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## Surface phase transitions in BiFeO<sub>3</sub> below room temperature

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We combine a wide variety of experimental techniques to analyze two heretofore mysterious phase transitions in multiferroic bismuth ferrite at low temperature. Raman spectroscopy, resonant ultrasound spectroscopy, electron paraelectric resonance, x-ray lattice constant measurements, conductivity and dielectric response, and specific heat and pyroelectric data have been collected for two different types of samples: single crystals and, in order to maximize surface/volume ratio to enhance surface phase transition effects, BiFeO<sub>3</sub> nanotubes were also studied. The transition at  $T = 140.3$  K is shown to be a surface phase transition, with an associated sharp change in lattice parameter and charge density at the surface. Meanwhile, the 201 K anomaly appears to signal the onset of glassy behavior.

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### I. INTRODUCTION

Bismuth ferrite BiFeO<sub>3</sub> (BFO) is one of the most popular research materials in condensed matter physics at present.<sup>1,2</sup> Despite the intense activity, however, there remain a number of unanswered questions concerning its structure and phase diagrams. From the beginning<sup>3</sup> a large number of phases were reported as a function of temperature, and more recently<sup>4–9</sup> more as a function of hydrostatic pressure. The high-temperature end of the phase diagram, based upon the neutron studies of Arnold *et al.*,<sup>10,11</sup> involves an ambient rhombohedral  $R3c$  phase, a first-order transition to orthorhombic  $Pbnm$  near 1103 K,<sup>10</sup> and an isosymmetric  $Pbnm$ - $Pbnm$  Mott-like metal-insulator transition near 1220 K.<sup>11</sup> The powder neutron results show that the latter structure cannot be resolved by x-ray studies, because only the oxygen ions are significantly displaced; and it further suggests that there are no high- $T$  monoclinic or tetragonal phases, contrary to claims elsewhere.<sup>12–14</sup> However, because of Bi volatility at high temperature, uncertainties on the exact nature and symmetry of the high-temperature state still exist.<sup>15,16</sup> Equivalently, in some nonpowder thin-film specimens, a cubic  $Pm\bar{3}m$  phase is inferred a few degrees below the melting temperature of  $\sim 1225$  K (Ref. 13) but it still remains to be confirmed.<sup>17</sup>

Beyond the high-temperature phases, questions also remain about lower-temperature anomalies. The true nature and stability of its long-period ( $\sim 63$  nm), incommensurate cycloidal spin structure has been controversial<sup>18–26</sup> and there are a number of cryogenic phase transitions whose origin has not been clarified. For example, anomalies near 140 and 201 K have been interpreted as spin reorientation transitions,<sup>27,28</sup> analogous to those in orthoferrites such as ErFeO<sub>3</sub>, and evidence has also been reported for spin-glass behavior,<sup>29,30</sup> with an Almeida-Thouless line (AT line) terminating at 140 K,<sup>31</sup> a clear separation of field-cooled and zero-field-cooled susceptibilities beginning at 230 K, additional magnon light-scattering cross-section divergences near 90 and 230 K, and a bump in the dielectric constant near 50 K.<sup>32,33</sup> At  $\sim 30$  K, there are two anomalies: an extrapolated freezing temperature from a Vogel-Fulcher analysis of data (29.4 K). These studies therefore indicate up to six cryogenic anomalies at temperatures at 30, 50, 90, 140, 201, and 230 K. On the other hand, neutron diffraction experiments and other bulk-sensitive probes, such as single-crystal magnetometry, show no indication of any magnetic transition, with the spin cycloid seemingly unaltered all the way down to 4 K.<sup>19,26</sup> There is therefore a clear contradiction at the core of all these results that needs to be resolved.



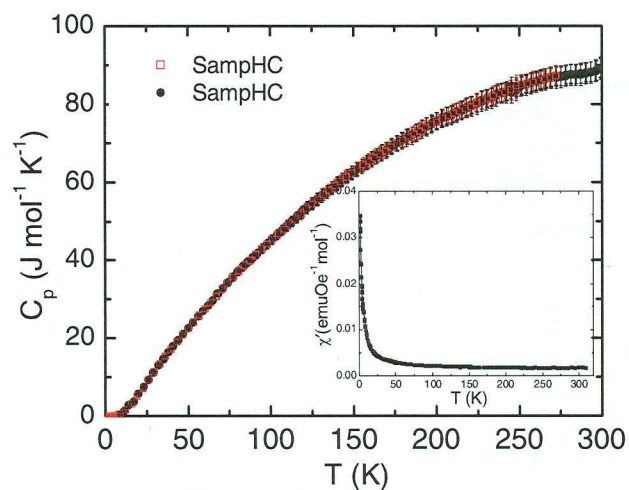


FIG. 1. (Color online) Specific heat at 0 and 1 T and ac magnetic susceptibility at 0 T (inset) as a function of temperature for BFO single crystal.

Probably the most thoroughly studied transitions are those at 140.3 and 201 K, reported independently by Cazayous *et al.*<sup>27</sup> and Singh *et al.*<sup>28</sup> These transitions are manifest in magnon Raman scattering as divergences in cross section, but they have remained controversial because they do not appear in careful measurements of bulk magnetometry or specific heat, such as those in Fig. 1. This has led to speculation that these may be anomalies of extrinsic origin (e.g., second phases, magnetic impurities, or simple artifacts). However, the measurement of Raman magnon linewidth narrowing<sup>27,28</sup> rules out magnetic impurities, as does the observation of critical exponents for Raman cross-sections<sup>33–35</sup> and Almedia-Thouless dependence for field-cooled and zero-field-cooled magnetization in thin-film samples.<sup>31</sup>

Very recently (2011), two papers have shed additional light on this aspect. Marti *et al.*<sup>36</sup> have shown, using impedance analysis and grazing incidence x-ray diffraction, that the surface layer (“skin”) of BiFeO<sub>3</sub> has a surface-confined phase transition,<sup>36</sup> and suggested that some of the cryogenic anomalies of BiFeO<sub>3</sub> may also be confined to its skin layer. Meanwhile, Ramazanoglu *et al.*<sup>37</sup> have shown that extremely small uniaxial pressures change the magnetic domain structure strongly, and from that inferred that the low-*T* transitions (at 140 and 201 K) may be linked to such phenomena, which mimic magnetic reorientation transitions like those in orthoferrites. Certainly the fact that the low-temperature anomalies tend to be clearer in surface-sensitive probes such as backscattering Raman experiments would support the idea that these transitions are confined in the surface. At the same time, the strong effect of stress on the magnetic configuration suggests that if the surface differs structurally from the interior, so it will also affect its magnetic behavior. In the present paper, we show that the 140 K transition in BiFeO<sub>3</sub> is indeed that of a surface phase, and we characterize its structural and electronic properties.

