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Olivier Herbinet, William J. Pitz, Charlie K. Westbrook. Detailed chemical kinetic mechanism for the oxidation of biodiesel fuels blend surrogate. Combustion and Flame, 2010, 157 (5), pp.893-908. 10.1016/j.combustflame.2009.10.013 . hal-00724929

## HAL Id: hal-00724929 https://hal.science/hal-00724929v1

Submitted on 23 Aug2012

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# Detailed chemical kinetic mechanism for the oxidation of biodiesel fuels blend surrogate

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#### Abstract

Detailed chemical kinetic mechanisms were developed and used to study the oxidation of two large unsaturated esters: methyl-5-decenoate and methyl-9-decenoate. These models were built from a previous methyl decanoate mechanism and were compared with rapeseed oil methyl esters oxidation experiments in a jet-stirred reactor. A comparative study of the reactivity of these three oxygenated compounds was performed and the differences in the distribution of the products of the reaction were highlighted showing the influence of the presence and the position of a double bond in the chain. Blend surrogates, containing methyl decanoate, methyl-5-decenoate, methyl-9-decenoate and n-alkanes, were tested against rapeseed oil methyl esters and methyl palmitate/n-decane experiments. These surrogate models are realistic kinetic tools allowing the study of the combustion of biodiesel fuels in diesel and homogeneous charge compression ignition engines.

**Keywords:** Methyl decanoate; Methyl decenoate; Surrogate; Oxidation; Biodiesel fuels; Kinetic modeling; Engine; Low temperature

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#### 1. Introduction

Many studies have been performed to characterize the effects of the addition of oxygenated fuels to gasoline and diesel fuels on the emissions in engines. It has been observed that the use of oxygenated species leads to a decrease of the emissions of pollutants in general [1], [2] and [3]. The combustion of biodiesel fuels in diesel engines allows lowering emissions of particulate matter, carbon monoxide and unburned hydrocarbons. A slight increase in the formation of nitrogen oxides is observed at some conditions. Biodiesel fuels have also the advantage of being alternative and renewable fuels contributing to the reduction of the dependence on crude oil importation and to environment preservation by lowering net emissions of carbon dioxide [4] and [5].

Biodiesel fuels are produced from mono-alkyl esters of long-chain fatty acids derived from vegetable oils and animal fats. These very large molecules are transformed into esters by reaction of transesterification with an alcohol. Methanol is commonly used but other alcohols, like ethanol, can also be employed. Most biodiesel fuels are made from rapeseed and soybean. Rapeseed and soybean derived biodiesels mainly contain the same five components: methyl palmitate ( $C_{17}H_{34}O_2$ ), methyl stearate ( $C_{19}H_{38}O_2$ ), methyl oleate ( $C_{19}H_{36}O_2$ ), methyl linoleate ( $C_{19}H_{34}O_2$ ) and methyl linolenate ( $C_{19}H_{32}O_2$ ). The average compositions of soybean and rapeseed biodiesel fuels are displayed in Fig. 1 [6]. These components have very similar structures (Fig. 2): a methyl ester group attached to a large hydrocarbon chain. One difference is the length of the chain (16 atoms of carbon for methyl palmitate, 18 for the others) and the other difference in the number of double bonds in the chain: no double bond, one, two or three double bonds. According to Fig. 1, most esters in soybean and rapeseed biodiesel fuels are unsaturated species. This justifies the development of detailed kinetic models for unsaturated methyl esters.



Fig. 1. Average composition of soybean and rapeseed biodiesels [6]. C16:0 = methyl palmitate, C18:0 = methyl stearate, C18:1 = methyl oleate, C18:2 = methyl linoleate and C18:3 = methyl linolenate.



Fig. 2. Structures of the main components in soybean and rapeseed biodiesels.

There have been many studies on the detailed chemical kinetics of methyl esters. Most of these studies have been on methyl butanoate ( $C_5H_{10}O_2$ ). The first detailed kinetic model for the oxidation of methyl butanoate was developed by Fisher et al. [7] in 2000. It was validated against limited available experimental pressure data in closed vessels [8]. More recently, this model has been used and revised by Metcalfe et al. [9] to reproduce experimental data obtained in a shock tube. Similarly Gaïl et al. [10] compared their experimental data obtained in a jet-stirred reactor, a variable pressure flow reactor and an opposed-flow diffusion flame with a slightly modified mechanism based on the work of Fisher et al. Dooley et al. studied methyl butanoate in a shock tube and in a rapid compression machine. They made further modifications to the methyl butanoate mechanism [11] to reproduce their experimental data and also literature data from a stirred reactor, flow reactor, and opposed-flow diffusion flame. Farooq et al. [12] measured the CO<sub>2</sub> yield from methyl butanoate pyrolysis in a shock tube and modified the methyl butanoate mechanism based on electronic structure calculations. These studies allowed clarifying the specific kinetic features due to the presence of the ester group.

The study of ignition delay times of methyl esters and biodiesel fuels droplets in microgravity showed that methyl butanoate is not a good surrogate for large methyl esters in biodiesel fuels [13]. Methyl butanoate is much less reactive than soybean biodiesel whereas larger species such as methyl decanoate and methyl dodecanoate have about the same reactivity as biodiesel. In their HCCI engine simulations of blends of soy-based biodiesel and ultra low sulfur diesel, Szybist et al. [14] speculated

that the cetane number of methyl butanoate is too low to account for experimentally observed changes in burn duration and phasing when the biodiesel concentration was changed.

