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intrusions

intrusions

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10448, F-63000 Gelatine as a crustal analogue: Determining elastic properties for modelling magmatic intrusions

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Abstract

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Research Highlights

- 2-5wt% gelatine mixtures at 5-10◦C are good crustal analogues for dyke or sill experiments
- The Young's modulus gelatine solutions evolves with time to a plateau
- This Young's modulus plateau correlates linearly with gelatine concentration
- The time to plateau depends on the room temperature, gelatine thickness and its thermal diffusivity
- ACCEPTED MANUSCRIPT • Gelatine's fracture toughness has a surface energy of $\gamma_s=1.0\pm0.1$ $\rm Jm^{-2}$

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Key words: Gelatine, Dyke, Sill, Magma, Analogue Scaling

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1 Introduction

 Analogue experimentation is an important technique in science and engineer- ing. In practice, it is the selection of appropriate analogue materials that is often the biggest challenge in developing a set of experiments that are geomet- rically, kinematically and dynamically scaled (sensu Hubbert (1937)). Exper- iments that meet these criteria can be considered a laboratory-scale version of the natural counterpart. In this paper we detail a series of experiments carried out to document the properties of gelatine, a widely used analogue for the Earth's crust.

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ggest challenge in developing a set of experiments that are
matically and dynamically scaled (*sensu* Hubb Gelatine is an ideal analogue for those modelling homogeneous, isotropic and $_{11}$ elastic materials, for example it has been used by mechanical engineers (e.g.Crisp (1952); Richards and Mark (1966)) and as a biological tissue analogue in the medical sciences (e.g. Righetti et al. (2004)). The use of gelatine in geological sciences has taken advantage of both its elastic and viscous properties, prov- ing especially fruitful in developing our understanding magmatic intrusions (dykes and sills) of volcanic feeder systems and their propagation dynamics in the Earth's brittle and elastic crust (e.g. Fiske and Jackson (1972); Pol- lard (1973); Pollard and Johnson (1973); Maaløe (1987); Hyndman and Alt (1987); McGuire and Pullen (1989); Takada (1990); Heimpel and Olson (1994); Takada (1994); McLeod and Tait (1999); Takada (1999); Dahm (2000); Muller $_{21}$ et al. (2001); Menand and Tait (2001); Ito and Martel (2002); Watanabe et al. (2002); Menand and Tait (2002); Walter and Troll (2003); Acocella and Tibaldi $23 \quad (2005)$; Rivalta et al. (2005); Cañón-Tapia and Merle (2006); Kavanagh et al. (2006); Mathieu et al. (2008); Kervyn et al. (2009); Menand et al. (2010); $_{25}$ Maccaferri et al. (2010); Taisne and Tait (2011); Taisne et al. (2011)). The photoelastic properties of gelatine have been of particular use to experimental

 geologists (e.g. Taisne and Tait (2011)) and civil engineers (e.g Farquharson and Hennes (1940); Crisp (1952); Tan (1947); Richards and Mark (1966)), where the internal stresses of a deformed gelatine can be visualised with the aid of polarised light. The prolific use of gelatine in the food industry has made a wealth of information available on its rheological properties (e.g.Watase and Nishinari (1980)). However, relatively few studies have documented the elastic properties of gelatine or how these evolve with time (e.g. Di Giuseppe et al. (2009)

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1980)). However, relatively few studies ha We present results from a series of experiments that investigate the elastic properties of gelatine over a range of concentrations and volumes. Firstly the material properties of gelatine are detailed, followed by a description of the experimental setup and the theoretical basis for our measurements. The ac- curacy to which the experimentalist can determine the Young's modulus of the gelatine is evaluated by considering the uncertainties involved in the mea- surement, the effect of the properties of the applied load used to make the measurements and any apparatus side-wall or floor effects. In particular, our experimental results are focused on how the Young's modulus of the gelatine evolves with time. We also determined the gelatine's fracture toughness, a measure of the material's resistance to the growth of a crack. To aid the ap- plication of the results, we present some scaling laws that are appropriate for the use of gelatine as an analogue for the Earth's crust in geological studies focused on the formation controls and propagation dynamics of magma-filled fractures.

2 Material Properties

a polypeptide tormed from the hydrolytic degradation
Murphy, 1992). It is classified as a 'physical gel' (e.g. 1)), meaning that during gelification Van der Waals force
ment of a complex and continuously connected three-di Gelatine is a polypeptide formed from the hydrolytic degradation of colla- gen (Ross-Murphy, 1992). It is classified as a 'physical gel' (e.g. Peyrelasse et al. (1996)), meaning that during gelification Van der Waals forces lead to the development of a complex and continuously connected three-dimensional network (lattice) of macromolecules (Djabourov et al., 1988a). The hydrogen bonds that are formed in this process are reversible and can be broken by changing temperature or pH (Djabourov et al., 1988b). From the onset, those working with gelatine have commented on its "fickle" nature (Richards and Mark, 1966). In order to use this material for quantitative modelling purposes, control needs to be kept on a range of factors including temperature, pH and gelatine concentration.

 Gelatine is a viscoelastic material so during deformation it can display both elastic and viscous behaviour. High stresses applied for a short timescale cause the gelatine to behave elastically, whereas small stresses applied over a long time period will produce a viscous response. Viscoelasticity is traditionally modelled with an arrangement of springs and dashpots that can reproduce a measured creep curve (e.g. Richards and Mark (1966)). The proportion of 68 elastic to viscous behaviour can be quantified by a phase shift δ angle, also known as the "loss angle" (Mezger, 2002):

$$
\delta = \arctan \frac{G''}{G'} \tag{1}
$$

 π_1 where G" is the energy loss (viscous-related) and G" is the energy stored τ_2 (elastic-related) for a given strain or strain rate. δ is equal to 0° for an ideal- τ_3 elastic material and 90 \degree for an ideal-viscous material. The transition from

 viscously dominated to elastically dominated behaviour (or vice versa) occurs at the 'gel-point' (Djabourov et al., 1988b), which is the condition where elastic ⁷⁶ and viscous energies are equal $(G^{\prime\prime} = G^{\prime}, \delta = 45^{\circ})$. Gelatine is in the 'sol-state' π (fluid) when G" > G' and $\delta > 45^{\circ}$, but is in the 'gel-state' (solid) when G' > G" ⁷⁸ and $\delta < 45^{\circ}$ (Ross-Murphy, 1992; Nelson and Dealy, 1993; Mezger, 2002). For gelatine, this marked change in mechanical properties can be brought about by changing the extent of deformation (strain) or temperature; the gel-point itself depends on time, temperature and concentration (Askeland et al., 2010; Di Giuseppe et al., 2009).

oldigity and δ > 45°, but is in the 'gel-state' (solid) where α (G² > G³ and δ > 45°, but is in the 'gel-state' (solid) where α (Ross-Murphy, 1992; Nelson and Dealy, 1993; Mezger, is marked change in mecha The focus of this paper will be on the ideal-elastic behaviour of gelatine. ⁸⁴ When a 2.5 wt% gelatine mixture at 10 °C is deformed at low strain it has ⁸⁵ G' two orders of magnitude higher than G" and $\delta < 1^{\circ}$ (Di Giuseppe et al., 2009). At these conditions the material is in the 'gel-state' and it is possible to assume an almost ideal-elastic behaviour. When this is the case, Hooke's Law is obeyed and deformation is recoverable when high stresses are applied 89 over short timescales: the applied stress (σ) is proportional to strain (γ) and 90 independent of the strain rate $(\dot{\gamma})$.

