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A methodology to construct a reduced chemical scheme for 2D-3D photochemical models: Application to Saturn

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Abstract 8

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We present a methodology to build a reduced chemical scheme adapted to the study of hydrocarbons in the atmospheres of giant planets and Titan. As an example, we have built a reduced chemical scheme, containing only 25 compounds and 46 reactions (including photolysis), which is well adapted to compute the abundance of the main hydrocarbons observed so far in the atmosphere of Saturn (CH₃, CH₄, C₂H₂, C₂H₄, C₂H₆, CH₃C₂H, C₃H₈ and C₄H₂). This scheme gives similar results, within the error bars of the model, as a 1D photochemical model using an initial chemical scheme containing 90 compounds and more than 600 reactions. As a consequence, such a methodology can be used to build a reduced scheme well adapted to future 2D (or 3D) photochemical models and GCMs.

Saturn, Photochemistry, Hydrocarbons, 2D photochemical Key words:

models 10

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1. Introduction 11

Recent Cassini and ground-based observations (Greathouse et al. 2005, Howett et al. 2007, Fouchet et al. 2008, Guerlet et al. 2009, Hesman et al. 2009, Guerlet et al. 2010) and observations gathered in the framework of the Herschel Guar-14 anteed Time Key Program "Water and related chemistry in the Solar System" (Hartogh et al., 2009) give unprecedented data on the structure and the composition of Saturn's atmosphere as a function of latitude and time. Interpretation

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of these data requires adapted models like general circulation model and 2D/3D18 photochemical models which are currently lacking. One limitation to the de-19 velopment of 2D/3D photochemical models is the complexity of the chemical 20 scheme (large number of compounds and reactions) required to study the evo-21 lution of hydrocarbons, which are the main trace species of the stratosphere. In 22 typical 1D photochemical models, the number of species can reach 100 and there 23 are more than 500 reactions. In fact, the aim of 1D modeling is to complete 24 the chemical scheme as much as possible in order to have the best description 25 of chemical processes occurring in the atmosphere and explain how light and 26 heavy molecules are produced. In 2D/3D modeling, it is not possible for the 27 time being to include such a large chemical scheme due to computational time 28 limitations. As a consequence, it is important to determine a reduced chemical 29 scheme, which is known to be representative of the main atmospheric chemical 30 processes. The problem is then to create such a reduced chemical scheme which 31 would be simple enough to be usable for 2D/3D models and whose results would 32 remain valid. 33

In the present paper, we present a methodology to build a reduced chemi-34 cal scheme validated to study the production of the main hydrocarbons in the 35 stratosphere of Saturn. In section 2, we present the photochemical model, in-36 cluding the background atmosphere, the initial chemical scheme and the method 37 used to study the propagation of uncertainties in the model. Mole fraction pro-38 files and their uncertainties are presented in section 3 and compared to recent 39 CIRS observations. The methodology used to build a reduced chemical scheme 40 is presented in section 4, the result is given in section 5 and discussed in section 41 6. 42

2. Photochemical model

2.1. Atmospheric model

⁴⁵ Our 1D photochemical model uses a fixed background atmosphere with fixed
⁴⁶ boundary conditions (no evolution with latitude and time). The temperature

profile presented in Fig. 1 has been synthesized by combining two different 47 observations. At pressure levels greater than 10^{-5} mbar, we used the tempera-48 ture profile derived from Cassini/CIRS data corresponding to a planetographic 49 latitude of 20° S (data provided by S. Guerlet), which is the latitude around 50 which the subsolar point was located at the time these data have been col-51 lected (in 2006). Details of the temperature profile retrievial can be found in 52 Fouchet et al. (2008) and Guerlet et al. (2009). At pressure levels lower than 53 10^{-5} mbar, we used data derived from Smith et al. (1983). A subjective ex-54 trapolation is done to connect the two points ($p = 10^{-5}$ mbar, T = 140 K) and 55 $(p = 10^{-7} \text{ mbar}, T = 420 \text{ K}).$ 56

⁵⁷ We used a non-uniform altitude grid with 124 levels from -184 km (pressure ⁵⁸ level $p \approx 10^4$ mbar) to 1580 km ($p \approx 10^{-7}$ mbar). The altitude reference (z = 0) ⁵⁹ corresponds to p = 1 bar. Two consecutive levels (z and $z + \Delta z$) are separated ⁶⁰ by a distance smaller than H(z)/5, where H(z) is the atmospheric scale height ⁶¹ at altitude z.

