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# **Superconducting Group IV Semiconductors**

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We present recent achievements and predictions in the field of doping-induced superconductivity in column IV-based covalent semiconductors, with a focus on Bdoped diamond and silicon. Despite the amount of experimental and theoretical work produced over the last four years, many open questions and puzzling results remain to be clarified. The nature of the coupling (electronic correlation and/or phonon-mediated), the relationship between the doping concentration and the critical temperature  $(T<sub>C</sub>)$ , which determines the prospects for higher transition temperatures, as well as the influence of disorder and dopant homogeneity, are debated issues that will determine the future of the field. We suggest that innovative superconducting devices, combining specific properties of diamond or silicon, and the maturity of semiconductor-based technologies, will soon be developed.

### **1) Introduction**

It was probably the discovery of a superconducting transition around 40 K in the rather simple  $MgB_2$  compound<sup>[1]</sup> that revived the interest for a specific class of superconducting materials, belonging to the so-called covalent metals<sup>[2]</sup>. These superconducting covalent systems (see box 1), including B-doped diamond<sup>[3]</sup>, silicon<sup>[4]</sup>, and silicon carbide<sup>[5,6]</sup>, Ba-doped silicon clathrates<sup>[7,8]</sup>, alkali-doped fullerenes<sup>[9,10]</sup> and the CaC<sub>6</sub> or YbC<sub>6</sub> intercalated graphites<sup>[11,12]</sup>, share the specificity of involving at least one relatively light element and of preserving strongly directional covalent bonds in their metallic state. The implications of this

covalent character are important in superconductors in which Cooper pairs are coupled through phonons. The use of perturbation theory to study the renormalisation of the electron-electron repulsion by the electron-phonon interaction leads to the so-called Eliashberg equations<sup>[13]</sup> and to the celebrated McMillan formula<sup>[13]</sup> relating, in an approximate way, the superconducting transition temperature  $T_c$  to an average phonon frequency  $\omega_{\text{in}}$ , the electron-phonon coupling parameter  $\lambda_{ep}$  and the screened and retarded Coulomb repulsion parameter µ\*:

$$
T_C = \frac{\hbar \omega_{\text{ln}}}{1.2k_B} \exp \left[ \frac{-1.04(1 + \lambda_{ep})}{\lambda_{ep} - \mu^*(1 + 0.62\lambda_{ep})} \right]
$$

Clearly, low atomic masses lead to high frequency phonon modes, which may enhance the  $\omega_{\text{in}}$  prefactor and thus T<sub>C</sub>. This is the basis of the so-called isotope effect. Furthermore, strong covalent bonding will lead both to large phonon frequencies and a large electron-phonon coupling potential  $V_{en} = \lambda_{en}/N(E_F)$ , with  $N(E_F)$  the density of states at the Fermi level, also contributing to enhance  $T_C$ . Even within a phonon-mediated coupling scenario, these criteria do not necessarily warrant a large  $T_c$  since increasing  $\lambda_{ep}$  may also lead to a lattice instability, and a large electron-phonon potential  $V_{ep}$  may be impaired by a low density  $N(E_F)$ . However, these simple considerations, as well as more elaborate surveys and predictions of a larger  $T_c$  <sup>[14-16]</sup>, have provided much incentive to study this class of materials.

The most familiar covalent systems are certainly diamond and silicon. The former can be considered as the prototype insulating material with unsurpassed incompressibility and hardness, and the latter is the textbook semiconductor, which has laid the grounds for today's electronic industry. When the doping concentration in semiconductors (or insulators) goes beyond a critical value, a metal-insulator transition (MIT) takes place (see box 2), turning the host material into a degenerate semiconductor with the Fermi level entering the valence (conduction) bands in case of *p*-type (*n*-type) doping, and eventually into a superconductor. Turning diamond into a metal clearly makes this system an ideal candidate for superconductivity as it offers all the qualities listed above, with very directional bonds and optical phonons in the 150 meV range (compared to a few tens of meV in classical metals). This is where recent breakthroughs in the synthesis of highly doped diamond<sup>[3]</sup>, silicon<sup>[4,17]</sup> and silicon-carbide<sup>[5,6]</sup> samples come in.