## II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

In addition to classical BiFeO<sub>3</sub> ceramic samples, single crystals and nanotubes were prepared. BFO single crystals were grown using a method similar to the original method proposed by Kubel and Schmid.<sup>38</sup> Adjusting the cooling rate allows growing of millimeter diameter rosettelike pyramidal crystals, as described by Burnett *et al.*<sup>39</sup> All crystals were polished parallel to the surface, which in rosette crystals is the (100) crystallographic plane. Samples typically larger than 1 × 1 mm<sup>2</sup> area and 300 μm thick were obtained. Optical quality crystal surfaces were obtained by polishing using 0.25 μm diamond paste. The remaining damaged surface layer and polishing scratches were removed by chemical mechanical polishing (CMP). CMP was performed usually for 30 min using SiO<sub>2</sub> colloidal solution (Syton) diluted with water in a 1:1 ratio. The BFO nanotubes were prepared via wet-chemistry synthesis: In a typical synthesis, Bi(NO<sub>3</sub>)<sub>3</sub>·5H<sub>2</sub>O was initially added to ethylene glycol to ensure complete dissolution followed by Fe(NO<sub>3</sub>)<sub>3</sub>·9H<sub>2</sub>O to yield a molar ratio in solution of Bi:Fe as 1:1.<sup>40,41</sup> The resulting mixture was stirred at 80 °C for 1 h, after which a transparent sol was recovered upon evaporation of the excess ethylene glycol. Droplets of the sol were deposited using a syringe onto a porous anodic alumina (AAO) template (Whatman Anodisc<sup>®</sup>) surface with application of pressure.<sup>42,43</sup> AAO membranes with different pore sizes, such as 200 and 100 nm, have been used. The resultant samples of AAO templates containing the BiFeO<sub>3</sub> precursors were subsequently oven dried at 100 °C for an hour and then preheated to 400 °C for three separate runs at a ramp rate of 5 °C/min in order to get rid of excess hydrocarbons and NO<sub>x</sub> impurities. The sample was further annealed at 600 °C for 30 min. BiFeO<sub>3</sub> nanotubes were isolated after removal of the AAO template, following its immersion in 6M NaOH solution at room temperature for 24 h. Thereafter, to retrieve reasonable quantities of nanotubes, the base solution was diluted in several steps with distilled water and lastly ethanol. Tubes were collected by centrifugation. The tubes were shown to be ferroelectric, with switching hysteresis. The nanotubes were subjected to electrical switching by applying a voltage across a single tube, with the Ir/Pt tip of an atomic force microscope serving as the top electrode. The measured piezoelectric constant hysteresis is quite large (about two thirds the value of PZT).

Raman spectroscopy measurements were performed using a Horiba Jobin Yvon T64000 spectrometer using an Ar<sup>+</sup> ion laser (514.5 nm) as excitation line. The single-crystal sample was placed on the hearth of a Linkam variable-temperature stage allowing measurements between 100 and 300 K. The elastic response of ceramic and single-crystal samples was investigated by resonant ultrasound spectroscopy (RUS). Details can be found in Ref. 44. For the present study, RUS spectra in the frequency range 0.1–2 MHz were collected in the temperature range ~10–295 K in a helium flow cryostat described by McKnight *et al.*<sup>45,46</sup> Electron paraelectric resonance (EPR) was also performed on the BFO nanotubes using a Bruker E580 system operating at a Larmor frequency of 9.7 GHz. The spectrometer is equipped with a low-temperature cryostat allowing measurements between 30 and 300 K.



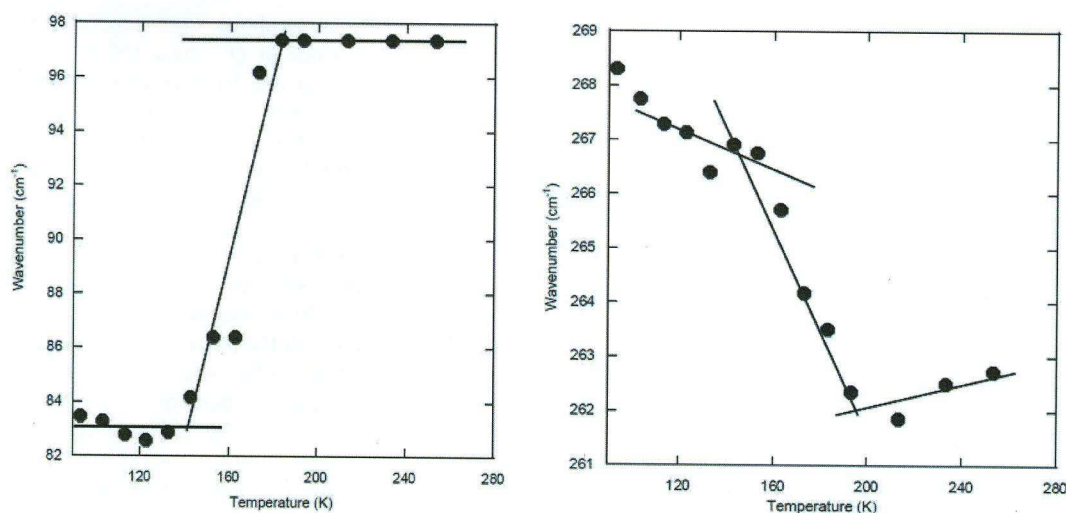


FIG. 2. Positions of two Raman peaks as a function of temperature, showing shifts beginning at 140 K, with sharp anomalies at 180 K, and further changes of slope at 200 K for a BFO single crystal.

