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Original article

Choosing simplified mixed models for simulations when data have a complex hierarchical organization. An example with some basic properties in Sessile oak wood (*Quercus petraea* Liebl.)

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Abstract – This paper focuses on the modeling of the variability of some properties in Sessile oak wood (five swelling coefficients and wood density). They are modeled with linear mixed models. The data have a seven-levels hierarchical organization. The variability at each level is modeled with a variance matrix. Unfortunately, a model with all variances has too many parameters to be usable, so preferably only one variance other than the residual is kept. A graphical procedure based on the comparison of residual variance in the different candidate models is used to detect this main level. Result shows that the main level of variability is the "tree" level or the "height within tree" level for five properties. We cannot conclude for the last property. For other properties, the residual variance in the model with a "tree effect" is reduced to 40% of the residual variance of the model without structuring of variability. If the applications of models deal with the variability of properties, this "tree level" cannot be neglected.

linear mixed model / Sessile oak / structuring of variability / "tree" effect

Résumé – Simplifier un modèle mixte destiné à effectuer des simulations lorsque les données ont une structure hiérarchique complexe. Exemple de quelques propriétés de base du bois de Chêne sessile (*Quercus petraea* Liebl.). Cet article traite de la modélisation de la variabilité de propriétés du bois de Chêne sessile (cinq coefficients de gonflement et la densité du bois). Ces propriétés sont modélisées à l'aide de modèles linéaires mixtes. Les données ont une organisation hiérarchique à sept niveaux. La variabilité à chacun de ces niveaux est modélisée par une matrice de variance. Cependant, le modèle avec toutes les variances comprend trop de paramètres pour être utilisable, aussi le choix est fait de ne tenir compte que d'une seule variance en plus de la variance résiduelle. On utilise une procédure graphique basée sur la comparaison des variances résiduelles des différents modèles candidats pour détecter le niveau principal de la variabilité. Ce niveau principal est ainsi le niveau « arbre » ou le niveau « hauteur dans l'arbre » pour cinq des propriétés. On ne peut pas conclure pour la sixième. Pour toutes les autres propriétés, la prise en compte d'un effet arbre permet de réduire la variance résiduelle à 40 % de la valeur obtenue dans un modèle sans structuration de la variabilité. Si la variabilité des propriétés est un facteur important pour les applications des modèles, ce niveau « arbre » ne peut pas être négligé.

modèle linéaire mixte / Chêne sessile / structuration de la variabilité / effet « arbre »

1. INTRODUCTION

Sessile and Pedunculate oaks (*Quercus petraea* Liebl. and *Q. robur* L.) predominate in the French forest resource (32% of the forest area is dominated by these two species). They occur in a large range of ecological situations, from the

Atlantic coast (mild climate) to the eastern borders (semi-continental climate), and from fresh valleys to dry south slopes as well as on a large range of parent bedrocks [18]. Pedunculate oak is more specialized in favourable site conditions [3] but, due to its pioneer habit, it is commonly present in under-optimal sites. Sessile oak has more pronounced characteristics of a social species, and can afford

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high levels of competition: therefore, it is widely tended according to the high forest regime. Pure, even-aged high forests of Sessile oak have been managed very precautiously for decades, and they provide now the best quality assortments (slow-grown trees, with long boles, "finely-grained" timber with light colour and low density, used for veneer, barrels, furniture). Nevertheless, the major part of the resource in both oaks is composed of coppice-with-standards (CwS) systems, i.e. stands inherited from past practices of coppicing, while keeping a low number of standards (20 to 100 large oaks per hectare). These standards differ markedly from high-forest-grown oaks: faster growth, shorter boles, and lower quality. Private owners, who cannot afford the very long rotations of public forests (180 to 250 years), more and more, favour semi-intensive management of oaks (by the CwS system or by enhancing future crop tree growth in high forest regimes). For these reasons, there is an increasing need for integrated simulation models, providing detailed outputs in terms of stand yield, tree growth and the main quality criteria, including log grading [15].

