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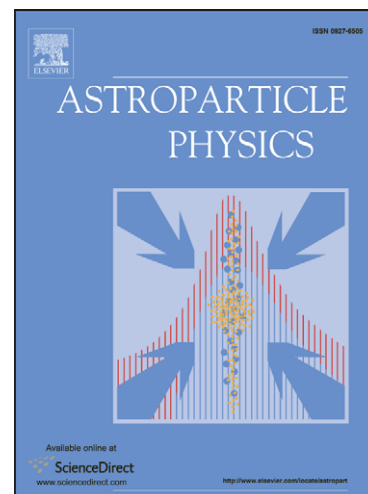
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Ultra High Energy Cosmic Rays: Anisotropies and Spectrum

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Abstract

The recent results of the Pierre Auger Observatory on the possible correlation of Ultra High Energy Cosmic Rays events and several nearby discrete sources could be the starting point of a new era with charged particles astronomy. In this paper we introduce a simple model to determine the effects of any local distribution of sources on the expected flux. We consider two populations of sources: faraway sources uniformly distributed and local point sources. We study the effects on the expected flux of the local distribution of sources, referring also to the set of astrophysical objects whose correlation with the Auger events is experimentally claimed.

1 Introduction

Ultra High Energy Cosmic Rays (UHECR) are the most energetic particles known in nature, with observed energies larger than 10^{18} eV. The detection of these particles, started already in the 50s with the pioneering experiments of Volcano Ranch in the USA and the Moscow University array in the USSR, poses many interesting questions mainly on their origin and chemical composition. In the recent years a new step forward in unveiling the nature of UHECR was done with the measurements performed by HiRes and AGASA first, and nowadays with the first results of the Pierre Auger Observatory in Argentina.

Soon after the discovery of the first UHECR event with energy around 10^{20} eV [1] it becomes clear that these extreme high energy particles could reach us only from the nearby universe; in other words, at the highest energies the universe contributing to the observed flux is definitively confined inside about 200 Mpc around us. In particular, if UHECR are mainly composed by protons, the interaction with the Cosmic Microwave Background (CMB) which produces a photo-pion production process, leads to the well known GZK suppression in the flux [2]. At energies around 5×10^{19} eV the visible universe in protons rapidly passes from Gpc scale to Mpc scale. On the other hand, if UHECR are mainly composed by nuclei, the photo-disintegration process suffered on astrophysical backgrounds (not only the CMB but also the Infrared/Optical Background (IRB)) causes

a strong depletion in the observed spectrum; this depletion occurs at energies that span from 2×10^{19} eV (for the lightest nuclei) up to 2×10^{20} in the case of Iron [3, 4]. At these energies, as for protons, the contributing universe rapidly decreases from Gpc to Mpc scale.

In the case in which the relatively nearby sources of UHECR are not uniformly distributed, as in the case of astrophysical sources, the arrival directions of the most energetics UHECR could reflect such anisotropy. This expectation depends mainly on the electrical charge of UHECR because of the effect of the intervening magnetic fields, in particular of the galactic magnetic field. In the case of protons the typical deflection angle on a μ -Gauss scale magnetic field and over Kpc distances is of the order of few degrees for particles with energy $E > 50$ EeV. With such angular resolution, inside distances at the Mpc scale, it is possible to resolve many interesting astrophysical objects that, according to several models, could be the sources of UHECR. Increasing the electric charge at $E > 50$ EeV, already in the case of Helium ($Z=2$), the deflection angle becomes larger than 10 degrees, arriving up to more than 50 degrees in the case of Iron ($Z=26$). Therefore, if UHECR are mainly composed by nuclei it will be nearly impossible to observe any correlation with sources.

Let us now discuss the experimental situation concerning signals of anisotropy in the arrival directions of UHECR. There are several experimental results that, in the past, claimed signals of anisotropy. In the energy range $0.1 < E < 10$ EeV an excess of events from the Galactic Center was reported by SUGAR and AGASA experiments [5]. This possibility was investigated also by the Pierre Auger collaboration that, with the data collected till March 2007, claimed a negative result that did not confirm the SUGAR and AGASA excess [6]. On the other hand, going to higher energies where the contributing universe is sensibly reduced, the AGASA collaboration searched for clusterings of events in the Northern sky founding a triplet whose chance probability was estimated to be of the order of 1% [7]. This triplet was found to be correlated with a HIRES high energy event [8]. The Pierre Auger collaboration found a deviation from isotropy for events above 52 EeV with a chance probability of less than 1% [9].

Another way of looking at anisotropy is to search for correlations in the direction of known astrophysical objects that could be the sources of UHECR. In this case, even if there is no excess over the expected background, the event sample could anyway exhibit a correlation with the direction of sources fixed a priori. In the past, searches of this kind were performed using a collection of data by different experiments and some hints of correlation were identified with a particular kind of AGN: the BL Lacertae objects (BL-Lacs), AGN with the jet pointed toward us [10]. This result was recently questioned by the Auger collaboration that performing the same search obtained a negative result [11]; it has to be pointed that the Auger observations refer to the southern hemisphere while all the other to the northern one.

Apart from the specific case of BL-Lacs, in general, there have been many speculations on whether AGNs are the actual sources of UHECR [12]. In this case the brightest and closest AGN could produce the UHECR observed on earth and the arrival directions of such particles could point back to their source. The large number of identified AGNs makes these objects a good candidate for studying possible correlations with UHECR.

The Auger collaboration performed a search for correlation of their events with AGNs from the 12th edition of the catalog of quasars and active galactic nuclei by Véron-Cetty and Véron [13] (VCV catalog). The correlation study is based on three main parameters: the maximum difference in angle between the UHECR arrival direction and the AGN

direction ψ_0 , the minimum energy of cosmic rays showing the correlation E_0 and the maximum red-shift of the correlated AGNs z_0 . Using the data collected between January 1 2004 and August 31 2007 the collaboration found that 20 out of 27 events correlated with at least one of the selected AGNs [14, 15]. In this analysis the parameters that minimize the probability of having a chance correlation with isotropic events were found to be $\psi_0 = 3.2^\circ$, $z_0 = 0.017$, $E_0 = 57$ EeV. An updated analysis of such correlation was performed with the cosmic rays events collected up to March 31 2009: 17 out of 44 independent events were found to correlate, within roughly the same choice of parameters of 2007. This updated analysis neither strengthens the case for anisotropy, nor does contradict the earlier results [16].

The HIRES collaborations performed the same analysis of the Auger collaboration for correlations between stereo events and AGNs from the VCV catalog but no significant correlation was found [17].

