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Aging-aware NaS battery model in a stochastic wind-storage simulation framework

Pierre Haessig, Bernard Multon, Hamid Ben Ahmed*,
Stéphane Lascaud, and Lionel Jamy[†]

Abstract

Dispatchability of wind power is significantly increased by the availability of day-ahead production forecast. However, forecast errors prevent a wind farm operator from holding a *firm production commitment*. An energy storage system (ESS) connected to the wind farm is thus considered to reduce deviations from the commitment. We statistically assess the performance of the storage in a stochastic framework where day-ahead forecast errors are modeled with an autoregressive model. This stochastic model, fitted on prediction/production data from an actual wind farm captures the *significant correlation along time* of forecast errors, which severely impacts the ESS performance. A thermo-electrical model for Sodium Sulfur (NaS) batteries reproduces key characteristics of this technology including charging/discharging losses, state-dependent electrical model and internal temperature variations. With help of a cost analysis which includes *calendar and cycling aging*, we show trade-offs in storage capacity sizing between deviation from commitment and storage costs due to energy losses and aging.

1 Introduction

In small islands which are not interconnected with a continental power grid, electricity production is often based on fossil fuels that are imported at a high cost. In such a context of expensive bulk electricity, wind turbines can be a profitable solution for electric power generation, wherever there is a strong enough

wind power potential. However, the small inertia of the grid in small islands makes it a challenge to stabilize the grid energy balance despite the high variability of wind power.

One way to compensate for the high variability of wind power is the deployment of wind power forecasting tools [1], with prediction horizons ranging from one hour to a few days. These tools, although based on advanced statistical regression techniques, cannot give perfect predictions. Their accuracy is qualified in the sense of either Root Mean Square Error (RMSE) or Mean Absolute Error (MAE), and is often about 5–15 % of the installed power capacity [2]. Small islands, though, can suffer from larger prediction errors.

Electricity storage is another way to compensate for the variability of wind power [3]. It is best used together with wind power forecast where it can *compensate forecast errors*. A call for proposal was launched in November 2010 by the French Electricity Regulation Commission (CRE), for the installation of a new kind of wind generation system, that would be more reliable (that is, dispatchable) as well as provide some ancillary services to the grid by including an Energy Storage System.

1.1 Increase in Wind Reliability with a Production Commitment

The increase in production reliability is mainly based on a mechanism of day-ahead production commitment implemented by the wind-storage system of figure 1. Each day, before 5pm, the wind production operator has to announce a *power production schedule* for each half-hour interval in the following day. This schedule $P_{grid}^*(t)$, based on a forecast $P_{pre}(t)$, is taken by the grid system operator as a *firm production commitment*. The actual power delivered to the grid $P_{grid}(t)$ should be kept as close as possible

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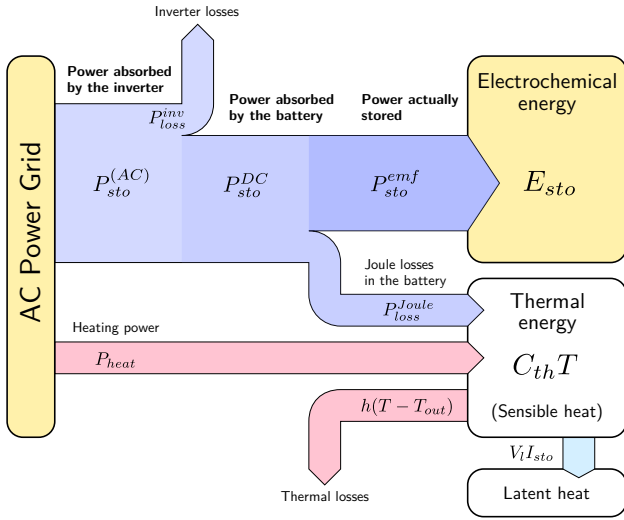


Figure 3: Energy flows (electrical and thermal) in the NaS battery model, represented during charging

NGK partner in the development of the NaS technology. Our model is similar in essence but using data from the manufacturer NGK (under a Non-Disclosure Agreement with EDF) which may explain small variations in the numerical results. In addition, we give more details on the thermal modeling.

