

Configurations of activity: from the coupling of individual actions to the emergence of collective activity

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1 Abstract

2

This paper presents and uses the notion of configuration of activity, which extends the Norbert Elias's original concept of social configuration (1966) based on the study and analysis of individual and collective activity. Although this concept embraces all types of social activities, in the present study we used it to describe and analyze various classroom activities during a primary school mathematics lesson. Individual action is described as being meaningful to the agent, according to semiological theory of course-of-action (Theureau, 2003).

The configuration of activity in the classroom is described as a collective activity with a global form embedded in a culture and emerging from the dynamics of points of articulation between individual actions. It presents the main characteristics of autonomous systems: (a) the emergence of an order, (b) the individuation of a form, (c) the existence of a unit with borders specified by the process of self-reproduction, and (d) the system sensibility to perturbation by outside events.

16 Using the concept of the classroom configuration of activity, this study allows for new

17 insights in the emergence of a teacher-pupils collaborative activity in the classroom.

18

19 Key words: activity, collective, emergence, classroom, mathematics, teaching

In the 6th grade classroom, pupils' desks are arranged to form four workgroups of 1 2 four pupils each. The pupils are reading a duplicated text of a math problem that they have to solve. As the teacher moves from group to group she asks questions to make sure 3 that the pupils understand the task. The pupils are involved in various activities: they 4 mark up their problem sheets with highlighters, use their electronic calculators, answer 5 questions, move around the classroom and talk to each other. The teacher monitors these 6 activities observing group dynamics, confirms correct answers, helping some pupils and 7 encouraging others, and confirming the correct answers. Although at first glance all these 8 activities seem to be chaotic and spontaneous, a closer look will reveal a certain level of 9 organization: the interaction between individuals forms a recognizable structure. These 10 complex and dynamic forms of interaction have been termed "configurations of activity" 11 (Durand, Saury & Sève, 2006), and their emergence in the classroom has become a focus 12 of educational research (Durand, 2005). 13

14 This paper presents and uses a theoretical and methodological approach for studying these configurations of activity through the description and analysis of a 15 16 classroom situation during a primary school mathematics lesson. We proceed in three steps: first, we introduce (a) the approach of "methodological situationism", the three 17 presuppositions it is based on, and the notion of the intrinsic dynamics of activity. We 18 then illustrate the concept of the configuration of activity through the case study of a 19 20 typical classroom teaching situation. Finally, we provide a detailed examination of this concept and an assessment of its relevance for educational activity description. 21

22

1 "Methodological situationism"

2 Our approach is grounded in the following theories: (a) situated action (or cognition) theories (Kirshner & Whitson, 1997), (b) activity theory (e.g. Engeström, Miettinen & 3 Punamäki, 1999), and (c) cognitive phenomenology (Varela, Thompson & Rosch, 1999). 4 It focuses on the articulation of social and individual dimensions of activity, making a 5 special emphasis on classroom activity. The approach differs from the current research 6 trends based on the assumption that collective activity depends on individual actions and, 7 for example, evolves from individual representations. From this perspective, 8 representations determine or prescribe collective activity. Our approach also differs from 9 those ones that assume the opposite, namely, that individual action depend on collective 10 activity. This assumption implies that the organization determines or prescribes 11 individual action. 12

Our approach is based on three presuppositions: (a) self-organization of individual 13 14 action, (b) lack of opposition between the individual and social dimensions of activity, and (c) fundamental semiosis basis of activity. The first presupposition is that individual 15 action emerge from the "activity - situation" coupling (Varela, 1979). This coupling 16 embraces the fundamental property of living and social systems, regardless of their level 17 18 of organization or complexity: living systems develop and maintain their structure through the exchange with the environment in a process of permanent self-organization 19 20 (Fuchs, 2006; Luhmann, 1995). The changing forms of this coupling result from the dynamics of life and from the viability of the system to its environment. In other words, 21 22 the organization of individual action is considered to be essentially autonomous, although extrinsic constraints on this coupling do occur (Theureau, 2002, 2003). The organization 23 24 of action and the meaning attributed to them by their agents should be considered by the researchers thus need to be taken into account by modalities other than the outside 25 "causes" of coupling (Andersen, Emmeche, Finnemann & Christiansen, 2000). From the 26 same perspective, the organization and meaning of collective activity proceed from the 27 articulation of individual action in accordance with the emerging dynamics that is 28 29 different from but analogous to the dynamics that characterizes individual action. When individual situations allow it, global cooperation emerges spontaneously, regardless of 30 precise rules or a central authority. Phenomena of this type have been described as "latent 31

organizations" by Starkey, Barnatt & Tempest (2000), or as "intelligent crowds" by
 Rafael (2003), in the context of new technology use.

The second presupposition is that the individual and the social are not two distinct 3 entities or ontological realities. Individuals form groups: although separate as ontological 4 entities, they are united by a common structure that distinguishes them from an "exterior" 5 in a dynamic and labile manner. The individual and the social are thus intrinsically 6 connected. Individuals attribute a meaning to the collective activity in which they are 7 involved insofar as the latter allows for the accomplishment of individual action. 8 According to Elias (1966, 1978, 1991), the concept of social configuration can be used to 9 describe and explain the interdependency of relationships, the tensions between 10 individual actions, and the relatively stable forms of this system of interdependence. 11 12 Social configurations are constructed by individual agents as they interact collectively in a certain situation, yet these configurations are independent of both individual intentions 13 14 and awareness. They are *gestalts* that stand out from the background. They are limited in space and time and can be described as emerging processes of distribution and dynamic 15 balancing of tensions. Social configurations are "concrete" in that they are "no more and 16 no less real than the individuals who make them up" (Elias, 1966, p.397). They are global 17 18 forms with ever-changing dynamics produced by interaction. They offer a potential for action, imposing balance and thus facilitating the achievement of goals. They present 19 20 opportunities both for addressing individual preoccupations and for achieving a social balance often based on individual goals that do not necessarily converge. 21

The last presupposition is that configurations of activity emerge from the meanings 22 that individuals attribute to their action and environment, yet these configurations may 23 24 never become meaningful in themselves. Each agent's action is based on semiosis; that is, 25 on processes of construction or attribution of meaning in direct and essential connection with the organization of their action (Theureau, 2002; Chaliès, Ria, Trohel & Durand, 26 2004). Agents interact only with issues that are meaningful to them. In other words, 27 agents are fundamentally and permanently engaged in the construction and reconstruction 28 of an "umwelt" (Uexküll, 1992), i.e. a meaningful situation. Our study adopts a situated 29 action approach in which the situation is defined as part of the objective environment 30 whose meaning is constructed by the agent We insist that activity must be studied as a 31

whole, that not only does the agent's action carry the imprint of the environment in which it unfolds, but also that the agent "has a situation" in Dewey's sense (1938/1963). This means that the agent has an irreducible point of view at the environment that generates meaning, and that cognition is mainly culturally situated, i.e. that the culture offers possible actions which are or are not actualised in context.