In the present paper, using the result of the Auger collaboration on correlations, we study the expected UHECR spectrum assuming that UHECR are mainly composed by protons. The dip model, proposed already in 2002 [18], is based on this assumption and explains the behavior of the observed spectrum by the pair-production energy losses suffered by protons on the CMB radiation field. Depending on the injection of protons at the source, the process of pair production on the CMB photons produces a dip in the expected spectrum on earth; this dip, placed in the energy range between 2×10^{18} and 4×10^{19} eV, is observed by different experiments: Akeno-AGASA, HiRes, Yakutsk [18].

The dip model was also studied in the framework of the results of the Auger collaboration; in [18] this comparison showed a good agreement of the Auger data of 2007 with the pair production dip. The new release of Auger data on the observed UHECR spectrum shows a steepening of the spectrum at the highest energies not much consistent with the predicted shape of the GZK cut-off, therefore showing a less significative agreement with a proton dominated spectrum [19]. Moreover, the chemical composition observed by the Auger collaboration favours a nuclei dominated spectrum progressively heavier in the energy region (4 - 40) EeV [20]. These two evidences have recently triggered a new possible explanation of the Auger flux in terms of a two component spectrum: a lighter (proton dominated) component at energies in the range (0.1 - 1) EeV and an heavier (nuclei dominated) component at higher energies [19]. Concerning energies below 10^{18} eV, some constraints can be found on the proton flux if the cosmic rays sources are optically thin and emit neutrinos [21].

A nuclei dominated spectrum at the highest energies is hardly compatible with the correlations observed by the Auger collaboration. In order to combine correlations and spectrum we consider here the case of a pure proton composition, with particles injected by two different classes of sources: homogeneously distributed at red-shift $z > z_0$ and a set of point sources at $z \leq z_0$. Our aim is also to determine possible features in the spectrum that can be connected with a particular local distribution of the sources.

The paper is organized as follows: in section 2 we discuss the model while in section 3 we compute the UHECR fluxes, studying also different choices for the contributing local sources; a discussion of the results and the conclusions take place in section 4.

2 The model

The approach used in this paper is based on the hypothesis of continuous energy losses (CEL) of the propagating protons. In the propagation through astrophysical backgrounds

(mainly CMB) the interaction of protons is naturally affected by fluctuations, with a non-zero probability for a particle to travel without losing energy. In the CEL approximation such fluctuations are neglected; as was shown in [18, 22, 23] this approach has a limited effect on the flux computation. Only at the highest energies ($E > 100$ EeV) fluctuations produce a deviation of the order of 10% of the CEL flux respect to the flux computed with a standard Monte Carlo simulation [23]. Under the CEL hypothesis the evolution of the proton energy is described by a simple differential equation, whose solution gives the proton energy $E_g(z)$ at any epoch z . One has:

$$\frac{dE_g(z)}{dz} = E_g(1+z)^3 \left| \frac{dt}{dz} \right| \beta_0((1+z)E_g), \quad (1)$$

being β_0 the rate of energy losses at red-shift zero suffered by protons on the CMB field, due to the processes of pair production and photo-pion production, as well as the losses suffered because of the adiabatic expansion of the Universe [18, 22]. The quantity dt/dz fixes the cosmology:

$$\left| \frac{dt}{dz} \right| = \frac{1}{H_0(1+z)\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}}, \quad (2)$$

where our choice for the Hubble constant and the matter/vacuum density are (throughout the whole paper) $H_0 = 70$ km/Mpc/s, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$.

Equation (1) can be solved fixing as initial condition the observed energy E on earth (at $z = 0$), obtaining the function $E_g(E, z)$ (with $E_g(E, z = 0) = E$).

As was shown in [18, 22, 23] the CEL hypothesis is very well suited to compute the expected flux of UHE protons from both a continuous distribution of sources as well as from a set of sparse point sources. In the present study, as discussed in the introduction, driven by the Auger collaboration results on anisotropy, we consider two different families of sources: continuous distributed at high red-shifts and a set of point sources in the local Universe. The red-shift z_0 that corresponds to the distance at which the distribution of UHECR events starts to feel the granularity of the local universe can be considered as a parameter of our building model. In our analysis we will consider two different possibilities to fix z_0 . In the first case we will directly refer to the Auger analysis, where z_0 is assumed to be the maximum red-shift of the AGNs, taken from the VCV catalog, whose position in the sky can be correlated with the Auger events. In this case, as measured by the Auger collaboration [9], the value is fixed to $z_0 = 0.017$. In the second case we will vary z_0 taking into account its physical role, as the maximum distance after which a distribution of UHECR sources, with a given number density, cannot be resolved by the detector in terms of single point sources, because of magnetic deflections. At energies larger than $E_0 = 57$ EeV the protons path length rapidly falls becoming less than 50 Mpc at $E > 100$ EeV. This fixes the scale of the parameter z_0 that should correspond to an angular distance not larger than $100 \div 300$ Mpc, therefore we will consider different values of z_0 in the range $z_0 = 0.01 \div 0.1$. In this context the choice of z_0 roughly corresponds to the so-called GZK sphere inside which the propagation of UHE protons is less affected by the photo-pion production process.

Let us now discuss the injection function associated to the sources. We will assume all sources of each population identical with injection given by:

$$Q(E_g) = k(\gamma_g) \frac{L}{m_p^2} (1+z)^m \left(\frac{E_g}{m_p} \right)^{-\gamma_g}, \quad (3)$$

being m_p the proton mass, L the source luminosity in UHECR, γ_g the injection power law index at the source, $k(\gamma_g)$ a normalization constant ($k(\gamma_g) = \gamma_g - 2$ for $\gamma_g > 2$ and

$k(\gamma_g) = [\ln(E_{max}/m_p)]^{-1}$ for $\gamma_g = 2$) and z the red-shift. The term $(1+z)^m$ describes the possible cosmological evolution of the source, i.e. the increase of luminosities and/or space densities with red-shift observed for many astronomical populations. In particular AGNs exhibit the evolution seen in radio, optical and X-ray observations (see [18] and references therein). Apart from L , γ_g and m another important parameter fixes the source behavior, namely the maximum energy that a proton can acquire at the source E_{max} . As we will discuss in the following this parameter is particularly important in fixing the flux behavior.