We summarize hereafter the boundary conditions of the model. At the lower 62 boundary, we set the mole fraction of H_2 , He, CH_4 and CO respectively to $y_{H_2} =$ 63 0.86, $y_{He} = 0.135$ (Conrath and Gautier, 2000), $y_{CH_4} = 4.5 \ 10^{-3}$ (Flasar et al. 2005, Fletcher et al. 2009) and $y_{CO} = 5.0 \, 10^{-10}$ (Cavalié et al., 2009). All other 65 compounds have a flux given by the maximum diffusion velocity v = -K/H66 where K is the eddy diffusion coefficient and H the atmospheric scale height at 67 the lower boundary. At the upper boundary, zero fluxes were assumed for all the 68 species except for atomic hydrogen and for some oxygen compounds (CO, CO₂ 69 and H_2O). H atoms are produced by photochemical processes at higher altitudes 70 in the thermosphere. We assumed a fixed downward flux for atomic hydrogen 71 at the upper boundary equal to $\Phi_H = -1.0 \times 10^8 \text{ cm}^{-2} \cdot \text{s}^{-1}$ following the work 72 of Moses et al. (2005). The photochemical model results are not particularly 73 sensitive to this value. The external source of oxygen in the atmosphere of Saturn could be in the form of infalling interplanetary dust particles (IDP), ring 75 and/or satellite material, or large comets. Recent submillimetric observations 76 favor a cometary origin for CO in the stratosphere of Saturn (Cavalié et al., 77



Figure 1: Temperature profile (in K) of Saturn's atmosphere adopted in the present photochemical model as a function of pressure p (in mbar). This atmospheric structure is inferred from two sources. From the bottom up to $p \approx 10^{-5}$ mbar: recent CIRS data (Fouchet et al., 2008) corresponding to a planetographic latitude of 20° S. For $p < 10^{-5}$ mbar: extrapolation using data from Smith et al. (1983).

2010). The abundance levels at which H₂O has been observed in the stratosphere 78 of Saturn implies that the source of H₂O is more likely to be a steady source 79 with an origin local to the Saturn system because of transport and condensation 80 issues (Moses et al., 2005). This is reinforced by the recent observation of active 81 plumes emanating from the south pole of Enceladus suggesting that this small 82 moon is likely to be the principal source of neutrals in Saturn's magnetosphere 83 (Smith et al., 2010). The source of H_2O should be soon definitely established 84 from Herschel observations (Hartogh et al., 2009). In the present model, we 85 used a simplified parametrization of the external input of oxygen compounds. 86 The external oxygen is assumed to be released in the upper atmosphere in the form of CO, H₂O and CO₂ with the following flux: $\Phi_{CO} = 1.5 \, 10^6 \text{ cm}^{-2} \cdot \text{s}^{-1}$, 88 $\Phi_{H_2O} = 1.5 \ 10^6 \ \mathrm{cm}^{-2} \cdot \mathrm{s}^{-1}$ and $\Phi_{CO_2} = 7.5 \ 10^4 \ \mathrm{cm}^{-2} \cdot \mathrm{s}^{-1}$ (Moses et al. 2000, 89

⁹⁰ Cavalié et al. 2009).