### **2) Superconducting semiconductors : from early predictions to recent discoveries**

The idea that semiconductors doped beyond the MIT could become superconducting was already discussed in the mid-sixties $[18,19]$ . Superconductivity was observed subsequently in reduced  $SrTiO<sub>3</sub>$  perovskite single crystals  $^{[20,21]}$  and in  $Ge_{1-x}Te$  alloys<sup>[22]</sup>. However, the interest in superconducting dopedsemiconductors did not last, probably because of the low critical temperatures (at most  $0.5K^{[21]}$ ).

We will not discuss here in detail the case of the fullerenes for which excellent reviews have been written (see for instance<sup>[23,24]</sup>). The evolution of the electronphonon coupling strength with cage curvature, the large value of the  $\omega_{\rm ph}/W$ (coupling phonon frequencies to electronic bandwidth) ratio, the proximity of a MIT driven by electronic correlations (see Box 2), and the local nature of the coupling phonons (Jahn-Teller modes) are however aspects that will be relevant to the cases of doped diamond and silicon as discussed below.

In 1995, it has been shown<sup>[7]</sup> that barium-intercalated  $Ba_8Si-46$  clathrates undergo a superconducting transition around 8 K (see also<sup>[2,8]</sup>). Silicon clathrates are 3D semiconductors made of face-sharing  $Si_n$  clusters (n = 20,24,28) as building blocks<sup>[25]</sup> (see box 1). Such systems are very close to standard silicon, each atom being fourfold coordinated with a local  $sp^3$  tetrahedral environment, but with a cage-like structure that allows large doping by intercalation at the centre of the cages. *Ab initio* calculations proved that the phonons involved in the transition were mainly the silicon network vibrational modes, while barium would serve as an *n*type dopant<sup>[26]</sup>. This was the first evidence that highly-doped column-IV  $sp^3$ covalent insulators, or semiconductors, could be turned into superconductors with a  $T_c$  exceeding a few Kelvin.

On the other hand, research efforts were also quite intense in the apparently distant field of superhard materials belonging to the B:C:N chemical composition triangle. While diamond still stands out as the hardest crystal known, the significant hardness of other materials such as  $B_4C$ , BN or  $BC_2N$  has stimulated creative synthesis strategies : in 2004, two groups<sup>[27,28]</sup> performed High Pressure High Temperature (HPHT) treatments to obtain carbon borides, but also got highly doped (2-3 at.%) polycrystalline diamond. Then, bridging the gap separating the super-hardness and superconductivity communities, doped diamond was found to be superconducting around  $4K^{3}$ , paving the way for systematic studies of superhard superconducting materials<sup>[29]</sup>. Since then, superconducting polycrystalline, single crystal or even nanocrystalline boron-doped diamond samples have been synthesized by a large number of groups using the original HPHT  $[30]$  techniques or alternative chemical vapor deposition growth techniques<sup>[31-35]</sup>, and transition temperatures up to 10 K have been reported $^{[36]}$ .

In 2006, using a gas immersion laser doping (GILD) technique (see box 3), which allows to dope silicon well beyond the thermodynamic solubility limit, a superconducting transition in highly boron-doped silicon was reported with a  $T<sub>C</sub>$ around 0.35 K for a boron concentration of the order of 8 at.  $\frac{6}{4,37}$ . Finally, a superconducting transition was also observed recently in boron-doped  $SiC^{[5,6]}$  with a  $T_c$  of 1.4 K. In all three cases (diamond, Si and SiC), boron was the source of hole-doping.

#### **3) Phonon-mediated or correlation-driven mechanisms ?**

The question "where are the electrons?" takes a special twist in doped semiconductors<sup>[38]</sup> since across the MIT, the Fermi level is expected to shift from an impurity band to a degenerate situation where it is located in the valence bands (for *p*-type doping, see box 2). The coincidence of the superconducting transition with the MIT in doped diamond has triggered much experimental and theoretical work to understand the character of the electrons at the Fermi level involved in the superconducting transition, and the origin of the attractive interaction leading to Cooper pairs. Indeed, when the Fermi level is located in a narrow electronic band, the so-called resonant valence band (RVB) model can explain a superconducting transition with a specific pairing mechanism, alternative to the standard phonon mediation. Besides the case of doped diamond $\binom{39}{39}$ , such a correlation-driven mechanism has for instance been proposed in the case of doped fullerenes  $[40,41]$ .