The first population of sources we consider here is a set of point sources with a steady isotropic emission and placed at different red-shifts (inside z_0) and along different directions. The flux of UHE protons produced by a single source at red-shift z^* can be written as [24]:

$$J_d(E, z^*) = \frac{1}{(4\pi)} \frac{Q_d(E_g(E, z^*))}{(1+z^*)(R(t_0)r)^2} \frac{\partial E_g(E, z^*)}{\partial E} \quad (4)$$

where Q_d is the injection function of a single local source, $E_g(E, z)$ is the solution of the losses equation (1) and $(\partial E_g/\partial E)$ is given in [18, 22]. Using as before the standard cosmology, the source distance as function of the red-shift is given by

$$R(t_0)r = \frac{c}{H_0} \int_0^{z^*} \frac{dz}{\sqrt{(1+z^3)\omega_m + \omega_\Lambda}}. \quad (5)$$

The flux of UHE protons produced by a homogeneous distribution of sources can be written as the integral over the comoving volume of the flux by a single source [18]:

$$J_h(E) = \frac{1}{(4\pi)^2} \int dV \frac{Q_h(E_g(E, z))}{(1+z)(R(t_0)r)^2} \frac{\partial E_g(E, z)}{\partial E}. \quad (6)$$

The quantity Q_h represents the number of particles injected per unit time, energy and volume by the homogeneous distribution of sources

$$Q_h = n_s Q_h(E_g) \Theta(z - z_0) = k(\gamma_g) \frac{\mathcal{L}_h}{m_p^2} (1+z)^m \left(\frac{E}{m_p^2} \right)^{-\gamma_g} \Theta(z - z_0) \quad (7)$$

being $\mathcal{L}_h = n_s L_h$ the emissivity of the homogeneous distributed sources, i.e. the number of particles injected (in UHECR) per unit time and volume. As discussed above, in equation (7) we have added a Θ -term because we assume the homogeneous distribution only at red-shift larger than z_0 . The (comoving) volume integral in equation (6) can be easily transformed in a red-shift integration [18], being the maximum red-shift of integration z_{max} the solution of the equation $E_g(E, z_{max}) = E_{max}$.

Let us point out that the flux (6) from homogeneously distributed sources is characterized only by the emissivity \mathcal{L}_h (number of particles emitted per unit time and volume), which entangles two physical informations: the luminosity of sources in UHECR and their number density. This fact is a natural consequence of the hypothesis of unresolved sources at red-shift $z > z_0$. On the other hand, in the case of local sources, the number of expected events depends only on the source luminosity as follows from equations (3) and (4), being the information on the sources number density already in the local (resolved) distribution.

As anticipated in the introduction, we are mainly interested in the effects on the UHECR flux of the local distribution of sources, therefore we should take into account

the number of events expected in a fixed direction. To compute it we introduce the relative acceptance ω of the detector following [25]. The number of the detected CR events are indeed distributed in the sky depending on both the real celestial anisotropy and the detector relative exposure ω .

The relative exposure, that depends only on the declination δ , is normalized as:

$$2\pi \int \omega(\delta) \cos \delta d\delta = \Delta\Omega_m ,$$

being $\Delta\Omega_m = \pi \sin^2 \theta_m$ and $\theta_m = 60^\circ$.

In the case of point sources the angular dependence of the expected flux will be also affected by the direction associated to the contributing source. Being $\hat{\Omega}^*$ this direction we can rewrite the expected flux taking into account its angular dependence as

$$4\pi J_d(E, z^*) \delta_D(\hat{\Omega} - \hat{\Omega}^*) ,$$

here and in the following δ_D is the Dirac delta function. The specific direction $\hat{\Omega}^*$ can be expressed in terms of the equatorial terrestrial coordinates (α, δ) simply using the transformation

$$\delta_D(\hat{\Omega} - \hat{\Omega}^*) = \frac{1}{\cos \delta} \delta_D(\alpha - \alpha^*) \delta_D(\delta - \delta^*) .$$

Taking into account the Auger observatory acceptance function and the angular dependence due to point sources, we can rewrite the total expected UHECR flux as a function of the equatorial terrestrial coordinates as:

$$J_{tot}(E, \alpha, \delta) = \omega(\delta) \left[J_h(E) + \sum_i J_d(E, z_i) \frac{4\pi}{\cos(\delta)} \delta_D(\alpha - \alpha_i) \delta_D(\delta - \delta_i) \right] , \quad (8)$$

being J_h the contribution to the flux due to the homogeneous distributed sources and J_d the flux of the local point sources placed at red-shifts z_i and with equatorial terrestrial coordinates (α_i, δ_i) . Using equation (8) it is possible to determine the number of events at energy $E \geq E_0$ expected to be collected during a time ΔT and in the whole field of view of the Auger observatory with an effective area S_{eff} :

$$N(\geq E_0) = S_{eff} \Delta T \int_0^{2\pi} d\alpha \int_{\delta_{min}}^{\delta_{max}} d\delta \int_{E_0} dE J_{tot}(E, \alpha, \delta) \cos \delta; \quad (9)$$

using equation (8) and the integrated acceptance of the experiment $\mathcal{E} = \Delta\Omega_m S_{eff} \Delta T$, we can rewrite equation (9) as

$$N(\geq E_0) = \mathcal{E} \left[\int_{E_0} dE J_h(E) + \frac{4\pi}{\Delta\Omega_m} \sum_i \omega(\delta_i) \int_{E_0} dE J_d(E, z_i) \right]. \quad (10)$$

As we will discuss in the next session, equation (10) will be used to normalize theoretical fluxes to the observations. Once determined its correct normalization to experimental data, we can compute the total expected flux in the whole field of view of the Auger observatory simply using equation (8), so that the total flux will be

$$\begin{aligned} J_{UHECR}(E) &= \frac{1}{\Delta\Omega_m} \int_0^{2\pi} d\alpha \int_{\delta_{min}}^{\delta_{max}} d\delta J_{tot}(E, \alpha, \delta) \cos \delta = \\ &= J_h(E) + \frac{4\pi}{\Delta\Omega_m} \sum_i \omega(\delta_i) J_d(E, z_i) \end{aligned} \quad (11)$$

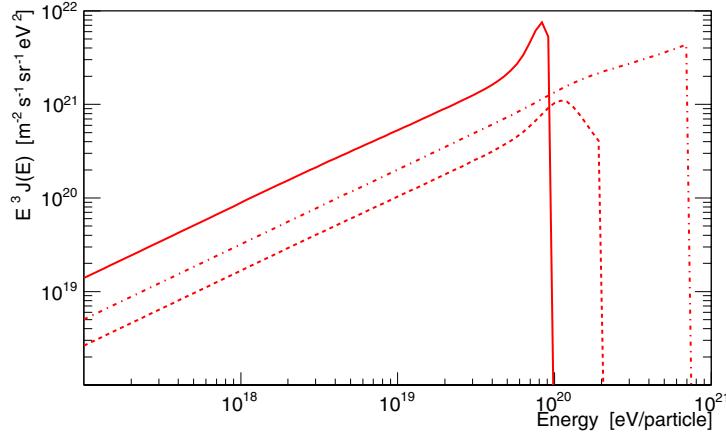


Figure 1: The calculated flux of UHECR (multiplied by E^3) from 3 sources of the Auger correlated sources (see text). The curves represent the spectra obtained taking into account the individual characteristics of Cen A ($z = 0.001$, $M_B = -14.4$, dot-dashed line), NGC 5506 ($z = 0.007$, $M_B = -17.9$, dashed line), NGC 7591 ($z = 0.017$, $M_B = -21.6$, full line), the injection parameters $\gamma = 2.2$, $E_{max} = 10^{21}$ eV, and cosmological evolution $m = 5$.

and the behavior of the expected flux J_{UHECR} can then be directly compared with the observed Auger spectrum. The second term in the right hand side of equation (11) depends on the particular distribution of local sources considered through their declinations, distances (red-shift) and intrinsic luminosity. In the next session we will discuss peculiar features that appear in the spectrum related to the particular distribution of local sources considered.