Figure 3 gives an overview of the of thermal and electrical energy flows in the model of the ESS and its environment. It shows how energy is *transformed*, *stored*, and partly *lost* in a NaS battery. We now describe this battery model, emphasizing the specific features of NaS technology both in its electrical behavior (section 2.2) and its thermal one (2.3).

2.1 Description of the model structure

We model a NaS battery composed of N modules as shown in figure 4. Those NGK modules are the basic building blocks of the ESS, with ratings of 350 kWh/50 kW. Each module is in turn made of a series-parallel arrangement of $n_s \times n_p = 32 \times 12 = 384$ NaS cells. A diagram of the internal structure of a NaS cell can be found in [7].

Our ESS model leverages this *modular hardware structure* by working internally at the scale of one module. Equal *power sharing* is assumed to perform the downscaling from the ESS to the module, i.e. $P_{mod} = P_{sto}/N$. Therefore, our model is fully *sizable*¹ in terms of ratings by simply changing the number¹

¹For the convenience of our sizing study we assume that the integer N can be an arbitrary real number which is acceptable if $N \gg 1$. It is the case in La Réunion island with $N = 20$

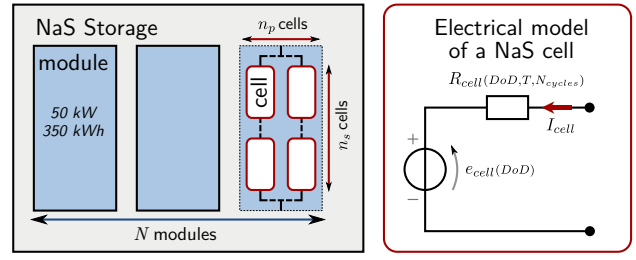


Figure 4: Description of the NaS battery assembly of modules and cells along with the electrical model of one cell

of modules N . Rated power and energy scale proportionally since the “E/P ratio” is fixed at 7.2 hours.

Electrical specifications like the electromotive force e_{cell} and internal resistance R_{cell} (see fig. 4) are specified for one NaS cell instead of a module. We thus scale these cell variables to the module level by assuming equal current sharing (i.e. $I_{cell} = I_{mod}/n_p$) and equal voltage sharing leading to

$$e_{mod} = e_{cell} n_s \text{ and } R_{mod} = R_{cell} n_s / n_p.$$

Our model is a state space model with 3 state variables:

- DoD (in Ah), the charge discharged from one NaS cell
- N_{cycles} , the number “equivalent full cycles” which represents the State of Aging.
- T (in °C), the temperature of a NaS module

Their evolution is governed by equations (1), (2) and (3) which we now introduce.

2.2 Electrical model of a battery cell

Like Hussien *et al.*, we model the NaS cell (see fig. 4) by a *voltage source* e_{cell} accounting for the electromotive force (emf) and an *internal resistance* R_{cell} which captures the output voltage drop. The accuracy (and complexity) of this Thévenin model stems from its dependence on all three state variables (DoD, T, N_{cycles}).

Figure 5 illustrate the highly non-linear dependency of the resistance in the cell DoD and the temperature T . In addition, the resistance *increases with cycling aging* proportionally to $\sqrt{N_{cycles}}$. The emf is constant at 2.075 V for low DoD and then decays linearly [7].