Oak-based ecosystems are also particularly important for other functions than just yield: structuring of landscapes, species and ecosystem conservation (associated broadleaves in the understorey), biodiversity [19], conservation of genetic diversity [21]. In the perspective of future climate change, forest managers anticipate that especially Sessile oak might play a crucial role, due to its well-known drought-tolerance. Furthermore, recent studies have shown that the productivity of oaks has steadily increased over the past century [4, 7]: the possible nutritional deficiencies that might occur (especially on poor soils) are of particular importance for forest managers and forest policy-makers.

In these multiple regards, it seems important to maintain a sufficient degree of genetic variability in oak stands, in order to preserve the adaptive capacities present in the natural populations. But this management objective, in turn, requires a better knowledge of tree-to-tree variability, at all levels of management: regional resource evaluation, forest planning methods, stand silvicultural projections. In the past years, advances in growth modeling made it possible to simulate Sessile oak stand dynamics under contrasted site-silviculture conditions [16]. Although there is still much individual-tree growth variation, which is not accounted for by the model, we have thought preferable to concentrate first on the tree-to-tree variability for wood quality features (namely wood density and behavior of timber during drying). Indeed, previous work by Polge and Keller [17] had shown that (i) silviculture strongly influences the properties of oak wood (larger rings are associated with higher density), and (ii) the density variation between trees within a stand is very large.

In this paper we present an analysis of the structuring of variability for some important wood characteristics of Sessile oak: five swelling coefficients and the wood density. This variability is a major problem to suitably model the properties. Zhang et al. [22] showed that inter-tree variation represents a large part of the total variation in Sessile oak, but they did not take into account other potential sources of variability as the applied silviculture or site growth conditions. Therefore, we have to study the structuring of the variability before taking it into account.

Between 1992 and 1995, an important research programme was undertaken, with the objectives of describing and modeling the variability of Sessile oak growth, morphology and wood quality, based on appropriate sampling plans and use of available statistical methods (mixed models). This programme associated the Office National des Forêts (French Forestry Office) and our research teams at INRA-Champenoux, working in the fields of growth and yield, silviculture and wood science. The main aspect of this Project was the constitution and analysis of a large collection (82) of commercial-size Sessile oaks, covering the major sources of variability which are present in the species: regional populations (ranging from Normandy to Alsace), site qualities (except on calcareous bedrocks, where the dry sites occupied by oaks can hardly provide large diameters), silvicultural systems (coppice-with-standards and high forest). These 82 trees were intensively described: stem analyses, mapping of annual rings and sapwood-heartwood, measurement of several wood quality criteria (density, swelling, colour, spiral grain, multiseriate wood rays) on both standard small-size samples and industrial-size boards.

Our data have a hierarchical organization. Each level of the hierarchy could be a level of structuring of the variability. This paper studies the decomposition of the variability through the different levels of hierarchy. If possible, the best model should take into account all the significant levels of variability. But such a complex model is too complicated to be useful for further simulations, so that only the main levels have to be retained.

This paper studies the evolution of the variability through the different levels of the hierarchy, in order to detect the main level of variability to be included in a model relevant for use in simulations, and thus to obtain a good compromise between the heaviness and efficiency of the model.

2. MATERIALS, SAMPLING AND MEASUREMENTS

The sample used here is a collection of 82 mature Sessile oak trees (*Quercus petraea* Liebl.). It was designed in order to answer two series of questions:

 describe and model the dynamics of stem taper and the distribution of sapwood inside the tree; study the local effect of ramifications; analyse the variation of these phenomenons when trees differ by the general vigour and morphology;

- model the variability of local wood properties (density, swelling, color, spiral grain, multiseriate wood rays) as functions of position inside the tree (age from the pith, vertical level) and ring width.