3 Fluxes

Following the analysis developed by the Auger collaboration, we will take the local sources from the 12th edition of the VCV catalog which includes the sources that contribute to the observed anisotropy in the Auger events. The correlation signal claimed by the Auger collaboration is based on the fact that the directions of 20 out of 27 UHECR events [15] collected between January 1 2004 and August 31 2007 with $E \geq 57$ EeV are correlated (within $\psi_0 = 3.2^\circ$) with the directions of astrophysical objects (with $z \leq z_0 = 0.017$) in the VCV catalog¹. It means that corresponding to the direction of 20 UHECR events there is at least one source in the catalog with these selection parameters. To select the actual source we consider the source power, choosing the most luminous (taking the absolute magnitude in the B band) corresponding to the direction of an individual UHECR event. Therefore we are implicitly assuming that UHECR luminosity is proportional to the photon luminosity.

In figure (1) we show the calculated fluxes of three sources of this list as an example. One can see the difference between the cut-off due to the different red-shifts of the AGNs, the fluxes being calculated with $E_{max} = 10^{21}$ eV and with the intrinsic luminosity of the source from the catalog. Our sample includes sources with absolute magnitude (in the B

¹In this paper we use the first Auger collaboration result on correlation since the list of correlated events reported in [15] is the only one available in literature.

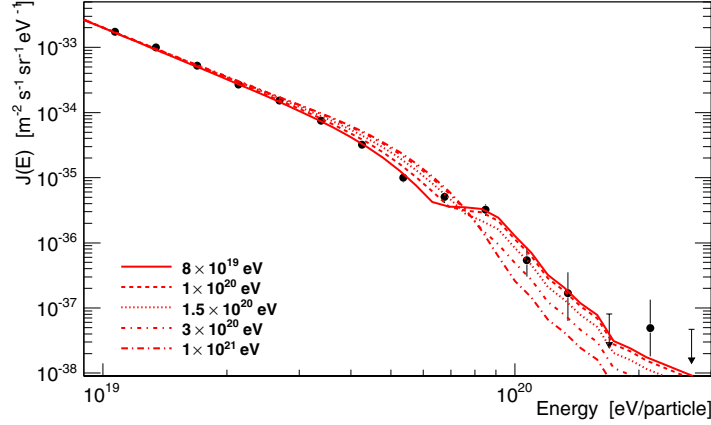


Figure 2: The calculated flux of UHECR as the sum of the two contributing populations with different values of the maximum injection energy for the homogeneous distribution, compared with the Auger spectrum (the upper limits correspond to 68% CL). The local sources are the VCV objects correlated with Auger highest energy events (see text). The maximum energy for the local sources is fixed at 10^{21} eV. All the models have been normalized fixing the observed number of events as specified in the text.

band) in the range $-21.6 < M_B < -14.4$, that corresponds to photon luminosity in the range $4.5 \times 10^{40} < L < 3.4 \times 10^{43}$ erg/s, with a mean value of 8.5×10^{42} erg/s.

Among injection parameters, the evolution constant m and the injection spectral index γ_g affect the shape of the spectrum to a large extent. A fit procedure to determine their best values, separating the two components, is difficult and rather uncertain because of their correlation. For simplicity we then assume the pair (γ_g, m) to be the same for the two source populations. It has to be pointed out that under this assumption the choice of the parameters is strongly guided by low energies ($E < 20 \div 30$ EeV) and therefore the parameter values are mainly fixed comparing theoretical spectra and Auger data in this energy region.

In the present paper we compare our theoretical results with the Auger spectrum released in 2009 [27, 28]. To allow a better agreement with the dip model [18] the Auger energy scale has been shifted towards higher energies by 20%². This shift is compatible with the systematic uncertainties in the energy determination quoted by the Auger collaboration and is also supported by a recent analysis of the muon content in the Auger data [29], which indicate an energy scale increased by about this factor. Using the Auger spectrum with the shifted energy scale we find a good agreement with our model in the scenario with a strong cosmological evolution ($m = 5$) and an injection power law index $\gamma_g = 2.2$. In the following we will always keep fixed these two parameters at the values quoted here, this assumption roughly agrees also with the recent spectrum analysis performed by the Auger collaboration [27].

To normalize the theoretical flux we determine the number of events corresponding to the Auger exposure equating to experimental data. Since we consider two populations of sources, we have to integrate separately the two fluxes in the high and low energy ranges. In the lower energy range ($3.8 < E < 48$ EeV) the total flux is dominated by the homogeneous distribution, while in the higher energy range ($60 < E < 240$ EeV) the local sources could play the leading role.

²Hereafter we will use for the Auger data this new energy scale.

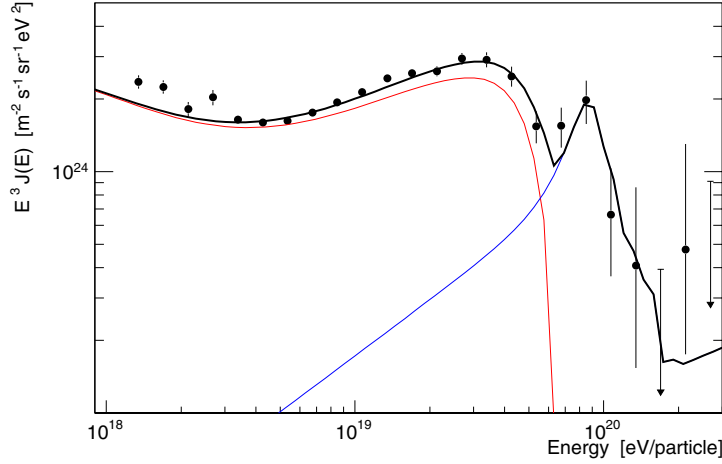


Figure 3: The calculated flux of UHECR as the sum (black line) of the two contributing populations multiplied by E^3 . The local sources are the VCV objects correlated with Auger (see text). E_{max} is 8×10^{19} eV for the homogeneous distribution (red line), 10^{21} eV for the local sources (blue line).