6

Classroom activity analysis

7 The course of action approach is part of a wider research program aimed at analyzing teachers' and pupils' classroom activity in various subject matter contexts at different 8 9 curriculum levels. These studies focus on the teaching process (Durand, 1999; Durand, Saury & Veyrunes, 2005), classroom preoccupations and emotions of the beginning 10 teachers (Bertone, Méard, Ria, Euzet & Durand, 2003; Ria, Sève, Theureau, Saury & 11 Durand, 2003), the interaction between beginning and cooperative teachers (Chaliès, Ria, 12 Trohel & Durand, 2004), teacher-pupils classroom conflicts (Bertone, Meard, Flavier, 13 Euzet & Durand, 2002; Flavier, Bertone, Hauw & Durand, 2002), and the distance 14 learning process (Leblanc, Durand, Saury & Theureau, 2001). Although all these studies 15 provide new insights into the teaching and learning process and interaction, none of them 16 examine the collective activity in the classroom. This is the scope of the present study... 17

To understand configurations of activity, one must examine the construction 18 processes of activity-situation coupling, focusing on the meaning attributed to the 19 environment within which agents act. This approach emphasizes the importance of the 20 agent's point of view. In the classroom, for example, an individual agent's action partly 21 22 depends on the individual action of other agents: this interdependence can be termed "individual activity – situation" coupling. This coupling is at the origin of the 23 configuration of activity within which it unfolds, and yet is also made possible by it. 24 25 Individual actions of agents are meaningful to each of them insomuch as they can 26 articulate these actions among themselves and in accordance with the configuration of collective activity that emerges from these actions. However, each agent only considers 27 configuration issues that are meaningful to him/her, but might not have the same meaning 28 to another agent. This means that: (a) agents do not have a global and thorough 29 understanding of the configuration of activity in which they are involved, and (b) the 30

configuration needs to be analyzed by the researcher from a dual point of view: (a) a 1 point of view of an external observer, which can be metaphorically termed the "point of 2 view of the configuration"; and (b) a point of view of an agent, termed the "point of view 3 of the actor", or the internal point of view. The researcher uses agents' verbalisation to 4 interpret their experience during action. These methods of observation, coupled with self-5 confrontation interviews where agents are invited to comment on their own action while 6 being video recorded, give the researcher an opportunity to coordinate the two points of 7 view on action. 8

9 In this study, we refer to collective configuration of activity and *not* to configuration 10 of collective activities. Unlike both individualistic and collectivistic approaches, this 11 approach focuses on the emerging activity-situation coupling and has been termed 12 "methodological situationism" (Theureau, 2002, 2003).

Our approach to classroom activity has been influenced by (a) Doyle's concept of 13 14 classroom ecology (1986) that describes the classroom organization and management as a structured, singular, complex and interactive process, resulting from a set of processes 15 16 and dispositions carried out by the teacher to assure a supportive classroom environment for pupils; (b) the interactionist approach that maintains the idea of "social construction 17 18 of the reality" (Schütz, 1970) and considers the way that actor's interpret the classroom reality (Allen, 1986; Mehan, 1979); and (c) the distributed cognition approach that 19 20 emphasizes the collective and cultural aspects of action and interaction between actors and between them and the outer world, placing them within network sustaining 21 22 trajectories of participation in which cognition is socially distributed (Barab & Kirshner, 2001; Roth, 2001; Salomon, 1993) and supported by objects (Saxe, 2002). 23

Our approach is aimed at explaining collective activity in an educational setting by: (a) giving similar importance to individual action and collective activity; (b) adopting the actors' point of view; (c) taking into account the meaning they construct about their action; (d) adopting a qualitative methodology that provides a detailed description of global interactions in the classroom (and not only dyadic interactions); (e) focusing on phenomenon that are not pre-defined.

30

The intrinsic dynamics of action

We describe individual action and its articulation within the semiological theory of the course of action (Theureau, 2003). This theory models the level of individual action that is meaningful to the agent, i.e., the level that can be shown, told and commented on by him or her. Course-of-action theory presupposes that this level of organization is relatively autonomous in relation to other levels of analysis, but that it represents the agent's global action (Theureau, 2003).

The individual course-of-action consists of a flux of action which includes three 7 main components: (a) preoccupations, (b) perceived meaningful aspects of the situation 8 and (c) cognitive elements of generality (i.e., knowledge). The preoccupations correspond 9 to all the possibilities of action, relatively indeterminable and limited in time, that are 10 open to the agent in a given situation (i.e. "Help pupils"). They emerge from the 11 possibilities linked to the agent's past. These preoccupations are blurred, indeterminate 12 (Ex.: "Help the pupils establish links between important numbers" or "Get the pupils 13 back on task"). At the same time, these preoccupations are specified in the action by the 14 aspects of the situation which the agent perceives and which are meaningful to him (Ex.: 15 "The pupils haven't noticed the important indications" and "The pupils are becoming 16 discouraged"). This refers to the knowledge present in cognition in the unfolding 17 18 situation but arising from past courses-of-action (Ex.: "Highlighting helps the pupils to find the key information' and "Finding the key information helps to solve a problem"). 19

20

21 Table 1: Example of action unit components

22 Actions and verbalizations in the classroom and self-confrontation interviews

23 [A pupil makes a sigh of discouragement]

24 <u>Teacher (in the classroom)</u>: Give me a highlighter!

25 <u>Teacher</u> (during a self-confrontation interview): OK, let's do it again! So, here I'm going 26 to highlight, because they haven't done it: This annoys me, and I want them to see it! I 27 want them to see that it's over here — it's over here that it counts... There you go, here's 28 one, and then the other!