2.2.1 Cell DoD evolution

DoD is governed by a *charge counting* equation, given here in discrete time (Euler explicit integration

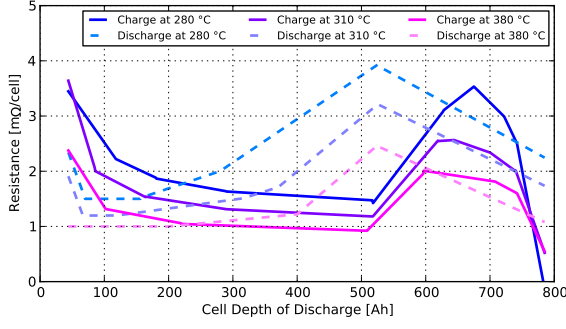


Figure 5: Internal resistance of a NaS battery cell, as a function of cell Depth of Discharge, module Temperature and charge/discharge state.

method). We choose the receptor convention, meaning that the cell current is positive when battery is charging:

$$DoD(t + \Delta t) = DoD(t) - I_{cell}(t) \cdot \Delta t \quad (1)$$

2.2.2 Cycling aging model

Cycling is accounted as “equivalent full cycles” by summing the absolute value of charge exchanges². This method is also named “Ah throughput” by Bindner *et al.* [8] and is of common use for lead-acid batteries:

$$N_{cycles}(t + \Delta t) = N_{cycles}(t) + \frac{|I_{cell}(t)| \Delta t}{2 C_{cell}} \quad (2)$$

where C_{cell} is the NaS cell usable capacity (~600 Ah). Because the cell resistance increases with the number of cycles N_{cycles} , we can indeed speak of a “cycling aging” model. The effect of time in the absence of cycling (i.e. “calendar aging”) is not captured in this model.

2.3 Thermal model of a battery module

Thermal modeling of a NaS battery is of prime importance because of the strong effect of the temperature on the internal resistance (fig. 5). The modeling of thermal energy flows (fig. 3) is done at the scale of the *module* which contains the 384 cells in a thermally insulated container filled with sand and weighs about 3 tons. Using a typical value of 1 kJ/K/kg for the average specific heat capacity,

²Counting is sometimes done for discharge current only. It is similar in essence to our counting by just removing the coefficient 1/2 in eq (2). Counting the power instead of the current is another common variation.

we set the module thermal capacity $C_{th} = 3$ MJ/K, which is in good agreement with other observations.

The balance of thermal flows include *Joule losses* which generate heat as $R_{mod} I_{mod}^2$ and the *reversible latent heat flow* of the charge-discharge reaction. It is an exiting heat flow proportional to the electric current $V_l I_{mod}$ where the entropy term [9] V_l is positive because the NaS battery charging ($I_{mod} > 0$) is an endothermic reaction while discharging ($I_{mod} < 0$) is exothermic. $V_l \approx 50$ mV $\times n_s$ for a full battery and reaches 100 mV when discharged [9]. There are also heat losses to the outside according to a linear model $\propto (T - T_{out})$ and an embedded electric heater P_{heat} to compensate for these losses. Combining all these thermal flows gives the thermal model of a NaS module:

$$C_{th} \frac{dT}{dt} = R_{mod} I_{mod}^2 - V_l I_{mod} - P_0 \frac{T - T_{out}}{T_0 - T_{out}} + P_{heat} \quad (3)$$

2.4 Power-current relationships

Although NaS electrical behavior is described by a voltage-current model, the model input is a power P_{sto} . Therefore a *power-to-current conversion* is required to apply state equations (1) (2) and (3). For a given current I_{mod} , the power absorbed by a module is:

$$P_{mod} = e_{mod} I_{mod} + R_{mod} I_{mod}^2 \quad (4)$$

where the first term is the chemically stored power (P_{sto}^{emf} on fig. 3) while the second term is Joule losses.

Solving for I_{mod} in (4), we get a power-to-current conversion formula:

$$I_{mod}(P_{mod}) = \frac{P_{mod}}{e_{mod}} \frac{2}{1 + \sqrt{1 + 4 R_{mod} P_{mod} / e_{mod}^2}} \quad (5)$$

In order to evaluate the State of Energy of the ESS ($SoE = E_{sto} / E_{rated}$), we also use a *charge-to-energy* conversion. The cell DoD is converted into a stored energy E_{cell} which is then scaled up to ESS level as $E_{sto} = (n_s n_p E_{cell}) \times N$.