There have been relatively few studies on the chemical kinetics of large methyl esters. A model for the oxidation of a large ester, methyl decanoate (Fig. 3), was developed by Herbinet et al. [15]. This model contains 8580 reactions and 3034 species. It was compared with rapeseed oil methyl esters experiments by Dagaut et al. [16]. The agreement between experimental and computed mole fractions is satisfactory and one feature of this model is its ability to reproduce the early formation of carbon dioxide due to the presence of the ester group. The model was also compared with n-decane ignition delay times in a shock tube. Computed ignition delay times were in very good agreement with n-decane experiments, except at the lowest temperature where methyl decanoate was a little bit less reactive than n-decane. These similarities in the reactivity have important implications in the development of surrogate models: n-alkanes can be very good surrogates for the reactivity of methyl esters of similar size [15]. The methyl decanoate model was reduced and used to model extinction and ignition of laminar non-premixed flames containing methyl decanoate [17].



Fig. 3. Structures of methyl decanoate, methyl-5-decenoate and methyl-9-decenoate.

Methyl decanoate has no double bond whereas most esters in biodiesel fuels are unsaturated species. The presence of double bonds has an influence on the formation of unsaturated species, which are known to be precursors of soot. Their presence also affects the reactivity of the fuel mixture by restricting some low temperature reactions such as RO<sub>2</sub> isomerisations, allowing addition of radicals to the double bond, and leading to the formation of resonantly stabilized radicals.

Zhang et al. [18] studied saturated and unsaturated  $C_9$  esters experimentally in a motored engine. They found that the presence of the double bond in the unsaturated  $C_9$  ester reduced the reactivity of the fuel/air mixture compared to the saturated  $C_9$  ester. They said that the lower reactivity in the low temperature regime can be explained by reduced amounts of 6- and 7-member transition states formed during the oxidation of the unsaturated methyl ester. The present work intends to provide reliable detailed kinetic models for the oxidation of two esters having one double bond, methyl-5-decenoate and methyl-9-decenoate (Fig. 3), in order to develop blend surrogate mechanisms more representative of biodiesel fuels. Methyl-9-decenoate was chosen because the double bond is at the same position as the one in methyl oleate and at the same location as the first double bond in methyl linoleate and in methyl linolenate. Methyl-5-decenoate has been chosen to highlight the influence of the position of the double bond in the chain. These two models have been compared with rapeseed oil methyl esters experiments of Dagaut et al. [16]. To obtain improved surrogate mixture models to represent biodiesel fuels, models of binary and tertiary mixtures are compared to experimental measurements of binary component mixtures and of rapeseed oil methyl esters.

#### 2. Description of the chemical kinetic mechanisms

The unsaturated and saturated methyl esters under investigation have similar molecular structures: they have a  $C_{10}$  hydrocarbon chain and a methyl ester group. The difference is the presence of a double bond in the hydrocarbon chains of methyl-5-decenoate and methyl-9-decenoate (Fig. 3). Because of the similarities, some species generated by the reactions of unimolecular initiation and H-atom abstraction were already included in the previous methyl decanoate mechanism [15]. Thus the two sub-mechanisms for the oxidation of methyl-5-decenoate and methyl-9-decenoate were developed from the previous model for the oxidation of methyl decanoate by adding the chemistry specific to these unsaturated species.

The two sub-mechanisms were developed by using the reaction classes from Curran et al. [19] and [20], but accommodations were required to take in account the specific chemistry due to the presence of the double bond and of the ester group. The reaction classes from Curran et al. were reviewed in the previous methyl decanoate paper [15] and the emphasis is given on the specific reactions due to the double bond in the present paper. The elementary steps and associated rate constants involved in detailed chemical kinetic models are also presented by Battin-Leclerc in a review about the low-temperature combustion of hydrocarbons [21].

#### 2.1. High temperature part

The first steps considered in the consumption of the fuel were unimolecular initiation reactions. Their rate constants were specified in the reverse recombination direction, except for the scission of allylic C–C bonds which was considered in the forward direction. A rate constant of  $1.0 \times 10^{16} \times exp[-71000 \text{ (cal mol}^{-1})/RT] \text{ s}^{-1}$  was used for this last reaction [22]. Rate constants of other reactions of recombination are given in Table 1 for methyl-5-decenoate and in Table 2 for methyl-9-decenoate.

Reaction of recombination	Rate constant (cm <sup>3</sup> mol <sup>-1</sup> s <sup>-1</sup> )		
$\left(H_{3}C - CH_{3}\right)$ + H'	$1.0  imes 10^{14}$		
$H_{3C}$ $H_{2}$ $H_{3}$ $H_{$	$3.0 \times 10^{13}$		
$H_{3C}$ $H$	$3.0 \times 10^{13}$		
$H_3C$ $CH_2^{\bullet}$ + $\overset{O}{\overset{U}{\overset{U}{\overset{O}{\overset{O}{\overset{O}{\overset{O}{\overset{O}{$	$1.8  imes 10^{13}$		
$H_3C$ $CH_2^{-}$ $+$ $H_2C^{-}$ $O^{-}CH_3^{-}$	$8.0 \times 10^{12}$		
$H_3C$ $CH_2^{-}$ + $H_2C^{-}$ $O_0^{-}CH_3^{-}$	considered through the reverse direction (see text)		
H <sub>3</sub> C CH' + H <sub>2</sub> C' O CH <sub>3</sub>	$8.0  imes 10^{12}$		
H <sub>3</sub> C CH <sup>2</sup> + HC O CH <sub>3</sub>	$8.0  imes 10^{12}$		
$H_3C$ $CH_2$ + $H_2C$ $O$ $CH_3$	considered through the reverse direction (see text)		
$H_3C^{-CH_2^{\circ}} + H_2C^{\circ} - CH_3$	$8.0 \times 10^{12}$		
CH <sub>3</sub> + H <sub>2</sub> C·	$3.0 \times 10^{13}$		

Table 1. Unimolecular initiations for methyl-5-decenoate.