*Ab initio* calculations within density functional theory performed on highly-doped diamond<sup>[42-47]</sup>, silicon  $[4,48]$  and silicon carbide<sup>[49]</sup> consistently led to the picture that in the percent doping range, the Fermi levels lies a few tenths of an eV below the top of the valence bands. These results where obtained either within the virtual crystal approximation  $(VCA)^{[42-44]}$  or supercell  $(SC)^{[45-47]}$  calculations for various cell geometries and doping concentrations. Furthermore, the effect of disorder on the electronic properties was studied with the coherent potential approximation  $(CPA)^{[50]}$  leading again to the picture of a degenerate system with the Fermi level entering the valence bands broadened by disorder. This degenerate picture with no signature of an impurity band has been rapidly confirmed by experimental angleresolved photoemission experiments performed on diamond films<sup>[51]</sup>. Additional evidence for deep localized states in the gap came from element-sensitive soft X-

ray emission and absorption spectroscopy, together with the conclusion that in the bulk of a superconductive sample, the Fermi level of the normal state was lying below the top of the valence band, in a region where boron-related delocalized states are also present<sup>[52]</sup>. However, these theoretical and experimental results were obtained in the very large doping limit, away from the MIT transition, and the question of what happens close to this transition remains open.

In the absence of a narrow impurity band, the best guess for explaining the superconducting transition is the phonon-mediated mechanism. *Ab initio* simulations explored this mechanism by calculating the electron-phonon coupling parameter  $\lambda_{ep}$  again within a variety of VCA and SC approaches. For typical doping concentrations of a few percent,  $\lambda_{ep}$  was found to range between 0.3 and 0.5, values which are consistent with the experimental  $T<sub>C</sub>$  values assuming that the retarded Coulomb pseudo-potential  $\mu^* \sim 0.1$ , a typical value for metals. However, the absence of substitutional disorder in *ab initio* SC and VCA calculations, as well as the possibility to adjust the parameter  $\mu^*$ , may impair the conclusiveness of such calculations. It is worth noting in this respect that the very large value of the phonon energy  $(\sim 120 \text{ meV})$  is comparable to the Fermi energy, leading potentially to a much weaker screening and a larger µ\* value than in usual metals. Furthermore, Migdal's theorem  $[53]$ , which exploits the decoupling of electronic and phonon energies to remain at lowest order in treating the electron phononinteraction as a perturbation, is in principle violated, so that strong non-adiabatic effects and deviations from the standard Bardeen-Cooper-Schrieffer (BCS)<sup>[54]</sup> theory may be expected. However, accurate dynamical mean-field theory calculations in the case of fullerenes, presenting a similar electron to phonon energy ratio, led to the conclusion that for  $\lambda_{ep}$  lower than  $\sim 0.5$ , the standard Migdal-Eliashberg approach and more accurate many-body treatments of electronelectron and electron-phonon interactions provide equivalent results<sup>[41]</sup>. From an experimental point of view, scanning tunnelling spectroscopy measurements $[55]$ performed on boron-doped diamond led to a  $2\Delta(T)/k_BT_C$  ratio with a thermal dependence perfectly matching the BCS weak-coupling limit<sup>[13]</sup> ( $\Delta(T)$  being the temperature-dependent quasiparticle band gap). Such a weak coupling limit is indeed expected for electron-phonon coupling since  $T_c$  is much smaller than the characteristic phonon energy. However, this result does not exclude any other weak coupling mechanism. Recent attempts at isotopic  ${}^{12}C$  by  ${}^{13}C$  substitution in polycrystalline superconducting samples grown by  $HPHT^{[30, 56]}$  provide preliminary evidences for a strong isotope effect on  $T_c$ : the reported exponent is larger than unity, possibly indicating intense Cooper pair breaking<sup>[57]</sup>.

If one assumes that the electron-phonon coupling scenario is valid, one still has to answer the question: « where are the phonons? », or, rather : "which phonons contribute to the coupling with the electrons?". The role of low-momentum optical modes has been emphasized by VCA simulations  $[42-44]$ . An analysis of the phonon sidebands appearing as Fermi edge replica in photoemission spectra [58] and of the softening of zone-centre optical modes in inelastic X-ray scattering has been interpreted in this sense  $[59]$ , although the observed softening was significantly smaller that that predicted by VCA. On the other hand, SC calculations for diamond  $[45-47]$  lead to a spectral distribution of the electron-phonon coupling parameter with a major contribution from the dopant-related stretching mode. A Kramers-Kronig analysis of reflectivity measurements [60] supports a possible contribution of boron-related vibrational modes. However, the experimental identification is difficult as the B-C stretching modes frequencies lie in the continuum of bulk diamond modes. Localized dopant-related vibrations could be easily identified in boron-doped silicon, since the B-Si stretching frequency is 60  $cm^{-1}$  above the bulk silicon zone-centre optical modes<sup>[4]</sup>. Clearly, the influence on  $T_c$  of isotopic substitutions  $({}^{11}B$  by  ${ }^{10}B)$  will bring much insight intoon the relevance of dopant-related modes  $^{[56, 61]}$ . However, the amount of substitutional boron in samples of distinct isotopic contents is quite difficult to control with the experimental precision needed to provide unquestionable evidence for an isotope effect.