Temperature-dependent x-ray diffraction data on single crystals was performed from 80 to 300 K using a high-resolution two-axis x-ray diffractometer in Bragg-Brentano geometry (focalization circle with diameter of 50 cm) with the Cu-K $\beta$  radiation ( $\lambda = 1.3922 \text{ \AA}$ ) issued from a 18 kW rotating anode (Rigaku). In addition, we also performed grazing incident diffraction (GID) experiments at ID01 beamline at European Synchrotron Radiation Facilities (ESRF, Grenoble, France). We chose 7 keV and  $0.2^\circ$  as incidence angle, thereby limiting our information depth to a few nanometers. The BiFeO<sub>3</sub> crystal was cooled using the Oxford Cryojet blowing cold nitrogen gas on the sample, while the temperature was measured in the gas stream by a thermocouple attached at one side of the crystal (1 mm thick). The crystal employed was the same one as in the GID high-temperature study.<sup>36</sup>

The ac impedance ( $Z$  modulus and the  $\delta$  phase) was measured on a single crystal from 80 to 400 K on cooling and heating using an Agilent 4294A impedance analyzer with frequencies from 1.5 kHz up to 1 MHz. Silver paste was used as top and bottom electrodes. The current discharge or pyroelectric current was also recorded between 100 and 300 K using a Keithley electrometer.

Finally, we also performed first-principle calculations to study the potential role played by the vacancies in the properties. The calculations have been performed with the SIESTA code.<sup>47,48</sup> Two approximations for the exchange-correlation energy have been tested: the local density approximation (LDA) and the generalized gradient approximation in the form of Perdew, Burke, and Ernzerhof (GGA-PBE).<sup>49</sup> Troullier-Martins pseudopotentials have been used. Semicore electrons ( $3p$  for Fe,  $5d$  for Bi) are explicitly treated as valence electrons. The equivalent plane-wave cutoff for the grid is 200 Ry in the LDA case and 400 Ry in the GGA case. The excitation energy defining the range of the atomic orbitals is 0.01 Ry. The periodic parts of the Kohn-Sham wave functions are expanded on a basis of numerical atomic orbitals of double-zeta type (plus polarization orbitals). A single-zeta  $7s$  type orbital is added in the basis set of Bi.

### III. RESULTS

#### A. Elastic changes in BiFeO<sub>3</sub> below room temperature

As already mentioned, the low- $T$  phase transitions were evidenced using Raman spectroscopy techniques, especially in the low-wavelength region through the analysis of the magnetic field cooling (MFC) versus zero field cooling (MZFC) regime and the study of the electromagnons.<sup>23,24</sup> The Raman spectrum measured at 80 K on a single crystal shows no significant change compared to that at room temperature. However, it is known that any static and/or dynamic changes in the structure should, in principle, lead to a variation in the phonon behavior, and the analysis of the wave number, intensity, and/or linewidth evolution of the whole spectra as a function of temperature is expected to give insight into those changes. Figure 2 shows typical temperature dependences of the wavelength position for two different Raman bands. Several features are noteworthy. First, all the Raman phonon modes, and not only those related to the electromagnons,<sup>23,24</sup> show changes in the low-temperature regime: Whatever the mode, a change of slope occurs at 140 K. However, the sign of the slope change (softening versus hardening) is different for different modes. At higher temperature, a new change of slope appears either at 200 K or higher or unexpectedly at 180 K. As an example, the  $E$ -type phonon mode position at around  $80 \text{ cm}^{-1}$  [Fig. 2(a)] is nearly constant at  $\sim 83 \text{ cm}^{-1}$  from 80 to 140 K and then continuously increases until 180 K, reaching a value of  $\sim 97 \text{ cm}^{-1}$  that remains constant until room temperature. Note that the same behavior was found in several different samples including single crystals and ceramics.

Phonon frequencies are directly linked to interatomic forces, so the fact that all the Raman lines shift in the 140–200 K range signals that changes in the elastic constants are taking place. In order to test the extent to which these are related to changes in elastic properties, single-crystal and ceramic samples have been investigated by resonant ultrasound spectroscopy (RUS).<sup>42</sup> Elastic resonances are dominated by shearing motions and the measured elastic constants scale



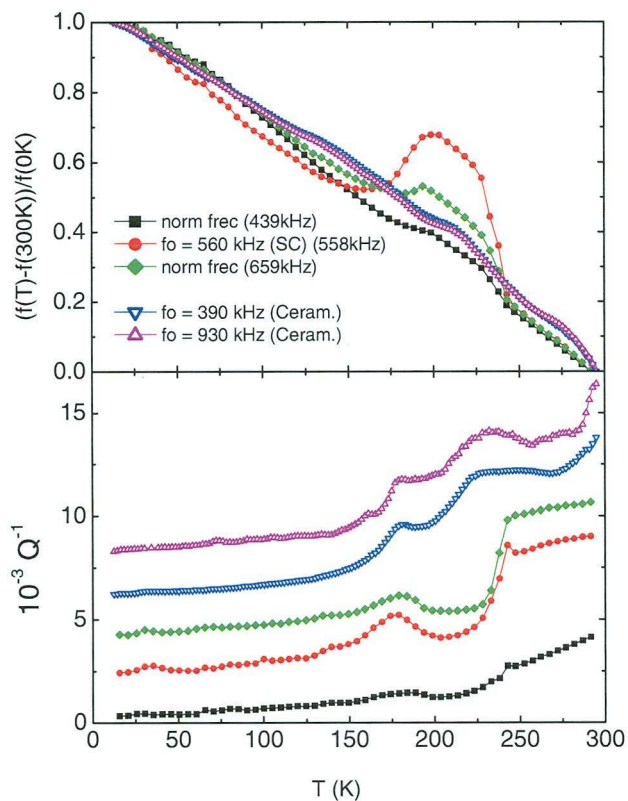


FIG. 3. (Color online) (Top) RUS results for a BFO single crystal (full symbols) and a ceramic sample (open symbols): The resonant frequencies increase between  $\sim 140$  and  $\sim 240$  K, indicating a hardening of the lattice between these two temperatures. (Bottom) The elastic loss (inverse of the quality factor) shows gradual increase above  $\sim 150$  K, with peaks at  $\sim 180$  K and at  $220$ – $240$  K depending on the sample.