29 **Preoccupations:** Help the pupils

30 – Help the pupils to establish links between important numbers

1 – Get the pupils back on task

2	Perceived meaningful aspects of the situation
3	 The pupils haven't noticed the important information
4	 The pupils are becoming discouraged
5	Elements of Generality (Knowledge)
6	 Finding key information helps to solve a problem
7	 Highlighting helps the pupils to find key information
8	
9	Collective activity results from the synchronic and diachronic coupling of several
10	agents' courses-of-action. This coupling results from multiple points of articulation
11	between two courses-of-action, that is, local relations of interdependence (mutual
12	dependence). Points of articulation occur between two (or more) courses-of-action when
13	one or more components of one agent's course-of-action correspond to one or more
14	components of the other agent's course-of-action. This articulation is produced by the
15	convergence or divergence of preoccupations and actions, like, for example, in a situation
16	of supervision in a teacher education program (Chaliès, Ria, Bertone, Trohel & Durand,
17	2004).
18	Our research approach extends beyond the interaction between two agents, focusing
19	on the collective activity of several agents. The configuration of activity in its changing
20	dynamics is studied based on collective articulation of preoccupations and actions of the
21	participating agents at a given moment.
22	
23	A case of collectively solving a mathematics problem
24	
25	This case study is an excerpt from a considerably more extensive research program
26	(Durand, Saury & Veyrunes, 2005). We have chosen it because it perfectly illustrates
27	some typical situations observed during mathematics lessons.
28	The teacher conducted a mathematics lesson in Year 6 class (the highest level of
29	primary school in France) in a small rural school with only three classes. There were

eighteen 11-year-olds in the classroom. Six lessons were video-recorded and analyzed 1 based on the notion of proportionality. One of these lessons was selected as 2 representative of a configuration of math problem solving activity. Two types of data 3 were collected and analyzed: (a) data of pupils' and teachers actions' observation: 4 recordings of classroom actions with a video camera; (b) data from self-confrontation 5 interviews held immediately after the lesson. After the teacher and the researcher had 6 closely examined the video recording, the teacher was invited to comment on her actions, 7 i.e. to explain what she was doing, what she was thinking about, what she perceived and 8 9 what she felt at a particular moment. The researcher's role was to identify specific events and to encourage the teacher to comment on her own action while avoiding a posteriori 10 interpretations, generalizations, or explanations that were not directly connected with 11 these actions. 12

13

Data processing was carried out in five stages:

14 <u>Stage 1</u>: Chronological presentation of collected data. For this purpose, a three-15 column table was created. Column 1 comprises the traces of the activity in the classroom: 16 *verbatim* transcription of participants' verbalizations, pupils' work, and schemas made by 17 the teacher. Column 2 comprises the video file of pupils' and teachers' behaviours and 18 interactions along with their full description. Column 3 comprises the *verbatim* 19 transcription of self-confrontation interviews corresponding to the teacher-related data in 20 Column 1.

Stage 2: Identification of components. Detailed examination of participants' 21 behaviours and communications in the classroom and during the self-confrontation 22 interview. Preoccupations were identified and categorized. Based on the responses to the 23 24 following questions: What are the agent's preoccupations at the time under study? Pupils' preoccupations were identified by inferences performed during self-confrontation 25 interviews and based on pupils' behaviour and verbalizations, on researchers' experience 26 of the classroom (all of them have been teachers), and on their expertise in the course-of-27 action theory. Inferences made by the researchers in a blind procedure achieved a 92%-28 level of agreement; disagreements were resolved through follow-up discussions between 29 the researchers". Perceived meaningful aspects of the situation were identified and 30 categorized using the responses to the following question: what perceived or remembered 31

1 elements of the situation were meaningful to the agent at a moment of study?

<u>Stage 3</u>: Linking the teacher's and pupils preoccupations with those of the students
by noting the convergence and divergence between them.

4 **Stage 4**: Study of the points of articulation in the configuration of activity. The 5 points of articulation were determined based on what elements of the situation are 6 meaningful to agents in the situation: if a certain element of the situation (in this case, for 7 example, the math problem) is meaningful to two or more agents, it is considered to be an 8 articulation point in the configuration of activity.

9 <u>Stage 5:</u> Description of the dynamics of the configuration of activity, i.e., the 10 tensions and the balance resulting from the coupling of courses-of-action in the 11 classroom.

During a follow-up discussion between two researchers, they resolved any existing disagreement about the decomposition of courses-of-action, the component categorization, and the convergence/divergence of preoccupations, achieving 97% of agreement. After consulting with the third researcher, they achieved a full agreement (100%).

During the lesson, the pupils were asked to solve a proportion problem using a scale (see Figure 1).

19	YEAR 6 PROBLEM SITUATION (1)
20	A boy wants to build a model car.
21	He can choose between two sizes:
22	– a 1:45 scale model (9 cm long and 3.2 cm wide)
23	– a 1:20 scale model (22 cm long and 7 cm wide)
24	He wants to build the one that is really bigger, the one that would be
25	bigger if he saw them both in the street.
26	Which one should he choose?
27	
28	Tips:
29	1) – Think about the scales presented in the text
30	(Relationships between units) cm-cm
31	2) – Think about the tables that show the real car-model relationship

1

2

3

Individual actions during math problem-solving

Figure 1. Facsimile of the problem given to the pupils

Teachers' individual actions. The class was divided into groups of four or five pupils in four work areas; in each area, pupils' desks were put together. Once the problem sheets were handed out and the problem was read out loud, the pupils started searching for the solution. The first responses given by Gerald, Gregory, Justine, and Charlotte¹ were invalidated by the teacher. In the 25th minute, Gerald suggested a solution that involved dividing one scale by another one. The teacher invalidated this suggestion with a simple "no".

In the 29th minute, the teacher confirmed Justine's response pointing out that she had spotted an important piece of information, that is, that the two models were of different size. The teacher's preoccupations were: (a) *to confirm Justine's response*, (b) to *stimulate Justine's involvement in the given task so that she would continue working*, and (c) *to prevent the pupils in Charlotte's group from confusing the numerical data of the two models*.