### **4) Greatness and misery of superconducting doped diamond and related compounds**

Why should we bother about superconducting semiconductors ? Clearly, doping an insulator to turn it into a metal does not sound like the most straightforward way to obtain a good superconductor. As briefly mentioned in the introduction, the first answer lies in the strength of the electron-phonon coupling. As a matter of fact, in covalent metals, the electron-phonon potential  $V_{ep}$  turns out to be extremely large. This is precisely due to the covalent character of the bonding.

Along that line, *p*-type doped diamond is exceptional: the deformation potential associated with the zone-centre optical modes of diamond  $(sp<sup>3</sup>]$  bonds) was estimated<sup>[42,43]</sup> to be ~ 50% larger than that associated with the  $E_{2g}$  mode in MgB<sub>2</sub><sup>[42]</sup>. It may then sound surprising that the largest T<sub>C</sub> in doped diamond (~10K) is significantly smaller than in  $MgB_2$  (39 K). The explanation lies in different values of  $N(E_F)$ . While the layered  $MgB_2$  compound benefits from a strong 2D density of states, the density of states in 3D materials slowly rises with the square root of the Fermi energy. Larger chemical doping, alternative charge injection

techniques, or patterning into low dimensionality geometries, are potential solutions that remain to be explored.

A couple of interesting attempts to estimate quantitative bounds for the maximum phonon-mediated superconductivity in covalent metals have been proposed  $r$ ecently<sup>[14-16]</sup>. The analysis of the density of states and so-called effective McMillan-Hopfield parameter<sup>[15]</sup> led to the conclusion that, in randomly substituted cubic B<sub>x</sub>C compounds, T<sub>C</sub> could increase with doping up to 60 K for x ~0.3 within a rigid band model and assuming that  $\mu^*{\sim}0.12$ . Similarly, it was also predicted<sup>[16]</sup> that  $T_c$  could be equivalent to that of  $MgB_2$  in the cubic  $BC_5$  structure. Previous *ab initio* calculations suggested that carbon-doped boron icosahedra could be very good candidates for high  $T_{\text{C}}\text{s}^{[62]}$ .

Experimentally, however, the relation between boron content and  $T_c$  is quite unclear. The above mentioned  $BC_5$  structure has recently been synthesized using an HPHT technique  $[63]$ , but the nanocrystalline nature of this phase precluded any characterization of the superconducting properties so far. Similarly, a highly-doped diamond-like  $BC_{1.6}$  structure was synthesized<sup>[64]</sup>, but no trace of superconductivity was reported. Furthermore, it has been observed that increasing the doping concentration of diamond above a few percents does not necessarily lead to higher  $T_c$ s and that similar boron contents could lead to a wide range of  $T_c$  values<sup>[31-34]</sup>. This was suggested to result from the clustering of boron in inactive dimers<sup>[65,66]</sup> or from an increase in interstitial boron content<sup>[65]</sup>. The aggregation of boron at grain boundaries in polycrystalline diamond has also been recently reported in HPHT synthesized samples $^{[67]}$ .

An alternative route to high critical temperatures relies on the cage structures. The efficiency of  $sp<sup>3</sup>$  bonding in driving a large electron-phonon coupling, has been first highlighted in superconducting fullerenes<sup>[68]</sup>. It has been shown through a combination of experimental and theoretical studies that  $V_{ep}$  increases dramatically from C<sub>60</sub> to C<sub>28</sub><sup>[69]</sup> and finally C<sub>20</sub><sup>[70]</sup> cages. Indeed, by reducing the radius of the cage, one increases the  $sp<sup>3</sup>$  character of the bounds. Similar effects can be observed in carbon nanotubes where the coupling strength increases with decreasing diameter<sup>[71]</sup>, consistently with the evolution of the superconducting transition from 0.3 K in large diameter tubes<sup>[72]</sup> to 14 K in 4 Å diameter tubes synthesized in AlPO<sub>4</sub> zeolite channels<sup>[73]</sup>. Several other carbon-based structures with a large percentage of  $sp^3$  bonds have been synthesized<sup>[74]</sup> but have only been considered so far for their application as ultra-hard materials  $[75,76]$ . These arguments for the increase of the electron-phonon coupling strength from  $sp^2$  to  $sp^3$  bonding should however be treated with care as confinement effects in small fullerene cages play an important

