## Supplementary Tables and Figures

## Supplementary Tables

Supp. Table 1: Results of Profile Likelihood and Hessian-Based Calculations of Confidence Intervals (Using PottersWheel fitting toolbox). All results conclude to non-identifiability of model parameters, due to infinite confidence intervals.

Parameter	Identifiability	Lower CI (PL)	Upper CI (PL)	Lower CI (Hessian)	Upper CI (Hessian)
mN	practically non-ident.	0	Inf	0	In
dNE	practically non-ident.	0	Inf	0	Ir
rE	practically non-ident.	0	Inf	0	1.3972e+24
mE	practically non-ident.	0	Inf	0	Ir
dEM	practically non-ident.	0	Inf	0	2.7777e+11
mM	practically non-ident.	0	Inf	0	1.7880e+29
rP	practically non-ident.	0	Inf	0	1
mP	practically non-ident.	0	Inf	0	1
mP0	practically non-ident.	0	Inf	0	1
mN	practically non-ident.	0	Inf	0	li
mN	practically non-ident.	0	Inf	0	1
dNE	practically non-ident.	0	Inf	0	1
rE	practically non-ident.	0	Inf	0	1
mE	practically non-ident.	0	Inf	0	1
dEM	practically non-ident.	0	Inf Inf	0	ا 2.7456e+2
mM	practically non-ident.	0		0	
rP	practically non-ident.	0	Inf	0	
mP	practically non-ident.	0	Inf	0	
mP0	practically non-ident.	0	Inf	0	1
Results for	Lm data:	Lower CL (PL)	Lipper CL (PL)	Lower CL (Hessian)	Upper CL (Hession)
Parameter	Lm data:	Lower CI (PL)	Upper CI (PL)	Lower CI (Hessian)	Upper CI (Hessian)
Parameter	Lm data: Identifiability practically non-ident.	Lower CI (PL)	Upper CI (PL)	Lower CI (Hessian)	Upper CI (Hessian)
Parameter MN dNE	Lm data: Identifiability practically non-ident. practically non-ident.	Lower CI (PL)	Upper CI (PL)	Lower CI (Hessian)	Upper CI (Hessian)
Results for Parameter mN dNE rE	Lm data: Identifiability practically non-ident. practically non-ident. practically non-ident.	Lower CI (PL) 0 0	Upper CI (PL) Inf Inf	Lower CI (Hessian) 0 0 -1.9032	Upper CI (Hessian)
Results for Parameter mN dNE rE mE	Lm data: Identifiability practically non-ident. practically non-ident. practically non-ident.	Lower CI (PL) 0 0 0 0	Upper CI (PL) Inf Inf Inf	Lower CI (Hessian) 0 -1.9032 -9.9575e-06	Upper CI (Hessian) 1 -1.903 -9.9575e-C
Results for Parameter mN dNE rE mE dEM	Lm data: Identifiability practically non-ident. practically non-ident. practically non-ident. practically non-ident.	Lower CI (PL) 0 0 0 0 0 0	Upper CI (PL) Inf Inf Inf Inf	Lower CI (Hessian) 0 0 -1.9032 -9.9575e-06 -0.0300	Upper CI (Hessian) -1.903 -9.9575e-( -0.030
Parameter MN dNE rE mE deM mM	Lm data: Identifiability practically non-ident. practically non-ident. practically non-ident. practically non-ident. practically non-ident.	Lower CI (PL) 0 0 0 0 0 0 0	Upper Ci (PL) Inf Inf Inf Inf	Lower CI (Hessian) 0 -1.9032 -9.9575e-06 -0.0300 -0.1000	Upper CI (Hessian) -1.90 -9.9575e-0 -0.03 -0.100
Results for Parameter mN dNE rE mE dEM mM rP	Lm data: Identifiability practically non-ident. practically non-ident. practically non-ident. practically non-ident. practically non-ident. practically non-ident.	Lower CI (PL) 0 0 0 0 0 0 0 0 0	Upper CI (PL) Inf Inf Inf Inf Inf	Lower CI (Hessian) 0 -1.9032 -9.9575e-06 -0.0300 -0.1000 -0.0158	Upper CI (Hessian) - 1.903 - 9.9575e-( - 0.030 - 0.100 - 0.015