17 The teacher's preoccupation with helping the pupils to understand the reduction ratio was expressed by a reference to "their life outside school". The teacher thus commented 18 19 on her own action: "So, now I am trying to help Justine because I know she goes walking with her uncle... [...]. So I say: OK, who has ever run a kilometre? And I am waiting for 20 Justine to say...: I do, every Saturday I go walking with my uncle. We take the model 21 diagram, we look at it, and... When you put your foot on the diagram, you can see that it 22 goes over the edge?" The teacher's preoccupations at that moment were: (a) to help 23 Justine by evoking a meaningful experience outside school, (b) to help Justine understand 24 the reduced scale presented on the diagram, and (c) to keep Justine focused on the 25 prescribed task. 26

In the 38th minute, Justine came up with a new suggestion. Although the girl had figured out the relationship between the width of the first model and its scale, she had divided instead of multiplying. The teacher asked her to encircle a different answer on a worksheet than the 3.2 that Justine was focused on. She wanted the pupils to compare the

1

This group of pupils is thereafter called Charlotte's group.

length and width of the cars in relation to their respective scales by multiplying the dimensions of each model by its scale, and then to compare the results. For Model one: $9 \ge 45 = 405$ and $3.2 \ge 45 = 144$ and for model two: $22 \ge 20 = 440$ and $7 \ge 20 = 140$. Her preoccupation was: *to invalidate incorrect suggestions*.

Because two of the four groups could not find the right solution, the teacher decided 5 to help them. In the 42nd minute, she went to the blackboard and gave additional 6 explanations. She focused her attention on the pupils who experienced difficulties in the 7 two groups. Using drawing, she illustrated the scale ratio, pointing out that 1 cm on the 8 scale corresponds to 20 cm or 45 cm (depending on the scale) of a real car. Her 9 preoccupations were: (a) to help the pupils find and perform the multiplications to be 10 carried out, (b) to help the pupils understand the problem using an example from a real-11 life situation, and (c) to keep the pupils involved in a given task. The teacher Justine's 12 answer with a big smile and an exclamation of satisfaction". Her preoccupation was to 13 validate on Justine's suggestion. 14

15

16 **Table 2.** Excerpt from classroom verbalizations (Minute 42)

Classroom verbalizations	Video and Behaviours description
Teacher:1 cm on the model	
Justine: I know!	1 cm 45 cm
Teacher: Means, in real life, 45 cm	
Justine: 1 cm on the model is just 1 cm,	_1 22
but on a normal big car that will be 40 cm	
uh, 45 cm.	Facsimile of the schema drawn on the blackboard
Teacher: Yes, that's right! So, think about	by the teacher (Minute 42)
this: if you have 2 cm?	
Pupil: You have to multiply!	
Justine: 45 multiplied by 2!	
Teacher: Ahhhh!	
Pupil: 45 multiplied by 22!	
Teacher: Ahhhh!	

In the 54th minute of the lesson, having realized that the pupils were not on the right track, the teacher returned to Charlotte' group and repeated her explanation. During the self-confrontation interview, the teacher said that the period of time between the 54th and 58th minutes was quite difficult. She reviewed and marked up the text of the problem in order to help the pupils identify the important information using a highlighter.

- 6
- 7 **Table 3.** Classroom and self-confrontation verbalizations (Minute 54)

Classroom	Video	and	Behaviours Self-confrontation
verbalizations	description		verbalizations

Teacher: Give me a Teacher holds out her right hand Teacher: Justine gives her a highlighter highlighter!

Grégory Gérald Do we agree that this this are and the measurements of the little car?

Gerald: Yes! Justine: Yes!

this

Justine Charlott Charlotte in-knee, leans over the Teacher: The numbers which

document and watches how the are... boom! That one with Teacher: And that this teacher is highlighting the text. the Gerald also leans forward and this one, that's all. measurements of the does the same.

Gerald (in a whisper):

other little car? OK?

are

I see!

and

At this time, Gerald leans over Teacher: And I want them to his copybook and sets to write.

Charlotte (in a loud Charlotte sits up clapping her here, and that makes, there... voice): I see! hands

So. let's have another look! So, I'm going to highlight, because it hasn't been done: It's annoying me, and I want them to see! Researcher: What are you highlighting, the numbers?

that one, and this one with

Researcher: Are you highlighting the four numbers on the photocopy?

see that it's over here, over

There is one and then there is another one!

Researcher: You separate the two of them, why? What do you expect?

Teacher: I want her to say: 'but, the two others, then, and the two others, but look: here's one that goes with this one!'

2 The teacher used a highlighter to mark up relevant information. By highlighting the model dimensions, she drew the pupils' attention to essential data. But she also wanted 3 the pupils to detect a relationship between a scale drawing and an actual object. 4 According to her, understanding this relationship should have helped them realize that the 5 length and width of the two models were of the same measurement domain, and that the 6 non-highlighted numbers represented scale factors (1:45 and 1:20). She wanted the pupils 7 to establish a relationship between the two scales and their respective groups of 8 measurement data. Her preoccupations were: (a) to help the pupils from Charlotte's 9 group find the right equation, (b) to help the pupils from Charlotte's group to see the 10 relevant relationship between the numbers, and (c) to keep the pupils involved in a given 11 task. 12

The teacher was interrupted by Charlotte and Gerald, each of whom came up with a 13 14 solution. First, Gerald suggested multiplying the length of the model by its width, thus getting what he erroneously named "perimeter" (in fact, the surface area). Gerald seemed 15 16 to have interpreted the act of highlighting two pairs of numbers (3.2 and 9 and 22 and 7) as an evidence of a relationship between the two numbers of each set, and not as an 17 18 indication of a link between a set of two numbers and a corresponding scale. So, he simply chose to multiply the two numbers of each set. Gerald's suggestion was perceived 19 20 by the teacher as wrong, and her preoccupation was: to invalidate Gerald's suggestion.

21

1

Table 4. Verbalizations in the classroom and the self-confrontation interview (Minutes
 55-56)

Classroom verbalizations	Video and Behaviours	Self-confrontation
	descriptions	verbalizations
Gerald: So, there, in fact, we	Gerald speaks to the	Researcher: So, when he
did 3.2 times 9 and get 28.8.	teacher ; Charlotte, in-	says that what do you say?
Teacher: Why did you do 3.2	knee on her chair, looks	Teacher: I say to myself:
times 9?	at the teacher	but he hasn't understood yet,
Gerald: Because that's the		because in my mind, there is
width and that's the length.	Gerald points to the	this plan that I am waiting

Teacher: And what does that numbers on the problem for. And it's true that I didn't mean, when you've done this? sheet.