role[77]. Furthermore, recent *ab initio* calculations of the deformation potential in graphene indicates values which are definitely not negligible when compared to  $diamond$ <sup>[77,78]</sup>.

As mentioned in section 2, the potential properties of those cage structures have also been illustrated in the case of the silicon clathrates, which are all  $sp<sup>3</sup>$  siliconbased cage-like structures. Contrary to fullerenes, the atoms in clathrates have four neighbours and all *sp* 3 bonds are fully saturated without any dangling bond character. Due to the presence of pentagons that frustrates the formation of bonding *p*-states at the top of the valence bands, electronic bands flatten as compared to their diamond analogue, leading to a large density of states $[80]$ . Furthermore, the cage structure allows large (endohedral) doping and provides much more flexibility in the doping chemistry. In particular, in barium-doped clathrates, the hybridization of the Ba 5d orbitals with the Si 3p orbitals further contributes to significantly enhance N(E<sub>F</sub>), leading to a rather large  $\lambda_{ep}$  value close to 1<sup>[8,26]</sup>. As a result, the transition temperature in barium doped Si clathrates is ~8 K for an all silicon based  $sp<sup>3</sup>$  materials that can be compared to the 0.35 K value found in boron-doped cubic silicon. Unfortunately, and despite several attempts, carbon clathrates have not yet been synthesized and their potential interest as superconducting materials remains limited to theoretical predictions of  $T_c$  as large as 77 K <sup>[81]</sup>. This speculated  $T_c$  can also be found in the figure of Box 1. Finally,  $C_nB_m$  clusters have been produced<sup>[82,83]</sup>, but to our knowledge the synthesis of BC clathrates has never been reported.

We conclude this section by mentioning the case of layered graphitic structures such as  $CaC_6$  or  $YbC_6^{[11]}$  and related structures (see also box 1). In contrast to MgB<sub>2</sub>, the Fermi level in CaC<sub>6</sub> or YbC<sub>6</sub> does not lie in the  $\sigma$ -band (in-plane  $sp^2$ covalent bonds) but remains located in the  $\pi$ -band (out-of-plane  $p_z$ -bonds). Nevertheless, the hybridization with intercalant states, the so called ζ-band, still ensures a rather large  $T_c$  value of up to 11.5 K, thanks to the existence of soft phonon modes. It is hence very tempting to look for systems combining the advantages of both systems: strong electron-phonon coupling of the covalent σband and interlayer states coupled with soft intercalant modes. A promising candidate was the  $Li_2B_2$  system for which the Fermi level indeed lies in both  $\sigma$  and ζ bands[84,85]. Unfortunately, the "accidental" loss of the π electrons leads to a hardening of the phonon modes and reduces  $\lambda_{ep}$  to ~ 0.6 as compared to MgB<sub>2</sub> for which  $\lambda_{\rm en} \sim 1.0$ . Many theoretical works have recently been devoted to the search foref new graphitic-like structures which would optimize the coupling with the various bands. Among those, systems such as  $BC_3^{[86]}$  or  $Li_xBC^{[87]}$  (x<1), with  $T_C$ 

values up to 150K, were predicted. Unfortunately these predictions have not been verified experimentally so far. The use of *ab initio* simulations to explore the thermodynamic stability of potential superconducting phases may prove quite useful in the future as illustrated recently in the case of the hypothetical antifluorite  $Be<sub>2</sub>B<sub>x</sub>C<sub>1-x</sub> phases<sup>[88]</sup>.$ 

