

Stability margins and model-free control: A first look

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Abstract—We show that the open-loop transfer functions and the stability margins may be defined within the recent model-free control setting. Several convincing computer experiments are presented including one which studies the robustness with respect to delays.

Keywords— Stability margins, phase margins, gain margins, model-free control, intelligent PID controllers, linear systems, nonlinear systems, delay systems.

I. INTRODUCTION

Stability margins are basic ingredients of control theory. They are widely taught (see, e.g., [1], [2], [9], [10], [11], [16], and the references therein) and are quite often utilized in industry in order to check the control design of plants, or, more exactly, of their mathematical models. The importance of this topic is highlighted by the following fact: the literature on theoretical advances and on the connections with many case-studies contains several thousands of publications! This communication relates stability margins to the recent *model-free* control and the corresponding *intelligent* PIDs [4], which were already illustrated by many concrete and varied applications (see, e.g., the numerous references in [4], and, during the last months, [3], [14], [17], [19], [20], [21], [24], [29], [30]).

Remark 1.1: Let us emphasize that our model-free control design and the corresponding intelligent controllers are most easily implementable (see [4], [12]).

Our aims are the following ones:

- 1) Practitioners of stability margins and other frequency techniques will recognize that their expertise still makes sense within model-free control.
- 2) The influence of delays in model-free control is analyzed for the first time.

Let us briefly explain our viewpoint. Take a monovariable system which is governed by unknown equations. Consider the *ultra-local* model [4]

$$\dot{y} = F + \alpha u \quad (1)$$

where

- u and y are respectively the input and output variables,

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- F subsumes the unknown parts, including the perturbations,
- α is a constant parameter which is chosen by the engineer in such a way that αu and \dot{y} are of the same magnitude.

Remember that Equation (1) applies not only to systems with lumped parameters, *i.e.*, to systems which are described by ordinary differential equations of any order, but also to systems with distributed parameters, *i.e.*, to partial differential equations (see, e.g., [13]). Close the loop with

$$u = \frac{-F_{\text{est}} + \dot{y}^* + \mathfrak{F}}{\alpha} \quad (2)$$

such that

- F_{est} is a realtime estimate of F (see Section II-C),
- y^* is a reference trajectory,
- the closed loop system is

$$\dot{e} + \mathfrak{F} = F_{\text{est}} - F \quad (3)$$

where $e = y^* - y$ is the tracking error,

- \mathfrak{F} is either a proportional controller

$$\mathfrak{F} = K_P e \quad (4)$$

or, sometimes, a proportional-integral controller

$$\mathfrak{F} = K_P e + K_I \int e \quad (5)$$

such that

$$\dot{e} + \mathfrak{F} = 0 \quad (6)$$

exhibits the desired asymptotic stability. For instance K_P in Equation (4) should be positive.

Equations (4)-(6) and (5)-(6) yield the usual open-loop transfer functions

$$T_{1OLP} = \frac{K_P}{s} \quad (7)$$

and

$$T_{1OLPI} = \frac{1}{s} \times \left(K_P + \frac{K_I}{s} \right) = \frac{K_P}{s} + \frac{K_I}{s^2} \quad (8)$$

Their *gain* and *phase margins* are by definitions those of the systems defined by Equations (7) and (8). Note that $F_{\text{est}} - F$ in Equation (3) should be viewed as an additive disturbance.

Our paper is organized as follows. Basics of model-free control are briefly revisited in Section II. Section III computes some open loop functions for iPID's, iPD's, iPIs, iPs as well as the corresponding stability margins. Several computer experiments are examined in Section IV, including the robustness with respect to delays. Concluding remarks are developed in Section V.

II. MODEL-FREE CONTROL: A SHORT REVIEW¹

A. The ultra-local model

Introduce the *ultra-local model*

$$\boxed{y^{(\nu)} = F + \alpha u} \quad (9)$$

where

- the order $\nu \geq 0$ of derivation is a non-negative integer which is selected by the practitioner,²
- $\alpha \in \mathbb{R}$ is chosen by the practitioner such that αu and $y^{(\nu)}$ are of the same magnitude,
- F represents the unknown structure of the control system as well as the perturbations.