The principles of the sampling plan were, on the one hand, to explore a large range of growth rates and stem morphologies, on the other hand, to cover most of the sources of variability that are encountered in the geographical area of the species distribution.

2.1. Tree selection

The sample is divided into 5 regions of contrasted climates: north of Alsace (sandstone hills and sandy-loamy soils in the plain), Plateau lorrain, Val de Loire, Basse-Normandie, Allier-Bourbonnais (Center of France). In each region, a large range of site quality was represented. In each combination (region \times site), stands belonging to two types of structure were prospected: usual high forest, coppice-with-standards.

Site quality was determined from an inventory of ground vegetation and the analysis of a soil core (1 m deep). The soil descriptions (nutrient richness and water regime) were summarized in each region and classified into 3 categories: good, medium and poor site quality, using expert knowledge of Sessile oak autecology [3].

In each family (region-site-structure), one or two stands were selected, containing a sufficient number of oaks larger than 40 cm in diameter. In each stand, two trees were chosen (occasionally only one tree, especially on very poor, humid sites where the mixture with Pedunculate oak was a problem), at distances of 30 to 200 m from each other. The site diagnostic was done at the proximity of preselected trees; the choice was revised until soil conditions were reasonably similar for the 2 trees of the same stand.

For tree selection, we looked for dominant (eventually codominant) individuals of "standard" quality, i.e. not excellent, but representative of the population that would be kept by silviculturists until the final harvest. Defects like leaning stems, basal curvature, excessive grain angle, frost cracks, abundant epicormics were rejected.

More detailed description of the sampling can be found in [8].

2.2. Wood sample preparation and measurement

On each tree, a disk has been taken at breast height (1-height) and another at half-height between breast height and the crown basis (2-height) for 52 trees.

From each disk, the radius with the biggest length from the pith to the bark and its opposite were cut (respectively called 1- and 5-stripe).

Sixteen-mm-sized cubes were cut from these stripes when air-dried. They were cut within areas exhibiting an homogeneous ring width and oriented according to the three orthotropic directions of wood (longitudinal, radial and tangential). Therefore the cubes of a same stripe are not necessarily closely related. There are nearly 8 to 12 cubes per stripe.

The first level of hierarchy in the data is based on the stand structure: high forest or coppice with standards.

The second one is the fertility of the stands with 3 modalities, good, medium or poor, nested in the stand structure. At this level, there are 6 different modalities (3 fertilities \times 2 structures).

The third level is the region. There are 5 regions with observations, but not all the $2 \times 3 \times 5$ combinations structure × fertility × region are concerned by the sampled stands. Only 26 combinations out of 30 are represented.

The fourth level is the stand level within structure \times fertility \times region. There are 1 to 4 stands per combination of structure \times fertility \times region and 46 modalities.

The fifth level is the tree level. There are 1 or 2 trees per stand with a total number of 82 trees.

The sixth one is the height level, 1 or 2 per tree, with a total of 134 modalities.

The last level is the stripe level: 2 stripes sampled per height and a total number of 268 modalities.

A total of 3285 cubes have been sampled from these stripes.

Table I presents the allocation of stands between the combinations structure × fertility × region, and *table II* the main characteristics of the 82 trees of the sample.

On each of the 3285 cubes sampled, the following measurements were done:

- density (kg m⁻³) in air-dried conditions (10% moisture content);

- longitudinal, radial and tangential dimensions (mm) of the air-dried cubes (10% moisture content) and above the fiber saturation point (taken here as 30% moisture content).

From these measurements and the moisture variation between the air-dried state and the fiber saturation point (here 20%), some coefficients were computed. These are:

- Longitudinal Swelling Coefficient LSC (%/%);

- Radial Swelling Coefficient RSC (%/%);

Tangential Swelling Coefficient TSC (%/%);

- Volumetric Swelling Coefficient VSC (%/%);

 Swelling Anisotropy (Aniso) which is defined by: Aniso = TSC / RSC (without dimension).

