alpha\mu,n}(\vec{k})$ . The derivatives of the transfer matrix  $dJ_{\alpha\beta}/d\vec{x}$ , appearing in the electron-phonon coupling  $g_{nn'}(\vec{k}, \vec{q}, \lambda)$ , lead to derivatives of the direction cosines and derivatives of the transfer integrals. The latter are evaluated as in Ref. [12] and are also listed in Table I. They have a strong influence on the final result.

According to the experimental result of Di Salvo *et al.* [8], we fix the phonon polarization vectors  $\vec{e}(\mu, \vec{q}, \lambda)$  involved in the CDW to the direction perpendicular to their respective  $\vec{q}$  vector, lying in the  $ab$  basal plane. This way, only the transverse phonon mode  $\lambda_{tr}$  will be considered in the following calculations.

The anomalous Green's function  $F_i(\vec{p}, \tau = 0)$  appearing in Eq. (5) is calculated as the Fourier transform of  $F_i(\vec{p}, z)$  given by (see Ref. [3])

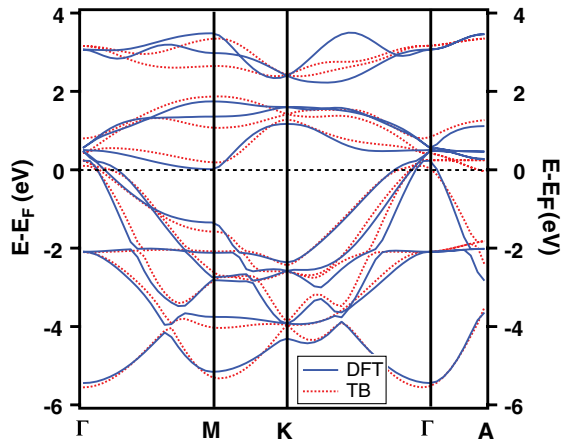


FIG. 1 (color online). Comparison of the band structure of 1T-TiSe<sub>2</sub> calculated with density functional theory and its fit within a TB approach.

$$F_i(\vec{p}, z) = - \frac{\Delta[z - \epsilon_c^{i+1}(\vec{p} + \vec{w}_{i+1})][z - \epsilon_c^{i+2}(\vec{p} + \vec{w}_{i+2})]}{\mathcal{D}(\vec{p}, z)}$$

(the index  $i$  runs cyclically over  $i = 1, 2, 3$ ) with the denominator being

$$\mathcal{D}(\vec{p}, z) = [z - \epsilon_v(\vec{p})] \prod_i [z - \epsilon_c^i(\vec{p} + \vec{w}_i)] - \sum_i |\Delta|^2 \prod_{j \neq i} [z - \epsilon_c^j(\vec{p} + \vec{w}_j)].$$

Here, the order parameter  $\Delta$  describes the intensity of the exciton condensate in the low temperature phase. The functions  $\epsilon_v$  and  $\epsilon_c^i$  describe the dispersions of the valence band and of the three conduction bands ( $i = 1, 2, 3$ ), respectively. The anomalous Green's function  $F_i$  is sensitive to the energies appearing in these dispersions near their extrema. We therefore cannot use the TB dispersions, which are too rough with this respect (however they are essential for the more global treatment needed to obtain the transfer integrals), but we need the formulas for  $\epsilon_v$  and  $\epsilon_c^i$  determined in a previous study from fits to ARPES data [2].

Finally, combining Eqs. (2) and (5), the amplitude of the ionic displacement for a single  $\vec{w}_i$  (and for transverse phonons) gets the following form

$$u_\mu(\vec{w}_i, \lambda_{tr}) = \frac{1}{\sqrt{M_\mu}} \frac{|\sum_{\vec{p}} F_i(\vec{p}, 0)[g_{ab_i} + g_{b_i a}]|}{\omega^2(\vec{w}_i, \lambda_{tr})}. \quad (6)$$

We now focus to the particular case of the Ti atoms, so that  $M_{Ti}$  describes the Ti atom mass. For the order parameter appearing in the anomalous Green's function, we consider a mean-field like temperature dependence of the form  $\Delta(T) = \Delta_0 \sqrt{1 - (T/T_c)^2}$  with  $T_c = 200$  K, where the zero value  $\Delta_0 = 115$  meV has been determined in our recent temperature dependent ARPES study [23]. In formula (6), we use a value of  $\omega(\vec{w}_i, \lambda_{tr}) = 6.3$  THz. In fact, it is the value estimated by Holt *et al.* at  $T \approx 150$  K for the transverse phonon mode, which softens at  $L$  at the transition [24]. This corresponds to a situation where the ionic displacement  $\vec{u}_{i\mu}$  is not too large, such that our first order