#### **5) Forthcoming potential applications**

In Superconducting-Normal (SN) junctions, phase coherent transport can be induced in the normal (N) conductor by the so-called proximity effect. The mismatch between the electron densities at the Fermi level and the existence of a Schottky barrier severely limits the leakage of Cooper pairs through the junction and the functionality of superconducting devices when the N element is a semiconductor<sup>[89]</sup>. In this respect, indium arsenide (InAs) is an exceptional semiconductor<sup>[90]</sup> since it can form Schottky-barrier-free contacts with metals. However, in this case, the Josephson current remains low due to disorder. The superconductivity of ultra-doped Si could then provide a new paradigm in the field of such junctions, since the two regions can be made out of the same material by simply changing the doping level, thus avoiding problems with interface Schottky barriers. The GILD technique allows fabrication of ultra-shallow highly doped regions with abrupt interfaces (< 2 nm/decade in boron concentration). This will allow the fabrication of mesoscopic SNS junctions with sub-micrometer separation between superconducting electrodes. Control of the Josephson current and the current-voltage characteristics could be achieved through additional capacitive gates which affect the electronic density in the normal region, leading to the fabrication of a Josephson field-effect transistor (JOFET)<sup>[91]</sup>.

The discovery of superconductivity in Si, SiC, and diamond also gives the possibility to design new superconducting NEMS (Nano-Electro-Mechanical Systems, for a review  $\sec^{[92]}$ ). In a monolithic device, superconducting electronics can now be integrated to a NEMS oscillator for quantum-limited detection of force, mass, charge, or displacement. The zero electrical dissipation and the absence of an additional metallic layer deposited onto the resonator increase the quality factor and the sensitivity of actual systems, and new fundamental effects could be observed due to the coherent nature of superconductivity (see for instance <sup>[93]</sup>). In particular, the outstanding physical, electronic, and thermal properties of diamond make this material unique for the development of NEMS devices. The unmatched Young modulus will allow the achievement of higher frequencies  $v$  (GHz)<sup>[94]</sup> than in stateof-the-art mechanical resonators and hence to reach the quantum limit ( $k_B T < h\nu$ ) at more accessible temperatures  $($   $~40mK)$ . The relatively high critical temperature

and a large second critical magnetic field, of a few Tesla, both larger than in conventional superconductors, also provide the possibility to operate at higher magnetic fields and to reach a stronger electromechanical coupling regime.

#### **6) Conclusions and open questions**

Since doped diamond stands out as the archetype of superconducting covalent metals, we may identify several short-term research directions dealing with this material, partly applicable to the other systems covered by this review:

- a) Further exploration of the dopant and host atoms isotope effects would certainly bring much information on the relevance of the phonon-mediated mechanisms and on the nature of the important vibrational modes (bulk optical states or localized boron-related modes). At this point, any experimental signature from the coupling phonons would be welcome.
- b) More detailed empty state spectroscopy (e.g. by inverse photoemission or high resolution X-ray absorption) complementing the published ARPES measurements<sup>[51]</sup>, would help to confirm the presence of an empty impurity band and/or deep inactive boron-related levels in order to understand the coupling mechanisms and the relation between impurity and free carrier concentrations.
- c) Calculations of T<sub>C</sub> and 2∆(T) within the recently developed density functional theory for superconductors [95,96] will suppress the need to adjust the  $\mu^*$  value. This approach was tested on several simple materials showing excellent agreement with experimental transition temperatures and quasiparticle band gaps.
- d) The nature of the superconducting transition (type I or type II) also has to be clarified. Tunnelling spectroscopy measurements unambiguously proved the existence of vortices in C:B epitaxial films<sup>[55]</sup> (i.e. type II superconductivity) and the high values of the critical fields observed in Si:B  $\sim 0.4T$  for  $T_{\rm C}$ ~0.35K<sup>[4]</sup>) strongly suggest that this system is a type II superconductor. On the other hand, superconductivity was found to be of type I in  $3C-SiC^{[5,6]}$  $(H_c \sim 0.01T$  for  $T_c \sim 1.4K$ ). Note that, in the dirty limit when the mean free path l is much smaller than the coherence length  $\xi$ ,  $\kappa$  (= $\lambda$ <sub>L</sub>/ $\xi$ ) is renormalized to  $\lambda_I/I$ ,  $\lambda_I$  being the London penetration depth and a clean type I superconductor  $(\kappa < 0.7)$  might be turned into a dirty type II superconductor.
- e) Another fundamental aspect in superconducting semiconductors is the new playground it offers for studying the interplay of disorder-induced localization, Coulomb interaction and superconductivity in the vicinity of a disorder-driven Mott-Anderson transition  $^{[97,98]}$  (see Box 2). For instance, T<sub>C</sub>

remains anomalously high down to the transition in boron doped diamond<sup>[99]</sup> whereas, in the BCS picture, it is expected to become exponentially small as  $\lambda_{ep}$  tends towards zero at the MIT. On the contrary, it was recently proposed <sup>[100]</sup> that close to a mobility edge (disorder induced MIT)  $T_c$  may only drop as  $\lambda_{ep}^{1/\gamma}$  ( $\gamma$  being a scaling exponent) suggesting that disorder may play a significant role in boron doped diamond. The simultaneity of these two transitions here offers new opportunities to study this issue in detail.