The crucial parameters that drive the flux behavior at the transition from a homogeneous to a local distribution of sources are the maximum energy E_{max} and the turning redshift z_0 . In the present paper we have considered a twofold analysis: fixing the value of z_0 , as in the Auger analysis, and varying the maximum energy of acceleration E_{max} or fixing the maximum energy varying the turning redshift z_0 . In the two following subsections we will discuss separately the results obtained under the two assumptions.

3.1 Maximum Energy Analysis

Let us start with the case in which the value of the turning redshift between local and homogeneous sources z_0 is fixed as in the Auger analysis. In this case $z_0 = 0.017$ corresponds to the redshift of the farther correlated source. This analysis assumes that the local discrete sources are only the sources that in the VCV catalog show a correlation with the Auger events. The best value for E_{max} of the local sources is 10^{21} eV. In figure (2) we show a comparison of the Auger data with theoretical spectra obtained through different choices of E_{max} for the homogeneous distribution of sources; the fluxes are normalized fixing the observed number of events as discussed above. The comparison with data above 3×10^{18} eV gives a χ^2/ndf of 0.45, 0.64, 1.3, 2.3, 2.7 for $E_{max} = 8 \times 10^{19}$, 1×10^{20} , 1.5×10^{20} , 3×10^{20} and 1×10^{21} eV respectively.

In order to develop our analysis we choose therefore the value of E_{max} for the homogeneous distribution that shows the best agreement with data: $E_{max_h} = 8 \times 10^{19}$ eV. It has to be noted that this choice is strongly driven by the small excess in the Auger spectrum data at 8.4×10^{19} eV (7×10^{19} eV with original energy scale). It lies at about $(1.5 \div 2)\sigma$ above the functions used to fit the spectrum [28], so the statistical significance of the excess is still rather poor and only new data can confirm or deny it.

We use as local sources the ones associated to the Auger correlated events. This list, obtained with the luminosity criterion described above, includes 17 independent sources since three of them are associated to two events. We use this set of independent sources. However we observe that even taking the 20 sources (with three repetitions among them) there are no substantial changes in the calculated flux apart minor differences at the high-

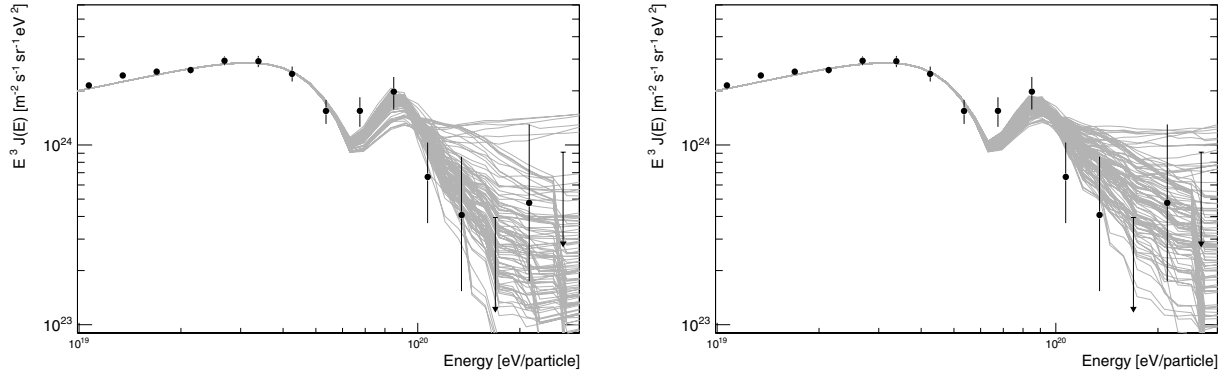


Figure 4: Left panel: the spectrum of UHECR multiplied by E^3 of 100 lists made of the 17 correlated sources and 8 sources extracted by the VCV catalog (with red-shift ≤ 0.017 and in the field of view of the Auger observatory) and with directions extracted from an isotropic distribution of sources in the field of view of the Auger observatory. Right panel: the spectrum of UHECR multiplied by E^3 of 100 lists made of the 17 correlated sources and 25 sources, with the same procedure of the left panel.

est energies, where statistics is still too poor to discriminate among different choices. This evidence is a direct consequence of the normalization procedure which recovers the lack of sources readjusting their luminosity. The spectrum obtained with the 17 independent sources of the VCV catalog is shown in figure (3).

As discussed in the last section, the normalization procedure fixes the emissivity of the homogenous distribution of sources ($z > z_0$) and the luminosity of the local distributed point sources ($z < z_0$). In particular, in the case of local sources we have assumed that the UHECR luminosity is proportional to the photon luminosity (taken from the catalog) with a single conversion factor common to all sources (our actual normalization parameter). Taking into account the number of local contributing sources and their distance from us we can easily determine the number density associated to these sources. Using the average UHECR luminosity of the local sources and their number density we can determine a reference value for the emissivity of local sources comparing it with the emissivity of the homogenous distribution, which is directly fitted from data. We obtain an emissivity of 1.9×10^{39} erg/(sMpc³) for the homogeneously distributed sources and a value of 2.4×10^{39} erg/(sMpc³) for the reference emissivity of local sources.

The published Auger result on correlation [14, 15] refers to an exposure sensibly lower³ (by about 30%) than in the recent published spectrum [27, 28], used here as reference. In the latter data, the number of collected events above 60 EeV (50 EeV with original energy scale) is 59 against the 17 sources we use in our calculation. The analysis of event multiplets is completely outside the aims of this paper, because we are only interested in the spectrum features. Nevertheless one should be aware of the fact that the 17 correlated sources cannot account alone for the observed high energy events. In ref. [15] the Auger collaboration sets a lower limit on the number of sources obtained from the ratio of doublets to singlets and based on the simple assumption that all the sources have the same apparent luminosity [30]; this limit turns out to be 61 sources. Then using our set of sources we are implicitly assuming that each source contributes with more than one event to the flux. The assumption we made to agree with the lack of multiplets is that the missing sources have the same astrophysical properties as the correlated sources and

³It has to be remarked that the difference in the exposures is not only due to the period of data taking, but also to the different selections cuts.