TABLE I. Transfer integrals (in eV) for 1T-TiSe<sub>2</sub>, obtained from TB fits to first-principles band structure [20]. Their derivatives (in eV/Å) are also shown in parenthesis.  $\epsilon_p = -2.0$  eV,  $\epsilon_{de} = 0.74$  eV,  $\epsilon_{d\gamma} = 1.2$  eV are the orbital energies. The same notation as in Ref. [12] is used. Indices 2 and 3 refer to Se-Se transfer integrals across the van der Waals gap and for second nearest neighbors in the same TiSe<sub>2</sub> layer, respectively.

Transf. Int. (Deriv.)		Transf. Int. (Deriv.)	
$t(pp\sigma)$	0.77 (-2.0)	$t(pd\pi)$	0.70 (-1.5)
$t(pp\pi)$	-0.054 (0.21)	$t(pp\sigma)_2$	0.63 (-1.6)
$t(dd\sigma)$	-0.35 (0.40)	$t(pp\pi)_2$	-0.028 (0.11)
$t(dd\pi)$	0.074 (-0.17)	$t(pp\sigma)_3$	0.61 (-1.5)
$t(dd\delta)$	-0.049 (0.18)	$t(pp\pi)_3$	-0.096 (0.37)
$t(pd\sigma)$	1.3 (0.83)		

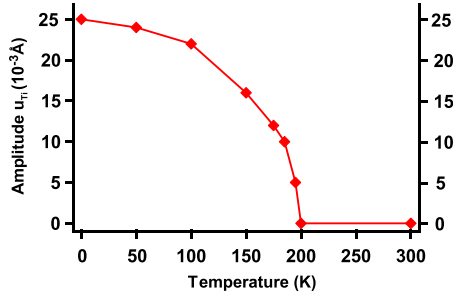


FIG. 2 (color online). Amplitude of the Ti ionic displacement for a single  $\vec{w}_i$ ,  $u_{Ti}(\vec{w}_i, \lambda_{tr})$  (the diamonds show the calculated values).

development of the electron-phonon coupling remains valid. Furthermore, the region close to  $T_c$  is avoided, where anharmonicities cannot be neglected in the bare Hamiltonian for the lattice  $H_{ph,0}$ .

Now all the necessary quantities to compute the amplitude of the ionic displacements in Eq. (6) are known. Figure 2 summarizes our numerical results. It shows a clear temperature dependence, following closely the behavior of the order parameter. Extrapolated to the lowest temperature, it reaches the value of  $u_{Ti}^{theo}(\vec{w}_i, \lambda_{tr}) = 0.025 \text{ Å}$ . Di Salvo *et al.* inferred from neutron diffraction experiments a displacement (also for a single- $\vec{w}_i$ ) of about  $u_{Ti}^{exp}(\vec{w}_i, \lambda_{tr}) = 0.04 \text{ Å}$  at 77 K [8]. Therefore our value, although being about 60% of the experimental one, reproduces the measured ionic displacement for Ti atoms within the correct order of magnitude, which is a substantial result, considering the approximations made in this calculation. The uncertainty on  $\omega(\vec{w}_i, \lambda_{tr})$  used in Eq. (6) may enhance or reduce this value by a factor of 2–3, but it still remains within the correct order of magnitude, in agreement with the main message of this letter.

In conclusion, we addressed the question of the appearance of a periodic lattice distortion in  $1T$ -TiSe<sub>2</sub>. Previously we gave strong support for the exciton condensation as a purely electronic mechanism responsible for the CDW phase in this material [2,3]. In this work, we elaborate in a tight-binding formalism a formula for estimating the ionic displacements produced by the presence of this exciton condensate through the electron-phonon coupling. The calculated amplitude of these ionic displacements is, at low temperature, of the same order of magnitude as what is experimentally found. This is thus the first quantitative estimation of the amplitude of the PLD observed in  $1T$ -TiSe<sub>2</sub> as a *consequence* of the exciton condensate phase. More generally, this result describes quantitatively how an excitonic insulator phase can give rise to a PLD through electron-phonon interaction.

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