 The elastic properties of a homogeneous and isotropic solid can be described ⁹² fully by a combination of the Young's modulus E (ratio of tensile stress to 93 tensile strain) and the Poisson's ratio ν (the relative contractive to expansive 94 response of the deformed material). For gelatine, $\nu \approx 0.5$ (e.g. Farguharson and Hennes (1940); Crisp (1952); Richards and Mark (1966); Righetti et al. (2004)) and is theoretically incompressible such that deformation results in no net volume change.

98 3 Experimental Set-up and Data Processing

3.1 Young's Modulus Experiments

 A series of twenty-six experiments were carried out to investigate the effect of time, gelatine concentration, volume, experimental apparatus dimensions and applied load properties on the calculated Young's modulus of solidified gelatine.

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solution was prepared by A gelatine solution was prepared by adding a measured quantity of approx- $_{105}$ imately 80 °C deionised water to the required weight of gelatine granules (260 Bloom, 20 Mesh, Pigskin Gelatine supplied by Gelita UK) to achieve the desired concentration (see Table 1). The use of deionised water is re- quired to produce a clear and transparent mixture which hinders bacterial growth, which would otherwise produce a cloudy appearance to the gelatine solid. This hot mixture was then poured into a specified container and any bubbles were removed from the surface using a spoon. To prohibit the for- mation of a toughened 'skin' on the gelatine surface by water evaporation, a thin layer of vegetable oil was poured on top. The container was then placed μ_1 into a temperature-controlled cold room at 5–10 °C (T_r), and the mixture 115 temperature (T_0) and time were recorded. The gelatine was left in the cold room for several hours until the mixture temperature had equilibrated with the surroundings.

 One way of calculating the gelatine's Young's modulus is to measure the de-flection imposed by a load applied to the gelatine's surface (Timoshenko and

Goodier, 1970):

$$
E = \frac{M_L g (1 - \nu^2)}{D_L w},\tag{2}
$$

122 where D_L is the diameter (m) of the cylindrical load, M_L is its mass (kg), w 123 is the displacement (m) caused, and q is the gravitational acceleration.

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s the diameter (m) of the cylindrical load, M_L is its ma
accement (m) caused, and g is the gravitational accelerat
nt of the Young's modulus commenced once the gelatine
a load placed on its free surface. The conta Measurement of the Young's modulus commenced once the gelatine was able to support a load placed on its free surface. The container was removed from the cold room to make the measurements and then replaced afterwards. All the oil was carefully removed from the surface of the gelatine prior to any mea- surement being taken, using a spoon and then paper towel in order to achieve complete contact between the load and the gelatine. The load was applied by carefully placing a rigid metallic cylinder of known mass and dimensions onto the gelatine surface (see Figure 1 for a schematic sketch of the experi- mental setup and Table 2 for experimental load properties). Using a digital micrometer attached to a fixed reference position, the displacement of the free 134 surface was measured (with an estimated error of ± 0.1 mm) and recorded by hand. The load was applied just prior to the measurement being made, and the total time in which it was in contact with the gelatine was approximately 30 seconds per measurement. E was calculated systematically for the duration of each experiment; measurements were made using each of the loads when possible approximately every one to two hours for up to 140 hours after the gelatine was prepared (nearly six days). For each time interval, the gelatine was at ambient room temperature for an interlude of less than ten minutes before being returned to the cold room. No experimental load was applied to ¹⁴³ the gelatine surface between time steps. The displacement measurement 'w' and the properties of the load were input into equation 2) to calculate the

Young's modulus of the gelatine solid.

Fine cold room T_r (5–10 °C), volume of gelatine V_{gel}
meter of the experimental container D_C (8.6–40.0 cm), th
 H_{gel} (4.1–27.0 cm), and applied load (with mass M_L of 25
eter D_L 20.0–85.6 mm) (see Tables 1 and 2) 146 The experimental series considers gelatine concentration C_{gel} (2-30 wt%), tem-¹⁴⁷ perature of the cold room T_r (5–10 °C), volume of gelatine V_{gel} (0.5 to 30 ¹⁴⁸ litres), diameter of the experimental container D_C (8.6–40.0 cm), thickness of ¹⁴⁹ the gelatine H_{gel} (4.1–27.0 cm), and applied load (with mass M_L of 25.5–2808.5 150 g and diameter D_L 20.0–85.6 mm) (see Tables 1 and 2). These experiments allowed the characterisation of the evolution of the Young's modulus of gela- tine over a range of conditions and for the factors affecting our measurements to be assessed.

3.2 Fracture Toughness Experiments

¹⁵⁵ The fracture toughness K_c is a measure of a material's resistance to the growth of a crack. The fracture toughness of gelatine solids was determined by ex- perimental means, measuring the pressure required to propagate an existing crack (following the analysis of Sneddon and Das (1971)). This experimen- tal method for calculating the fracture toughness of gelatine solid is briefly described by Menand and Tait (2002). However, the mathematical procedure is not detailed explicitly. Therefore, here we present the experimental proce- dure again and detail in the Appendix the mathematical method so that other experimentalists can replicate this.

 For these fracture-toughness experiments high-clarity pigskin-derived gelatine (acid, 200 bloom) was supplied in granular form by SKW Bio-Systems. The $_{166}$ gelatine mixture was prepared by first hydrating 5 to 8 wt% gelatine powder $\frac{1}{167}$ in distilled water, and then heating the solution to 60 °C until the powder was completely dissolved. Sodium hypochlorite was then added to the solution so

 that it contained 0.1 wt% of active chlorine, in order to prevent fungal and bacterial growth. This amount was kept small to minimise its potential effect on the gelatine mechanical properties.

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also a cubic acrylic tank (30 cm

ify for 48 hours at room temperature. A thin layer of silic

the gelatine surface in order to avoid evaporation durir

prevent the development of a gradient in The gelatine solution was poured into a cubic acrylic tank (30 cm wide) and left to solidify for 48 hours at room temperature. A thin layer of silicon oil was poured on the gelatine surface in order to avoid evaporation during solidifi- cation and prevent the development of a gradient in gelatine properties. The tank was only filled to two-thirds its height, immersing a metallic blade that was elliptical in cross-section and had been inserted 5 cm into the gelatine's base. The blade measured 20 cm in length with a 1 cm thickness at its base. Once the gelatine had solidified, the blade was carefully removed thus creating an empty edge-crack in the gelatine solid. Both the crack and the remaining part of the tank were then filled with water, and the tank was overturned so that in its final position the crack was oriented vertically and at the bottom of the gelatine solid (Figure 2a). An outlet enabled water to bleed off any excess pressure in the lower part of the tank, and so ensured the water pres- sure balanced precisely with the weight of the overlying gelatine. Thus there was no excess pressure within the crack. Moreover, the initial state of stress within the gelatine solid was hydrostatic. (The gelatine solid adheres to the ¹⁸⁸ tank walls and so there is no horizontal strain, $\epsilon_x = \epsilon_y = 0$. Using Hooke's law, the relationship between the three stress components is $\sigma_x = \sigma_y = \frac{\nu}{(1-\nu)}\sigma_z$; 190 and given that gelatine has a Poisson's ratio $\nu = 0.5$, $\sigma_x = \sigma_y = \sigma_z$.)

 These fracture toughness experiments were carried out at a room temperature ¹⁹² of 19 \pm 2^oC. At the beginning of an experiment, the Young's modulus of the gelatine was measured as described in Section 3.1 (using a load with diameter approximately one tenth of the tank width). The crack excess pressure was

Access the case of the tank remained nil. As more air entered

y increased until it was sufficient to fracture the gelatine

k (Figure 2c). The process was recorded by video car

ideo record the exact amount of air that w then increased by injecting air using a thin capillary which protruded into the crack (Figure 2b). During this injection of air, any excess water bled off ensuring that only the crack buoyancy increased; the excess pressure in the other water-filled part of the tank remained nil. As more air entered the crack, its buoyancy increased until it was sufficient to fracture the gelatine at the tip of the crack (Figure 2c). The process was recorded by video camera, and from this video record the exact amount of air that was present within the crack just prior to the gelatine fracture was measured. The Young's modulus of the gelatine was systematically varied between experiments, by changing the concentration of gelatine used during preparation, and the amount of air needed to propagate the initial crack was recorded, as summarised in Table 3.