Table I. Allocation of the stands and trees according to the combina-	•
tions structure \times fertility \times region.	

Structure	Fertility	Region	Number of stands	Number of trees
		Allier	2	4
		Alsace	4	8
	Good	Loir-et-Cher	1	2
		Lorraine	2	3
_		Normandy	2	4
		Allier	1	2
		Alsace	3	6
Hight forest	Medium	Loir-et-Cher	1	2
_		Lorraine	2	4
		Allier	2	4
	Poor	Alsace	1	2
		Lorraine	1	2
-		Normandy	2	4
		Allier	1	2
	Good	Loir-et-Cher	1	2
		Lorraine	2	3
		Normandy	1	2
		Allier	2	3
Coppice-with-		Alsace	1	2
Standards	Medium	Loir-et-Cher	3	5
		Lorraine	2	2
-		Normandy	2	4
		Allier	2	3
	Poor	Loir-et-Cher	1	1
		Lorraine	3	4
		Normandy	1	2
2 modalities	6 mod.	26 modalities	46 modalities	82 modalities

Table II. Main characteristics of the 82 Sessile oak trees sampled.

	Mean	Standard deviation	Mini- mum	Maxi- mum
Total height (m)	28.2	5.7	16.8	39.8
Ring number at breast height (years)	153.2	33.2	61	224
Diameter at breast height (cm)	62.3	14.2	42.3	104.1

Table III. Characteristics of the six properties measured on the 3285 cubes.

Property	Mean	Standard deviation	Minimum	Maximum
1000 × TSC (1000 × %/%)	363	68	97	637
1000 × RSC (1000 × %/%)	146	36	42	405
1000 × LSC (1000 × %/%)	12.1	5.1	-9.4	48.3
1000 × VSC (1000 × %/%)	540	106	216	959
100 × Aniso (no dimension)	254	41	106	479
Wood density (kg m ⁻³)	708	82	414	977

In addition, for each cube, the mean ring width (RW), the mean age from the pith (age) and the distance from the pith to the center of the cube (d) have been measured.

The five swelling coefficients and the density are the properties of interest. *Table III* presents the main characteristics of these properties measured on cubes.

3. MODELING THE PROPERTIES

All the properties could be modeled with a linear model with the same independent variables [14]:

$$y_{i} = \mu + \alpha \times 1/RW_{i} + \beta \times age_{i} \times \log(age_{i}) + \gamma \times \log(d_{i}) + e_{i}$$
(1)

where:

 $-y_i$ is the value of the property measured on the cube i;

 $-RW_{i}$ is the Ring Width for this cube;

 $-age_i$ is the average age from the pith for this cube;

 $-d_{i}$ is its distance from the pith;

 $-\mu$, α , β and γ are the coefficients of the regression;

 $-e_{i}$ is the residual of the model.

In this model, the independent variables RW_i , age_i and d_i appear respectively within the functions $1/RW_i$, $age_i \times \log(age_i)$ and $\gamma \times \log(d_i)$. A preliminary work showed that

these last forms were better adapted to model our dependent data than the original ones.

The residual of model (1) is supposed to be identically and independently distributed according a centered Normal Law with variance σ_e^2 . In fact, the independence assumption between the residuals could be strongly non-verified in various ways.

First, several authors as Degron and Nepveu [6], Guilley et al. [11, 12], Guilley [10] have showed that observations coming from the same tree are closer each to other than observation coming from different trees. They have called that the "tree effect". The model (1) is a general model available for the whole population of trees. But if we focus on a particular tree, it will follow its own model. That is the model adapted to this tree will have the same general expression, but with other values for the parameters. The "tree effect" is the difference on the parameter values between the general model and the model adapted the particular tree.