Table 2. Unimolecular initiations for methyl-9-decenoate.

The fuel consumption reactions considered were reactions with small radicals. These reactions include both abstraction of H-atoms by radicals and addition of radicals to the C–C double bond. H-atom abstractions from the fuel by H, CH<sub>3</sub>, C<sub>2</sub>H<sub>3</sub>, C<sub>2</sub>H<sub>5</sub>, O, O<sub>2</sub>, OH, HO<sub>2</sub>, CH<sub>3</sub>O, and CH<sub>3</sub>O<sub>2</sub> were considered. The distinction was made between alkylic (primary, secondary), allylic (secondary), vinylic (secondary and tertiary) H-atoms, and the two H-atoms bonded to the carbon atom adjacent to the carbonyl group (S<sub>CO</sub> H-atoms) (Fig. 4). Like in the case of methyl decanoate, we used H-atom

abstraction rates from tertiary bonds in other molecules for SCO H-atoms because they have C–H bond energies similar to those of tertiary C–H bonds. Kinetic parameters are those recommended by Curran [23]. The activation energy for abstractions of secondary H-atoms by OH radicals used in the initial version of the methyl decanoate mechanism [15] was wrong. The correct value of -35 cal mol<sup>-1</sup> (and not -3500 cal mol<sup>-1</sup>) is used in the present version of the methyl decanoate model as well as in the other models given as supplementary material. This change can have an influence on the reactivity of the fuel in the low temperature region under some conditions. Reactions of addition of H-atoms, HO<sub>2</sub> and OH to the C–C double bond of the reactant were already included in the methyl decanoate mechanism [15].



Fig. 4. Different types of H-atoms considered for the H-atom abstractions. P = primary alkylic, S = secondary alkylic adjacent to the carbonyl group, AS = secondary allylic, VS = secondary vinylic and VT = tertiary vinylic H-atom.

Subsequently, we assembled reactions and estimated rate constants to consume the fuel radicals formed by the H-atom abstraction reactions. These reactions include radical decompositions and isomerizations. Reactions of decomposition of fuel radicals were written in the reverse direction (addition of radicals to double bonds) and kinetic parameters are from a review of Curran [23] and from the methyl butanoate study [7]. As in the methyl decanoate model, the kinetic parameters for the reactions of addition of radicals to the oxygen of the C=O bond were updated from the study of the methyl radical addition to the C=O bond by Henry et al. [24].

Reactions of isomerizations through 3–6 member rings cyclic transition states were considered. Isomerizations involving the abstraction of vinylic H-atoms were not written because of their very high activation energies. An extra strain correction of 15 kcal  $mol^{-1}$  was added to the activation energy when the cyclic transition state had an embedded double bond [25].

The decomposition of alkenyl, allylic and vinylic radicals leads to the formation of unsaturated species. H-atom abstractions and retroene reactions were considered in a systematic way for these species. Only unimolecular decomposition by scission of allylic bonds was written for unsaturated primary products because this type of bond is weaker than an alkylic bond. Isomerizations of alkenyl,

allylic and vinylic radicals were also written. The rate constants for decomposition of these radicals were specified through reverse additions. The kinetic parameters used for these reactions are the same than those presented in the reactant section above.

#### 2.2. Low temperature part

The low temperature mechanism was built in the same way as in the case of methyl decanoate. Some accommodations were required to take in account the presence of double bonds and of vinylic and allylic H-atoms.

The first steps to consider in a low temperature mechanism are radical addition to  $O_2$ , for radicals deriving from the H-atom abstractions from the reactant. For these R +  $O_2$  reactions, mesomeric forms need to be considered when R is allylic, to account for the two possible positions of the radical site. Fig. 5 displays the two limit structures of the allylic radical obtained by H-atom abstraction from methyl-9-decenoate and the two corresponding reactions of addition to  $O_2$ . Reactions of addition to  $O_2$  of radicals coming from the reactions of unimolecular initiation were considered in the case of methyl-9-decenoate (they were already included in the methyl decanoate mechanism), but not in the case of methyl-5-decenoate in order to substantially reduce the size of the model. This is justified by the fact that unimolecular initiations are not important in the low temperature region. The reactions of addition to  $O_2$  involving radicals deriving from the addition of OH to methyl-9-decenoate and methyl-5-decenoate were written and the specific reactions of decomposition of the new radicals through the mechanism of Waddington were considered (k =  $5.36 \times 10^{12} \times T^{-0.8} \times \exp[-10790$  (cal mol<sup>-1</sup>)/RT s<sup>-1</sup>]) [26]. The mechanism of addition followed by a decomposition through a 4-member ring cyclic transition state proposed by Lodhi and Walker for allylic radicals was taken in account (k =  $1.7 \times 10^9 \times T \times \exp[-26228$  (cal mol<sup>-1</sup>)/RT s<sup>-1</sup>]) [27].



Fig. 5. The two possible reactions of addition to  $O_2$  of the allylic radical obtained by H-atom abstraction from methyl-9-decenoate.