3 Stochastic NaS Storage Simulation Results

For the purpose of assessing our simulation model in a stochastic framework, we feed our NaS model with a storage request $P_{sto}^*(k)$ modeled as the AR(1) process mentioned above:

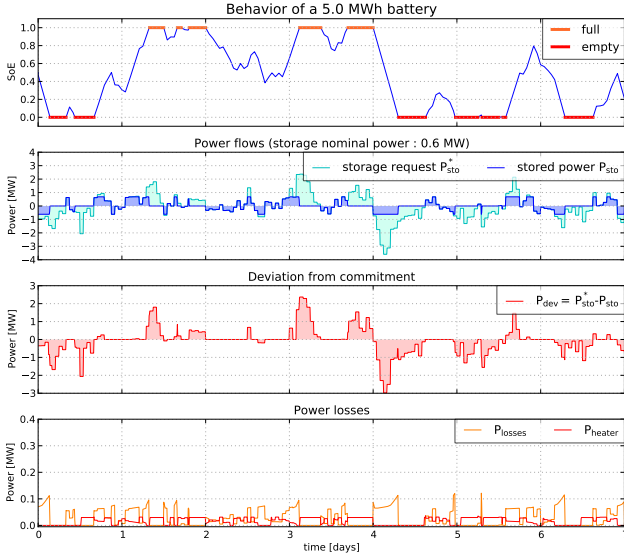


Figure 6: A week-long stochastic trajectory of a 5 MWh NaS storage system

$$P_{sto}^*(k) = \phi P_{sto}^*(k-1) + \sigma_P \sqrt{1 - \phi^2} \varepsilon(k) \quad (6)$$

where $\{\varepsilon(k)\}$ is a sequence of independently and identically distributed (IID) zero-mean random variables of unitary variance. For our simulation, we use a Gaussian noise: $\varepsilon(k) \sim \mathcal{N}(0,1)$. $\phi = 0.8$ is the *correlation* between two successive timesteps (hours). σ_P is the standard deviation of the process. Considering a wind farm with a rated power P_{nom} of 10 MW and assuming 10 % RMS error [2] we thus have $\sigma_P = 1$ MW.

As explained in previous work [5], this model does captures well the correlation structure of day-ahead forecast errors but does not account for an optimized bidding strategy (where P_{grid}^* can be different from P_{pre}). It is suitable, though, to test our numerical NaS storage model. Only the resulting storage performance are sub-optimal.

3.1 Example of a stochastic trajectory

Figures 6-7 show an example of a week-long trajectory from our stochastic NaS storage simulation tool, fed by model (6) as an input to a 5 MWh and a 15 MWh battery. Simulation timestep Δ_t is 0.1 hour (except 1 hour for (6)).

One can see how the State of Energy (SoE) increases when there is a positive inflow of power P_{sto} and decreases otherwise. For this article, we assume the use of a simple storage management policy which is “store the ideal storage request P_{sto}^* whenever it is *feasible*”. That is, $P_{sto} = P_{sto}^*$ at all times