 The fracturing of the gelatine solid was analysed within the Linear Elastic Fracture Mechanics framework, according to which a crack propagates once the stress intensity factor at its tip K_I exceeds the fracture toughness K_c of the solid host (Griffith, 1921). Measuring the height of air present in the crack enabled us to calculate the pressure distribution within the crack and thus the stress intensity factor at its tip following the method of Sneddon and Das (1971) (see Section 4.2 and Appendix). We thus measured the height of air just prior to the crack propagation, and equated the calculated stress intensity factor with the gelatine fracture toughness.

3.3 Data Processing

 Data processing was undertaken in order to identify and quantify potential sources of uncertainty in the Young's modulus measurements before analysing the results. To account for experimental uncertainties, both the effect of the dimensions of the applied load relative to the size of the experimental con tainer and also the effect of the propagation of errors in the Young's modulus calculation have been considered. A data weighting procedure has then been carried out before modelling the experimental results.

3.3.1 Effect of Applied Load and Container Size

 We calculate the Young's modulus of gelatine by measuring by how much its free surface is deformed by an applied load. In doing so, we effectively assume that the gelatine solid is semi-infinite. However, the finite lateral dimensions of the gelatine container and distance to its base may have an important effect by restricting the movement of the deformed gelatine.

contract and Container Size
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is deformed by an applied load. In doing so, we effective
datine solid is semi-infinite. However, the finite lateral d
ine container and d Figure 3 shows the relationship between the calculated Young's modulus and the relative size of the applied load diameter and the experiment container $231 \left(D_L/D_C\right)$. Data from eight experiments at one time interval are shown (22) ₂₃₂ hours curing at 10 $^{\circ}$ C). These experiments have equal gelatine concentration (2.5 wt\%) , but a range of volumes $(0.5-30 \text{ litres})$, measured by Loads 1–8 in ten container sizes (see Table 1). Pearson product-moment correlation coefficients (r) were calculated for each experiment:

$$
r = \frac{S_{xy}}{\sqrt{S_{xx}S_{yy}}},\tag{3}
$$

where

$$
S_{xx} = \sum (x - \overline{x})^2
$$
\n
$$
S_{yy} = \sum (y - \overline{y})^2
$$
\n
$$
S_{xy} = \sum (x - \overline{x})(y - \overline{y}), (4)
$$

239 and x and y are experimentally determined variables (in this case E and ²⁴⁰ D_L/D_C). The correlation coefficient ranges from -1 to +1; r=+1 indicates $_{241}$ a positive linear correlation, $r=-1$ suggests a negative linear correlation, and

of the contention is experiment 3, where $r=0.38$). Howe
0% the correlation is poor and in this region the experiment
10 of avoiding sidewall effects. Providing this is the case, e,
an be used to calculate the Young's mod ²⁴² $r=0$ when no correlation is found. In the region $D_L/D_C > 10\%$ the results ²⁴³ show a strong positive correlation $(r \geq 0.65)$, implying interaction between the applied load and container walls is producing artificially high Young's modulus ²⁴⁵ calculations (an exception is experiment 3, where $r=0.38$). However, when ²⁴⁶ $D_L/D_C < 10\%$ the correlation is poor and in this region the experimentalist can be confident of avoiding sidewall effects. Providing this is the case, equation 2 holds and can be used to calculate the Young's modulus of the gelatine. Note that from the experiments shown, only experiments with a larger volume (20– 30 litres) with Young's modulus measured with loads 3–8 fall into this category.

 The Young's modulus measurements may also be affected by the distance to the base of the experimental container. If we assume the gelatine is semi- infinite and behaves as a purely elastic solid, we can estimate the stresses variation with depth induced by a load applied to the surface. The largest 255 stress component induced by a load σ_0 is the vertical component σ_z , which can expressed as (Timoshenko and Goodier, 1970):

$$
\sigma_z = \sigma_0 \left[1 - \frac{8z^3}{\left(1 + 4z^2\right)^{3/2}} \right],\tag{5}
$$

²⁵⁸ where z has been normalised by the diameter of the load D_L . Following this expression, the stress induced by the load at a depth ten times its diameter is only 0.4% of that imposed by the load at the surface.

 We therefore recommend that both the lateral and vertical dimensions of the container be at least ten times the diameter of the load to avoid both container sidewall and base effects.

3.3.2 Propagation of Errors

 The uncertainty associated with the Young's modulus (equation 2) was cal- culated according to the principles of the 'Propagation of Errors' (Bevington and Robinson, 2003), where the relative error is expressed as:

$$
\frac{\Delta E}{E} = \sqrt{\left(\frac{\Delta M}{M}\right)^2 + \left(\frac{\Delta D_L}{D_L}\right)^2 + \left(\frac{\Delta w}{w}\right)^2},\tag{6}
$$

where:

270 w = $\beta + X_1 - X_0$. (7)

ording to the principles of the 'Propagation of Errors' (1

on, 2003), where the relative error is expressed as:
 $\sqrt{\left(\frac{\Delta M}{M}\right)^2 + \left(\frac{\Delta D_L}{D_L}\right)^2 + \left(\frac{\Delta w}{w}\right)^2},$ $+ X_1 - X_0.$ $+ X_1 - X_0.$ \bullet \bullet \bullet \bullet \bullet \bullet \bullet ²⁷¹ β is the thickness of the load, X_0 is the distance to the unloaded surface and X_1 ²⁷² is the distance to the surface of the applied load (both X_1 and X_0 are measured ²⁷³ relative to a fixed point of reference). Values of M, D_L , β , X_1 and X_0 used in the calculation are averages of three separate and successive measurements. β , X_1 and X_0 have independent random errors such that calculated values of ²⁷⁶ w have an absolute error (Δw) :

$$
\Delta w = \sqrt{\Delta \beta^2 + \Delta X_1^2 + \Delta X_0^2}.
$$
\n(8)

 Following this, the 'compound uncertainty' associated with each measurement $_{279}$ of w is calculated as ± 0.3 mm. As the Young's modulus of the gelatine in- creases with time, correspondingly the deflection caused by the applied load 281 decreases. Therefore the magnitude of w relative to Δw increases with time, as 282 does the compound uncertainty associated with $E(\Delta E/E)$. This is illustrated by the increasing size of the Young's modulus error-bars with time (Figure 4).

3.3.3 Weighting the data

oad (an average of three successive measurements). So for
te dataset from experiment 25 (4-litres of 2.5 wt% gelating d14 time intervals at which the Young's modulus vas
8 (where possible). The Young's modulus calculation At each time interval, E was calculated using the deflection caused by each individual load (an average of three successive measurements). So for example, ²⁸⁷ the complete dataset from experiment 25 (4-litres of 2.5 wt% gelatine; Figure 5) comprised 14 time intervals at which the Young's modulus was measured by loads 3–8 (where possible). The Young's modulus calculations were thus 290 based on a total of 294 measurements of X_0 and X_1 . In order that all the measurements for each experiment could be considered in the analysis, a data weighting process was carried out.

 To account for the uncertainties associated with each Young's modulus mea-²⁹⁴ surement, the data were weighted (W) taking into account both the precision of the measurement and also the applied load used to take the measurement. Table 4 shows the quantitative weightings (depending on the uncertainty in ²⁹⁷ E; $W_{\Delta E}$) and qualitative weightings (depending on the applied load used; $W_{\Delta Load}$).