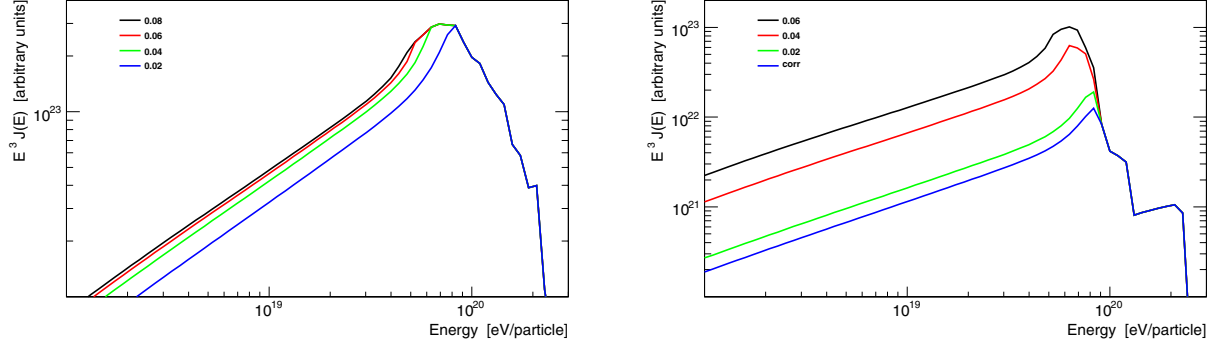


Figure 5: Left panel: UHECR flux from the complete set of sources which fall in the Auger field of view taken from the VCV catalog at redshift less than $z_0 = 0.02, 0.04, 0.06, 0.08$ (as labelled). Right panel: UHECR flux from one set of VCV sources made of the 17 correlated sources and N_{add} sources extracted from the VCV catalog in the field of view of Auger (with redshift $z < z_0$ as labelled); N_{add} is chosen to keep the density n_{corr} fixed with redshift. The curve labelled *corr* corresponds to the flux of the Auger correlated sources with $z_0 = 0.017$.

so they are representative of the whole set of “true” sources.

Let us now check this assumption and investigate how the characteristics of the missing sources can influence the calculated flux. We consider here a set of sources made of the 17 correlated sources and of N_{add} added sources, chosen from the VCV catalog (with their characteristic values of red-shift and luminosity) in the field of view of the Auger observatory and with $z \leq 0.017$. The directions of the N_{add} sources have been then replaced with directions extracted from an isotropic distribution in the field of view of the Auger observatory. The choice of N_{add} is fixed by the correlation signal: the events from the 17 local sources are correlated by construction. N_{add} is then set to 8 or 25 to agree with the published correlation results of 70% and 40% in [14] and [16] respectively.

The results are shown in figure (4). From the comparison we observe that substantial changes in the calculated flux are visible only at the highest energies, where we can not discriminate among different lists because of the data statistics; we also observe that there are not changes between the example with $N_{add} = 8$ and $N_{add} = 25$ because the normalization procedure readjusts the flux.

The analysis presented here assumes that the maximum energy of acceleration changes with the class of sources, with a larger maximum energy associated to the local sparse sources and a lower one for the homogeneously distributed. While this assumption enables a very good fit of the experimental data seems poorly justified from an astrophysical point of view.

3.2 Turning Redshift Analysis

The analysis presented so far takes the parameter z_0 fixed as in the Auger study of correlation ($z_0 = 0.017$); in this case, as follows from the discussion above, the only relevant parameter to fit the spectrum is the maximum energy E_{max} associated to local sparse sources and uniform distributed sources. Let us now change our point of view using z_0 as a free parameter to fit the observed spectrum; in this case we will keep the maximum energy fixed to the same value for both local and faraway sources. As discussed in the previous section the possible value of z_0 could not be too different from the so-called

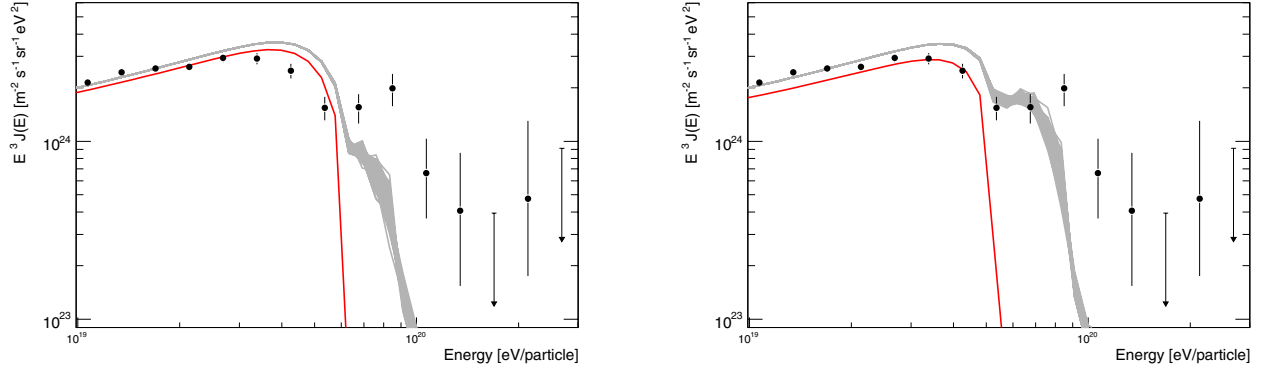


Figure 6: The spectrum of UHECR (multiplied by E^3) produced by an homogeneous distribution of sources at $z > z_0$ (red continuous line) and local discrete sources at $z < z_0$. The local sources correspond to 100 lists made of the 17 Auger correlated sources at $z < 0.017$ and N_{add} sources in the field of view of Auger at $0.017 \leq z \leq z_0$ extracted from the VCV catalog with fixed density n_{corr} (see text). Left panel $z_0 = 0.04$ and right panel $z_0 = 0.06$.

GZK-sphere, the distance inside which UHE protons are less affected by the photo-pion production process. This typical distance depends on the particles energy: for a proton of $E > 50$ EeV it lies in the range of $100 \div 300$ Mpc. Therefore the values of z_0 we are interested in lay in the range $z_0 \simeq 0.01 \div 0.1$.

Changing the parameter z_0 respect to the Auger analysis of correlation introduces a new uncertainty in our analysis, because we are not anymore guided by the Auger result in choosing the contributing local sources. The local AGN as listed in the VCV catalog are much more numerous respect to the list of 17 sources whose position shows a correlation with the Auger events. Moreover, as pointed out above, the possible values of z_0 are relatively low with $z_0 \leq 0.1$ which corresponds to a distance of around 400 Mpc. Inside this radius the VCV catalog can be considered quite accurate being a complete sample of the local Universe.