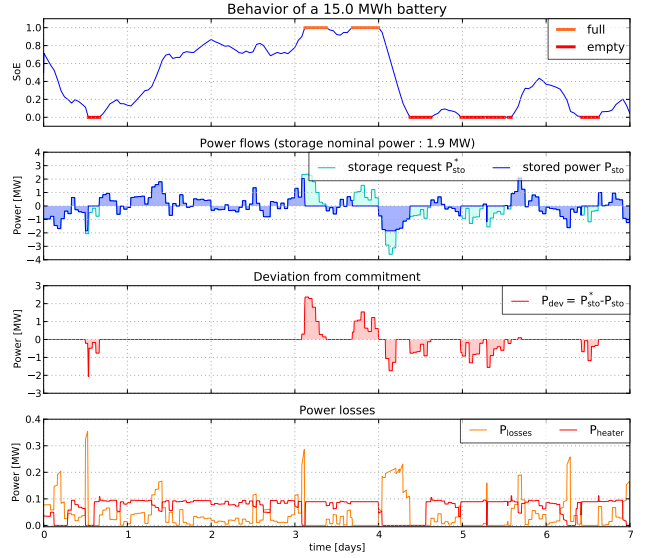


Figure 7: A week-long stochastic trajectory of a 15 MWh NaS storage system

where the storage is neither empty nor full. When this condition is met, the deviation from schedule P_{dev} is zero. The lower panel shows both losses P_{losses} (Joule and inverter³) and heating power consumption P_{heat} of all N modules.

3.2 Stochastic simulation for performance assessment

Simulation is repeated massively to collect sample trajectories of random time series such as those on figure 6. These samples are used to statistically estimate performance metrics. We use the \bar{X} notation for the mathematical expectation $\mathbb{E}[X]$ of any random variable X .

In figure 8, we present these metrics for a range of 100 values of battery capacity, from 1 MWh to 50 MWh simulated for *one month* (30 days). For each of these capacity values, we collect $N_{samp} = 1000$ *independent sample trajectories* (but vectorized in the same simulation loop) of 30 consecutive days on which to compute the following performance metrics:

- mean absolute deviation (MAD) from the commitment $|P_{dev}|$ (upper panel, in red)
- average electric losses \bar{P}_{losses} and heating power consumption \bar{P}_{heat} (middle panel)
- average aging, as capture by the equivalent cycle counting model (2) (lower panel)

³inverter losses (see fig.3) are 5 % of $|P_{sto}^{DC}|$, i.e. a 95 % efficiency model.

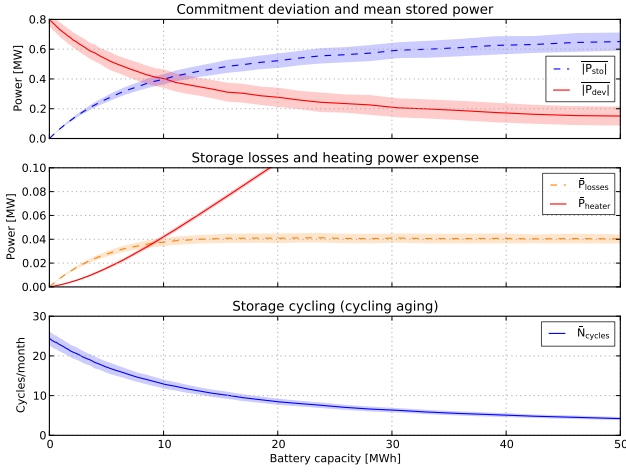


Figure 8: Parametric analysis of the NaS storage capacity sizing (with parameters $\phi = 0.8$, $\sigma_P = 1$ MW for the forecast error model (6))

We estimate these expectations by taking first the average along time on each of the N_{samp} trajectories. Then we average on all samples to produce one point of the plotted lines. The filled color intervals show the standard deviation among the different trajectories (i.e. the *inter-month variability*), which is quite high for MAD but much lower for power losses or aging.

From figure 8, it is clear that the bigger the ESS capacity, the lower the deviation from commitment. Also, a bigger capacity generates less storage aging. However, thanks to the thermo-electrical model, one can see that a *too big* energy storage is *detrimental* to the overall system efficiency, mainly because of heating power consumption, which are asymptotically proportional to the ESS capacity.

Therefore, we now put a (monetary) weight on each of these metrics, to search for an optimal storage capacity.

4 Cost analysis of the storage sizing

4.1 Cost model

Our cost model is a sum of all *storage costs* accounting for losses and aging and a *penalty cost* for commitment deviation. We actually compute *expected cost* using expected values from the simulations.