Reactions of  $RO_2$  isomerization to QOOH through 5–8 member cyclic transition states were considered. Rate constants used for these reactions depend on the number of atoms in the cyclic

transition state and on the type of H-atoms which is shifted (Table 3). Subsequently, QOOH radicals react by reactions of decomposition to cyclic ethers, by reaction of decomposition to olefins +  $HO_2$  and by reactions of addition to  $O_2$  leading to OOQOOH radicals. As in the case of methyl decanoate, only the isomerizations of OOQOOH radicals to ketohydroperoxide + OH were written. Reaction of decomposition of ketohydroperoxide to OH and a radical by breaking of the O–O bond were taken in account. At this time, we have not considered the direct reaction of  $RO_2$  to olefin +  $HO_2$  [28] since it was not included in the corresponding methyl decanoate mechanism. However, we will consider this reaction path in future work. Rate constants of all these reactions are identical to those used in the methyl decanoate mechanism [15].

Number of atoms in the ring of	Type of H shifted	٨	h	E.
the cyclic transition state	(see Figure 4)	A	D	Ea
5 atoms ring	Р	$1.00\times10^{11}$	0.0	29.40
	S	$1.00\times10^{11}$	0.0	26.85
	S <sub>co</sub> <sup>1</sup>	$1.00\times10^{11}$	0.0	24.10
	AS	$1.00  imes 10^{11}$	0.0	22.35
	VS	$1.00  imes 10^{11}$	0.0	30.70
	VT	$1.00\times10^{11}$	0.0	28.65
6 atoms ring	Р	$1.25\times10^{10}$	0.0	24.40
	S	$1.25  imes 10^{10}$	0.0	20.85
	S <sub>CO</sub> <sup>1</sup>	$1.25  imes 10^{10}$	0.0	19.10
	AS	$1.25  imes 10^{10}$	0.0	16.35
	VS	$1.25  imes 10^{10}$	0.0	25.70
	VT	$1.25\times10^{10}$	0.0	22.65
7 atoms ring	Р	$1.56 imes10^{09}$	0.0	22.35
	S	$1.56 imes10^{09}$	0.0	19.05
	S <sub>CO</sub> <sup>1</sup>	$1.56 imes10^{09}$	0.0	17.05
	AS	$1.56 imes10^{09}$	0.0	14.55
	VS	$1.56 imes10^{09}$	0.0	23.65
	VT	$1.56  imes 10^{09}$	0.0	20.85
8 atoms ring	Р	$1.95  imes 10^{08}$	0.0	25.55
	S	$1.95  imes 10^{08}$	0.0	22.05
	S <sub>co</sub> <sup>1</sup>	$1.95  imes 10^{08}$	0.0	20.05
	AS	$1.95\times10^{08}$	0.0	17.55
	VS	$1.95\times10^{08}$	0.0	26.85
	VT	$1.95  imes 10^{08}$	0.0	23.85

Table 3. Rate constants of the reactions of isomerization of  $RO_2$  to QOOH (k = A × T<sup>b</sup> × exp(E<sub>a</sub>/RT)) (units: kcal, cm<sup>3</sup>, mol).

<sup>a</sup> It is assumed that this type of H-atom react in a similar way than a tertiary H-atom because the bond energies of the C–H bonds are very close.

#### 2.3. Thermodynamic properties

Standard enthalpies of formation ( $\Delta H_f^{\circ}$ ), entropies (S), and specific heats (Cp) of the species involved in the two models were calculated using the THERM program from Ritter and Bozzelli [29]. This program is based on the group and bond additivity methods and the statistical thermodynamics approach proposed by Benson [30]. The thermodynamic data are stored as two sets of 7 polynomial coefficients (Chemkin formalism).

As for methyl decanoate, we used the C–H bond dissociation energy (94.1 kcal mol<sup>-1</sup>) proposed by El-Nahas et al. for C–H bonds in the alpha position of the carbonyl group of the ester function [31].

#### 3. Results and discussion

The models of oxidation of methyl-9-decenoate and methyl-5-decenoate were compared to experimental data from the literature. The only unsaturated ester for which data exist in the literature are methyl crotonate ( $C_5H_8O_2$ ) [32] and  $C_9$  methyl esters [18]. Methyl crotonate is too small for a comparison with large esters such as methyl-9-decenoate and methyl-5-decenoate. Similar to the proposed biodiesel surrogate methyl butanoate, methyl crotonate cannot account for the low temperature reactivity of large esters because some reactions leading to branching (e.g. isomerizations of peroxy radicals) are not possible due to the short length of the alkenyl chain. The two models were also compared with rapeseed oil methyl esters oxidation experiments in a jet-stirred reactor [16]. Rapeseed (or canola) oil methyl esters mainly contain unsaturated species, the most abundant being methyl oleate (Fig. 1). This species has one double bond such as methyl-9-decenoate and methyl-5-decenoate. It is also larger, but it is assumed that these esters have similar reactivities as it is the case for saturated methyl esters larger than  $C_8$  [33] and for n-alkanes larger than  $C_7$  [34] and [35].

Reactivities of methyl decanoate, methyl-9-decenoate and methyl-5-decenoate were compared and the differences in the distributions of the products of the reaction were highlighted. The models were then combined together with a model for the oxidation of n-heptane to obtain new blend surrogate models more representative of biodiesel fuels.