To solve the ambiguity in the choice of local contributing sources we have considered two different recipes. In the first recipe we have fixed the local density of sources assuming that it corresponds to the density of the 17 Auger correlated sources: $n_{corr} = 10^{-5} \text{ Mpc}^{-3}$. In this case in the redshift range $0 \leq z \leq 0.017$ we have used only the 17 Auger correlated sources and at larger redshift $0.017 \leq z \leq z_0$ we have added a set of N_{add} sources, chosen from the VCV catalog in the field of view of the Auger observatory, with the same density n_{corr} of the local correlated sources. In the second recipe we have simply taken the all VCV sources inside z_0 , without assigning any special role to the sources tagged in the Auger analysis.

In order to understand the effect of the parameter z_0 on the flux from local sources, in figure 5 we show the flux computed using the sources of the VCV catalog placed at red-shift $z < z_0$ for different values of the parameter z_0 (as labelled) and using the two recipes introduced above. In the right panel of figure 5 we have fixed the density of the local sources at n_{corr} (first recipe); the lowest curve corresponds to the flux from the 17 Auger correlated sources within $z_0 = 0.017$ used in the previous analysis. In the left panel of figure 5 we have used the all VCV sources inside z_0 as labelled (second recipe). From figure 5, independently of the assumptions on the local density of sources, it is evident that increasing the number of the discrete sources, by taking larger values of z_0 , the expected

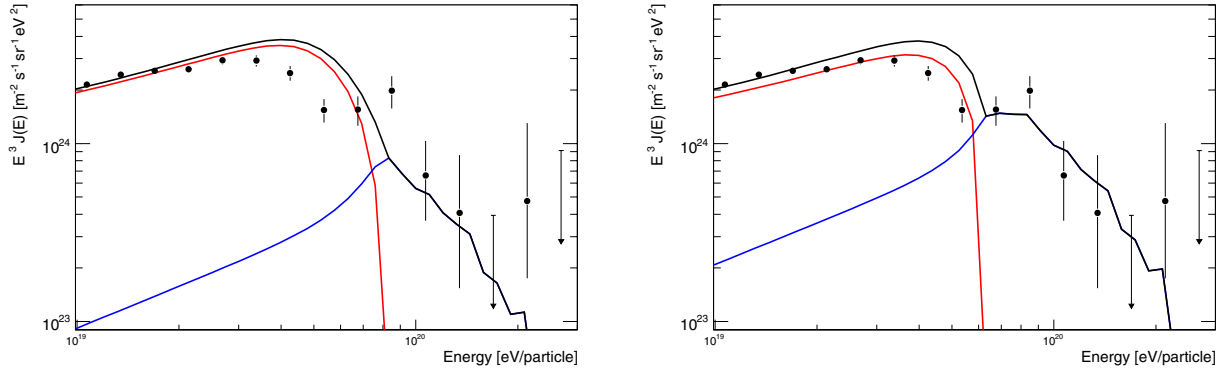


Figure 7: The spectrum of UHECR (multiplied by E^3) produced by an homogeneous distribution of sources at $z > z_0$ (red continuous line) and local sources at $z < z_0$. The local sources correspond to all VCV sources inside z_0 and in the field of view of Auger. Left panel $z_0 = 0.02$ and right panel $z_0 = 0.04$.

contribution of the local (discrete) universe becomes more relevant at the lowest energies with a gradual shift of the flux maximum toward lower energies.

The flux of the homogeneous distributed sources also depends on the choice of z_0 . In our analysis we have assumed the homogenous distribution characterized by a cut-off in redshift with a null injection at $z < z_0$ (see equation (7)). Therefore, increasing z_0 it is reduced the size of the Universe contributing with homogeneous sources and the corresponding contribution to the total flux will be reduced. This reduction is expected at the highest energies where the particles contributing to the flux are produced nearby. In other words the flux of homogeneous sources will show a suppression at high energy with a reduced value of the cut-off energy increasing z_0 .

In the following analysis we will consider the same source model for all sources: homogeneous and discrete, fixing, as before, an injection power law $\gamma_g = 2.2$, an evolution parameter $m = 5$ and assuming the same maximum energy $E_{max} = 3 \times 10^{20}$ eV for all sources.

In figure 6 we show the flux computed using, as discussed above, our first recipe: fixing the contributing sources at $z \leq 0.017$ to the 17 Auger correlated sources and assuming that the density $n_{corr} = 10^{-5} \text{ Mpc}^{-3}$ remains constant with redshift. In figure 6 the value of z_0 is fixed to $z_0 = 0.06$ (right panel) and to $z_0 = 0.04$ (left panel). The red continuous line shows the contribution of the homogenous sources. The contribution of the local sources, shadowed band, is characterized by the uncertainty in the choice of the sources in the redshift range $0.017 \leq z \leq z_0$ with 100 different possible lists of VCV sources in the field of view of Auger contributing to the flux. The best fit emissivities for homogeneous and local sources are respectively $2 \times 10^{39} \text{ erg}/(\text{sMpc}^3)$ and $5.6 \times 10^{38} \text{ erg}/(\text{sMpc}^3)$ for $z_0 = 0.06$, and $5 \times 10^{38} \text{ erg}/(\text{sMpc}^3)$ in the case of $z_0 = 0.04$.

As follows from figure 6 the highest energy part of the observed flux cannot be well described by the theoretical spectrum. The disagreement at the highest energies can be understood taking into account the effects of the sources added at redshift larger than 0.017. These sources increase the contribution to the flux of the local universe at low energy and, consequently, increase the jump in the flux between its maximum and minimum values. These effects, together with the relatively low maximum energy $E_{max} = 3 \times 10^{20}$ eV, imply that the highest energy part of the observed flux cannot be well described by the theoretical spectrum.

A better agreement with Auger data can be obtained following our second recipe in

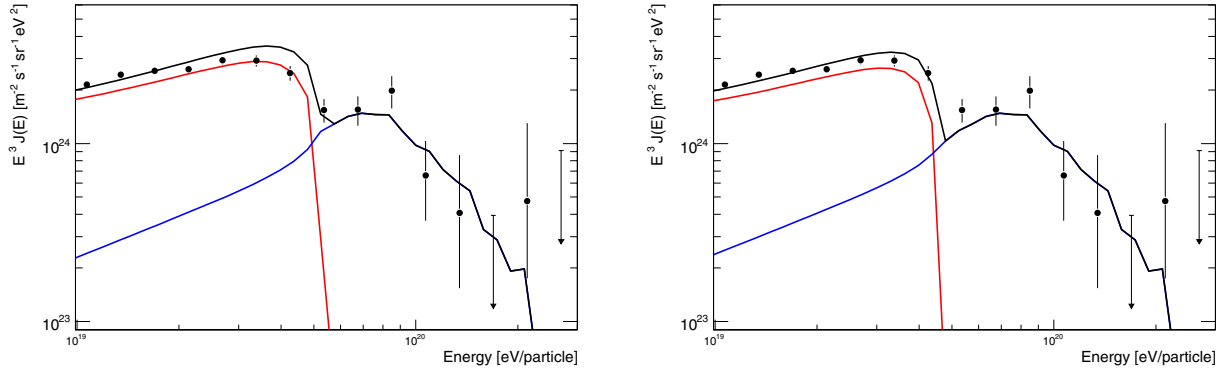


Figure 8: The same as in figure 7 with $z_0 = 0.06$ (left panel) and $z_0 = 0.08$ (right panel).