 Weighting the Young's modulus data was straightforward, with high precision 300 data $(\Delta E/E \leq 5\%)$ being weighted most highly $(W_{\Delta E} = 8)$. In comparison, weighting the applied loads could only be done qualitatively. Loads 1, 2 and 302 8–11 had low weightings ($W_{\Delta Load} = 1$ or 2) as these had the highest D_L/D_C values and so their data were most likely to suffer from container sidewall ef-³⁰⁴ fects (see Figure 3). Loads 6 and 7 were also weighted poorly ($W_{\Delta Load} = 2$ and 4, respectively), as their relatively high thicknesses causing stability issues). Load 5 exerted the lowest pressure and so inflicted only a small deflection to the gelatine surface; this deflection became increasingly small (and so mea- sured with higher uncertainty) as the gelatine's Young's modulus increased 309 during cooling. Therefore, Load 5 was weighted relatively low $(W_{\Delta Load} = 4)$.

310 Loads 3 and 4 were weighted most highly $(W_{\Delta Load} = 8)$, deemed to have the most favourable balance between causing a deflection of the gelatine surface that could be measured to high precision, whilst experiencing minimal inter-action with the container sidewalls.

the container sidewalls.

the container sidewalls.
 \therefore the weights $(W_{\Delta E} + W_{\Delta Load})$ was used to give an overall

tum. This procedure enabled the 'best' data to bave the

n the modelling results, whilst enabling all the 314 The sum of the weights $(W_{\Delta E}+W_{\Delta Load})$ was used to give an overall weighting for each datum. This procedure enabled the 'best' data to have the strongest influence on the modelling results, whilst enabling all the data to be included in the analysis process.

4 Results

4.1 Young's Modulus of Gelatine

 By measuring the deflection caused by a load applied to the surface of the solidified gelatine, we have been able to document the evolution of the gela- tine's Young's modulus relative to a number of parameters. These will now be considered separately.

4.1.1 Effect of Time

³²⁵ Figure 5 shows the Young's modulus evolution with time of a 4-litre 2.5 wt% sse concentrated gelatine mixture kept at $5 \degree C$ (Experiment 25). The results show that, over the range of experimental conditions reported here, the gelatine is not able to support an applied load until it has a Young's modulus of approxi- mately 1000 Pa. The Young's modulus then evolves exponentially with time to reach a plateau maximum value after which, as long as the experimental con-ditions are unchanged, the Young's modulus can be considered approximately

 constant with time. This exponential relationship between Young's modulus of the gelatine and time was documented for all the experiments:

$$
E = E_{\infty} (1 - e^{-\frac{t}{\tau}}), \tag{9}
$$

 $\mathcal{L}_{\infty}(1-e^{-\frac{L}{\tau}})$,

(the Young's modulus plateau; Pa) and τ (hr) are both e

tants determined from the exponential fit, and t is time
 \mathcal{L}_{∞} and τ vary depending on V_{gel} , T_r and C_{gel} (see Tal

as 335 where E_{∞} (the Young's modulus plateau; Pa) and τ (hr) are both empirically 336 based constants determined from the exponential fit, and t is time (hr). The 337 values of E_{∞} and τ vary depending on V_{gel} , T_r and C_{gel} (see Table 5). As 338 it is not feasible to wait for E_{∞} to be reached during the timescale of an 339 experiment, we define $0.9E_{\infty}$ as an "effective" Young's modulus plateau and ³⁴⁰ $t_{0.9E_{\infty}}$ as the time taken to reach within 10% of E_{∞} . These values are provided as a guide for the experimentalist in Table 5. The only effects of decreasing ³⁴² the room temperature from 10 °C to 5 °C were to increase the rate of Young's 343 modulus increase with time and so decrease $t_{0.9E_{\infty}}$.

 The values of Young's modulus plateau reported on Table 5 were all measured with loads 3–8, so that in these experiments the height of gelatine was at least 2.7 times as large as the greatest load diameter. Therefore, according to equation (5), the stress at the base of the gelatine layer induced by the loads was less than 5% of their value, and the potential effect of the base of the tank on these values of Young's modulus plateau was neglected.

 It should be noted that both the use of deionised water and the storing of the $_{351}$ gelatine mixtures in a cold room (set at 5–10 °C) led to the inhibition of bac- terial growth in the media. Thorough cleaning of the experimental container was also vital. Following these methods, our data shows that once the gelatine mixtures have reached their plateau in Young's modulus they can maintain this up to 140 hours after the initiation of the experiment.

4.1.2 Effect of Concentration

³⁵⁷ For low concentrations ($\geq 2 \text{ wt}\%$ and $\lt 5 \text{ wt}\%$), the Young's modulus plateau (E_{∞}) of gelatine is linearly correlated with the concentration of the mixture ³⁵⁹ (with a Coefficient of Determination $R^2 = 0.9992$), as shown in Figure 6 for ³⁶⁰ equal V_{gel} and H_{gel} (Experiments 16, 25–28). Values of E_{∞} were calculated ac- cording to models fit to weighted Young's modulus data for a range of applied loads (see Section 4.1.1). It is unclear whether or not this linear relationship can be extrapolated to more highly concentrated gelatine mixtures.

latine is linearly correlated with the concentration of the
fficient of Determination $R^2 = 0.9992$), as shown in Fi
nd H_{gel} (Experiments 16, 25–28). Values of E_{∞} were calce
models fit to weighted Young's modulus $_{364}$ Highly concentrated mixtures of gelatine (\geqslant 5 wt%) proved difficult to work with, both in terms of preparing the experiments and then measuring their Young's moduli during the gelification process. During preparation of the mix- tures, difficulties were encountered dissolving such highly concentrated mix- tures and also removing all bubbles from the highly viscous solution was un- achievable so that creating a homogeneous solid was not possible. Once the mixtures were in the 'gel-state' additional problems arose when attempting to measure their Young's moduli. When the loads were applied to these very rigid solids they were insufficient to cause a deflection of the gelatine surface that could be measured precisely; even the heaviest applied loads (Loads 9–11, see Table 2) caused such small deflections that the calculated Young's modulus value would have very large errors.

 Due to the problems associated with these experiments we present only average Young's moduli for each experiment (Experiments 29–33); these were averaged from measurements taken from the time when the gelatine was deemed to have reached its Young's modulus plateau, an assumption verified by the lack of correlation between Young's modulus and time (indicated by a low r; see Table 6). The results suggest that more strongly concentrated gelatines have a higher

 Young's modulus plateau strength, though the associated standard deviations of the data were so large we were unable to evaluate whether this relationship continues the linear trend identified in Figure 6.

 The experimental setup and method described here to measure the Young's modulus of gelatine solids proved unsuitable for highly concentrated mixtures. In order to quantify the Young's modulus of highly concentrated gelatine 388 mixtures (≥ 5 wt% gelatine mixtures, where the Young's modulus $\geq 20,000$ Pa), equipment more often associated with measuring the strength of rocks would be required. These tests are however beyond the scope of this study.

$391 \quad 4.1.3$ Effect of Volume

mental setup and method described here to measure th
gelatine solids proved unsuitable for highly concentrated
 $>$ quantify the Young's modulus of highly concentrated
 \geq 5 wt% gelatine mixtures, where the Young's modulu 392 Volume appears to have no impact on the Young's modulus plateau (E_{∞}) of the gelatine mixtures, as experiments that used the same concentration 394 gelatine, stored at the same T_r , evolved to give the same value of E_∞ (± 500 Pa; 395 Figure 7). The small discrepancy between modelled values of E_{∞} is assumed to be related to errors associated with the properties of the applied load and the measuring technique, as described above (Section 3.3.1). There is a broadly positive correlation between the volume of gelatine and the time taken to reach the plateau in Young's modulus (modelled from the weighted data), i.e. larger volumes of gelatine take longer to reach their Young's modulus plateau.