#### 3.1. Comparison of the models with experimental data

The detailed kinetic models for methyl-9-decenoate and methyl-5-decenoate were compared with rapeseed oil methyl esters oxidation experiments in a jet-stirred reactor at 10 atm over the temperature range 800–1400 K [16]. Experiments were carried out at a residence time of 1 s, a stoichiometric ratio of 0.5 and high dilution in nitrogen. Species leaving the reactor were analyzed by gas chromatography (FID and TCD for their quantification; GC/MS for their identification). Mole fraction profiles were given for methane, hydrogen, carbon dioxide, carbon monoxide, oxygen and 1-alkenes from ethylene to 1-heptene. Dagaut et al. did not report any data about the formation of unsaturated methyl esters in this paper.

The simulations were run in the same conditions as the previous ones with methyl decanoate [15] assuming constant numbers of carbon and oxygen atoms resulting in a slight variation of the number of hydrogen atoms and so of the equivalence ratio (0.496 instead of 0.5). Inlet mole fractions used for the simulations were  $8.18 \times 10^{-4}$  for the ester (methyl-9-decenoate or methyl-5-decenoate), 2.44  $\times 10^{-2}$  for oxygen and 9.75  $\times 10^{-1}$  for nitrogen. Fig. 6 displays the comparison of the two models with experimental data. The general agreement between experimental and computed mole fraction is

satisfactory for methyl-9-decenoate. Computed mole fractions of ethylene are under-predicted of about a factor two compared to the experimental data whereas computed mole fractions of acetylene are over-predicted. Methyl-5-decenoate is less reactive than the two others fuels (methyl-9-decenoate and methyl decanoate) as computed mole fractions are smaller for CO and  $CO_2$  and larger for  $O_2$  in the case of methyl-5-decenoate. Computed mole fractions of ethylene are comparable to those obtained with the methyl-9-decenoate model and computed mole fractions of acetylene are also over-predicted below 900 K but the over-prediction is much more significant. The over-prediction of acetylene by the two models is explained by some approximations made in the secondary mechanism. For some species, reactions of decomposition were written in a global way by considering the formation of small species such as acetylene, carbon oxides, methane, etc. The effect of these reactions on the mole fraction of acetylene is likely a more realistic end product than acetylene in the conditions of this study.



Fig. 6. Comparison of the model predictions with rapeseed oil methyl esters experiments in a jetstirred reactor (■ experimental data [16], - - methyl decanoate model, - methyl-9-decenoate model, •••••• methyl-5-decenoate model, - - - ternary blend model).

According to the comparison in Fig. 6, it seems that the model for methyl decanoate (the saturated ester) gives a better prediction that the two other models. But note that a limited number of species were quantified in this study and that the formation of unsaturated esters was not mentioned. Thus it is difficult to discriminate which of these three models is best for simulating rapeseed oil methyl esters (except in the case of the methyl-5-decenoate model which is not reactive enough). The advantage of the models for the two unsaturated esters is that they predict higher levels of unsaturated species, which is in agreement with the observations of Sarathy et al. [32], who performed a comparative experimental study of the oxidation of methyl butanoate ( $C_5H_8O_2$ ) in a jet-stirred reactor. Their study showed that higher level of unsaturated species (acetylene, propyne, benzene), which are precursors of soot, were detected in the case of methyl crotonate.

Fig. 7 displays the flow consumption paths of the three esters at high temperature (900 K) and the conditions of Fig. 6. These species are mainly consumed by H-atom abstractions by radicals such as OH, H and by the diradical O. In the case of methyl decanoate, the most important consumption path is the abstraction of the H-atoms attached to the carbon atom adjacent to the carbonyl group of the ester function. In the case of the two unsaturated esters, most important paths are abstractions of the allylic H-atoms and the abstraction of the H-atoms attached to the carbon atom adjacent to the carbonyl group of the ester function. Abstractions of vinylic H-atoms also occur at this temperature, but they only represent about 2% of the consumption of the reactant. Unsaturated esters are also consumed by reactions of addition of OH radicals and of H-atoms to the double bond. In the case of methyl-9-decenoate (ester with the double bond at the end of the chain), note that the reactions of addition to the secondary sp<sup>2</sup> carbon atom are more important than the reactions of additions to the tertiary sp<sup>2</sup> carbon atoms.



Fig. 7. Flow decomposition paths of esters in the high temperature region (900 K): (a) methyl decanoate; (b) methyl-5-decenoate; (c) methyl-9-decenoate.

Fig. 8 displays the flow consumption paths for the three esters at low temperature (650 K) and the conditions of Fig. 6. The main routes of consumption are also the H-atom abstractions. At this temperature only H-atom abstractions by OH radicals play a role. For methyl decanoate, the most important path is the abstraction of the H-atoms attached to the carbon atom adjacent to the carbonyl group of the ester function. For the two unsaturated esters, the prevalent consumption routes are the abstractions of allylic H-atoms and then of the H-atoms attached to the carbon atom adjacent to the carbonyl group of the ester function. Note that the abstractions of vinylic H-atoms do not occur at this temperature. Reactions of addition of OH to double bonds still occur at low temperature whereas the reaction of addition of an H-atom to the secondary carbon atom in methyl-9-decenoate is the only one which plays a role.



Fig. 8. Flow decomposition paths of esters in the low temperature region (650 K): (a) methyl decanoate; (b) methyl-5-decenoate; (c) methyl-9-decenoate.