with  $f^2$  (where  $f$  are the frequencies of resonance peaks). The inverse mechanical quality factor, usually given as  $Q^{-1} = \Delta f / f$ , is a measure of anelastic losses associated with the application of a dynamic shear stress. Results for  $f$  and  $Q^{-1}$  obtained from different resonance peaks are given in Fig. 3.

Resonance frequencies, normalized to their value at 300 K, all decrease with increasing temperature, consistent with thermal softening of the lattice. A deviation from the linear thermal softening starts to appear around 150 K, with a steep increase (elastic stiffening) between  $\sim 175$  and  $\sim 200$  K. An equivalently steep drop back to the baseline occurs between  $\sim 225$  and  $\sim 250$  K. The breaks in slope of resonance frequencies of the single-crystal sample near 150 and 200 K coincide with breaks in slope of the Raman data (Fig. 2).

Frequency data for resonances of the ceramic sample do not show these sharp features, but data for  $Q^{-1}$  (elastic losses) from both the ceramic and single-crystal samples show similar anomalies in the temperature range of interest: (i) There is a slight break in the slope of the baseline variation in the vicinity of 150 K, from relatively low and fairly constant losses at low temperatures to a trend of increasing loss with increasing temperature; (ii) all the resonances show a peak in  $Q^{-1}$  centered on  $\sim 180$  K, and (iii) there is a further peak or break in slope at  $\sim 240$  K for the single-crystal data, and less

well resolved anomalies above  $\sim 225$  K for the ceramic sample. The break in the slope of  $Q^{-1}$  near 150 K is reminiscent of increasing dissipation due to disordering of protons during heating of the mineral lawsonite,<sup>46</sup> though the magnitude of the effect is much smaller. If the analogy is correct, some element of structural or magnetic disordering occurs within the samples above  $\sim 150$  K. Increasing dissipation implied by the  $Q^{-1}$  data could be understood as implying that the structure stable above  $\sim 150$  K has more disorder (static or dynamic) in comparison with the structure stable at lower temperatures.

All in all, the RUS measurements indicate significant coupling of strain with the changes in structural or magnetic properties identified in other measurements, and suggest the presence of a dissipative—perhaps disordered—state in the temperature range 150–250 K. The measurements, however, do not allow discrimination between phase transitions which occur within the bulk of the sample from one which only occurs within the skin. We nevertheless note that elastic properties probed by sound-propagation measurements (which are only sensitive to bulk as the sound wavelength is of the order of hundreds of micrometers) show no anomalies at all in this temperature range.<sup>40</sup>

### B. Evidence of skin layer phase transitions

In order to gain further insight into these low-temperature elastic anomalies, x-ray diffraction (XRD) was also used. In particular, to discriminate between surface and bulk contributions, we will compare data collected in grazing incidence diffraction (GID) and standard coplanar geometry. The grazing incidence measurements were performed in the ID01 line at the ESRF synchrotron in Grenoble. In contrast to the bulk-sensitive coplanar diffraction, GID allows tuning of the information depth by tuning the incidence angle and/or the photon energy. Following the approach of the preceding high-temperature study,<sup>36</sup> we monitored only the changes in the length of the reciprocal space vectors (modulus of  $q$ ) rather than both their length and direction (vector  $q$ ). This allows for evidence of structural changes confined in skin layers while circumventing the alignment difficulties inherent to single crystals with strong twinning and mosaicity.

Figure 4 (open symbols) shows the relative change of  $|q|$  for the (202) reflection measured on a single crystal as a function of temperature in the heating regime from 100 to 300 K. The bulk temperature dependence displays no hint of structural change inside the crystal in this temperature range, and only a subtle change in thermal dilatation coefficient from  $6.4 \times 10^{-6} \text{ K}^{-1}$  to  $9.4 \times 10^{-6} \text{ K}^{-1}$  at 180 K—which is also the temperature of the first peak in anelastic loss. In contrast, the surface-sensitive data for the (101) peak reveal an abrupt expansion up to  $\sim 1\%$  between  $T = 140$  K and  $T \approx 180$  K (Fig. 4, solid symbols). This anomaly was not detected in coplanar diffraction where the information depth surpasses a few micrometers. This indicates that the structural change is confined in a surface layer. The surface layer thickness cannot be stated beyond the upper bound placed by the penetration depth of the coplanar geometry (micrometers), but the sample is nevertheless the same for which a transition at  $T^* = 550$  K was estimated to be within the topmost 10 nm. It appears that in addition to the phase transition occurring at 550 K, the surface



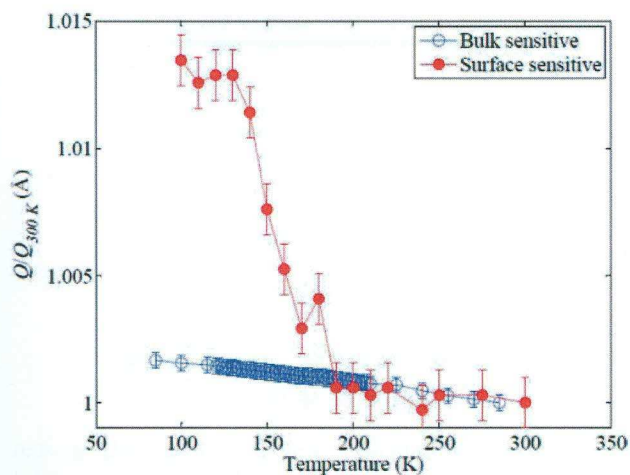


FIG. 4. (Color online) Relative change of the reciprocal lattice vector  $|g|$  as a function of temperature probing the bulk of a single crystal (blue open symbols) and the topmost surface (red solid symbols). The surface data show a rapid expansion of the lattice parameter upon heating above 140 K, and this feature is absent from the bulk.

layer undergoes at least another phase transition at  $\sim 140$  K, reinforcing the view that it has its own phase diagram very different from that of the bulk.