4.1.4 Effect of Layer Thickness

 The time to reach the Young's modulus plateau value appears to correlate $\frac{403}{403}$ well with the time needed for the gelatine to cool down to T_r , and so we can use this correlation to predict the time an experimentalist would have

The algorithm of the set of PMP, PP or Perspex (PMMA)
fusivity for these thermoplastic polymers is about 10^{-7} m
gnitude lower than that of gelatine. Therefore, to a lead
solid cools down by conducting its heat through to wait until the gelatine Young's modulus has reached its plateau value. The thermal diffusivity of gelatine is assumed to be that of its solvent, that ⁴⁰⁷ is water: $\kappa = 1.4 \, 10^6 \, \text{m}^2 \, \text{s}^{-1}$. The different containers used in the Young's modulus experiments were made of PMP, PP or Perspex (PMMA), and the thermal diffusivity for these thermoplastic polymers is about 10^{-7} m² s⁻¹, one order of magnitude lower than that of gelatine. Therefore, to a leading order, a gelatine solid cools down by conducting its heat through its upper surface, $_{412}$ and the time t needed for thermal equilibrium is:

$$
t = \frac{H_{gel}^2}{\kappa},\tag{10}
$$

414 where H_{gel} is the height of the gelatine solid in the container. Figure 8 com-415 pares this cooling time with the time $t_{0.9E_{\infty}}$ taken to reach 90% of the Young's 416 modulus plateau E_{∞} for gelatine mixtures of various concentrations (2 wt%) 417 to 5 wt%), but all cured at the same temperature of 5 °C (Experiments 13–19 and 25–28, Table 1). We find reasonable agreement with a best linear fit:

$$
t_{0.9E_{\infty}} \simeq (29.0 \pm 8.7) + (2.6 \pm 1.2) \frac{H_{gel}^2}{\kappa}.
$$
\n(11)

 Equation (11) gives experimentalists a first-order estimate of the time they 421 would need to wait for before a 2 wt% to 5 wt% gelatine solid cured at 5 $°C$ reaches its Young's modulus plateau.

4.2 The fracture toughness of solidified gelatine

 The stress intensity factor K_I at the tip of a two-dimensional, edge crack of height h can be expressed as:

$$
K_I = \alpha \overline{\Delta P} \sqrt{\pi h},\tag{12}
$$

 where α is a dimensionless factor that accounts for the conditions at the solid boundary (Sneddon and Das, 1971; Lawn, 1993; Menand and Tait, 2002), and $\overline{\Delta P}$ denotes the averaged excess pressure within the crack:

$$
\overline{\Delta P} = \frac{1}{h} \int_{0}^{h} \Delta P(z) \, \mathrm{d}z,\tag{13}
$$

 $\frac{1}{h} \int_{0}^{h} \Delta P(z) dz$,
the vertical distance with origin at the reservoir-gelatine.
Determining the value of α is a mixed problem, which
dge of the elastic solid is a free boundary (Sneddon and D
case in our experime $\frac{431}{431}$ where z is the vertical distance with origin at the reservoir-gelatine interface (Figure 2a). Determining the value of α is a mixed problem, which simplifies when the edge of the elastic solid is a free boundary (Sneddon and Das, 1971), 434 as was the case in our experiments. We measured the value of the coefficient α using the method of Sneddon and Das (1971), summarized in the Appendix.

436 Griffith (1921) and Irwin (1957) showed that the fracture toughness K_c of an ideal elastic and brittle solid is related to its Young's modulus E by the following theoretical relationship:

$$
K_c = \sqrt{2\gamma_s E},\tag{14}
$$

 γ_s is the surface energy of the solid. This is the energy required to create a unit surface area within that solid, and is thought to depend only on the composition and temperature of the solid (Griffith, 1921).

 The calculated values of gelatine fracture toughness are shown in Figure 9. Despite some scattering, we find that equation 14 fits reasonably well these values, and that our best fit is:

$$
K_c = (1.4 \pm 0.1) \sqrt{E}.
$$
\n⁽¹⁵⁾

 This equation and Figure 9 show that provided the viscous behaviour of gela-tine solids is negligible and deforms essentially elastically, gelatine solids be-

449 have as ideal elastic and brittle solids in that their fracture toughness K_c and their Youngs modulus E follow the theoretical relationship (equation 14) expected for such solids.

We find a best estimate for the gelatine surface energy:

$$
\gamma_s = 1.0 \pm 0.2 \text{ J m}^{-2}. \tag{16}
$$

best estimate for the gelatine surface energy:
 $0 \pm 0.2 \text{ J m}^{-2}$.
 μ , this value is similar to the surface energy of brittle mornond $(\gamma_s = 6 \text{ J m}^{-2})$, silicon $(\gamma_s = 1.2 \text{ J m}^{-2})$, silicon $^{-2}$), silicon $^{-2}$), sil Remarkably, this value is similar to the surface energy of brittle monocrystals 455 such as diamond ($\gamma_s = 6$ J m⁻²), silicon ($\gamma_s = 1.2$ J m⁻²), silicon carbide ⁴⁵⁶ ($\gamma_s = 4$ J m⁻²), silica ($\gamma_s = 1$ J m⁻²), sapphire ($\gamma_s = 4$ J m⁻²), magnesium 457 oxide ($\gamma_s = 1.5 \text{ J m}^{-2}$), or lithium fluoride ($\gamma_s = 0.3 \text{ J m}^{-2}$) (Lawn, 1993). 458 We note, however, that in principle γ_s should depend on the composition and 459 temperature of the solid (Griffith, 1921), and so the exact value of γ_s may vary from one type of gelatine to the other. But given the rather small range of values for brittle monocrystals, which are also similar to that for gelatine, ⁴⁶² we believe $\gamma_s = 1.0 \pm 0.2$ J m⁻² is a fair estimate for acid, pig-skin derived gelatine with Bloom values between 200 and 260. Experiments carried at lower temperatures than reported here will either result in higher Youngs moduli or take less time to reach their Youngs modulus plateau, but their fracture toughness will scale correspondingly following equation 15.

5 Geological Applications

 Di Giuseppe et al. (2009) summarise the application of gelatine as an analogue material for studying tectonic scale processes. They concluded low concentra- tion gelatine mixtures (∼2.5 wt%) could be an appropriate analogue for upper crustal deformation experiments. Complementary to this, we now present scal-

 ing laws appropriate for studying magmatic intrusion dynamics. The scaling for this case is distinct to that presented by Di Giuseppe et al. (2009) as the stress and strain relations are different, and in particular the strain rates for dyke propagation are many order of magnitude faster than those of tectonic processes.

5.1 Scaling gelatine for experiments on dyke and sill propagation dynamics

gation are many order of magnitude faster than those contain reasons are districted, unto in particular and solutions and the manuscript and side propagation and dynamic similarity with its natural counterpart then can obs An ideal scaled experiment has an analogue material that obeys geomet- ric, kinematic and dynamic similarity with its natural counterpart (Hubbert, 1937); only then can observations and results of the experiment be used to un- derstand the behaviour of the natural system. Others workers have presented simple scalings for the use of gelatine in its elastic-state as a crustal analogue for studying the propagation dynamics of magma-filled fractures (Acocella ⁴⁸⁴ and Tibaldi, 2005; Cañón-Tapia and Merle, 2006). We now expand on these to present a comprehensive guide for scaling gelatine for this type of geological experiment.