Fig. 9 displays the reactive flow consumption paths of the radical md3j (a representative fuel radical of methyl decanoate whose structure is defined in Fig. 9) at 650 and 900 K, a pressure of 10 atm, and a residence time of 1 s. At both temperatures, this radical is obtained from methyl decanoate through the abstraction of a secondary H-atom by OH radicals ([Fig. 7] and [Fig. 8]). At low temperature, the radical md3j mainly reacts by addition with oxygen forming a ROO radical. This ROO radical isomerizes to three QOOH radicals, md3ooh2j, md3ooh5j and md3ooh6j. The radical "md3ooh2j" (the QOOH species on the left in Fig. 9a) mainly leads to an ester with one double bond and a HO<sub>2</sub> radical by  $\beta$ -scission decomposition. It also reacts by second addition to O<sub>2</sub> to form a OOQOOH radicals which then decomposes to a ketohydroperoxide and an OH radical. The radical "md3ooh6j" (the QOOH species on the right in Fig. 9a) mainly leads to the formation of a 5-member ring cyclic ether and an OH radical. It also reacts by second addition to  $O_2$  to form a OOQOOH radicals which then decomposes to a ketohydroperoxide and an OH radical. The radical "md3ooh5j" (the QOOH radical in the middle in Fig. 9a) reacts through three channels: (1) by a second addition to  $O_2$ followed by a reaction of decomposition to ketohydroperoxide and OH; (2) by a reaction of decomposition to a 4-member ring cyclic ether and OH; (3) by a reaction of  $\beta$ -scission decomposition forming a 1-olefin and a keto-ester. The decomposition of ketohydroperoxide through the breaking of the O–O bond leads to low temperature chain branching and accelerates the oxidation rate of the fuel.



Fig. 9. Flow decomposition paths of the radical md3j (formed from methyl decanoate): (a) in the low temperature region (650 K) and (b) in the high temperature region (900 K).

At high temperature (900 K, Fig. 9b), the radical md3j mainly isomerizes forming other  $C_{11}$  alkyl-ester radicals and decomposes forming olefins and esters with one double bond at the end of the chain. The addition of  $O_2$  still occurs at 900 K. The QOOH radicals deriving from this addition mainly react by  $\beta$ -scission decompositions and decompositions to cyclic ethers whereas the second addition to  $O_2$  is not observed any more.

#### 3.2. Comparison of the reactivity of the three methyl esters

The models of oxidation of methyl decanoate, methyl-9-decenoate and methyl-5-decenoate were used to compare their reactivity. Fig. 10 displays the variation of ignition delay times with the temperature for the three species. Simulations were performed at a pressure of 1 atm and at stoichiometric conditions in air. The predictions show very close reactivities for the three esters with the main differences being visible in the negative coefficient temperature (NTC) region. Methyl-9-decenoate, with the double bond at the end of the alkyl chain, has the shortest ignition delay times and is the most reactive methyl ester component. The least reactive component is methyl-5-decenoate with a double bond in the middle of the carbon chain. Methyl decanoate (with no double bond) has a reactivity that lies in between the two other molecules. This comparison shows that the presence and the position of a double bond in the alkyl chain of a fuel component are very important in determining its reactivity. Vanhove et al. performed the experimental study of the influence of the position of the double bond in the reactivity of the three hexene isomers in a rapid compression machine [36]. They showed that the 1-hexene is the most reactive and that 3-hexene is the least reactive. Modeling studies showed that at low temperature, 1-hexene mainly leads to the formation of branching agents (ketohydroperoxides) whereas 2- and 3-hexenes mainly lead to the formation of di-olefins and low reactive HO<sub>2</sub> radicals [25] and [37]. Unfortunately, there are no shock tube or rapid compression machine experimental data in the literature showing the direct comparison of the reactivity of a n-alkane with the reactivities of the alkene isomers having the same number of carbon atoms.



Fig. 10. Comparison of the reactivity of methyl esters under shock tube conditions (stoichiometric fuel/air mixtures at 1 atm).

According to the kinetic analysis of the model performed at 900 K, the slight difference in the reactivity between methyl decanoate and methyl-9-decenoate could be explained by a higher level of allyl radicals ( $CH_2=CH-CH_2\bullet$ ) in the case of methyl-9-decenoate and consequently a higher level of radical  $\bullet$ OH radicals through the reaction  $CH2=CH-CH_2\bullet + HOO\bullet = CH2=CH-CH2-O\bullet + \bullet OH$  (concentrations of HOO• radicals are similar in both cases).

According to the comparison between the different models (at jet-stirred reactor and shock tube conditions, [Fig. 6] and [Fig. 10]), methyl-9-decenoate seems to be a better surrogate for the unsaturated esters in real biodiesel fuels than methyl-5-decenoate. This is because of the location of the double bond in the chain. In methyl-5-decenoate it is located in the middle between two short CH<sub>2</sub> chains making low temperature chain branching more difficult, whereas in methyl-9-decenoate it is at the end of the chain resulting in a longer CH<sub>2</sub> chain and providing more chain branching. Note that the double bond in methyl-9-decenoate is at the same position as the one in methyl oleate and as the first one in methyl linoleate and methyl linolenate.