The eddy diffusion coefficient K(z) (in cm²·s⁻¹) is presented in Fig. 2. This

⁹² coefficient, together with the methane mole fraction at the lower boundary,

⁹³ gives a satisfactory profile of methane in comparison with Voyager/UVS and

94 Cassini/CIRS data (Fig. 3).



Figure 2: Eddy diffusion coefficient (solid line) and molecular diffusion coefficient of CH_4 (dashed line) (expressed in $cm^2 s^{-1}$) as a function of pressure (mbar). The methane homopause is located around 10^{-5} mbar in agreement with Smith et al. (1983).

95 2.2. Chemical model

In the present study, we used the review of the hydrocarbon chemistry at low temperature described in Hébrard et al. (2006) and Hébrard et al. (2009) for Titan's atmosphere. The initial chemical scheme, associated rate constants and uncertainty factors of reaction rates have been extracted from these two papers. The chemical scheme includes 90 compounds (H, H₂, He, hydrocarbons and oxygen compounds), 549 reactions and 59 photodissociation processes. The list of reactions can also be provided upon request and will soon be included in the

KIDA database (http://kida.obs.u-bordeaux1.fr/). The photodissociation rates have been computed with a mean zenith angle obtained from a subsolar point located at 20°S a solar declination equal to -20° . Their uncertainty factors have been set to $F_J = 1.5$ (Dobrijevic and Parisot, 1998).

107 2.3. Uncertainty propagation

The overall precision of photochemical models is highly sensitive to the un-108 certainties in the rate coefficients used in the chemical scheme. Since the conti-109 nuity equations are non-linear and strongly coupled, it is necessary to use global 110 sensitivity methods to study how these uncertainties propagate in the photo-111 chemical model (Dobrijevic et al., 2010b). The present model is similar to the 112 model used in Dobrijevic et al. (2010a). We used a Monte-Carlo approach to 113 generate 500 profiles as a function of altitude. This number is a good com-114 promise between the computation time and the statistical significance of the 115 distributions. 116

117 3. 1D photochemical model results

Figs. 3, 4 and 5 present, for each compound of interest, the 500 profiles 118 generated by our Monte-Carlo procedure and the initial profile. Initial pro-119 files (black solid lines) correspond to profiles obtained with the initial chemical 120 scheme and the nominal values of chemical rate constants. The type of distrib-121 ution of mole fractions depends on the compound and can vary with altitudes: 122 distributions are not always normal or log-normal. In this case, quantiles are 123 useful measures to represent the distributions. Figures show the 5th and 15th 124 20-quantiles and the 1st and 19th 20-quantiles, which give the intervals contain-125 ing respectively 50% and 90% of the profiles. Uncertainty on the CH_4 profile 126 (due to uncertainties on reaction rate coefficients) is very low, much lower than 127 the uncertainties of observations, because the CH₄ profile is mainly controlled 128 by the eddy diffusion coefficient. On the contrary, uncertainties on other profiles 129 derived from the model are much greater than those of observations, especially 130 for C_3 and C_4 compounds. 131

The aim of the present study is to present a methodology to derive a very 132 reduced chemical scheme, not to compare our model to all the previous obser-133 vations (taken at different times with different techniques and different spatial 134 resolutions). In order to validate our initial scheme and our 1D photochemical 135 model, we restrict the comparisons with recent data that correspond to the same 136 latitude (around 20° S) and epoch (2006). In particular, the set of data pub-137 lished by Guerlet et al. (2009) and Guerlet et al. (2010) gives the opportunity 138 to compare our model with consistent data acquired by the same instrument 139 and analyzed with the same procedure. 140

Taking uncertainties into account, our model is in relatively good agreement 141 with CIRS observations at the subsolar point. All the observational data are 142 within the 1st and 19th 20-quantiles of our model. This shows that chemical 143 processes included in the initial chemical scheme and physical processes im-144 plemented in the model are representative of the main processes that govern 145 the composition of Saturn's stratosphere. To go deeper into the comparison of 146 the model with CIRS data, it would be necessary to compare synthetic spec-147 tra generated from our Monte-Carlo profiles with the CIRS spectra. Such a 148 work deserves a dedicated study. The aim here is not to adjust some model 149 parameters to have a perfect agreement between the model and observations (if 150 possible), but only to have a good agreement to construct a reliable reduced 151 chemical scheme. 152