 Unlike tectonic processes, which occur on a length scale comparable with the thickness of the crust, dyke propagation is characterised by a much smaller length scale. This characteristic length scale is the buoyancy length L_b , as defined by Taisne and Tait (2009), which is the length over which magma buoyancy driving ascent balances resistance from rock fracture:

$$
L = L_b = \left(\frac{K_c}{\Delta \rho g}\right)^{\frac{2}{3}},\tag{17}
$$

 ψ ₄₉₃ where L_b is the length of the buoyant head region of the propagating dyke, K_c is the fracture toughness of the intruded medium and $\Delta \rho$ is the density

 difference between the intruding fluid and its surroundings. Dyke propagation is determined by a local buoyancy balance in the inflated head region of the dike, independent of the total buoyancy of the magma column between source and tip (Lister and Kerr, 1991; Taisne and Tait, 2009). In this case the reduced ⁴⁹⁹ gravity (q') is the relevant parameter for scaling the dyke driving force:

$$
g' = \frac{\Delta \rho}{\rho_{solid}} g.
$$
\n(18)

 $_{501}$ The timescale for the experiments is obtained by combining L_b (equation 17) and g' (equation 18):

$$
T = \sqrt{\frac{L_b}{g'}} = \rho_{solid}^{\frac{1}{2}} K_c^{\frac{1}{3}} (\Delta \rho g)^{-\frac{5}{6}}, \qquad (19)
$$

and from this the dyke velocity scale follows easily:

$$
U = \frac{L_b}{T} = (\Delta \rho g)^{\frac{1}{6}} K_c^{\frac{1}{3}} \rho_{solid}^{-\frac{1}{2}}.
$$
\n(20)

there and Kerr, 1991; Taisne and Tait, 2009). In this case the relevant parameter for scaling the dyke driving for $\frac{\Delta \rho}{\rho} g$.

ale for the experiments is obtained by combining L_b (equation 18):
 $\frac{\overline{L_b}}{g'} = \rho_{solid}^$ This approach provides the appropriate scales (length, time and velocity) for each experiment, as one varies one parameter or another, and so provides the sos appropriate scaling factors $L^* = \frac{L_l}{L_n}$, $T^* = \frac{T_l}{T_n}$ and $U^* = \frac{U_l}{U_n}$:

$$
L^* = \left(\frac{K_c^*}{\Delta \rho^*}\right)^{\frac{2}{3}},\tag{21}
$$

510
$$
T^* = \rho_{solid}^{*\frac{1}{2}} K_c^{*\frac{1}{3}} (\Delta \rho^*)^{-\frac{5}{6}}, \qquad (22)
$$

$$
U^* = (\Delta \rho^*)^{\frac{1}{6}} K_c^* \frac{1}{3} \rho_{solid}^{* - \frac{1}{2}}, \tag{23}
$$

where [∗] refers to the ratio of the parameter values measured at the laboratory (subscript l) and natural (subscript n) scale.

 $_{514}$ Finally, the driving buoyancy pressure (P_b) scale for dykes is:

$$
P_b = \Delta \rho g L_b,\tag{24}
$$

 which leads to deformation of the host medium around the head of the dyke. The elastic pressure scale (P_e) associated with this deformation is:

$$
P_e = \frac{E}{2(1 - \nu^2)} \frac{\psi}{L_b},
$$
\n(25)

s to deformation of the host medium around the head of
pressure scale (P_e) associated with this deformation is:
 $\frac{E}{\nu(1-\nu^2)}\frac{\psi}{L_b}$,
 $d \nu$ are the Young's modulus and Poisson's ratio of the ele
 ν , and ψ is the where E and ν are the Young's modulus and Poisson's ratio of the elastic host, $\frac{520}{20}$ respectively, and ψ is the thickness (i.e. the opening) of the dyke head. These two stress scales balance each other during dyke propagation (e.g. Lister and Kerr (1991)), which gives:

$$
E = 2(1 - \nu^2) \Delta \rho g \frac{L_b^2}{\psi}.
$$
\n(26)

 The Poisson's ratio for gelatine solids is $\nu \approx 0.5$, whereas that of rocks lies 525 usually between 0.25 and 0.3. As a result, the factor $2(1-\nu^2)$ varies by 15–20% between nature and laboratory experiments, and the Young's modulus scale factor simplifies as:

$$
E^* = \Delta \rho^* L_b^* \left(\frac{L_b}{\psi}\right)^*.
$$
\n
$$
(27)
$$

 Strictly speaking, field measurements made on the geometry of fossilised dykes inform only on the final static state once solidification has taken place, and not on the geometry of propagating dykes. The discrepancy between the propa- gating and the final static geometry will certainly be important for those dykes that reached the surface because their thickness will decrease as magma erupts at the surface and elastic deformation of surrounding rocks is released. However, because of mass balance the discrepancy should be marginal for

 the majority of dykes, which stall in the crust and do not reach the surface; notwithstanding potential volume change due to solidification, the volume of a propagating dyke should be the same as the volume of a static dyke. This caveat aside, we can use the geometrical measurements made on solidified dykes as proxies for their geometry during propagation.

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coxies for their geometry during propagation.

Tatio $\frac{\psi}{L_b}$ of solidified dykes in nature is typically o ⁵⁴¹ The aspect ratio $\frac{\psi}{L_b}$ of solidified dykes in nature is typically of the order of $10^{-4} - 10^{-3}$ (e.g. Gudmundsson (2011); Kavanagh and Sparks (2011)), and μ ₅₄₃ on the order of $10^{-2} - 10^{-1}$ in gelatine experiments. Taking the following ⁵⁴⁴ values as representative for natural dykes: $K_c = 10^7$ Pa m¹, $\Delta \rho = 100$ kg ⁵⁴⁵ m⁻³, $\rho_{solid} = 2800 \text{ kg m}^{-3}$, and for experimental conditions: $K_c = 100 \text{ Pa m}^{\frac{1}{2}}$, 546 $\Delta \rho = 1000 \text{ kg m}^{-3}$ (air) or $\Delta \rho = 10 \text{ kg m}^{-3}$ (water), $\rho_{solid} = 1000 \text{ kg m}^{-3}$, one gets:

$$
L^* = 10^{-4}(air) \qquad \text{or} \qquad L^* = 2 \times 10^{-3}(water), \tag{28}
$$

$$
T^* = 2 \times 10^{-3} (air) \qquad \text{or} \qquad T^* = 9 \times 10^{-2} (water), \tag{29}
$$

$$
U^* = 5 \times 10^{-2} (air) \qquad \text{or} \qquad U^* = 2 \times 10^{-2} (water), \tag{30}
$$

$$
E^* = 10^{-6} - 10^{-5}(air) \qquad \text{or} \qquad E^* = 2 \times 10^{-6} - 2 \times 10^{-5}(water). (31)
$$

 $_{552}$ In the experiments, $L_l \simeq 5$ cm with air or $\simeq 1$ m with water; this corresponds in 553 nature to $L_n \simeq 500$ m, which seems reasonable. Likewise, a velocity of a couple of mm/s (water) or cm/s (air) in the experiments would give dyke velocities on the order of 0.1–0.5 m/s in nature, in good agreement with estimates of dykes velocities (White et al., 2011). As for elastic deformation, the Young's $_{557}$ modulus of rocks typically lies in the range $E_n = 10^9 - 10^{10}$ Pa, and so properly scaled experiments should involve gelatine solids with Young's modulus in the range $E_l = 10^3 - 10^5$ Pa when air is used as a magma analogue, or

 $E_l = 2 \times 10^3 - 2 \times 10^5$ Pa when water is used instead. Both ranges include values that have typically been used in dyke and sill experiments, and the data presented in this paper shows that $2-5$ wt% of gelatine is sufficient to reach this range of Young's modulus plateau (Figure 6).