I've found it!

That!

Gerald: (At the same time) Well, the perimeter, and after we're going to do 22 times 7! Teacher: You're going too fast, Gerald, you're panicking! Calm down!

Gerald: 22 times 7, and here we get 28.8 for 3.2 times 9, here, so we'll get ...

Teacher: What will you get with that? Explain it to me, you...

Gerald: The perimeter!

Teacher: The perimeter?

Gerald: Yes, of the car, of course...

Teacher: The perimeter!

Charlotte: Teacher, understood!

Ι

Gerald : Yes... but no. but...And then we'll do 22 times 7, we'll get the result and we'll do 3.2 times 9... 28.8 so, look, and then we will do a ...

Charlotte: Teacher ...

her pen.



Charlotte looks at the teacher Gerald points out

alternately the numbers in the problem sheet and in his copybook

The teacher is staring at Gerald for an instant

The teacher turns to

consider that there might be Charlotte hits on the others, and then, when he Charlotte: Oh no! Teacher! table, then points out the said: "we only need to text of the problem with multiply this by this and it gives that", I say to myself: OK, he he says has understood, but that's not

what I expected! [...]

Teacher: On top of that, he's talking about the perimeter, and I say to myself, he's talking to me about the perimeter—but he's going to work out the area, yes... OK: he's really... lost it!

Teacher : When he talked about the perimeter, I said to myself: OK, he hasn't understood... and that's precisely it, because there is some vocabulary which is for me, well... when he's talking to me, for me it's revealing... There we are, I say to myself, he's talking about the perimeter, he hasn't understood anything! Researcher: You've understood, but you stop him....

17

Teacher : Oh yes, I get it	Gregory; Gerald leans Teacher: Yes, I understood
	over his copybook ; what he wanted to say, but I
	Charlotte looks at the stop him because for me, its'
	teacher not the right plan!

The teacher invalidated Gerald's suggestion in three stages: (a) she asked him to 2 explain the equation, (b) she expected him to "talk about the surface area" of the model, 3 4 while Gerald insisted on using the term "perimeter", and (c) she asked him about his use of this word. For her, Gerald's second mistake was to talk about perimeter instead of 5 area. She expected him to correct his error, which seemed to her to reveal a wider lack of 6 understanding of the situation. She asked him to explain his reasoning, leaving alone the 7 8 wrong use of terminology. As soon as she realized that Gerald's explanation was not getting him closer to the right answer she briskly interrupted him. Her preoccupations 9 10 during this exchange were: (a) to have Gerald explain his reasoning, and (b) to invalidate Gerald's suggestion. 11

1

12 Charlotte's suggestion started at the same moment as Gerald's. The teacher let 13 Charlotte talk after having listened to Gerald. Charlotte used her pen to successively point 14 to relevant pairs of numbers, indicating the model measurements and the scales. She 15 pointed to number 9, then to the scale 1:45, then to number 3.2, and again to 1:45. She 16 did the same for the other model, indicating 22 and 1:20, and then 7 and 1:20. Charlotte 17 emphasized her actions with deictics (repetition of "*that and that*").

The validation of Charlotte's suggestion was direct. The following conversation 18 shows how the teacher was interpreting the solution offered by Charlotte while 19 confirming it at the same time (see Table 5). The text of the problem mediated the two 20 21 protagonists' actions because it was physically at the centre of the interaction. A 22 sequence of gestures accompanying Charlotte's explanation, coupled with her discourse, was interpreted by the teacher as a sign of comprehension of the scale ratio multiplicative 23 nature. She assumed that Charlotte had realized that to make a scale model bigger, she 24 had to perform multiplication. The teacher therefore did not insist that Charlotte 25 demonstrate her equation. Her preoccupation in that case was to validate Charlotte's 26 27 suggestion.

 Table 5. Classroom and self-confrontation verbalizations (Minute 57)

descriptionverbalizationsCharlotte: Look, Teacher, ICharlotte points out the numbers in the problemResearcher: Yes, yes and when she says: 'we're going to do', what is your interpretationCharlotte: The length is 9 cm.The teacher approves over his copybook, thenTeacher: Multiply!Charlotte: So, this at leastGerald writes, leans over his copybook, thenResearcher: Multiply?Teacher: The length is 9 cm.Gerald writes, leans over his copybook, thenResearcher: Wultiply?Teacher: The length is 9 cm.raises his hand.Researcher: Why?Charlotte: So, thereTeacher: YesTeacher: YesCharlotte: So, hereFreacher: Yes!Teacher: You don't knowCharlotte: We have to doThe teacher nods her head.Researcher: You don't knowTeacher: Yes!The teacher nods her head.Should be bigger.Charlotte: And afterThe teacher nods her head.Researcher: So, you think that should be bigger?Teacher: Yes!Charlotte points out the numbers in the text of the problem.Researcher: So, you don't ask should be bigger?Charlotte: And afterAt cach 'yes', the teacher nods her head.Researcher: But you don't ask yourself the question When should be bigger?Charlotte: Yes!Charlotte is pointing out teacher: Yes!Researcher: For you, that should be bigger?Teacher: Yes!Charlotte is pointing out teacher: Yes.Researcher: For you, that should be bigger, butTeacher: Yes!Charlotte is pointing out teacher: Yes. <th>Classroom verbalizations</th> <th>Video and Behaviours</th> <th>Self-confrontation</th>	Classroom verbalizations	Video and Behaviours	Self-confrontation
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Teacher: Yes!Researcher: For you, thatCharlotte: That and thatmeans multiplication?	Charlotte: And after, we will	Charlotte is pointing out	she says "that and that"?
<u>Charlotte</u> : That and that means multiplication?	do		Teacher: No, in fact
	Teacher: Yes!		Researcher: For you, that
Teacher: Yes! Teacher: Well, we multiply	Charlotte: That and that		means multiplication?
	Teacher: Yes!		Teacher: Well, we multiply

<u>Charlotte</u>: And that... <u>Teacher</u>: Yes! <u>Charlotte</u>: And that... <u>Teacher</u>: And yes! Gerald: teacher, I don't mean that! that and that, we have to "do"...