### C. Electronic properties of the BiFeO<sub>3</sub> surface

Impedance analysis is an effective tool to probe the electronic properties of surface layers. In particular, it has been noted that Maxwell-Wagner behavior usually arises whenever there is a substantial difference in conductivity between the bulk and interfacial regions; at low enough frequencies, the contact impedance dominates and the interfacial properties are evidenced.<sup>42,43,47,50</sup> Indeed, this appears to be the case also for our single crystals (Fig. 5).

The impedance shows a strong frequency dependence typical of two lossy dielectric components in series.<sup>42,43,47</sup> However, a sudden drop of the impedance (which is equivalent to a sudden increase of the capacitance) is also observed at 140 K, which is frequency independent and thus corresponds to a true phase transition. The fact that the jump in the impedance is bigger for lower frequencies is consistent with the phase transition occurring at the interface of the crystal, in a behavior analogous to that observed in the interfacial  $T^*$  transition at 550 K.<sup>36</sup> The surface transition appears to be first order, as attested by the sharpness of the jump and by the difference in the critical temperatures in cooling and heating regime (Fig. 5, right). This is also consistent with the change in the unit cell volume observed in the grazing incidence diffraction results shown in Fig. 4. Recently, Kumar *et al.* (Ref. 51) have discovered abrupt onsets of in-plane dielectric loss at 550 and 201 K by using interdigital electrodes, which are more sensitive to in-plane surface impedance. This complements our data and supports our interpretation as surface transitions.

In order to test the electronic properties of the surface, we also performed pyroelectric measurements. These are shown in Fig. 6. The results show a very sharp and sudden peak

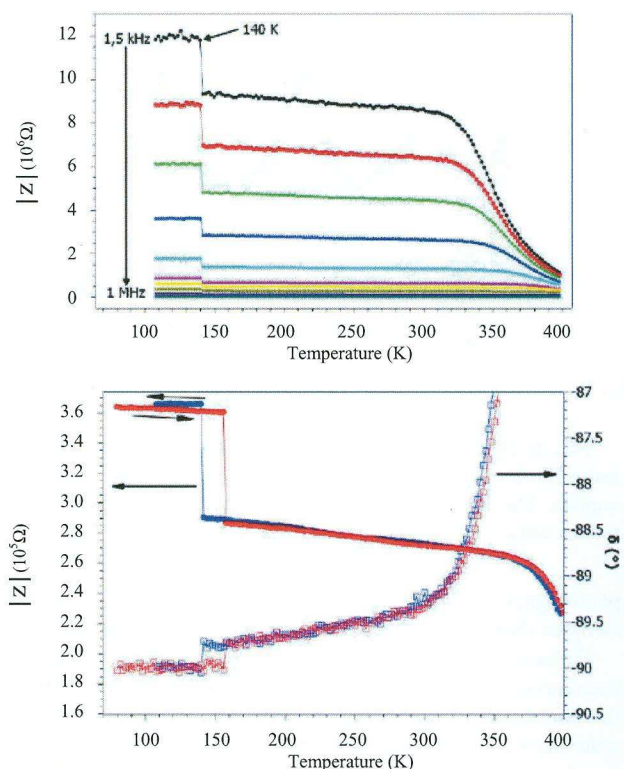


FIG. 5. (Color online) (Top) Z modulus versus temperature and frequency; (bottom): Z modulus and impedance phase angle as a function of temperature on heating and cooling showing a first-order phase transition at  $\sim 140$  K for a BFO single crystal.

in pyroelectric current near 140 K. We measured the current discharge both for zero-field-cooling-and-heating regime and for zero-field-heating-after-field-cooling regime; in addition to the 140 K anomaly, the field-cooled sample shows a further broad anomaly around 200 K, plus a sharp jump at 280 K. The last anomaly is ascribed to artifact during the measurement. It is worth mentioning that the anomalies at  $\sim 140$  and  $\sim 200$  K are observed in many different samples, included some with unprocessed surfaces, indicating that those anomalies are not related to chemical etching or mechanical polishing effects.

Unlike in a classical ferroelectric phase transition, where the pyroelectric peak position in temperature does not depend on the poling history of the sample, here the field-cooled sample has the peak at a significantly lower temperature (5 K less) than the zero-field-cooled one. This shift of peak position toward lower temperatures is a fingerprint of a thermally stimulated current: a current that is generated by emission of a trapped charge from a trap level in the forbidden gap of BFO.<sup>52</sup> So, while pyroelectric currents are often related to changes in polarization, here we believe that the current we measured is *not* due to ferroelectricity but to charge injection and thermally stimulated emission from trapping centers. When the skin layer undergoes the phase transition, the Fermi level is likely to experience an abrupt rearrangement. As a result, interfacial defect states below the Fermi level might cross over above it and release their charge, causing the abrupt thermally stimulated peak in current. The electronic mechanism for the 140 K pyroelectriclike anomaly is also consistent with electron