A model with a "tree effect" can be written as follows:

$$y_{ij} = (\mu + m_i) + (\alpha + a_i) \times 1/RW_{ij} + (\beta + b_i) \times age_{ij} \times log(age_{ij}) + (\gamma + c_i) \times log(d_{ij}) + e_{ij}$$
(2)

where:

- $-y_{ij}$ is the value of the measured property at the cube j in the tree i,
- $-m_i, a_i, b_i$ and c_i are the coefficients of the "tree effect" for the tree i,
- other notations are the same as in (1).

Here, the residual e_{ij} is supposed to be identically and independently distributed according a centered Normal Law with variance σ_e^2 as in (1). If we were focusing especially on these individual trees without consideration for all other trees, the associated effect would be a fixed one. But since the trees of the sample are considered as randomly taken from the whole population, the associated "tree effect" is a random effect. Model (2) contains fixed and random effects: it is a mixed model.

Second, even when a "tree effect" has been taken into account, the independence assumption between the residual of the model could no be verified. This is especially the case when the data are spatially or time structured [9]. In these cases, there could exist a significant correlation between the residual of successive observations. This correlation is called an autocorrelation. In our case, data were collected along stripes. However, we have verified that our cubes were sufficiently distant from each other to the autocorrelations to be non significant. We have then considered them as negligible. Hence, the basic model we retain for our properties is the model (2) with a "tree effect" but an independent structure within the residual.

The segregation of random variables of the model between variables depending on the tree and a residual depending on the cube is a way of structuring the total variance of the observations, taking into account the links between cubes belonging to the same tree.

The variance associated to the "tree effect" absorbs the variability at the tree level; the variance at the cube level is a "residual" variance.

Model (2) takes into account only information from the cubes (age, ring width, distance from the pith) and from their allocation between trees. It does not take into account other levels of the hierarchy as the stand structure or the region. But each of these levels could be a source of variability, and this variability should be taken into account.

A generalization of the model (2) for several levels of the hierarchy could be:

$$y_{ijklm...} = (\mu + m_i + m_{ij} + m_{ijk} + m_{ijkl} + m_{ijklm} + ...) + (\alpha + a_i + a_{ij} + a_{ijk} + a_{ijkl} + a_{ijklm} + ...) \times 1/RW_{ijklm...} + (\beta + b_i + b_{ij} + b_{ijk} + b_{ijkl} + b_{ijklm} + ...) \times age_{ijklm...} \times log(age_{ijklm...}) + (\gamma + c_i + c_{ij} + c_{ijk} + c_{ijkl} + c_{ijklm} + ...) \times log(d_{ijklm...}) + e_{ijklm...}$$
(3)

The indices i, j, k, l, m, ... represent the successive levels of the hierarchy.

The interpretation of the additional coefficients is the same as for the model (2): each parameter at a given hierarchical level represents the difference between the model at this level and the model at the previous level.

Obviously, such a model is too complicated to be really useful. It has to be simplified by neglecting the levels of the hierarchy where the variability is low. The fewer levels the final model will contain, the easier will be the estimation of the parameters and the easier the model will be used for further simulations.

In the following, we will try to answer the following question: if only one level other than the cube level (the residual) can be kept, which one has to be chosen? So we intend here to eliminate all models with more than one hierarchical level other than the residual.

The traditional methodology to answer such a question uses statistical tests. This method needs the biggest model to be studied in order to test the hypothesis "All the parameters for a level of the hierarchy are null". In our data, there are unfortunately confusions between some levels of the hierarchy: for example there are 10 stands with only one tree and 30 trees with only one height level. The number of parameters needed by the biggest model and the confusion between levels make the power of tests be low. So we propose another strategy to be used in such case, which occurs in many occasions.

Since we intend to keep a model with only one level of the hierarchy, we have compared all the models corresponding to this definition available from our data. We have then studied a succession of models with the same form as in (2), but where the "i" index represents successively the stand structure level, the stand structure \times fertility level, and all the

others hierarchical levels (stand structure \times fertility \times region, tree, height and stripe). For comparison, we studied a model with only the cube level of variability id est the residual: it is the model written with (1) that we called the model at the "Total" level.