We use the following cost parameters:

- battery calendar lifetime: $t_{life} = 15$ years
- battery cycling lifetime: $N_{life} = 5000$ full cycles

- battery unit cost : $c_{batt} = 280$ k€/MWh
- electricity selling price : $c_{elec} = 150$ €/MWh (to price lost and heating power)
- commitment deviation cost : $c_{dev} = 150$ €/MWh (expensive fee, but we discuss this choice later)

Storage cost C_{sto} computed over a period of time t is the sum of *calendar*, *cycling*, *losses* and *heating* costs:

$$C_{sto}(t) = c_{batt} E_{rated} \left(\frac{\bar{N}_{cycles}(t)}{N_{life}} + \frac{t}{t_{life}} \right) + c_{elec} (\bar{P}_{losses} + \bar{P}_{heat}) t \quad (7)$$

Cycling aging models are already used for storage sizing [10], but not always coupled to calendar aging as in (7).

Commitment deviation penalty C_{dev} is:

$$C_{dev}(t) = c_{dev} \overline{|P_{dev}|} t \quad (8)$$

The total cost we wish to minimize is their sum:

$$C_{tot}(t) = C_{sto}(t) + C_{dev}(t) \quad (9)$$

Also, instead of computing these costs over an arbitrary period of time t , they are scaled in €/MWh by comparing them with the corresponding expected wind power production:

$$\tilde{C}_{sto} = \frac{C_{sto}(t)}{\bar{P}_{prod} t}, \quad \tilde{C}_{dev} = \frac{C_{dev}(t)}{\bar{P}_{prod} t}, \quad \tilde{C}_{tot} = \frac{C_{tot}(t)}{\bar{P}_{prod} t} \quad (10)$$

and supposing a 20 % (1750 hours/year) load factor for our $P_{nom} = 10$ MW farm, this gives an average production of $\bar{P}_{prod} = 2$ MW. Finally, the scaled total cost is:

$$\tilde{C}_{tot} = \frac{1}{\bar{P}_{prod}} \left(c_{batt} \left(\frac{\overline{|P_{sto}|}}{2N_{life}} + \frac{E_{rated}}{t_{life}} \right) + c_{elec} (\bar{P}_{losses} + \bar{P}_{heat}) + c_{dev} \overline{|P_{dev}|} \right) \quad (11)$$

Costs, scaled by (10) are plotted on figure 9 as a function of the storage capacity. Detailed storage costs are depicted on the upper panel. It shows that *calendar* and *cycling* are the two biggest costs in the 0–10 MWh range while *heating* overtakes cycling beyond 20 MWh (as expected from figure 8).

Adding the deviation penalty (lower panel) show that, at first, \tilde{C}_{dev} decreases faster than \tilde{C}_{sto} increases. This gives room for an optimal storage value of $E_{rated}^* = 8.5$ MWh for a total cost of about 51 €/MWh