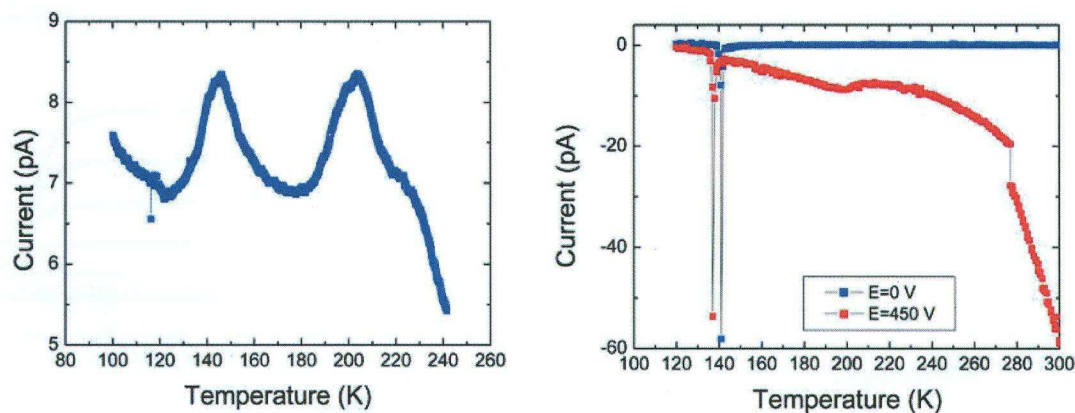


FIG. 6. (Color online) Discharge current anomalies in  $\text{BiFeO}_3$  single crystals. (Left) pristine samples show two clear anomalies at  $\sim 140$  and  $\sim 200$  K, though in subsequent runs (right) only the 140 K anomaly is clear, although the 200 K anomaly is still visible for field-cooled samples. The field-cooling dependence of the peak temperature for the 140 K anomaly indicates that this pyroelectriclike current is due to the sudden carrier emission from trap levels triggered by the surface phase transition.

paramagnetic resonance results in large surface-to-volume samples ( $\text{BiFeO}_3$  nanotubes), discussed in the following.

Because the analyses above emphasize surface phase transitions, it seems useful to prepare samples which maximize the surface-to-volume ratio. To this aim, we prepared BFO nanotubes and characterized them via EPR, which is sensitive to relatively small volumes. The EPR curves are fitted with a Lorentzian line shape when the sample is purely insulator and the line is perfectly symmetric, or with a Dysonian-type function when the line is asymmetric reflecting the conduction component:  $\text{EPR}_{\text{Dysonian}} = \text{Absorption} \times \cos(\alpha) + \text{Dispersion} \times \sin(\alpha)$ . The asymmetry is described by the parameter  $\alpha$  and its value for insulators is zero and 1 for a full conductor.<sup>53</sup>

It is clear from the EPR data (Fig. 7) that the sample's conductivity is maximum at  $\sim 140$  K and that the conductivity behavior changes again, less abruptly, at  $\sim 200$  K. Therefore, the EPR data for the nanotubes also indicate an increase in surface charge density at 140 K, consistent with detrapping trap levels; the charge released at 140 K causes the large pyroelectriclike current observed in Fig. 6.

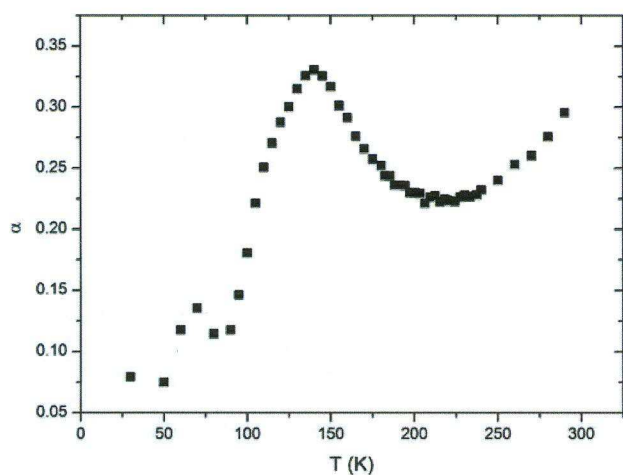


FIG. 7. Alpha parameter reflecting the asymmetry of the EPR curves for BFO nanotubes.

Also relevant to the results here, we note that  $\text{BiFeO}_3$  samples with large surface-to-volume ratios (e.g., nanocrystals) have been shown to display spin-glass behavior.<sup>54</sup> Glassy effects are well known for small particles of antiferromagnets in general, where the lack of spin compensation at the surface is thought to frustrate the long-range magnetic order (e.g.,  $\text{NiO}$ <sup>55,56</sup>). Three EPR observations (Fig. 8) are similar to those known in other spin glasses, especially that in  $\text{Cd}_{1-x}\text{Mn}_x\text{Te}$ :<sup>57</sup> (1) The gyromagnetic ratio is  $g > 2$  above the apparent spin-glass transition at  $T_{sg} = 140$  K and  $g =$  approximately 2.0 below; (2) the decrease in  $g$  value at 140 K is rather abrupt with temperature and nearly 1% in magnitude; (3) there is a divergence in EPR linewidth that satisfies a dependence  $\Gamma = \Gamma_0 + \Gamma_1 \exp[-T/T_f]$ , as shown in Fig. 8, with an extrapolated freezing temperature  $T_f = 33 \pm 3$  K that is in good agreement with that measured independently as  $29.4 \pm 0.2$  K.<sup>29</sup>

We note also that the EPR susceptibility of the nanotubes is increased between 125 and 200 K, which is essentially the same temperature range (bearing in mind the sample difference between the nanotubes and the single crystals) where structural disorder has been inferred from elastic spectroscopy. This suggests that the structural disorder has its replica in the magnetic behavior. We note also that the glassy fitting to the EPR linewidth (Fig. 8, middle) departs from the actual data below the skin transition temperature, suggesting a transition from a glassy or magnetically soft state to a more rigidly ordered configuration, the details of which are at this point unknown. We nevertheless emphasize that it is not easy to distinguish magnetoelectric spin glasses from crystals with domain-wall pinning,<sup>58,59</sup> both of which would be consistent with the magnetic and elastic results. An extremely fine pattern of domains has in fact been observed in the near-surface region of  $\text{BiFeO}_3$ <sup>60,61</sup> so this is not out of the question.