To compare all these models, some information criteria such as Akaike's Information Criteria and its derivatives [1, 2] could be used. These criteria measure the adequacy of a model to the data (the log likelihood of the model) but including a penalty function that depends on the number of parameters used by the model. If several models can be used for a given data set, these criteria allow a classification between them in order to choose the most adapted. The advantage of this methodology is that it theoretically allows comparing kinds of models (nested or not) for a given data set. Unfortunately, their properties have been established for a number of observations that tend to infinity. In our case, we have to compute the value of the parameters at some levels with a low number of modalities. For example, there are only 6 modalities of the level fertility × structure. It is very far from asymptotic conditions, especially for variance parameters. In such case, estimations of variance can be strongly biased and model selection based on the Information Criteria is also strongly biased: the probability of selecting a wrong model is important. In fact, this methodology applied to our case leads to the selection of the last model of the hierarchy for all properties except the wood density. But the detailed results from these models show that the estimations are not very stable. In addition, with the information criteria methodology, all the levels of the hierarchy are used in the same way, we do not use the fact that they are nested.

For all these reasons, we have preferred to use a graphical - and pragmatic - method that allows studying the evolution of the results through the successive levels of the hierarchy. The method we used is based on the assumption that one level of the hierarchy is more important for the structuring of the variability than the others. That is, the variability at this level is high compared to the variability at the other levels. In the ideal case, it is the only level that has a real effect. If the level of the hierarchy used in the model is not detailed enough (for example: the level of interest is the "tree" level, but the level used is the "stand" level), the residual variance of the model will contain some relevant information. This value of the residual variance will be greater than it should be. If the level used is too detailed (for example, the "height within tree" level whereas the true level is the "tree level"), the residual variance will be unbiased, but the model will use more degrees of freedom than necessary.

A hierarchical level is interesting if its introduction in the model makes the residual variance strongly decrease. But this introduction could be expensive in terms of degrees of freedom of the model. The number of degrees of freedom is directly linked to the number of modalities at the last level of the hierarchy taken into account. It seems to be natural to plot the estimation of the residual variance obtained for each model against the number of degrees of freedom it used.

Estimations of the model parameters have been done using the REML methodology [5] using SAS[®] Software [20]. The best model will be the one where the residual variance begins to be stabilized, that is when the relative variation of the residual variance is lower than the relative variation of the number of degrees of freedom needed by the model. If the design were perfectly balanced between the hierarchical levels, the progression of the number of degrees of freedom from one level to the next would be geometrical. In this case, it is natural to represent the data with a logarithmic scale. In this case, the thresholds are at the inflexion points, when the curves become concave.

4. RESULTS

Table IV presents the residual variances obtained for each of the six properties for the eight studied models. In order to

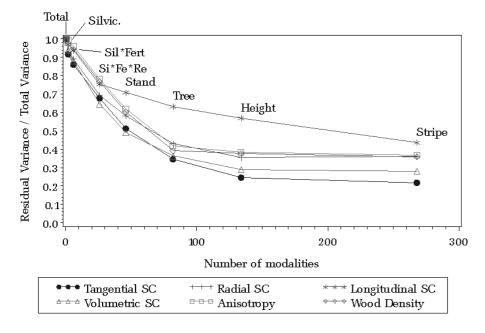
compare the variation between properties with the same scale, *figure 1* shows the data of *table IV*, but for each property, the residual variance has been divided by the variance obtained from the model (1). *Figure 2* presents the same data with a logarithmic scale. It must be underlined that these results are not a decomposition of the total variance between the different levels, but the comparison of the variance taken into account by the model using only one level of hierarchy.

As expected, *table IV* and *figures 1* and 2 show that the residual variance decreases when the number of modalities at the given hierarchical level of the model increases. For Radial Swelling Coefficient, Anisotropy and Wood Density, the decrease is low after the tree level. For Tangential Swelling Coefficient and Volumetric Swelling Coefficient, this is after the "height" level. For the Longitudinal Swelling Coefficient, there is a break in the slope at the "region × fertility × stand structure" level but the decrease of the residual variance continues at the stripe level.