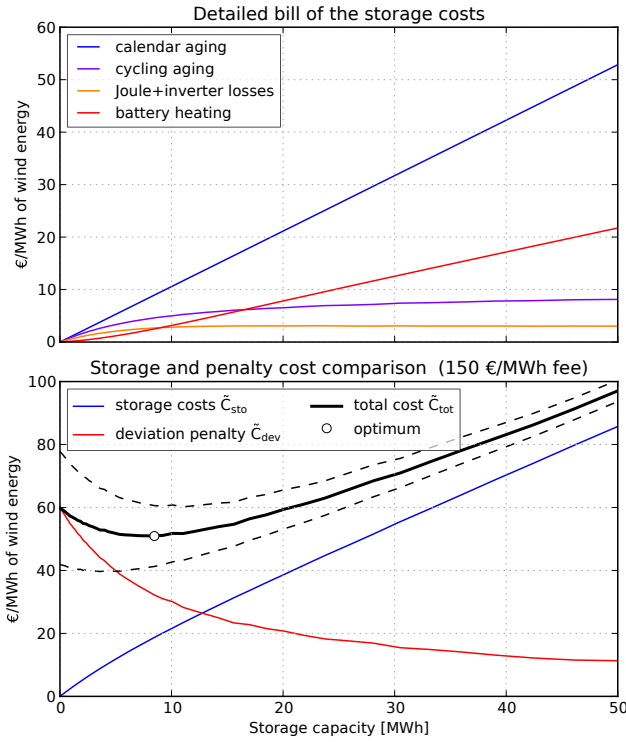


Figure 9: Cost analysis of the storage sizing, with sensitivity to a $\pm 30\%$ variation of the deviation penalty fee (dashed lines)

(32 € for penalty and 19 € for the storage). With this storage sizing, the MAD performance criterion $|P_{dev}|$ is reduced by almost 50 % compared to the no-storage situation. This is a good though not tremendous improvement.

Finally, we want to emphasize that, though the penalty fees and storage costs may seem high, the wind operator is still profitable because post-storage earning is $c_{elec} - \tilde{C}_{tot} \approx 100$ €/MWh (which is to be further split between wind farm amortization, operation cost and profit). This profitability comes from the hypothesis of a electricity selling price $c_{elec} = 150$ €/MWh which may look high but should be judged from an island grid perspective where coal baseload production is no less than 100 €/MWh.

4.2 Sensitivity to the model parameters

Among the many parameters that could be changed, we vary the two we perceive as the most uncertain.

4.2.1 Penalty Cost

We vary the penalty cost parameter c_{dev} by $\pm 30\%$ because of the absence of shared guidelines to choose the penalty scheme. Total cost \tilde{C}_{tot} recomputed with

altered penalty is plotted with dotted lines on figure 9. One can clearly observe a major effect of lowering the penalty price: the optimal capacity choice falls close to zero. Further trials show that below $c_{dev} = 70$ €/MWh, the optimal cost lies at $E_{rated} = 0$ (no storage) which means that the grid must bear all the forecast errors.

Therefore, for given storage costs and a given behavior of the forecast error, we identify a range of penalty cost which leads to *reasonable decrease* of the commitment deviation. In our case this range is about 100–200 €/MWh.

4.2.2 Stochastic input model

The AR1 model (6) was introduced [5] to capture the main trend of forecast error interdependence along time. This dependence is entirely captured by the inter-hour correlation coefficient ϕ which we now vary for two reasons: the uncertainty coming from the AR1 model fitting procedure and because the AR1 captures the *main trend* but not the fine structure of forecast error interdependence [11].

Results from simulations with ϕ varied in the realistic 0.7–0.9 range show that any increase in ϕ leads to a $\tilde{C}_{dev}(E_{rated})$ curve which decreases more slowly. Therefore \tilde{C}_{tot} gets flatter, the optimal capacity gets smaller and the commitment error reduction even smaller.

Because the storage behavior is quite sensitive to the behavior of the forecast error, an ongoing measurement campaign should help sharpen the forecast error model.

5 Conclusion

We report a thermo-electrical model for NaS battery storage, taking into account aging effect, used for a performance assessment in the context of a day-ahead production commitment of wind power.

Our numerical model fits in a vectorized stochastic simulation framework which uses an autoregressive noise model as the storage request. Results from our stochastic simulations show the importance of thermal modeling of a NaS battery, especially to compute the heating power consumption, which can severely affect the overall system efficiency.

Our performance assessment based on Mean Absolute Deviation from commitment is translated into a cost analysis by means of a simple linear cost model which includes both calendar and cycling aging. Cost analysis shows that using a storage in the

range of $P_{nom} \times 5-10$ h is profitable when the deviation fee is quite high ($\sim 100-200$ €/MWh).

Finally, our results should not be taken as a real storage sizing. Indeed, the management of our wind-storage system is sub-optimal because no commitment bidding strategy and no advance energy management policy are used. Future work on these strategies will enrich our wind-storage simulation framework.

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