 These calculations suggest gelatine experiments for magmatic intrusion prop- $\frac{1}{2}$ s₅₅₅ agation (dykes or sills) carried out at ~5–10 °C and with gelatine concen- trations of 2–5 wt% are adequately scaled geometrically, kinematically and dynamically.

6 Conclusions

ange of Young's modulus plateau (Figure 6).

alations suggest gelatine experiments for magnatic intrustes or sills) carried out at \sim 5-10 °C and with gelatin

2-5 wt% are adequately scaled geometrically, kinematy,

y.
 We present results from a series of experiments that quantify the evolution of the elastic properties of gelatine with time. At $5-10$ °C gelatine is in the 'gel- state', over the range of stresses and strain rates presented here, and behaves like a solid, with almost ideal-elastic deformation. The Young's modulus of gelatine evolves with time, modelled best by an exponential relationship, with E evolving to a plateau value that would theoretically be achieved after an infinite amount of time. At low gelatine concentrations ($\lt 5$ wt%) the plateau Young's modulus depends linearly on the concentration of gelatine, and differ- ent volumes of equally concentrated gelatine evolve to the same plateau value. The method we use to measure the Young's modulus of the gelatine requires that the diameter of the load is $\leq 10\%$ the diameter of the experimental con- tainer and thickness of the gelatine solid in order for side-wall and base effects to be avoided; larger dimensions relative to the gelatine solid will affect and lead to artificially high calculated values. Fracture toughness measurements show the K_c of gelatine follows the same relationship as ideal elastic-brittle

 solids: it is proportional to the square-root of the Young's modulus multiplied 585 by twice its surface energy, which was calculated experimentally as 1.0 ± 0.2 586 J m^{-2} .

and photoelastic properties of gelatine mean

e easily visualised and monitored, giving the experimenta

the propagation dynamics of magmatic intrusions. How

to be taken when using gelatine as an analogue for the

t. Thes The transparent nature and photoelastic properties of gelatine mean deforma- tions can be easily visualised and monitored, giving the experimental geologist insight into the propagation dynamics of magmatic intrusions. However, cau- tion needs to be taken when using gelatine as an analogue for the Earth's $_{591}$ elastic crust. These type of experiments are best carried out at 5–10 °C in order for the viscous component of gelatine's deformation behaviour to be negligible. At these temperatures gelatine is a good analogue for magmatic in- trusion propagation in Earth's elastic crust; using gelatine concentrations from $595 \text{ V} \textdegree$ 2–5 wt% will ensure gelatine is adequately scaled geometrically, kinematically and dynamically.

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reviewer are thanked for thoughtful comments which improved the manuscript.

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8 Appendix

611 In the fracture toughness experiments, the pressure distribution (ΔP) within the crack just prior to its propagation was:

$$
\Delta P(z) = (\rho_g - \rho_w) \, gz, \qquad 0 \le z \le z_l,\tag{32}
$$

$$
\Delta P(z) = \rho_g gz - \rho_w gz_l, \qquad z_l \le z \le h,\tag{33}
$$

Lure toughness experiments, the pressure distribution (Δ

ast prior to its propagation was:
 $= (\rho_g - \rho_w) gz$, $0 \le z \le z_l$,
 $= \rho_g gz - \rho_w gz_l$, $z_l \le z \le h$,

the level of the air-water interface within the crack (z_l

s full of 615 where z_l is the level of the air-water interface within the crack $(z_l = 0$ when 616 the crack is full of air), ρ_g and ρ_w are the density of the solid gelatine and 617 water, respectively. The density of air ρ_a is assumed to be negligible. Following 618 Sneddon and Das (1971), by expressing this crack excess pressure as $\Delta P(z)$ = ⁶¹⁹ $\overline{\Delta P} f(z)$, the value of α in equation (12) is then determined by calculating the 620 value $Λ(1)$, where Λ is the solution of the following integral:

621
$$
\Lambda(z) - \int_{0}^{1} \Lambda(u)L(z, u) du = \frac{2}{\pi} \int_{0}^{z} \frac{f(s) ds}{\sqrt{z^2 - s^2}}, \qquad 0 \le z \le 1,
$$
 (34)

 where z has been normalised with respect to the crack height h, u and s are integration variables, and:

$$
L(z, u) = \frac{16zu}{\pi^2} \left[\frac{z^2 + u^2}{(z^2 - u^2)^3} \ln\left(\frac{z}{u}\right) - \frac{1}{(z^2 - u^2)^2} \right], \quad \text{if } z \neq u,
$$
 (35)

and:

$$
L(z, u) = \frac{4}{3\pi^2 u}, \qquad \text{if } z = u. \tag{36}
$$

 Equation (34) was solved using the gaussian quadrature method. This leads to *n* linear equations:

$$
\Lambda(x_i) - \sum_{j=1}^n w_j L(x_i, x_j) \Lambda(x_j) = \frac{2}{\pi} \int_0^{x_i} \frac{f(s) \, \mathrm{d}s}{\sqrt{x_i^2 - s^2}}, \qquad (i = 1, 2, \dots, n), \quad (37)
$$

 $-\sum_{j=1}^{n} w_j L(x_i, x_j) \Lambda(x_j) = \frac{2}{\pi} \int_{0}^{\infty} \frac{f(s) ds}{\sqrt{x_i^2 - s^2}},$ (*i* = 1,2,..., *n*)

d in order to determine the values $\Lambda(x_1)$, $\Lambda(x_2)$, ..., $\Lambda(x_1, x_2,..., x_n$ and their respective weights $w_1, w_2,..., w_n$ (a

from Abram 630 to be solved in order to determine the values $\Lambda(x_1)$, $\Lambda(x_2)$, ..., $\Lambda(x_n)$, using ⁶³¹ the values $x_1, x_2, ..., x_n$ and their respective weights $w_1, w_2, ..., w_n$ (as listed in 632 Table 52.8 from Abramowitz and Stegun (1964)). The value of α is then:

$$
\alpha = \Lambda(1) = \frac{2}{\pi} \int_{0}^{1} \frac{f(s) \, ds}{\sqrt{1^2 - s^2}} + \sum_{j=1}^{n} w_j L(1, x_j) \Lambda(x_j).
$$
\n(38)

 The gelatine fracture toughness K_c was then equated with the stress intensity 635 factor (12), using the average excess pressure $\overline{\Delta P}$ measured just prior to the α ₆₃₆ crack propagation and the corresponding value of α (equation 38).

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CCEPTED MANUSCRIPT Table 1: Table of experimental conditions. C_{gel} = gelatine concentration (wt%), M_{gel} = mass of tested gelatine plus water mixture (kg), V_{gel} = volume of tested gelatine plus water mixture (litres), H_{gel} = thickness of gelatine mixture (± 0.5) cm), D_C = container diameter (± 0.1 cm), T_r = cold room temperature, T_0 = starting temperature of gelatine mixture $(\pm 0.5 \degree C)$. Experimental containers were circular in cross-section, except those indicated by [∗] which were square (measuring 40 cm x 40 cm) and † which were oblong (measuring 50 cm x 30 cm). H_{gel} was calculated retrospectively from the container surface area and tested volume.

Table 2: Properties of the experimental loads: $\beta =$ thickness (\pm 0.1 mm), M_L = mass of load (\pm 0.1 g), D_L = diameter of load (\pm 0.1 mm). In all cases the data are mean averages of three measurements. Loads are cylindrical.

 \overline{a}

Table 3: The values of gelatine fracture toughness K_c determined from eight successful experiments. z_l is the level of the air-water interface within the crack just prior to its propagation; $z_l = 0$ when the crack is full of air. $\overline{\Delta P}$ is the corresponding averaged excess pressure. The gelatine and water densities, ρ_g and ρ_w , were both measured to within 4 kg m⁻³ and 1 kg m⁻³, respectively, and the air level z_l to within 2.5 mm.