#### D. Role of Bi vacancies in $\text{BiFeO}_3$ properties

Surface reconstruction/relaxation can explain some of the above experimental features. However, it is worth mentioning that some defects, more predominant at the surface, might



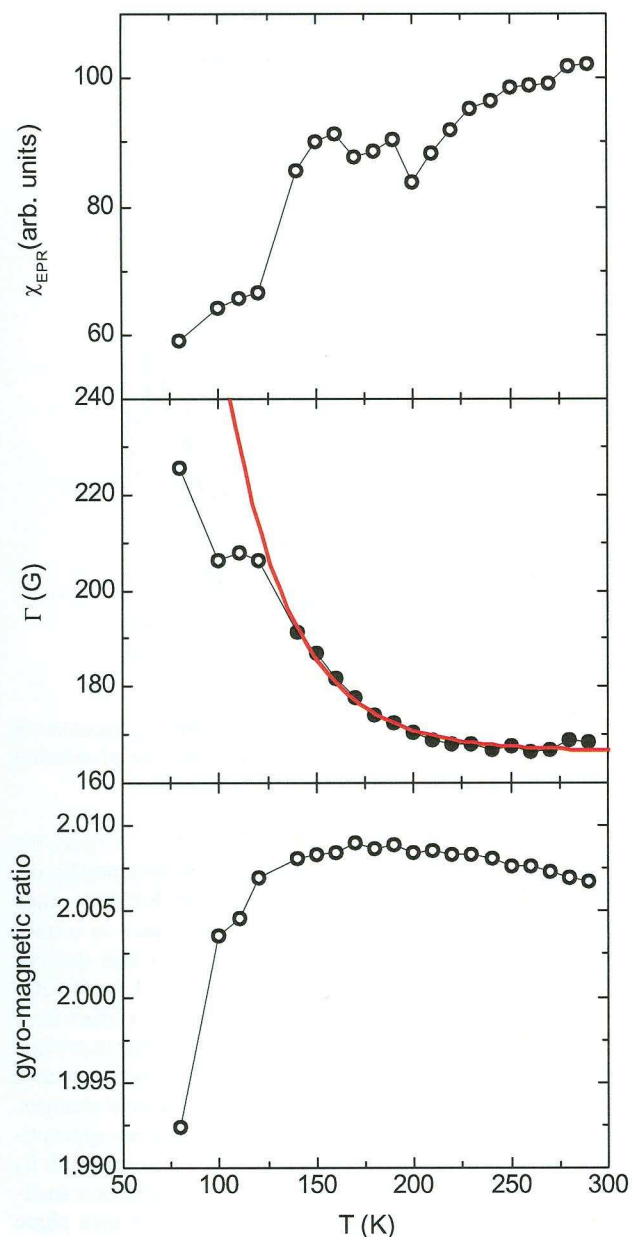


FIG. 8. (Color online) (Top panel) Electron paramagnetic susceptibility, showing an increase between  $\sim 125$  and  $200$  K, which is close to the temperature range where elastic softening and anomalous skin expansion has been detected; (middle panel) an exponential fitting to the EPR linewidth yields an extrapolated freezing temperature of  $\sim 33$  K; the experimental data depart from the glassy fit for temperatures below  $140$  K; (lower panel) the gyromagnetic factor also shows a rather abrupt drop below the skin transition temperature. The EPR susceptibility shows a sharp drop at  $201$  K, whereas the  $g$  value (bottom panel) shows a broad maximum near this temperature. These data have been obtained for BFO nanotubes.

be also a plausible explanation. Therefore, to gain further insight into the role of defects as a possible origin of the experimental observations, we performed some first-principle density-functional calculations by introducing some defects which can exist at the surface of BFO samples. Due to

bismuth volatility, the most likely defects are Bi vacancies. We first optimized bulk BFO in its  $R3c$  phase (both in LDA and GGA) and used the lattice constant obtained to build a  $2 \times 2 \times 2$  supercell (thus containing 80 atoms), whose shape and volume was kept fixed. Then Bi vacancies were introduced in the supercell, in different charge states  $(0, -1, -2, -3)$ . In the case of charged defects, neutrality is insured by adding a background compensating jellium. Finally the atomic geometries were optimized by using a conjugate-gradient scheme, so as to obtain Cartesian components of atomic forces below  $0.04$  eV/Å. Figure 9 shows the electronic density of states (DOS) versus energy for stoichiometric (black curve) and nonstoichiometric BFO supercells containing Bi vacancies.

The calculated LDA energy band gap for stoichiometric BFO is  $0.8$  eV, an underestimate compared with the experimental value  $2.74$  eV;<sup>13</sup> this underestimate is typical of LDA calculations. The main effect of Bi vacancies, whatever the charge of the defect, is to introduce energy levels within the band gap. These levels can explain the trapping-detrapping process suggested by our electrical measurements.

It is also interesting to remark that Bi vacancies modify the magnetism of the system. Electrons are rearranged giving rise in some cases to a net magnetic moment probably associated with a hole polaron. This rearrangement which can occur within the surface may then explain the concomitant magnetic anomalies observed in the magnon spectra and in the EPR susceptibility. The possibility of the existence of a polaron within the close surface is reinforced because this charge-phonon coupling would also explain the anomalies observed in XRD, Raman, and RUS data. Therefore, Bi vacancies as a possible origin of the experimental observations give a plausible explanation, although further calculations are required to have a better understanding of the physics of the BiFeO<sub>3</sub> surface, including intrinsic effects such as surface tension and polar termination.

#### IV. DISCUSSION

The grazing incidence XRD results show unambiguously that the anomaly at  $140$  K corresponds to a surface phase transition. Its key features are an abrupt change in unit cell volume (which expands by  $1\%$  on heating, Fig. 4), and a concomitant change in electronic structure, with an impurity level crossing the Fermi level and releasing charge, as signaled by the field-dependent pyroelectriclike discharge (Fig. 6) and increased conductivity inferred from ac impedance (Fig. 5) and EPR analysis (Fig. 7). *Ab initio* calculations suggest that Bi vacancies may be at the origin of the impurity levels (Fig. 9). The Raman spectra also show that the  $140$  K anomaly is strongest in the magnon peaks, and EPR confirms that this transition affects the magnetic structure, as also suggested by the first-principle calculations.