More generally, it will be desirable to increase  $T_c$  in each system. Aluminum doping of silicon has for instance been calculated to be more effective than boron for superconductivity  $[48]$ , but its substitutional incorporation at levels in the at. % range remains a challenge. An insulator-to-metal transition has been recently induced by aluminium doping in 4H-SiC epilayers<sup>[101]</sup> but without any evidence for superconductivity. Although *ab initio* calculations can provide useful hints about alternative materials and favourable stoichiometries or dopants, progress in this direction is now limited by material preparation issues. Various hypothetical systems such as carbon clathrates, highly doped (20 to 30%) cubic diamond,  $Li_xBC$  have been predicted to yield large  $T_c$  values but the synthesis of such systems remains elusive.

A lower disorder may also be beneficial  $[97]$ . Recent improvements of the growing process (GILD technique) increased the critical temperature of Si:B by a factor  $2^{[102]}$ . As mentioned, Si:B might also play a fundamental role in the development of SNS based devices. The use of (InAs-based) JOFETs hasve so far been hampered by low critical Josephson current and interface disorder. A silicon-based technology could then open the way to the possibility of fabricating flexible proximity circuits, in which several parameters of the normal and the superconducting electrodes could be tuned to achieve new effects in quantum electronics.

#### **Box 1 : Covalent structures**

It is well-known that under ambient conditions, carbon crystallizes mainly in the diamond  $(sp^3)$  and layered  $(sp^2,$  graphite) structures. In its graphite form the Fermi level (E<sub>F</sub>) lies *within* the π bands formed by  $2p<sub>z</sub>$  out-of-plane orbitals (Fig. 1a). The *lateral* superposition of these orbitals is expected to lead to a small electronphonon coupling constant. However, what makes those systems particularly interesting is the possibility of modulating their electronic structure by doping. Vibrations perpendicular to the plane, as well as intercalant modes, can for instance couple quite efficiently with the nearly-free-electron-like band that crosses  $E_F$  in the intercalated CaC<sub>6</sub> compound (so-called  $\zeta$  band, Fig. 1b) leading to  $T_c$  values of up to 11K.

However, the best coupling constant is expected to be obtained for the lower energy  $\sigma$  band which arises from in-plane  $2p_{xy}$  orbitals ( $sp^2$  coupling, see picture 1c). Indeed, the direct *axial* superposition of atomic orbitals makes them very sensitive to atomic vibrations leading to high electron-phonon coupling constants. Bringing the Fermi level into the  $\sigma$  band can be achieved either by depleting the  $\pi$ band or by merging both  $\pi$  and  $\sigma$  bands in the same energy range. The former case occurs upon B substitutional doping as in the graphitic  $BC_x$  structure (with  $x < 3$ ). The latter case is that of the  $MgB_2$  structure (Fig. 1c). Indeed, although isovalent to graphite, in this case the presence of  $Mg^{2+}$  atoms induces a large overlap of  $\pi$ and  $\sigma$  bands both crossed by the Fermi level leading to  $T_c \sim 39K$ . Following the same strategy, a very promising candidate is  $Li<sub>x</sub>BC$  in which  $T<sub>C</sub>$ s of up to 150K have been predicted but not verified so far.

On the other hand, in the 3D  $sp^3$  phase, such as clathrates (cage structure, Fig. 1e) or diamond, states around the gap all present directional  $\sigma$  bonds and the difficulty here is to dope the system in order to place the Fermi level in the valence or conduction bands (see box on the metal-insulator transition).  $T_{\rm C}$ s of the order of a few Kelvin have already been observed in 3 to 6% doped diamonds but several theoretical papers suggest that  $T_{\text{CS}}$  could even exceed that of  $\text{MgB}_2$  in doped carbon clathrates (F@C-34, Fig. 1h), cubic  $BC_5$  phases and highly doped diamond (Fig. 1f) up to the zinc-blende structure (Fig. 1g). To date, only the  $BC_5$  structure has been reported experimentally but evidence for superconductivity is still missing.