B. Intelligent controllers

1) *Generalities*: Close the loop with respect to Equation (9) via the *intelligent controller*

$$u = \frac{-F_{\text{est}} + y^{*(\nu)} + \mathfrak{F}(e)}{\alpha} \quad (10)$$

where

- F_{est} is a realtime estimate of F ,
- y^* is the output reference trajectory,
- $e = y^* - y$ is the tracking error,
- $\mathfrak{F}(e)$ is a functional of e such that the closed-loop system

$$e^{(\nu)} + \mathfrak{F}(e) = F_{\text{est}} - F \quad (11)$$

exhibits a desired behavior. If, in particular, the estimation is perfect, *i.e.*, $F_{\text{est}} = F$, then

$$e^{(\nu)} + \mathfrak{F}(e) = 0 \quad (12)$$

should be asymptotically stable, *i.e.*, $\lim_{t \rightarrow +\infty} e(t) = 0$.

2) *Intelligent PIDs*: If $\nu = 2$ in Equation (9), *i.e.*,

$$\boxed{\ddot{y} = F + \alpha u} \quad (13)$$

Close the loop via the *intelligent proportional-integral-derivative controller*, or *iPID*,

$$\boxed{u = \frac{-F_{\text{est}} + \ddot{y}^* + K_P e + K_I \int e + K_D \dot{e}}{\alpha}} \quad (14)$$

where K_P , K_I , K_D are the usual tuning gains. Combining Equations (13) and (14) yields

$$\ddot{e} + K_D \dot{e} + K_P e + K_I \int e = F_{\text{est}} - F$$

$K_I = 0$ in Equation (14) yields the *intelligent proportional-derivative controller*, or *iPD*,

$$\boxed{u = \frac{-F_{\text{est}} + \ddot{y}^* + K_P e + K_D \dot{e}}{\alpha}} \quad (15)$$

Such an iPD was employed in [3].

¹See [4] for more details.

²The existing examples show that ν may always be chosen quite low, *i.e.*, 1, or 2. Most of the times $\nu = 1$. The only concrete example until now with $\nu = 2$ is provided by the magnetic bearing [3], where the friction is negligible (see the explanation in [4]).

If $\nu = 1$ in Equation (9), we recover Equation (1). The loop is closed by the *intelligent proportional-integral controller*, or *iPI*,

$$\boxed{u = \frac{-F_{\text{est}} + \dot{y}^* + K_P e + K_I \int e}{\alpha}}$$

K_I may often be set to 0. It yields the *intelligent proportional controller*, or *iP*,

$$\boxed{u = -\frac{-F_{\text{est}} + \dot{y}^* + K_P e}{\alpha}}$$

C. Estimation of F

Assume that F in Equation (9) may be “well” approximated by a piecewise constant function F_{est} . According to the algebraic parameter identification developed in [7], [8], rewrite, if $\nu = 1$, Equation (1) in the operational domain (see, *e.g.*, [31])

$$sY = \frac{\Phi}{s} + \alpha U + y(0)$$

where Φ is a constant. We get rid of the initial condition $y(0)$ by multiplying both sides on the left by $\frac{d}{ds}$:

$$Y + s \frac{dY}{ds} = -\frac{\Phi}{s^2} + \alpha \frac{dU}{ds}$$

Noise attenuation is achieved by multiplying both sides on the left by s^{-2} . It yields in the time domain the realtime estimate

$$F_{\text{est}}(t) = -\frac{6}{\tau^3} \int_{t-\tau}^t ((\tau - 2\delta)y(\delta) + \alpha\delta(\tau - \delta)u(\delta)) d\delta$$

where $\tau > 0$ might be “small”.

Remark 2.1: As in our first publications on model-free control, $F_{\text{est}}(t)$ might also be obtained by estimating the noisy derivative of y (see [5], and [18], [15]).