<u>Researcher</u>: She said "do", she didn't say "multiply"? <u>Teacher</u>: Mm... But in fact, when she showed me the numbers, when she made those gestures "that and that", I said yes! <u>Researcher</u>: What does it mean, that? <u>Teacher</u>: That there is a

relationship between the two!

1

Pupils' individual actions. Between the 20th and 25th minute, Charlotte, Gerald, Justine and Gregory came up with some ideas (Table 6). Gerald, Justine and Gregory suggested division. Charlotte thought that the problem contained a "trick" and assumed that she had found it. Gerald quickly abandoned his suggestion to divide, which was ignored by the teacher.

Together with Justine, he interpreted the measurements totally ignoring the notion of 7 scale, and decided that the biggest "real car" would be the one corresponding to the 8 model with bigger dimensions. Justine's, Charlotte's and Gerald's preoccupations at that 9 moment were: (a) to suggest division as a possible way to solution, (b) to obtain 10 validation, (c) to facilitate the task, and (d) to make a good impression. Four pupils in the 11 12 group assumed that math operations were required to solve the problem. Gerald, Justine and Gregory suggested division, Charlotte a sum. Charlotte's preoccupations were: (a) to 13 find a hidden trick, and (b) to make a good impression. 14

15

16 **Table 6.** Classroom verbalizations (Minutes 20 to 25)

Classroom verbalizations	Video and Behaviours description
Justine: Teacher, I think I've found something.	The teacher leans over the four pupils.

Gerald: 22 divided by 7.	She listens to their suggestions.
Justine: For the22 divided by 7.	Gerald looks in turn at the teacher,
Gregory: 3 leaves 1. Yes: 3 times 7 is 21, leaves 1.	Justine, Gregory and Charlotte while
Charlotte: I've found a trick! I've found a trick!	they are speaking. Charlotte leans
Teacher: So	towards the teacher, and, smiling, talks
Charlotte: I've found the trick, Teacher!	to her.
Teacher: Why do you believe there's a trick,	
Charlotte?	
<u>Charlotte</u> : Well, because there, it makes 1/20	
Teacher: Yes	
Charlotte: And that there, 1/40.	Charlotte points out the scales in the
<u>Teacher</u> : 45, yes	text of the problem.
Charlotte: 45	Gerald turns to the teacher and raises
Teacher: Yes.	his hand before speaking to her.
Gerald: Ah, I think I've got it, Teacher!	
Charlotte: And, since it's not the same number, it	
can't be that this one bigger because already there,	
it's 2 cm and there it's 7 cm. So, you need to add	Charlotte looks at the teacher, waiting.
something and it'll increase the number	Gerald turns again to the teacher,
Gerald: Teacher, I think I've got it!	raises his hand before speaking.
Teacher: You believed right from the start that the	Justine points out the text of the
two cars are not the same?	problem with her finger. The teacher
Justine: Well, no, no. This one is smaller because	listens and then leans over Charlotte.
9 cm and 3.2 cm. And that this one is 22 and 7 cm.	
Charlotte: So if you add this and that it will give a	Gerald takes advantage of a brief
result. And there is something we have to add	moment of silence to speak up.
here. But I don't know what	
Gerald: No. Otherwise, Teacher, we should do a	
40, a 45, divided by 20	
Charlotte: No, but that's not what I mean. It's just	
that, there isIt looks like there, it's this one	

that's going to win. Because if you add things on to this, it'll give a big result and we'll drop this one... <u>Teacher</u>: And what makes you say that it will give

a big result?

<u>Charlotte</u>: I don't know, I don't know: that's the way it is!

1

2 Justine indicated that 1 cm on the model corresponded to 45 cm of the actual car surface. She came close to the expected solution. She unsuccessfully tried to explain to 3 the teacher (minute 35) that the ratio 1: 45 could be added as many times as necessary. 4 She suggested a solution which involved adding the number that corresponded to 1 cm on 5 the scale. The teacher did not understand Justine's reasoning and thus did not realize that 6 she had almost found a solution. In this situation, Justine's preoccupations are the 7 8 following: (a) to use an iterative addition method to solve a problem and (b) to obtain a positive validation. 9

In the 54th minute, after the teacher had highlighted important numbers, Gerald immediately suggested a solution. He kept searching for a solution despite the teacher's repetitive demands for explanation and her rejections of his answers. His preoccupations were: (a) *to suggest a solution which involved calculating the perimeter* and (b) *to obtain positive validation*.

15 Charlotte then implicitly indicated her solution. She pointed to the numbers on the 16 problem sheet, accompanying her gestures with successive deictics ("*that and that*"). She 17 was careful about indicating the numbers to be used in an equation and did not provide an 18 equation that expressed the relationship between these numbers. She assumed that her 19 explanation was sufficient for the teacher. Her preoccupations were: (a) *to offer a* 20 *solution based on multiplication* and (b) *to obtain positive validation*.

21

The configuration of activity

The configuration of activity can be described from the individual action of the teacher and pupils. This section discusses the three dimensions of the configuration of activity: a process that emerges from (a) the coupling of individual actions and (b) the
points of articulation meaningful to the agents; and (c) a process that creates balance and
emerging order.

4

5 **Pupils' inquiry and its coupling with the teacher's action**.

The analysis of the pupils' courses-of-action demonstrates their attempts to find a
solution to the problem. In their search, they proceeded with a pragmatic inquiry (Dewey
1938/1963) whose progress was slow and complex; they used all available clues,
considering and abandoning many leads and, exploring until they found the solution.

10 At first, they thought that the answer was contained in the text. They assumed that a bigger "real car" would be the one with bigger measurements. They knew that some 11 12 problems could contain traps: Charlotte tried to figure out a possible trap. When Charlotte and Gerald's first suggestions were rejected by the teacher, the pupils continued their 13 14 search for (a) the correct equation and (b) the right numbers to use. They suggested addition, division and multiplication, manipulating the numbers in different ways. It 15 16 should be noted that the problem was composed by the teacher which led to her setting up her own expectation structure (to work out the problem, one needs to multiply the 17 18 dimensions of each model by its respective scale and then compare the results). This expectation structure led her to invalidate any proposals that did not rely on 19 20 multiplication, as not conforming to her expectations.