4. Reduction methodology

How to reduce a chemical scheme? A reduced chemical scheme is built by removing a set of reactions from the initial chemical scheme. Using this reduced chemical scheme, our 1D photochemical model should give results in agreement with the ones obtained with the initial chemical scheme. This agreement depends on a given criterion. Typically, the new results should remain close to a reference. Two reference results are then conceivable: results from a reference model and results from observations. Ideally, observations should be used as

¹⁶¹ a reference but we see in figures 3, 4 and 5 that error bars of the model are ¹⁶² greater than the error bars of observations. For this reason, a reference model ¹⁶³ has been preferred to a reference set of observables. The reference model is ¹⁶⁴ our 1D photochemical model that includes uncertainties propagation of rate ¹⁶⁵ constants.

Since only a few compounds have been observed to date and only a part of the atmosphere can be probed by various instruments, we have decided to limit the criterion presented above to a given list of compounds and we focus our study in the part of the atmosphere which lies between the 1 bar and 10^{-5} mbar pressure levels. The list of compounds corresponds to the ones that have been already detected in the atmosphere: CH₃, CH₄, C₂H₂, C₂H₄, C₂H₆, CH₃C₂H, C₃H₈ and C₄H₂ (with the exception of C₆H₆ for reasons detailed below).

The strength of the relationship between outputs (mole fractions) and in-173 puts (rate constants) can be evaluated by Rank Correlation Coefficients (RCCs) 174 in the presence of non-linearity in the model. RCCs convert a nonlinear but 175 monotonic relationship into a linear relationship by replacing the values of the 176 sampled inputs/outputs by their respective ranks. These correlation coefficients 177 can vary between -1 and 1; a positive value means that both correlated para-178 meters increase or decrease simultaneously. In the presence of nonlinear but 179 monotonic correlations, this simple procedure improves the resolution of sensi-180 tivity analysis (Helton et al., 2006). 181

In practice, RCCs are calculated using the logarithm of mole fractions and 182 rate constants. Rate constants with low RCCs (in absolute value) have weak 183 influence on the uncertainty of the mole fraction of a given compound. Removing 184 these reactions will have very little influence on the results of the model. This 185 means that below a given threshold (a given value of RCC), all the reactions can 186 be removed. The lower the RCC threshold, the greater the number of reactions 187 and compounds that remain in the reduced chemical scheme. Our criterion to 188 validate a reduced chemical scheme was the reproduction of a reference model 189 within a certain confidence interval. The confidence interval may be given by the 190 5th and 15th 20-quantiles or the 1st and 19th 20-quantiles for instance (this is 191

an arbitrary choice). The profiles of each target molecule should stay within the 192 confidence interval to consider the current reduced scheme as suitable. In the 193 following, the confidence interval is given by the 1st and 19th 20-quantiles in the 194 part of the atmosphere where the compounds are observed. The determination 195 of an optimal RCC threshold (which would give the most satisfactory reduced 196 scheme) is an empirically iterative procedure that can be tiresome since the new 197 reduced chemical scheme must be tested for each value of the RCC threshold. 198 A slight modification of this threshold can add or remove a few reactions in 199 the reduced chemical scheme. We have noticed, moreover, that the number of 200 runs in the Monte Carlo procedure can affect this "optimal threshold". As a 201 consequence, in order to limit the number of runs and tests, we did not make 202 an exhaustive study to search for the "optimal RCC threshold". 203