Supp. Table 2: Relationship between the parameters and the biological rates of the model. Graphic illustrations of biological rates are shown for the parameter values corresponding to the best result of the model using the influenza data. They correspond to the biological rate underlined in the third column.

	Notation	Corresponding	Evolution of the
	(symbol)	biological rates	biological rate
		$(d^{-1})$	$(d^{-1})$ during
			the response
Parameters which	μη δεμ	μη δεμ	
model constant	$\mu_N, \sigma_{EM}, \mu_0$	$\mu_N, \sigma_{EM}, \mu_0$	os Death Rate of
biological rates $(d^{-1})$	$\mu_M, \mu_P$	$\underline{\mu}_{M}, \mu_{P}$	0.7 Memory Cells
biological lates (d )			0.6
			0.3
			<sup>10</sup> 5 10 15 20 25 30 35
Parameters associated	$\delta_{NE}, \rho_E,$	$\delta_{NE}P, \ \underline{\rho_EP},$	1.75
with non constant	$ ho_P$	$\rho_P P$	1.5 Proliferation Rate of
biological rates $(d^{-1})$			1.25. Effector Cells
			1
			0.5
			0.25
Parameters associated	$\mu_E, \mu_P$	$\mu_E E, \mu_P E$	
with non constant		<u> </u>	o.s Death Rate of −
biological rates			0.7 Effector Cells
$(cell^{-1}.d^{-1})$			0.5
			0.4
			0.2-

## Supplementary Figures



Supp. Fig. 1: Frequencies of appearance of values of  $(\mu_N, \delta_{NE})$  among the acceptable parameter value sets for *Lm* infection. The height of red vertices indicates the percentage of parameter sets using the associated pair-value. For correlated parameters, values of one parameter are strongly associated with one or two values of the other parameter. Here, low values of  $\delta_{NE}$  are preferentially associated with high values of  $\mu_N$ .



Supp. Fig. 2: Uncorrelated parameter values. Frequencies of appearance of every pair ( $\delta_{EM}, \mu_M$ ) (left) and ( $\rho_E, \mu_M$ ) (right) among the acceptable parameter value sets are presented, for the three infections. The height of red vertices indicates the percentage of parameter sets using the associated pair-value. Uncorrelated parameters are characterized by a similar distribution of parameter values whatever the value of the other parameter. One observes no correlation between parameter values for experiments on Flu (top), VV (middle), and Lm (bottom).



Supp. Fig. 3: Total number of CD8 T cell counts and percentages of memory cells among the total CD8 T cell population predicted by the model for VV infection. For every parameter value set among the acceptable ones, the histograms of the number of simulations associated with a given count of total CD8 T cells (left panel) and with a given percentage of memory cells among the total CD8 T cell population (right panel) are presented, both at the end of the experiment (D47, top) and at D360 (bottom).



Supp. Fig. 4: Total number of CD8 T cell counts and percentages of memory cells among the total CD8 T cell population predicted by the model for *Lm* infection. For every parameter value set among the acceptable ones, the histograms of the number of simulations associated with a given count of total CD8 T cells (left panel) and with a given percentage of memory cells among the total CD8 T cell population (right panel) are presented, both at the end of the experiment (D34, top) and at D360 (bottom).



Supp. Fig. 5: **Pathogen count evolution.** For the 3 experiments (top left: Flu; Top right: VV; Bottom: Lm), the average evolution of the pathogen count, with standard deviation, is shown over the duration of each experiment. This evolution is computed from each individual evolution among the acceptable parameter value sets.