Now the question is what could be the origin of these anomalies. In the perovskite structure, two structural degrees of freedom can be considered; either atomic (polar) displacements or oxygen octahedral tilts. In the case of magnetic materials, as is BiFeO<sub>3</sub>, a third degree of freedom is the spin. Raman spectroscopy is very sensitive to oxygen octahedral rotations<sup>62</sup> and yet the number of peaks in the Raman spectra was not



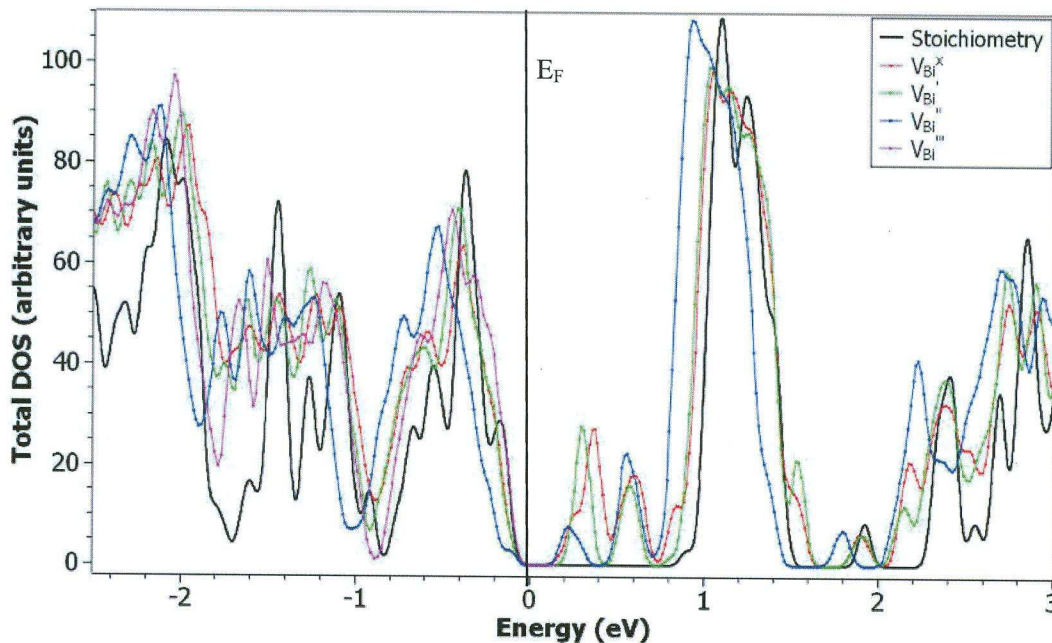


FIG. 9. (Color online) Density of states versus energy from *ab initio* calculations for pure BFO (black) and BFO with  $V_{\text{Bi}}$  vacancies in different charge states ( $V_{\text{Bi}}^x$ ,  $V_{\text{Bi}}^y$ ,  $V_{\text{Bi}}^z$ ,  $V_{\text{Bi}}^w$ ). The Fermi energy  $E_F$  corresponds to that of the stoichiometric system. In the case of defective systems, this energy lies in the gap, with localized states partially occupied.

observed to change as a function of temperature—though surface-sensitive UV Raman would be desirable to confirm this. The abrupt change in the lattice volume, as indicated by the grazing incidence XRD, points instead to a change in atomic distances without a change in symmetry. Given that the in-plane lattice parameters of the surface must be coherent with those of the skin, this means that a strong uniaxial strain is developed at 140 K, which is relevant because the uniaxial strain has recently been reported to have a very strong effect on the magnetism of  $\text{BiFeO}_3$ .<sup>37</sup> The change in unit cell volume is the likely culprit of the crossover of a shallow impurity level across the Fermi line, resulting in charge release from the defect level. *Ab initio* calculations suggest that the defect levels may be bismuth vacancies. Bismuth is known to be a fairly volatile element, and it is also significant in this respect that a disorder of the bismuth lattice has been reported for ultra-fine-grained  $\text{BiFeO}_3$ , where the surface-to-volume ratio is large.<sup>63</sup>

## V. CONCLUSIONS

The data presented here confirm the interpretation of the 140 K anomaly in  $\text{BiFeO}_3$  as a surface phase transition, with surface effects detected in very many different bulk single crystals and exacerbated in nanotubes owing to their very high surface-to-volume ratio. The main features of this phase transition are a sharp volume change without actual change of symmetry; sharp emission of charge at 140 K (pyroelectriclike current), and maximum in conductivity (peak in the  $\alpha$  parameter of the EPR Dysonian line shape), consistent with a crossover between an impurity level and the Fermi level, and structural and magnetic disorder between 140 and  $\sim 200$  K.

As was argued for its high-temperature  $T^*$  counterpart, the surface phase transition at 140 K is likely to be aided by the inherent complexity of the phase diagram of  $\text{BiFeO}_3$ , which is very sensitive to even small perturbations<sup>64</sup> such as surface tension or local strain fields around vacancies and defects. A melting of the Bi sublattice has been reported for  $\text{BiFeO}_3$  powders with a radius smaller than 9 nm (Ref. 65) if there were Bi vacancies at the surface layer, these would be able to provide both electronic impurity levels and local strain fields capable of explaining the electronic, magnetic, and structural changes.

More generally, these results indicate that it is not appropriate in general to treat  $\text{BiFeO}_3$  as a homogeneous material. Its skin layer is rather different from the bulk, having its own structural, electronic, and magnetic properties, and its own phase diagram that already includes at least two confirmed phase transitions at 140 and 550 K, as well as a probable glassy state between 140 and 230 K. Other anomalies reported for BFO as, for instance, that referred to as the Polomska transition,<sup>66</sup> which is associated with a spin-wave propagation<sup>67</sup> can be also attributed to skin effect.<sup>68</sup> The surface is at least as important as the bulk for functional devices, as it determines key properties such as magnetic exchange bias and conductive barrier height. It is therefore of utmost importance that its nature and properties be fully understood.

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