The students finally thought of multiplication: their proposals of addition had been invalidated (minutes 24, 34), as well as those of division (minutes 20, 35, 38). From minute 38 on, all the proposals were exclusively about multiplication. They then looked for the numbers to multiply. The hints given by the teacher were aimed at bringing them to successive multiplications (minute 42). Two students wanted to multiply 45 by 2. But this idea was not accepted, and the students did not grasp that 45 needed to be multiplied by 9 and then by 3.2.

In the 54th minute, Gerald came up with a solution: he suggested multiplying numbers to calculate what he called the "perimeter". He made an equation using the highlighted numbers. He realized that the nature of the model measurements (length and width) and their spatial grouping were *affordances* (Gibson, 1979; Norman, 1993), that is, the available resources. These measurements reminded him of another classroom work
that involved finding the perimeter and area of polygons. Unfortunately, he confused the
two notions.

Finally, Charlotte suggested her solution: she pointed to the numbers she was using
two by two. She did not demonstrate the equation because she assumed that her reasoning
was obvious to the teacher.

The pupils' proposals were made on the basis of diverse clues in association with the 7 teacher's actions, the actions of their classmates, and some elements found in the text as 8 clues: teacher's validations or invalidations and explanations, her mimics and solutions 9 offered by the pupils from the same group and from other groups, and the location of the 10 numbers in the text. Gerald's suggestion (minute 54) was consistent with both the clues 11 12 collected during the inquiry (one has to multiply) and with his school culture ("something" can be calculated using the length and width of a polygon). Charlotte's 13 14 suggestion was also consistent: she did not demonstrate her equation because she assumed that the solution was obvious to the teacher. The protagonists had collectively 15 16 come to conclusion that in order to solve the problem, one had to multiply. All that she had to do was to correctly indicate the numbers that had to be multiplied. Charlotte's 17 18 suggestion was also supported by a topological clue: the symmetrical organization of the 19 data on the problem sheet was an *affordance* for her, indicating the relation between the 20 measurements and the scales.

21

22 The configuration of mathematics inquiry activity

The configuration of activity emerges from the points of articulation between 23 24 individual actions of teacher and pupils. Individual actions are made possible in return by 25 these points of articulation. This concept accounts for the dynamic character of situational constraints which link the teacher and pupils by multiple "reciprocal dependencies" and 26 thus contribute to forming a collective. They thus allow for the emergence of the form 27 which inversely makes them possible. Articulation points are the situational constraints 28 29 that are meaningful to the teacher and pupils: (a) the nature of the pupils' work, (b) its spatiotemporal organization, (c) the presence and functioning of artefacts, and (d) the 30 types of interaction between agents. These constraints are only meaningful to certain 31

agents, and even then, the meaning is attributed according to a personal and partial 1 interpretation: what is meaningful in the problem at a given moment to one pupil is not 2 necessarily meaningful to the others at the same moment. These constraints nevertheless 3 play an essential role as they contribute to the emergence, balance, and maintenance of 4 the configuration in the classroom. Mathematical problem-solving requires that the pupils 5 conduct an inquiry to diminish the level of uncertainty of the situation which is initially 6 confusing and unpredictable. This motivates them to search for clues, to suggest various 7 hypotheses and to construct guaranteed assertions (Dewey, 1938/1963) until the solution 8 is found. 9

The spatiotemporal organization of the classroom and the nature of the pupils' work 10 render possible both cooperation and competition. This organization is situated in the 11 12 school culture (Gallego, Cole, & The Laboratory of Comparative Human Cognition, 2001): the organization of groups is linked to the ideas of "constructivist pedagogy" that 13 are frequently evoked in teachers' training centres. Their inquiry is simultaneously 14 cooperative and competitive (Rognin, Salembier & Zouinar, 2000) within each group and 15 16 between groups. According to these authors, the agents cooperate when they are engaged side by side in verbal or non-verbal interactions, when their actions are coordinated and 17 18 synchronized, and when the aims they pursue are equally coordinated. The articulation between the preoccupations of helping and accomplishing classroom work contributes to 19 20 the production of mutual intelligibility and shared understanding, the characteristics of cooperative activity (Rognin, Salembier & Zouinar, 2000) that help to regulate 21 coordination between agents. Improvised and informal processes - of validation, the 22 institution of actions, inquiry – take over from mechanisms of adaptation and self-23 24 organization. This allows the protagonists to coordinate to accomplish tasks related to 25 problem-solving or text reading. The suggestions made out loud by pupils from one group, followed by the teachers' validation or invalidation, are taken into account by 26 pupils from other groups. The pupils' search for solutions is re-directed by their need for 27 validation. The suggestions are similar to probes sent toward the teacher to collect clues. 28 29 They enable the pupils to progressively diminish the complexity of the problem and to eliminate hypotheses. 30

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Moreover, when one group tries to draw the teacher's attention as she moves around,

suggestions come not from the group but from competing individuals: each pupil is trying to create a positive image of him- or herself. This competitive urge prevents them from putting their suggestions and findings in writing, and solutions are thus never sufficiently developed for the students to arrive at true "problem-solving". These proposals cannot be validated by the students themselves

The artefacts used in this configuration have cognitive functions. They structure 6 individual action and the articulation of individual actions (Norman, 1993). The teacher's 7 help is structured by the word problem, in particular by the expectation structure she has 8 developed. This idea corresponds to the problem- solving pedagogy, advocated by the 9 French Department of National Education. Moreover, the choice of complex numerical 10 data (measures and scales) prevents younger pupils from making mental equations. By 11 asking for a comparison of the two vehicles requires comparing two sets of data (4 12 measures and 2 scales), making it more difficult to establish a correct relationship 13 14 between numbers.

The teacher-pupil's interaction, characterized by the pupils' requests for validation, 15 16 and the validations-invalidations of the teacher, narrows down the field of possibilities for the pupils' inquiry. When the pupils make their suggestions, validation is more or less 17 18 explicitly requested. These requests facilitate their task, helping them to avoid wasted time on dead ends. The suggestions flow in quick succession due to the pupils' 19 20 competitive preoccupations and to their interpretations of the teacher's reactions to their suggestions. Validations and invalidations of pupils' suggestions are given frequently. 21 22 Their frequency avoids dead time, refocusing pupils' individual actions, and helping them avoid wrong leads. The frequency of help also allows maintaining pupils' involvement in 23 24 their schoolwork.