The RCCs between mole fractions and rate constants combine the informa-20 tion of the main influent pathways in the chemical scheme, weighted by their 205 uncertainties. A first attempt has been made using the RCCs computed with 206 the 500 mole fraction profiles and the corresponding rate constants presented 207 previously. One limitation with this method, as stated by Carrasco et al. (2008), 208 is that uncertainty factors of some rate coefficients are very important, which 209 increase the intrinsic importance of some reactions. This methodology is well 210 adapted to derive the key reactions of the chemical scheme (Dobrijevic et al., 211 2010b), but not to construct a reduced scheme. For instance, we were not able to 212 find an interesting reduced scheme for C_3H_4 and C_4H_2 . Too many compounds 213 and reactions were necessary to produce vertical profiles in agreement with the 214 reference model for these two compounds. This explains also why we did not 215 include C_6H_6 in our model. The other reason is that the chemistry of C_4 , C_5 216 and C_6 compounds is not well known. In particular, many reactions and com-217 pounds are lacking in the initial chemical scheme (see for instance Dobrijevic 218 and Dutour 2007). Consequently, we consider that it is not pertinent to search 219 for a reduced scheme that matches the vertical profile of C_6H_6 . 220

In a second attempt, we set all the uncertainty factors to a given value F. Carrasco et al. (2008) stated that the value of F does not change significantly

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the reduced schemes. We chose F = 1.5 for all photodissociation processes 223 and reactions. We have generated 500 profiles using a Monte-Carlo procedure 224 and then computed the RCCs for all the compounds we were interested in 225 and all the reaction rates. After a few attempts, we set the RCCs threshold 226 to 0.2. This led us to a reduced scheme with 33 compounds and 54 reactions 227 (including photolysis). Four compounds of this scheme were not produced (they 228 appeared only as a reactant) and thus were removed from the scheme. Thirteen 229 compounds did not appear as a reactant, but only as a product. Some of 230 these sink compounds were relatively abundant (compared to the compounds of 231 interest) and were then removed, as well as their corresponding reactions. It was 232 not possible to remove all the sinks because too many reactions were concerned. 233 However, sink compounds with low mole fractions do not alter the abundance 234 of main compounds. In the end, the reduced chemical scheme contains only 25 235 compounds and 46 reactions (including 18 photodissociations) listed in tables 236 1 and 2. As a result, we have reduced the number of compounds by 72%, the 237 number of reactions by 92% and the computation time by a factor 100. 238

Table 1: List of the 25 compounds of the reduced chemical scheme

 $C; {}^{1}CH_{2}; CH_{3}; CH_{4}$ $I_{2}; C_{2}H_{3}; C_{2}H_{5}; C_{2}$

 $C_{2}H_{3}$; $C_{2}H_{5}$; $C_{2}H_{4}$; C_{2} ; $C_{3}H_{5}$; $C_{2}H_{4}$; C_{2} ; $C_{3}H_{5}$; $C_{3}H_{6}$; $C_{3}H_{8}$; I_{2} ; $C_{4}H_{6}$; $C_{4}H_{4}$; $C_{6}H_{4}$;

; C₂H₆

5. Photochemical model results with the reduced chemical scheme 239

; $\tilde{C}_{4}H_{2}$;

 C_2H_2 ; (CH₃C₂H C_4H_3

In order to be valid, the reduced scheme must be in agreement with the refer-240 ence model. So, the steady state abundances of the main compounds computed 241 using the reduced scheme were compared to the reference model in figures 6, 7 242 and 8. For all the compounds, the agreement is very good: profiles lie between 243 the 5th and 15th 20-quantiles in the middle atmosphere (especially where the 244 compounds have been observed, typically between 10 mbar and 10^{-2} mbar). 245



Table 2: Reduced chemical scheme: Photolysis reactions (R1 to R18) and chemical reactions (R19 to R46). Rate constants, cross sections, photolysis rates and uncertainty factors are given in Hébrard et al. (2006) and Hébrard et al. (2009).