III. OPEN-LOOP TRANSFER FUNCTIONS

A. Definitions

Assume that in Equation (10) \mathfrak{F} may be defined by a transfer function $T_{\mathfrak{F}}$. Then Equation (12) yields the transfer function

$$T_{\nu OL} = \frac{T_{\mathfrak{F}}}{s^\nu} \quad (16)$$

which is called the *open-loop transfer function* of the system defined by Equations (9) and (10). If $\nu = 2$, and with an iPID, the open-loop transfer function (16) of the system defined by Equations (13) and (14) becomes

$$\boxed{T_{2OLPID} = \frac{K_P}{s^2} + \frac{K_I}{s^3} + \frac{K_D}{s}} \quad (17)$$

It becomes for an iPD:

$$\boxed{T_{2OLPD} = \frac{K_P}{s^2} + \frac{K_D}{s}} \quad (18)$$

If $\nu = 1$, and with an iPI, the open-loop transfer function of the system defined by Equations (1) and (4) or (5), the corresponding open-loop transfer functions were already given by Equations (7) and (8).

Remark 3.1: Notice that T_{1OLPI} and T_{2OLPID} are expressed by Formulae (8) and (18), which are identical if we exchange K_P, K_I with K_I, K_D .

B. Stability margins

1) *iP*: Setting $s = j\omega$ in Equation (7), where

- ω is a non-negative real number,
- $j = \sqrt{-1}$,

gives $T_{1OLP}(j\omega) = \frac{K_P}{j\omega} = -j\frac{K_P}{\omega}$. Since $K_P > 0$ and $\omega \geq 0$, we obtain the following margins:

$$\text{PhaseMargin}_{1OLP} = 90^\circ$$

and

$$\text{GainMargin}_{1OLP} = +\infty$$

2) *iPI*: Setting as above $s = j\omega$ in Equation (8) yields a complex quantity where the imaginary part is $-j\frac{K_P}{\omega}$. Therefore

$$\text{GainMargin}_{1OLPI} = +\infty$$

and

$$\text{PhaseMargin}_{1OLPI} = \tan^{-1}\left(\frac{K_P\omega_m}{K_I}\right)$$

where

$$\omega_m = \sqrt{\frac{K_P^2 + \sqrt{K_P^4 + 4K_I^2}}{2}}$$

is such that the module of T_{1OLPI} is equal to 1. A phase margin of 45° , for instance, is obtained by setting

$$\omega_m = \frac{K_I}{K_P}$$

K_P and K_I are then related by the equation

$$\frac{K_I}{K_P} = \sqrt{\frac{K_P^2 + \sqrt{K_P^4 + 4K_I^2}}{2}}$$

3) *iPD*: It suffices according to Remark 3.1 to replace, in the expressions related to the *iPI*s in Section III-B.2, K_P and K_I respectively by K_D and K_I .

4) *iPID*: It follows from Equation (17) that the stability margins necessitates here the famous Cardano formulae which give the roots of third degree algebraic equations (see, e.g., [28]). A single root is moreover real. Then

$$\text{GainMargin}_{2OLPID} = \frac{K_I}{K_D K_P}$$

and

$$\text{PhaseMargin}_{2OLPID} = \tan^{-1}\left(\frac{K_D\omega_m^2 - K_I}{K_P\omega_m}\right)$$

where

$$\omega_m = \sqrt{A + \frac{B}{C} + D}$$

A, B, C, D are given by

$A =$

$$\begin{aligned} & \left(\frac{K_I^2}{2} + \frac{K_P^6}{27} - \frac{K_P^2(2K_I K_P - K_D^2)}{6}\right)^{2/6} \\ & - \left(\frac{K_D^2}{3} + \frac{K_P^4}{9} - \frac{2K_I K_P}{3}\right)^{3/6} \\ & + \left(\frac{K_I^2}{2} + \frac{K_P^6}{27} - \frac{K_P^2(2K_I K_P - K_D^2)}{6}\right)^{1/3} \end{aligned}$$