#### 3.3. Surrogate blends

Models were assembled for blend surrogates in order to better represent the oxidation of real biodiesel fuels. A blend composed of methyl decanoate and n-heptane was already presented in a previous paper. It was compared to rapeseed oil methyl esters oxidation experiments in a jet-stirred

reactor [16] showing satisfactory agreement between experiment and modeling. This model is compared here to recent experiments of the oxidation of a blend of n-decane and methyl palmitate in a jet-stirred reactor over a wider range of temperatures (550–1100 K) including the NTC region [38]. Experiments were performed at a pressure of 106 kPa, a residence time of 1.5 s, and stoichiometric conditions with high dilution in helium. Fuel inlet mole fraction was set to  $2 \times 10^{-3}$ , oxygen mole fraction to  $3.568 \times 10^{-2}$  and helium mole fraction to 0.96232. The mole composition of the fuel mixture was 74% of n-decane and 26% of methyl palmitate. Simulations were performed at the same conditions of pressure, temperature and residence time. The mole fractions were adjusted in order to keep the carbon content and the ester group content constant and to remain at stoichiometric conditions. Inlet mole fraction of methyl decanoate was kept equal to 5.2  $\times$  10<sup>-4</sup>, n-heptane mole fraction was set to  $2.56 \times 10^{-3}$ , oxygen mole fraction to  $3.622 \times 10^{-2}$  and helium mole fraction to 0.9607. [Fig. 11] and [Fig. 12] display the comparison between the modeling and the experimental results. The agreement between computed and experimental data is satisfactory for most species. Conversions of n-decane and methyl palmitate reproduce well the shape and position of the S-shape curve due to the negative coefficient of temperature, except that the two models seem to be too reactive in the range 800-900 K. The mole fraction profiles of species such as methane, acetylene, carbon oxides, methanol, methyl acrylate, 5-hexene methyl ester are rather well reproduced by the model. Methyl acrylate and 5-hexene methyl esters are characteristic intermediates from methyl ester oxidation. At high temperature, the over-prediction of some species can be explained in terms of the overconversion of fuel from 800 to 900 K mentioned earlier. However, mole fractions of ethylene and propyne are under-predicted for temperatures above 900 K. The predicted formation of acetaldehyde and propanal is too high at low temperature whereas propanone is under-predicted for all temperatures. 8-Nonene methyl ester is under-predicted because the alkyl chain in methyl decanoate in too short to account for the formation of a large methyl ester with one double bond at the end of the chain.



Fig. 11. Comparison of the n-heptane/methyl decanoate model (——) with n-decane/methyl palmitate jet-stirred experiments (■) [38]. Conversion of reactants and mole fraction profiles of hydrocarbon products.



Fig. 12. Comparison of the n-heptane/methyl decanoate model (--) with n-decane/methyl palmitate jet-stirred experiments ( $\blacksquare$ ) [38]. Mole fraction profiles of oxygenated compounds.

To more accurately simulate the oxidation of rapeseed oil methyl esters, a model for the oxidation of a ternary blend composed of methyl decanoate, methyl-9-decenoate and n-heptane was used to model the same oxidation experiments reported in Fig. 6 [16]. Simulations were performed at the same conditions as in the experiments except that inlet mole fractions were adjusted to match the carbon and the ester group contents and to keep a stoichiometric ratio of 0.5. Inlet mole fractions of methyl decanoate, methyl-9-decenoate, n-heptane, oxygen and nitrogen were  $2.50 \times 10^{-4}$ ,  $2.50 \times 10^{-4}$ ,  $5.00 \times 10^{-4}$ ,  $2.47 \times 10^{-2}$  and  $9.74 \times 10^{-1}$ , respectively. The comparison between the blend surrogate model and the experiments is displayed in Fig. 6. The agreement between computed and experimental mole fractions is globally satisfactory for most species.

Under the conditions of the stirred-reactor study, the methyl decanoate model is slightly more reactive than the methyl-9-decenoate model (the mole fractions of oxygen are smaller in the case of the saturated ester as visible in Fig. 6). The reactivity of the blend model is the same as the reactivity of the methyl decanoate model; this is because the most reactive species fixes the reactivity of the blend. This is also the case for the main products of the reaction such as CO,  $CH_4$ , and  $C_2H_4$ , the formation of which highly depends on the reactivity of the fuel. For some other minor products, such as acetylene, the prediction of the blend model lies in between the predictions of the two neat models.

Note that mole fractions of large 1-olefins such as 1-hexene are well reproduced by the model whereas under-estimation was expected due to the short size of the  $CH_2$  chains in the surrogate compounds. This good agreement is explained by the fact that rapeseed biodiesel fuel is mainly composed of methyl oleate with one double bond in the middle of the chain and with two groups of  $CH_2$  chains located on each side of the double bond and of similar size as the  $CH_2$  chains in the surrogate compounds.

#### 3.4. Comparisons to motored engine experiments

Zhang and Yang [18] have recently performed experiments on the oxidation of saturated and unsaturated  $C_9$  methyl esters in a motored engine. For each  $C_9$  methyl ester, they measured the intermediate species in the exhaust of the engine as the compression ratio was increased. At low compression ratios, little reaction of the methyl ester was observed. As the compression ratio was increased, the amount of reaction increased until finally autoignition of the fuel/air mixture occurred and only carbon dioxide and water were observed in the exhaust products. To provide further confidence in the behavior of our models of  $C_{10}$  methyl esters, we used them to represent the  $C_9$  methyl esters oxidation in these experiments.

We expect the reactivity of these large  $C_9$  and  $C_{10}$  methyl esters to be similar because the reactivity of the large methyl ester is largely determined by the length of  $CH_2$  chains contained in the hydrocarbon chain attached to the ester group. If there is a sufficient number of  $CH_2$  groups in a series,  $RO_2$  isomerizations will be very fast leading to low temperature reactivity in the engine. At least three  $CH_2$ 

groups in a row are needed to allow 6-member transition states which have the fastest isomerization rates. If the  $CH_2$  chain length is longer, more 6-member isomerizations are possible leading to more reactivity. One can compare the length of the  $CH_2$  chains in the  $C_9$  methyl esters examined in the engine study (Fig. 13) with that of the  $C_{10}$  methyl esters in our model (Fig. 3). We chose to compare the methyl-2-nonenoate with a five  $CH_2$  group chain with the methyl-5-decenoate with two groups of three  $CH_2$  chains. The three  $CH_2$  chains give sufficient length to allow  $RO_2$  isomerizations with 6-member transition states.