Fig. 1: Symbolic representation of various crystalline superconducting phases. Transition temperature values followed by a question mark indicate hypothetical materials and theoretical predictions. The structures have been grouped according to the electronic states participating in the electron-phonon coupling  $(sp^3, sp^2)$  -bonds, or interlayer states).

#### **Box 2 : Metal-Insulator Transition**

At T=0, semiconductors are insulators with their highest occupied electronic band and their lowest unoccupied electronic band of delocalized states separated by an energy bandgap with a chemical potential located at midgap. Randomly distributed chemical impurities or structural defects, leading to localized states within this forbidden gap, may liberate (donor centers) or capture (acceptor centers) electrons. At non-zero temperature, the number of free carriers in the bands will depend on the ratio of the ionization energy of these centers (respectively  $E_d$  and  $E_a$ ) to the temperature, yielding an activated electrical resistivity intermediate between that of an insulator and that of a metal (see fig. 2a).

In heavily doped semi-conductors, the impurity energy levels begin to aggregate into a narrow range of energy, a so-called "impurity band", a misleading term since the wave-functions remain localized. Moreover, the dispersion of energy levels due to disorder contributes to the spatial localization of electronic states (Anderson localization). At higher concentration, when the impurities are close

enough, quantum overlapping of their wave-functions tends to delocalize them, leading to a metallic behavior at zero temperature with a Fermi level pinned inside the impurity band (see fig. 2b). Mott showed that this simplified one-electron picture fails, and that the conduction mechanism would remain thermally activated even if the impurities were regularly spaced<sup>[103]</sup>. Indeed, because of Coulomb repulsion, the spin degenerated half-filled impurity band splits into an empty band and a full band (see fig. 2c). Upon further doping, these two bands cross each other and the Metal-Insulator Transition (MIT) takes place (see fig. 2d).

However, at such doping levels, screening of the impurities modifiesy the ionization energy itself. Zero temperature model calculations have shown consequently that, at the transition, the impurity-band states associated withto the doping atoms become energetically unfavorable : upon adding one more impurity to the critical concentration, all these states become extended. Their energies now lie near the edge but within the band of delocalized states. Screening of the crystal host electrons by these new free carriers emphasizes this effect by narrowing the intrinsic bandgap energy<sup>[104]</sup> (see fig. 2e).



Fig. 2 : Evolution of the electronic density of states (DOS) and band structure with increasing p-type doping from a) to d). Colored area represents filled states.

#### **Box 3 : Gas Immersion Laser Doping**

Substitutional doping of semiconductors up to the alloying range is hampered by the solubility limit of the doping impurity into the host lattice. Above this limit the solid solution becomes thermodynamically unstable, leading to phase separation and formation of aggregates. Among the various out-of-equilibrium techniques developed to overcome this limitation, laser-assisted processes are well adapted to silicon, germanium, and their alloys. A laser burst melts the surface of the crystal during a few tens of nanoseconds. After the burst, the speed of re-crystallization is on the order of  $10^{10}$  K/s, slow enough to allow crystal reconstruction on the underlying non melted template, but fast enough to prevent impurity diffusion and precipitation. Doping atoms can be introduced by pre-implantation (Laser Thermal Anneal or LTA) or in situ by exposure of the surface to impuritycarrying gas molecules in a vacuum chamber (Gas Immersion Laser Doping or GILD), as illustrated below.

Recently, the GILD technique has been applied to induce superconductivity in silicon by boron doping. In-situ real time monitoring of the transient reflectivity at a 675 nm wavelength allowed to adjust the power and duration of the pulses for optimal doping and to ensure that the dopant incorporation profile was flat with an abrupt interface. High-resolution XRD measurements and secondary ion mass spectroscopy on the doped layers demonstrated a maximum doping level of the order of 10% atomic (i.e.  $\sim 5.10^{21}$  at/cm<sup>3</sup>) for typically 500 subsequent laser shots. Note that this substitutional concentration is far above the critical threshold for the MIT (a few 10<sup>18</sup> at/cm<sup>3</sup>) and even above the solubility limit ( $\sim 10^{20}$  at/cm<sup>3</sup>). Unfortunately, this technique, well-adapted to silicon and germanium, can not be applied to most of the other semiconducting compounds (including diamond).



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