$$B = \frac{K_D^2}{3} + \frac{K_P^4}{9} - \frac{2K_I K_P}{3}$$

$C =$

$$\begin{aligned} & \left(\frac{K_I^2}{2} + \frac{K_P^6}{27} - \frac{K_P^2(2K_I K_P - K_D^2)}{6}\right)^{2/3} \\ & - \left(\frac{K_D^2}{3} + \frac{K_P^4}{9} - \frac{2K_I K_P}{3}\right)^{1/6} \\ & + \left(\frac{K_I^2}{2} + \frac{K_P^6}{27} - \frac{K_P^2(2K_I K_P - K_D^2)}{6}\right)^{1/3} \end{aligned} \quad (19)$$

$$D = \frac{K_P^2}{3}$$

Remark 3.2: Since model-free control encompasses to some extent nonlinear control, the above calculations yield a kind of nonlinear generalization of stability margins (see Section IV-A). Remember that the stability margins for nonlinear systems have been studied in a number of publications (see, e.g., [25]).

IV. NUMERICAL ILLUSTRATIONS

The equations of the systems considered below are only given for achieving of course computer simulations.

A. A nonlinear academic example

1) *Description and control*: Consider the stable single-input single-output system

$$\ddot{y} + 4\dot{y} + 3y = 3\dot{u}^2 + 2u^3 \quad (20)$$

Our ultra-local model is

$$\dot{y} = F + u \quad (21)$$

i.e., $\nu = 1, \alpha = 1$ in Equation (9). We employ the *iP* controller (4) where $K_P = 1$. The gain and phase margins are given by Section III-B.1, as in many concrete systems.

2) *Some computer experiments*: According to the above control scheme, a “good” estimation of F in Equation (21) plays a key rôle. Equations (20) and (21) yield the following expression which is used for comparison’s sake.

$$F = \frac{3\dot{u}^2 + 2u^3 - 4u - \dot{y} - 3y}{4}$$

Figure 1 displays excellent results with a sampling time interval $T_{\text{est}} = 0.01\text{s}$ for estimating F .³ The results shown in

³ $T_{\text{est}} = 0.01\text{s}$ is also equal to the sampling time period.

Figures 2 and 3 are respectively obtained for $T_{\text{est}} = 1\text{ s}$ and $T_{\text{est}} = 10\text{ s}$. The damages are visible. Figure 3 demonstrates that the results with $T_{\text{est}} = 10\text{ s}$ cannot be exploited in practice.

Remark 4.1: Let us emphasize that corrupting noises are neglected here for simplicity's sake.

B. A linear academic case

1) *Description and control:* Consider the unstable single-input single-output linear system

$$2\dot{y} - 3y = u \quad (22)$$

Equation (21) is again used as an ultra-local model. The loop is closed via the iP controller (4) with some suitable gain K_P . As above, in Section IV-A.1, the gain and phase margins are given by Section III-B.1. Stability is therefore ensured with a good robustness. Figure 4 displays simulations with $K_P = 1$, a sampling time period $T_e = 0.01\text{ s}$, and an additive Gaussian corrupting noise $N(0, 0.03)$ on the output. The trajectory tracking is excellent.

2) *Robustness with respect to a delayed control:* Introduce a time lag τ in the control transmission. The transfer function of (22) is no more

$$\frac{1}{2s - 3}$$

but

$$\frac{e^{-\tau s}}{2s - 3}$$

Remark 4.2: Such delays, which might occur in practice, have already been studied in the literature (see, e.g., [22], [23], [27]).

Remark 4.3: Systems with transfer functions of the form

$$T(s)e^{-\tau s}$$

where $T \in \mathbf{R}(s)$ is a rational function, are according to [6] the most usual linear delay single-input single-output systems. It is also well known that they are used for approximating “complex” nonlinear systems without delays (see, e.g., [26]). It has been emphasized in [4] that such approximations are becoming useless when applying model-free control design.