From these results, we conclude that the main level of variability is the "tree" level for RSC, Anisotropy and Wood

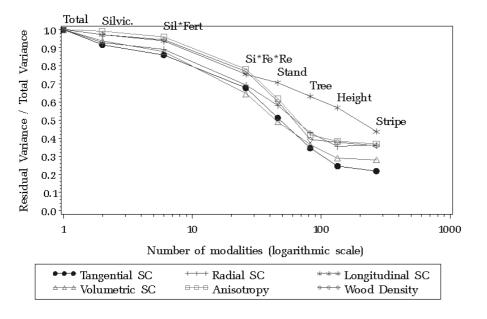
Table IV. Values of the residual variances obtained for the six properties in relation with the last level of the hierarchy taken into account.

							-	
Level	Modalities	TSC	RSC	LSC	VSC	Anisotropy	Density	
Total	1	3 165	584	23.4	6 808	1 261	3 248	
Stand structure	2	2 940	541	22.8	6 445	1 252	3 168	
Fertility	6	2 768	520	21.8	6 065	1 202	3 066	
Region	26	2 269	411	17.3	4 815	959	2 515	
Stand	46	1 762	345	16.3	3 771	766	1 984	
Tree	82	1 255	256	14.6	2 959	529	1 339	
Height	134	762	208	12.6	1 947	457	1 156	
Stripe	268	679	211	9.7	1 879	439	1 094	



Residual variance of mixed-effects models

Figure 1. Evolution of the ratio between the residual variance and the total variance according to the hierarchical level taken into account.



Residual variance of mixed-effects models

Density, the "height" level for TSC and VSC, and we cannot conclude for LSC. This last result could be explained by the precision of the values of the properties (*table V*). The precision on the value of the properties has been computed from the precision of the basic measurements on the cubes (dimensions, moisture contents and weight) and from the logarithmic derivatives of the formulae that give the values of the properties from these measurements.

The precision of the measure is bad for LSC. This is due to the fact that the absolute longitudinal deformation is of the same order than the precision of the measurement (0.04 mm for the deformation versus 0.02 mm for the precision of this measurement). We assume that imprecision of the measurement for LSC hides the structuring of the variability.

5. DISCUSSION

From the previous results, we consider that the main levels for structuring of variability are either the "tree" level, either the "height" level, according to the property modeled, or the "cube" level for the residual. All others levels are considered as negligible.

Except for the Longitudinal Swelling Coefficient, the residual variance in the model with a "tree" level is about 40% of the residual variance of the model without structuring of variability (cf. *table IV*). The structuring of the variability cannot be ignored.

Figure 2. Evolution of the ratio between the residual variance and the total variance according to the hierarchical level taken into account (logarithmic scale).

Table	V.	Mean	relative	errors	of	measurement	computed	on	the
3285 c	ube	es.							

Property	Mean Relative Error of measurement
TSC	9.8%
RSC	10.7%
LSC	56.4%
VSC	13.0%
Anisotropy	11.5%
Wood Density	0.5%

In fact, in the models with a "tree level", the variability associated to the levels from "stand structure" to "stand" are absorbed by the "tree" level, whereas the "height" level and the "stripe" level are included in the residual. For simplification of the models, these variabilities are considered at only two levels, but it should be remembered that these variabilities contain a part of variability from other levels.

We used only the information on the trees available in this study. It was not possible to take into account some other sources of variability that can have a non-negligible effect such as genetics. Further studies including a genetic information will perhaps modify the relative importance we give to the tree level comparing to the others levels.