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26 The inquiry in mathematics: a balanced configuration of activity.

This configuration of activity presents a state of balance established between tensions. Tensions are provoked by (a) convergence – divergence of agents' preoccupations and (b) the constraints linked to the points of articulation in the configuration of activity. These two types of tension are closely articulated because constraints modify the agents' goals by opening and closing possibilities for action.

Pupils' preoccupations with obtaining validations, making a good impression, or 1 2 facilitating the task are articulated with the teacher's preoccupation with keeping them involved in a given task. These preoccupations are somewhat divergent: while the teacher 3 expects the pupils to be involved in a problem-solving task, stimulated by the need for the 4 right solution, the pupils expect the teacher's immediate validation, approval, or an easier 5 way to find the solution. However, these expectations transform into actions which, for 6 the teacher, manifest the pupils' involvement. At the same time, the teacher's 7 preoccupations with helping pupils and pupils' preoccupations with finding the solution 8 9 are largely convergent: they correspond to similar expectations, linked to the search for a correct answer. In spite of the profound divergence between some of the preoccupations 10 and expectations of the agents, a state of balance is achieved and the configuration 11 becomes viable. 12

Moreover, certain tensions in this configuration of activity are linked to points of 13 14 articulation and, in particular, to the use of a word problem and the forms of interaction in the classroom. The teacher's choices during the conception of this problem caused 15 16 substantial difficulties for the pupils. They considered a large number of calculations and relations between the numbers. This explains the long duration of their inquiry (85 min.), 17 18 a high number of incorrect answers, the recurring moments of discouragement, and the teacher's need to constantly sustain their involvement. However, this involvement did 19 20 remain high, and an hour later the pupils were still searching actively and suggesting solutions. At the same time, the problem itself became a factor of tension balance, 21 22 mediating the pupil's inquiry and the teacher's help.

The forms of interaction contribute to the balance of the configuration. They are 23 24 characterized by the opening of interaction windows (Gal-Petitfaux, 2003) that provide 25 possibilities for individual action. They contribute to the validation - invalidation of suggestions: when the teacher opens an interaction window with Charlotte (minute 20), 26 putting aside the suggestions of other pupils (Justine, Gerald and Gregory), they perceive 27 it as an implicit rejection of their suggestions. Moreover, when the teacher interacts with 28 29 one of the pupils, the opening of this interaction window allows the others to develop various preoccupations of searching for the solution, but also those of distraction. There 30 is no doubt that these forms of interaction are also supported by the constructivist 31

pedagogy taught in teachers' training centres. This pedagogical approach insists that the pupils have to "all learn by themselves" and to "construct their knowledge". And finally, these forms of interaction allow for the conduct of the inquiry and for the problem solving. In mathematics, they help achieve the state of relatively comfortable balance for the actors, enabling pupils to solve problems and the teachers to keep them involved in a given task..

7

Formalization of the notion of configuration of activity

8 Although configurations of activity were studied during a mathematics lesson in 9 primary school, they concern all types of social activities. We can observe their 10 emergence in the classroom during different lessons, on the field in team sports (Elias, 11 1966), in orchestras, offices, workshops, restaurants, etc.

In the classroom, configurations are limited in time by the teacher's and pupils' 12 individual actions and by the articulation of these actions. Therefore, even when the 13 teacher instructs the pupils to start working, it may be not sufficient: the pupils need to 14 become deeply involved in the task. In the classroom space or in specialized rooms, 15 configurations are limited by the phenomenal capabilities of the agents: they cannot see 16 through the classroom walls or hear farther than a few meters. These are shared situations 17 (Durand Saury & Sève, 2006), simultaneously experienced and given by the sensorial, 18 19 perceptive and cognitive capacities of the agents.

Although configurations are emergent forms, they may be embedded in both the 20 professional culture of teachers and the academic culture of pupils; in turn, their viability 21 22 (i.e. their stability-in-time associated with the possibility for both teacher and pupils to 23 satisfy their intentions) constitutes to and perpetuates these cultures. Their stability can also be explained by limitations of the teacher's intervention: configuration allows the 24 25 teacher to conciliate multiple and contradictory constraints in a multidimensional and 26 very complex task, as Doyle showed (1986), and we can hypothesize that the classroom configurations stability is linked to this aspect of teachers' work. 27

The emergent properties of configurations are not incompatible with the fact that the most viable configurations become components of the school culture (Gallego & al., 2001) which are inscribed in teachers and pupils' culture. These components of a local culture are "near at hand" every time the agent wants to act in a particular context. This
cultural inscription allows configurations to self-perpetuate in time and space through the
intermediation of agents' memory and the artefacts that transport them (Lemke, 2000): a
blackboard, a ruler, the desk arrangement — they all contribute to the emergence of
identical configurations of activity in different places and at different moments.

The agents have only slight and partial consciousness of these configurations, and the 6 configurations do not result essentially from the agents' conscious "determinations" (to 7 form work groups, to find a solution, etc.). But determinations, as well as knowledge (of 8 the problems of proportionality, etc.) and culture of both pupils (solving problems, 9 finding the calculations that need to be made, etc.) and teachers (ways of organizing 10 work, assigning tasks to pupils, etc.) (Gallego & al., 2001) form the material from which 11 12 the collective activity is configured. "Determinations", knowledge and culture contribute to the configurations that characterize an academic subject, a school grade, and even the 13 school in general. 14

Configurations of activity concern educational tasks, some of which are very old, 15 16 like collective oral reading or problem-solving. For example, configurations of the "taking turns" type are found in many school subjects. They persist in time and, when 17 18 needed, are reactivated by teachers who create certain conditions for their emergence. They are transported by artefacts (the blackboard, problem sheets, textbooks, etc.) that 19 20 ensure their semiotic function: artefacts are the memory of past actions and the support for rules of action and the typical way of doing things in school. In the history of 21 22 education, for example, configurations can be transformed by modifications of artefacts (textbooks) or the classroom space and by the slow evolution of norms and regulations in 23 24 the classroom.

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