Assume that we are doing the same computations as in Section IV-B.1, and, in particular, that F is estimated with the techniques presented in Section II-C. It amounts saying that we are in fact replacing Equation (21) by

$$y(t) = F + u(t - \tau)$$

The open loop transfer function becomes therefore

$$T_{1\tau OLP} = \frac{K_P e^{-\tau s}}{s}$$

Solving the equation

$$T_{1\tau OLP}(j\omega) = -1$$

yields

$$\tau_{\max} = \frac{\pi}{2K_P}$$

i.e., the maximum admissible time lag for stability.

3) *Computer experiments with delay:* Figure 5 displays an excellent stability obtained with a time lag $\tau = 0.2\text{ s}$ and $K_P = 1$. Then $\tau_{\max} \simeq 1.57\text{ s}$.

With the “high” gain $K_P = 10$, $\tau_{\max} \simeq 0.16\text{ s}$. Stability is then lost as shown by Figure 6.

V. CONCLUSION

We have demonstrated that the calculations related to stability margins may be easily extended to our recent model-free techniques, where they provide some new insight on the robustness with respect to delays. As already discussed in [4], delays, which remain one of the most irritating questions in the model-free setting, do necessitate further investigations.⁴ The key point nevertheless in order to ensure satisfactory performances is in our opinion a “good” estimate of F . This question, which

- has been summarized in Section II-C,⁵
- might become difficult with very severe corrupting noises and/or a poor time sampling,

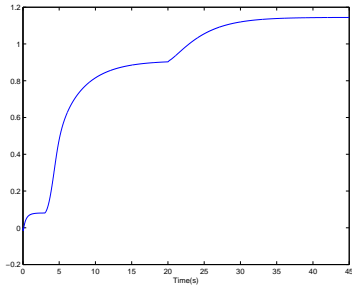
seems unfortunately to be far apart from the stability margins techniques.

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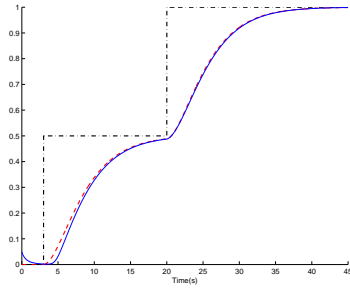
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⁴See also [13].

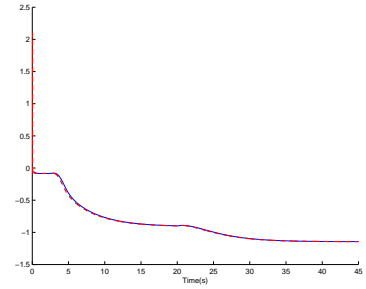
⁵The introduction lists the references of many successful concrete examples.



(a) Control

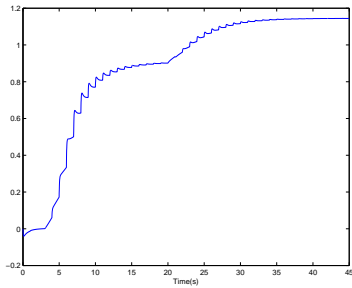


(b) Setpoint (- -, black), Reference (- -, red) and Output (-, blue)

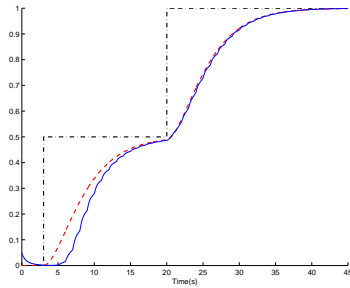


(c) F (- -, red) and F_{est} (-, blue)