 \sharp The crack was initially 5.0 ± 0.2 cm high in all experiment, except in experiment 129 where it was 10 cm high.

$Quantitative\ W$	$\Delta E/E$ (%)	$W_{\Delta E}$
	$< \! 5$	8
	$5 - 10$	7
	$10 - 15$	$\sqrt{6}$
	$15\hbox{--}20$	$\overline{5}$
	$20 - 30$	$\overline{4}$
	$30 - 50$	$\overline{3}$
	$50 - 100$	$\overline{2}$
	>100	$\mathbf 1$
Qualitative \boldsymbol{W}	Applied Load	$W_{\Delta Load}$
	Load_1	$\mathbf{1}$
	Load ₂	$\mathbf{1}$
	Load ₃	8
	Load_4	8
	Load ₅	$\overline{4}$
	Load ₆	$\overline{4}$
	Load ₇	$\overline{2}$
	Load ₈	$\overline{2}$
	Load ₉	$\mathbf{1}$
	Load ₁ 0	$\mathbf{1}$
	Load ₁ 1	$\,1$

Table 4: Weightings (W) used to quantify the quality of Young's modulus measurement data. Quantitative-based weightings consider the uncertainty in $\Delta E/E$, whereas the effect of the load used to take the measurements could only be weighted qualitatively based on the results from Figure 2. The combined weightings $(W_{\Delta E} + W_{\Delta Load})$ are then used in the subsequent data analysis.

Table 5: Model results showing E_{∞} and τ values (correct to the nearest hour) for an exponential best-fit model $E = E_{\infty}(1 - e^{-\frac{t}{\tau}})$ of calculated gelatine Young's moduli against time for a select group of experiments with the same T_r (5 °C). As E_∞ can not be reached within the timescale of an experiment, we define $0.9E_{\infty}$ as an "effective" Young's modulus plateau. $t_{0.9E_{\infty}}$ is the time taken (correct to the nearest hour) to reach within 10% of E_{∞} . See Table 1 for experiment settings.

Table 6: Average Young's modulus of highly concentrated (≥ 5 wt%) gelatine mixtures. An average of 'n' measurements of the Young's modulus is shown $(\overline{E},$ correct to 2 s.f.), measurements were taken periodically using a range of applied loads for several hours after 16.5 hours curing at 5 ◦C. Calculated standard deviations (St. Dev.) indicate a high degree of uncertainty. The low Pierson Product-Moment Correlation Coefficients (r) suggests no correlation between the Young's modulus measurements and time, supporting the assumption that the measurements were all made when the Young's modulus had plateaued.

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Figure 1. Schematic illustration of the Young's modulus measurement procedure on a gelatine solid able to support an applied load. The deflection caused by a load placed on the surface of the solidified gelatine is measured, and this information is combined with the properties of the load to calculate the Young's modulus of the material.

Figure 2. Three successive photographs taken during a fracture-toughness experiment. (a) An edge-crack is initially created at the base of a gelatine solid, and filled with water. The initial reservoir pressure matches exactly the weight of the overlying gelatine solid. (b) Air is injected through a capillary and within the crack. Any potential reservoir excess pressure is released, so that only the crack buoyancy increases during air injection (see text). (c) When the crack buoyancy is high enough, the air-filled crack fractures the gelatine and propagates vertically.

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ith the properties of the load to calculate the Young's mod

here successive photographs taken during a fracture-toughn

nedge-crack is initially created throug Figure 3. Young's modulus (E) of 2.5 wt% gelatine solids, after approximately 22 hours curing at 10 ◦C, plotted against the diameter of the applied load relative to the diameter of the container (D_L/D_C) for loads 1-8 (Table 2) and five container sizes (Table 1). In the region $D_L/D_C > 10\%$ (unshaded) each experiment individually shows a positive correlation between E and D_L/D_C (see legend for Pearson product-moment correlation coefficients), indicating interaction between the load and container could produce artificially high calculated Young's moduli. Where D_L/D_C \lesssim 10% (shaded) there appears to be no correlation between E and D_L/D_C , and here sidewall affects can be neglected. When no error bars can be seen, the error is smaller than the symbol size.

Figure 4. Young's modulus evolution with time of 4-litres of 3 wt% gelatine stored at 5 °C (Experiment 26). The Young's modulus was calculated from the deflection caused to the gelatine surface by Load 3 (see Table 2). Error bars show the uncertainty in E increases with time.

Figure 5. Young's modulus evolution with time of 4-litres of 2.5 $\text{wt}\%$ gelatine stored at 5 ◦C (Experiment 25). The Young's modulus was calculated from the deflection caused to the gelatine surface by a range of applied loads (loads 3-8; see Table 2). An exponential relationship best fits the data $(E = E_{\infty}(1 - e^{-\frac{t}{\tau}}))$, where $E_{\infty} = 7003$ Pa and $\tau=19$ hr). E increases with time to an "effective plateau" (0.9 E_{∞}) of 6300 Pa after 44 hours curing $(t_{0.9E_{\infty}})$. The best-fit model (solid line) takes into account all measurements weighted according to $\Delta E/E$ and the load used (see Table 4). The outliers at ∼55 hours and ∼98 hours are from Load 7; these data have low weighting on the fitted trend due to this load having high thickness and small diameter that caused stability issues.

Figure 6. Modelled plateau Young's modulus (E_{∞}) of a range of gelatine concentrations C_{gel} (Experiments 16, 25–28). Each test volume was 4-litres and was kept at 5 °C (T_r) in an equivalent container. The best-fit model indicates there is a positive– linear correlation ($R^2 = 0.9992$) between E_{∞} and C_{gel} . More concentrated gelatine mixtures reach a higher Young's modulus plateau.

Experiments 16, 25–28). Each test volume was 4-litres and was

a equivalent container. The best-fit model indicates there is a

ation $(R^2 = 0.9992)$ between E_{∞} and C_{gel} . More concentrate

ation $(R^2 = 0.9992)$ betw Figure 7. Relationship between the modelled Young's modulus plateau $(E_{\infty} \pm \Delta E_{\infty})$ and gelatine mixture volume V_{gel} for 2 wt% gelatine mixtures cured at 5 °C (Experiments 13–19). The mean E_{∞} (dashed line) is shown and is most closely modelled by the 4-litre experiment (Experiment 16). The Pearson product-moment correlation coefficient (r = 0.64) indicates there is little or no correlation between E_{∞} and V_{gel} . Gelatine mixtures of the same concentration (C_{gel}) evolve to the same $E_{\infty} \pm 500$ Pa independent of volume.

Figure 8. Comparison of the time $t_{0.9E_{\infty}}$ needed to reach 90% of the Young's modulus plateau E_{∞} , with the conductive cooling time H_{gel}^2/κ given by equation 10. Data points correspond to experiments 13 to 19 and 25 to 28 (Table 1). These experiments had gelatine concentrations between $2wt\%$ and $5wt\%$, and were all cured at $5 °C$. The plateau time appears to correlate linearly with the cooling time: the curve is the best linear fit, $t_{0.9E_{\infty}} \simeq (29.0 \pm 8.7) + (2.6 \pm 1.2) \frac{H_{gel}^2}{\kappa}$ (equation 11, $R^2 = 0.3211$); 95% confidence limits are indicated by dashed lines.

Figure 9. The fracture toughness K_c of gelatine solids as a function of their Young's modulus E. The curve is the best fit through the data: $K_c = (1.4 \pm 0.1) \sqrt{E}$ (equation 18, $R^2 = 0.8196$, with the 95% confidence limits (dashed lines).

Figure 2

Remineminesse

Figure 3

Figure 4

Figure 7