Fig. 9 shows that the agreement for C_4H_2 between the reduced model and 246 the reference model is limited to pressure levels lower than about 10^{-3} mbar. 247 The mole fraction of CH_3C_2H (Fig. 8) obtained with the reduced model is not 248 in agreement with the initial model for pressure levels greater than about 10 249 mbar. So, the reduced chemical scheme proposed here is not perfect since it 250 does not produce profiles of CH_3C_2H and C_4H_2 that are reliable in the whole 251 part of the atmosphere studied here. Since high pressure and low pressure levels 252 are poorly constrained by observations, this discrepancy seems acceptable. If 253 necessary, it is of course possible to improve the situation by lowering the RCC 254 threshold. This would lead to a less reduced chemical scheme. 255

6. Discussion 256

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How to use this reduced scheme? A priori, the chemical scheme provided here 258 should be used with the same rate constants as the ones we used (see Hébrard et al. 2006; Hébrard et al. 2009). However, if the initial chemical scheme have to be changed (because some rate coefficients or uncertainty factors have to be up-

dated or some reactions have to be added), it is necessary to redo the procedure 261 presented in this paper to build a new reduced scheme. In particular, J. Moses 262 pointed out (personal communication) that the rate coefficient of reaction R34 263 might be overestimated (and that our uncertainty factor is underestimated). A 26 particular attention might be paid on this reaction in a future update of the 265 chemical scheme. Also, the methodology presented here gives a reduced scheme 266 with several sink compounds (with no destruction mechanisms). Although we 267 have eliminated most of these compounds, it is not possible to eliminate all the 268 reactions that involve sink compounds without changing significantly the results. 269 As a consequence, users of 2D/3D photochemical models should take care of the 270 presence of sink compounds by adding appropriate destruction mechanisms. 271

Is the reduced scheme suitable for other latitudes? The aim of this reduced 272 scheme is to be used in 2D/3D photochemical models. In order to test the valid-273 ity of our reduced chemical scheme, we have made a comparison of the model re-274 sults derived from the initial chemical scheme and the reduced chemical scheme 275 at different latitudes. Our reference model corresponds to the subsolar point at 276 20° S. We have tested 2 other latitudes: 60°S and 40°S. For these tests, only 277 the solar zenith angle has been changed (we used the same temperature profile). 278 For all compounds, the behavior of the model is the same whatever the chemical 279 scheme used. An example is shown in Fig. 10 for C_3H_8 . Other compounds are 280 even less affected by variation of the solar zenith angle. To be fully satisfying, 281 the validation should take into account the fact that temperature profiles also 282 vary with latitudes. For instance, Cassini data show that the temperature pro-283 file measured at 60°S is about 10 K higher than at 20°S (Guerlet et al., 2009). 284 It would be interesting to study how uncertainties of rate constants propagate 285 in the photochemical model when considering different temperature profiles and 286 solar zenith angles. One limitation we see is that many reaction rates have no 287 temperature dependence in our initial chemical scheme (because this temperature dependence is not known). It is essential to have a good description of the chemistry as a function of temperature to see a possible variation of error bars 290 of the model as a function of latitude. To do that, it would be necessary to 291

improve our chemical scheme in order to estimate the temperature dependence
of many reaction rates and to estimate their uncertainty factors. This kind of
work is beyond the scope of the present study.

Can we find a minimal chemical scheme? The reduced chemical scheme 295 presented here is not a minimal chemical scheme. To obtain a minimal scheme 296 from the reduced one, we might remove some additional reactions depending on 297 their RCCs. We could first remove one reaction at a time and check sequentially 298 the 46 reactions of the reduced scheme. If a reaction could be removed, then we 299 could try to remove another reaction and repeat this procedure as long as the 300 model results would be in agreement with the reference model. However, in such 301 a non-linear system, different sequences of removal might give different results. 302 As a consequence, a great number of runs are necessary to achieve this task. 303 Actually, since the initial chemical scheme is expected to be updated frequently, 30 we find it useless to try to find a minimal chemical scheme. 305

306 7. Conclusion

One major step in the development of 2D and 3D photochemical models is 307 to determine a chemical scheme that is both simple (i.e. it contains a small 308 number of compounds and reactions) and valid (i.e. the results of the model are 309 in agreement with a reference model). In the present paper, we have presented 310 a methodology to build a reduced chemical scheme. The reference model is 311 a 1D photochemical model that includes uncertainties of rate coefficients. The 312 screening of the chemical scheme is based on the correlations between outputs of 313 the model (mole fractions) and the inputs (rate coefficients). This methodology 314 is quite similar to the one used to determine key reactions of a photochemical 315 model (Dobrijevic et al., 2010a). We found a reduced chemical scheme where 316 about 70% of the compounds and 90% of the reactions have been removed from 317 the initial chemical scheme.