which the information on the 17 Auger correlated sources is neglected. In this case as discrete local sources we have considered the complete set of sources in the field of view of Auger present in the VCV catalog at $z < z_0$. In figure 7 we plot the flux obtained with two different values of $z_0 = 0.02, 0.04$, keeping the injection parameters fixed as above ($E_{max} = 3 \times 10^{20}$ eV, $\gamma_g = 2.2$ and $m = 5$) for all sources. The number of sources of the VCV catalog in the field of view of Auger inside $z_0 = 0.02$ is 346, with an associated density of 1.3×10^{-4} Mpc $^{-3}$; in the case of $z_0 = 0.04$ the number of VCV sources is 835 with a density 4×10^{-5} Mpc $^{-3}$. As follows from figure 7 the agreement with experimental data at the highest energies is improved. The source emissivities used to fit the Auger data in figure 7 are 2×10^{39} erg/(s Mpc 3) for the homogeneous sources and 6.5×10^{38} erg/(s Mpc 3), 4.5×10^{38} erg/(s Mpc 3) respectively in the case of $z_0 = 0.02$ and $z_0 = 0.04$.

The result of figure 7 is the effect of many sources present in the VCV catalog that stands nearby the observer. In the field of view of Auger there are around 60 sources of the VCV catalog inside $z < 0.005$. As follows from the Auger analysis these sources do not show any correlation signal nevertheless if added at the contributing sources of UHECR could provide a better description of the observations at the highest energies.

In figure 8 we have repeated the same analysis of figure 7 fixing the parameter $z_0 = 0.06$ (left panel) and $z_0 = 0.08$ (right panel). In the case of $z_0 = 0.06$ the number of sources of the VCV catalog is 1379 with a density of 2×10^{-5} Mpc $^{-3}$, while for $z_0 = 0.08$ the number of involved sources is 2064 with a density of 1.3×10^{-5} Mpc $^{-3}$. The emissivities of the uniform and discrete components, fitted from Auger data, are 2×10^{39} erg/(s Mpc 3) for homogeneous sources and 3×10^{38} erg/(s Mpc 3) for discrete sources with $z_0 = 0.06$ and 1.6×10^{38} erg/(s Mpc 3) in the case of $z_0 = 0.08$. The agreement among theoretical and observed spectra with $z_0 = 0.06, 0.08$ is further improved with the contribution of the homogeneous distributed sources restricted to lower energies respect to the case of lower z_0 . In the case of z_0 values larger than 0.08 the agreement with experimental data starts to become less good because of the substantial cut of the flux from homogeneous sources at the lowest energies. We can conclude that neglecting the correlation result and assuming that all VCV sources contribute to the flux the best fit value of the z_0 parameter is around 0.06.

4 Summary and Conclusions

In this paper we have studied the effects of a local distribution of sources on the UHECR spectrum. In the framework of the dip model we have considered a pure proton injection at the source distinguishing among two populations of sources: homogeneously distributed at $z > z_0$ and local point sources at lower redshift. Following the evidence of correlation published by the Auger collaboration [14, 15, 16] we have considered the VCV catalog of quasars and active galactic nuclei as point sources.

We have shown that under certain assumptions the local sources can induce observable features in the energy spectrum. In the framework of our model the parameters that play a leading role in fitting the experimental flux are the maximum attainable energy of protons at the source E_{max} and the turning redshift z_0 . We have considered two different scenarios. In the first scenario we have assumed the correlation observed by Auger and, according to the Auger analysis, we have fixed $z_0 = 0.017$ taking as local point sources only the 17 sources of the VCV catalog that show a correlation signal. In the second scenario we have neglected the correlation result leaving the parameter z_0 free and assuming that the contributing sources inside z_0 is the complete set of VCV sources.

In the first approach, taking for grant the correlation signal claimed by Auger, our best scenario corresponds to a choice of E_{max} that should be larger for the local sources respect to the maximum energy associated to the homogeneously distributed remote sources. Namely $E_{max} = 8 \times 10^{19}$ eV for homogeneous sources and $E_{max} = 10^{21}$ eV in the case of the local sources. The choice of the other injection parameters, namely $\gamma_g = 2.2$ and $m = 5$, was fixed comparing the Auger data [27, 28] with theoretical spectra at energies larger than 3 EeV. With our best choice for E_{max} the two-source model explains the small excess at about 8×10^{19} eV in the Auger data as due to the local sources. In this approach one obtains a very good fit of the experimental data paying the price of different maximum energies for the two source populations. This assumption is difficult to justify on astrophysical grounds.

In order to fix the same maximum energy for all sources, we have considered a second approach. Neglecting the Auger result on correlations, we have studied different choices for the turning redshift z_0 fixing the same injection parameters for all sort of sources, namely $\gamma_g = 2.2$, $m = 5$ and maximum energy $E_{max} = 3 \times 10^{20}$ eV. In this case the best choice for z_0 is $z_0 = 0.06$ and the observed spectrum can be fitted up to the highest energies in virtue of the presence of many (around 60) sources at very low redshift ($z < 0.005$) in the VCV catalog. Also in this case the two-source model explains the small excess in the experimental spectra at about 8×10^{19} eV as a feature connected with the local distribution of sources.

It has however to be noted that our model over-fits the experimental data on flux, therefore the χ^2 analysis cannot exclude a-priori other possibilities, as the case of a homogeneous distribution of sources at any red-shift [18]. In the present analysis we have not considered the possibility of nuclei dominated spectra at the highest energies. This case, favored by the observations of the Auger collaboration on the elongation rate [20], could be hardly consistent with the correlation result. Nevertheless, the possible correlation signal obtained with a mixture of protons and nuclei at the highest energies deserves a more detailed analysis.

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The recent results of the Pierre Auger Observatory on the possible correlation of Ultra High Energy Cosmic Rays events and several nearby discrete sources could be the starting point of a new era with charged particles astronomy. In this paper we introduce a simple model to determine the effects of any local distribution of sources on the expected flux. We consider two populations of sources: faraway sources uniformly distributed and local point sources. We study the effects on the expected flux of the local distribution of sources, referring also to the set of astrophysical objects whose correlation with the Auger events is experimentally claimed.