Fig. 13. Structures of C<sub>9</sub> methyl esters investigated in a motored engine study [18].

We simulated the oxidation of the C<sub>9</sub> methyl esters in the engine using a single zone, homogeneous, engine model provided in the Senkin code of Chemkin 3 [39], a numerical model we successfully used in simulating similar experiments for methyl decanoate [15]. We accounted for heat transfer losses in the CFR engine by lowering the intake temperature until similar reactivity was achieved in the model as in the experiment. In the engine experiments, the intake temperature was maintained at 523 K to fully vaporize the C<sub>9</sub> methyl esters. In the calculations, we lowered the intake temperature by 120 K to match the overall reactivity seen in the experiments. The CFR engine has thick metal block which is cooled with water so that we expect significant heat losses from the fuel–air charge to the combustion chamber walls. The calculations matched other experimental conditions: engine speed of 600 rev/s, fuel/air equivalence ratio of 0.25, intake pressure of 100 kPa, intake valve closing of 166° before top dead center (TDC), and exhaust valve opening of 153° after TDC. For the slider-crank formula in the engine model, the ratio of the connecting rod length to the crank-arm radius is 4.5.

Since this is a motored engine, it takes a number of engine cycles for the exhaust composition to reach steady-state. Since not all the contents of the combustion chamber are exhausted after each cycle, a residual fraction of species present at the end of the cycle needs to be added to the fresh fuel—air charge of the subsequent cycle (Fig. 14). This residual fraction was assumed to be equal to 1/(compression ratio) which approximately accounts for volume of gas remaining at TDC in the engine and that is not exhausted after the end of the exhaust stroke. To achieve steady-state concentrations at the end of the engine cycle, about nine cycles needed to be computed. For nine

cycles per compression ratio and the six compression ratios, 36 h of CPU time were used on a 3 GHz PC.



Fig. 14. Gases in the residual part of the cylinder were taking in account by considering consecutive cycles (ICE = internal combustion engine).

The comparison of the computed and measured results is shown in Fig. 15. The  $CO_2$  is quite well reproduced by the model and the CO is within a factor of 2–3. The profile shapes are well simulated by the model. For the hydrocarbon species, the  $CH_4$  is well reproduced and the  $C_2H_4$  and  $C_3H_6$  are reproduced within a factor of 2–4. The profile shapes of  $CH_4$  and  $C_2H_4$  are well simulated by the model. The model  $C_3H_6$  profile is shifted slightly to lower compression ratios compared to the experiments. As seen by the total carbon in the species measured by the experiments and computed in the model, the model is producing more of these species before high temperature ignition occurs at a compression ratio of 7.7. This discrepancy may be due to temperature inhomogeneities in the engine such as cooler regions near the walls and ring crevices with correspondingly different reactivities which are not treated by a single zone model. Probably a multizone model [40] is needed to address these inhomogeneities in the combustion chamber. After hot ignition, the total carbon in the model and experiment is nearly the same. The above model and experimental comparisons give some additional confidence that the model is performing in a reasonable way under engine conditions.



Fig. 15. Comparison of predicted and measured [18] species exhausted from the motored engine (fuel: methyl-5-decenoate (model), methyl 2-nonenoate (experiments). Equivalence ratio of 0.25 and 600 rev/min.

#### 4. Conclusion

In this study, models for two unsaturated esters, methyl-5-decenoate and methyl-9-decenoate, were built using the reaction rules for alkenes. Some adaptations were required in order to adapt these rules to the case of esters. Both models were compared with rapeseed oil methyl esters experiments in a jet-stirred reactor. This comparison showed that methyl-9-decenoate does a better job than methyl-5-decenoate in reproducing the reactivity and the mole fraction profiles of important species.

The comparison of ignition delay times computed with both mechanisms showed that methyl-9decenoate is more reactive than methyl-5-decenoate, in particular in the NTC region. The lower reactivity of methyl-5-decenoate is due to more difficult isomerizations over the double bond. Thus methyl-9-decenoate, with the double bond at the end of the alkylic chain, seems to be a better surrogate than methyl-5-decenoate for unsaturated esters in real biodiesel fuels. It is the length of the continuously-saturated carbon chain in the reactant that determines its reactivity because it sets the range of possible  $RO_2$  isomerizations.

Models of methyl decanoate, methyl-9-decenoate and n-heptane were combined in order to obtain a blend surrogate mechanism more representative of biodiesel fuels. This blend surrogate model was used to simulate rapeseed oil methyl esters experiments in a jet-stirred reactor. The model reproduced well the experimental mole fraction profiles of most species with good agreement. This model can also be used for the modeling of biodiesel fuels from various origins by adjusting the mole fractions of the three fuel components in the reactant mixture.

Finally, methyl-5-decenoate was used as a surrogate fuel to simulate the partial oxidation of methyl-2-nonenoate in a motored engine. The CO,  $CO_2$  and hydrocarbon species at the end of the engine cycle were similar in the measurements and simulations. These results give some confidence in the use of the chemical kinetic model under engine conditions.

#### Acknowledgments

This work performed under the auspices of the US Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344. We wish to thank Mr. Yu Zhang, Dr. Yi Yang, and Prof. André L. Boehman for details on the engine experiments and for the experimental data in tabular form.

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