It is not guaranteed that the reduced chemical scheme derived here for Saturn is well adapted for other giant planets and Titan. As a consequence, this work

- ³²¹ should be done again for other planets to check this specific point. Also, this
- ³²² work should be done again if the reference chemical scheme is different from the
- ³²³ one used in the present study.
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Figure 3: <u>Model</u>. Gray solid lines: Abundance profiles of CH₄ and C₂H₂ obtained after 500 runs. Black solid line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution. <u>CH₄ observations</u>. Lower atmosphere: CIRS Cassini data (Flasar et al., 2005; Fletcher et al., 2009). Upper atmosphere: UVS Voyager data from Festou and Atreya (1982) (triangle) and Smith et al. (1983) (diamond). <u>C₂H₂ observations</u>. Bold solid line: CIRS Cassini observations and 1- σ uncertainties at 20° S (Guerlet et al., 2009, 2010). Diamond: sub-solar IRTF data (Greathouse et al., 2005). Triangle: sub-solar CIRS Cassini data (Howett et al., 2007). Square: sub-solar CIRS Cassini data (Hesman et al., 2009).



Figure 4: <u>Model</u>. Gray solid lines: Abundance profiles of C_2H_6 and CH_3C_2H obtained after 500 runs. Black solid line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution. C_2H_6 observations. Bold solid line: CIRS Cassini observations and 1- σ uncertainties at 20° S (Guerlet et al., 2009, 2010). Diamond: sub-solar IRTF data (Greathouse et al., 2005). Triangle: sub-solar CIRS Cassini data (Howett et al., 2007). Square: sub-solar CIRS Cassini data (Hesman et al., 2009). C_3H_4 observation. and 1- σ uncertainties at 20° S (Guerlet et al., 2009, 2010).



Figure 5: <u>Model</u>. Gray solid lines: Abundance profiles of C_3H_8 and C_4H_2 obtained after 500 runs. Black solid line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution. Gray dotted line: 100% saturation profile. C_3H_8 and C_4H_2 observations. Bold solid line: CIRS Cassini observations and 1- σ uncertainties at 20° S (Guerlet et al., 2009, 2010). Square: IRTF data at -20° planetocentric latitude (Greathouse et al., 2006)



Figure 6: Red line: Abundance profiles of CH_3 and C_2H_2 with the reduced chemical scheme. Blue line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution.



Figure 7: Red line: Abundance profiles of C_2H_4 and C_2H_6 with the reduced chemical scheme. Blue line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution.



Figure 8: Red line: Abundance profiles of CH_3C_2H and C_3H_8 with the reduced chemical scheme. Blue line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution.



Figure 9: Red line: Abundance profiles of C_4H_2 with the reduced chemical scheme. Blue line: initial profile obtained with the initial chemical scheme. Black dotted line: median profile. Black dashed-dotted lines: 5th and 15th 20-quantiles of the distribution. Black long-dashed lines: 1st and 19th 20-quantiles of the distribution.

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Figure 10: Abundance profiles of C_3H_8 for different latitudes. Black lines: Initial chemical scheme. Gray lines: Reduced chemical scheme. The mean solar zenith angle corresponding to 20° S, 40° S and 60° S are respectively 51°, 54° and 63°.

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> This study concerns photochemistry of hydrocarbons in the atmosphere of Saturn.

> We present a methodology to derive a very reduced chemical scheme that can be used in future 2D (or 3D) photochemical models.

> Our reduced scheme of 25 compounds and 46 reactions gives similar results, within the Acception error bars of the model, than a 1D photochemical model.