In this study, all the effects associated to a given level of the hierarchy have been considered as random ones. If the models are to be used with focusing on some specific modalities (for example high forest versus coppice-with-standards), these modalities have to be introduced as fixed effects. To study the effect of the other levels of the variability, the reference model becomes the model with all fixed effects and with only the residual as random variable. Other models include all fixed effects, random effects of the other successive hierarchical levels and the residual. The same analysis could then be done in order to find the other levels of variability to include in the models.

This whole paper is devoted to the detection of the main level of variability. Once this level found, the modeling is not achieved yet. The covariance structure at this level has to be specified. It is not our intention to develop here the methodologies to be used for this. In this case, the likelihood ratio test become available and even the information criteria procedures if there are enough degrees of freedom at this level. As an illustration, the following equations present the model we have finally obtained for the density. Models for the other properties are not presented for overcrowding reasons.

The model for the density of cube j within the tree i is the sum of three parts: a fixed part, a random part at tree level and a residual. These parts are respectively:

- Fixed Part:

 $765.9 - 180.3/RW_{ij} - 70.18 \times age_{ij} \times \log(age_{ij})$ (4) - 197.9 \times age_{ij} \times \log(age_{ij}) / RW_{ij} - 27.44 \log(d_{ij}) + 44.58/h_{ij}

– Random Part at the tree level:

$$\begin{vmatrix} 1 \\ 1/RW_{ij} \\ age_{ij} \log(age_{ij}) \\ age_{ij} \log(age_{ij})/RW_{ij} \\ \log(d_{ij}) \end{vmatrix} \times \mathbf{u}_{i}$$
(5)

where \mathbf{u}_i is a centered normal vector with the variancecovariance matrix \mathbf{G} :

 $\mathbf{G} = \begin{bmatrix} 2129 & -1220 \\ -1220 & 6839 & 12075 \\ & 5685 \\ 12075 & 32666 \\ & & 306.4 \end{bmatrix}$

(the null components are not written)

Table VI. Decomposition of the variability in the final model.

Residual Part:
$$e_{ij}$$
 (6)

where e_{ij} follows a centered Normal law with variance σ_e^2 : $\sigma_e^2 = 1152$.

Units are:

- Wood density: kg m⁻³;
- Age (of the cube from the pith): centuries;
- *RW* (Ring Width): mm;
- d (distance from the pith to the center of the cube): dm;
- -h (height in the tree): m.

Units have been chosen in order to avoid numerical problems due to excessive differences of magnitude between the variance components.

We use the "v" notation for the transposition of vector \mathbf{v} and "log" for the natural logarithm.

We have used a method developed by Hervé [13] in an unpublished paper to compute the decomposition of the total variability between the three parts of the model for each property. These results are presented in *table VI*.

The random part is important, between 30% and 50% according to the property, always greater than the residual one. These results confirm the importance of taking into account the structuring of the variability in the models if the applications of these models deal with the variability within the population.

6. CONCLUSION

Since mixed model are not very easy to adjust, interpret and use, model based on them have to be carefully constructed. The structuring of variability is one of the characteristics that have to be studied for that.

Among the various possible sources of variability for swelling coefficients and wood density of Sessile oak, the "tree level" (or the "height within tree level" according to the property) is the main level structuring the variability. As a consequence, models intending to predict the distribution of these properties should at least take this level into account. Since trees are randomly taken from a population, this "tree effect" has to be defined as a random effect.

Property modelled	Level used for random effects	Fixed effects part	Random effects part	Residual part
TSC	Height	39.2%	50.7%	10.0%
RSC	Tree	50.8%	32.8%	16.4%
LSC	?			
VSC	Height	43.6%	45.5%	10.9%
Aniso	Tree	23.8%	48.8%	27.4%
Density	Tree	57.6%	34.7%	7.7%

Taking into account the structuring of variability has also consequences on the way of building future sampling. For a given total number of cubes, the actual estimation of the variance at the different levels of interest can be used to choose the number of modalities at each level (for example: number of trees, number of cubes per tree) ensuring the optimization of the assessment of variability in future sampling.

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