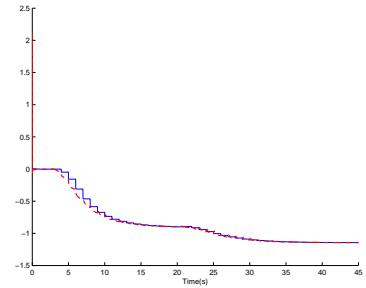
Fig. 1: $T_{est} = 0.01s$



(a) Control

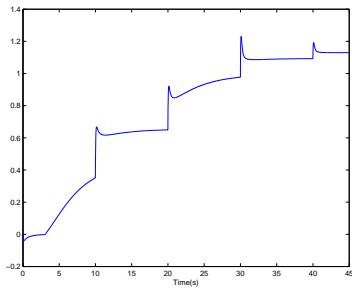


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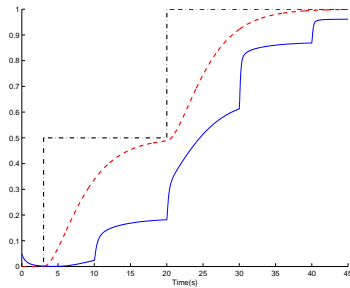


(c) F (- -, red) and F_{est} (-, blue)

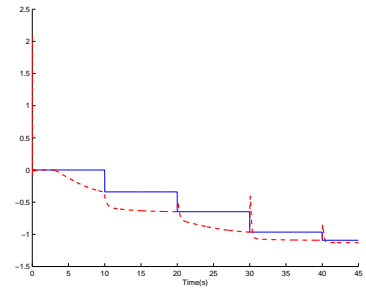
Fig. 2: $T_{est} = 1s$



(a) Control



(b) Setpoint (- -, black), Reference (- -, red) and Output (-, blue)



(c) F (- -, red) and F_{est} (-, blue)

Fig. 3: $T_{est} = 10s$

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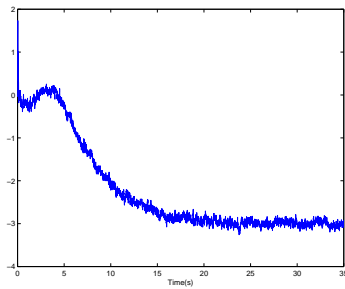
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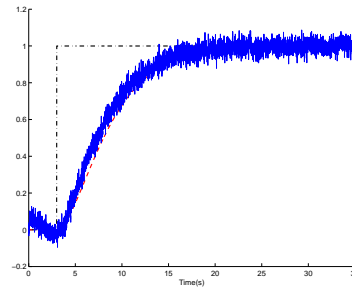
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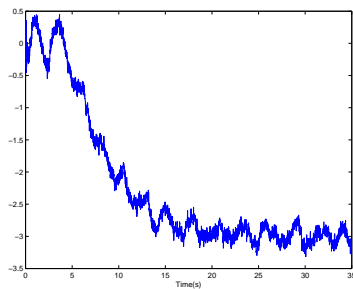


(a) Control

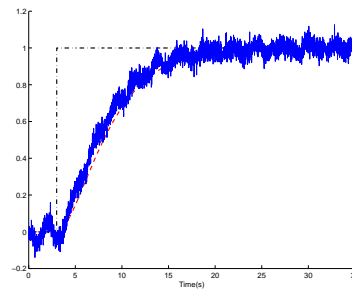


(b) Setpoint (-., black), Reference (- -, red) and Output (-, blue)

Fig. 4: Delay free

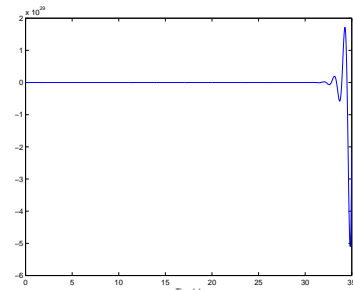


(a) Control

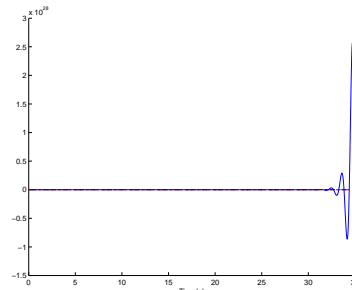


(b) Setpoint (-., black), Reference (- -, red) and Output (-, blue)

Fig. 5: Delayed control – $K_P = 1$



(a) Control



(b) Setpoint (-., black), Reference (- -, red) and Output (-, blue)

Fig. 6: Delayed control – $K_P = 10$

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