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Optimizing the Power Take Off of a Wave Energy Converter With Regard to the Wave Climate

Gaëlle Duclos, Aurélien Babarit, Alain H. Clément

Laboratoire de Mécanique des Fluides (CNRS-UMR6598) Ecole Centrale de Nantes 1, Rue de la Noë, 44300 Nantes, France

Considered as a source of renewable energy, wave is a resource featuring high variability at all time scales. Furthermore wave climate also changes significantly from place to place. Wave energy converters are very often tuned to suit the more frequent significant wave period at the project site. In this paper we show that optimizing the device neces-sitates accounting for all possible wave conditions weighted by their annual occurrence frequency, as generally given by the classical wave climate scatter diagrams. A generic and very simple wave energy converter is considered here. It is shown how the optimal parameters can be different considering whether all wave conditions are accounted for or not, whether the device is controlled or not, whether the productive motion is limited or not. We also show how they depend on the area where the device is to be deployed, by applying the same method to three sites with very different wave climate.

1 A Generic Wave Energy Device: Working Principle and Governing Equations

In this study, we shall use as an example a very simple point absorber device with a single degree of freedom. Namely, we will consider a submerged vertical cylinder constrained to move in heave motion only, under the action of wave excitation forces. The stroke of the vertical motion apart from the equilibrium position, denoted by $\zeta(t)$, is limited between $-b$ and $+b$ with *b* $= 5$ m to account for endstops (Fig. 1).

The body oscillates vertically under the action of excitation forces, radiation forces, restoring forces idealized here as a single spring of stiffness *k*, and a damping force proportional to the velocity (with damping coefficient B) supposed to model the action of the Power Take Off (PTO) mechanism. This generic system belongs to the same family as some real projects currently being tested in full scale.

A linear approach will be adopted here for modeling hydrodynamics, in such a way that the behavior of the body in waves will be governed by the following integro-differential equation:

$$
(M+\mu_{\infty})\ddot{\zeta}+\int_0^t \dot{\zeta}K(t-\tau)d\tau+B\dot{\zeta}+k\zeta=F_{\text{ex}}(t) \qquad (1)
$$

where one can recognize the Cummins' decomposition $[1]$ of the radiation forces into an instantaneous added mass term $\mu_{\infty} \ddot{\zeta}$ and a memory term expressed by a convolution product $\int_0^t \dot{\zeta}(\tau) K(t)$ −*d*. The kernel *K* of this integral, generally named *impulse response function*, or sometimes *retardation function*, depends essentially on the shape of the body. It can be computed directly in the time domain by using dedicated seakeeping BEM codes like ACHIL3D [2], TIMIT,.... But it can also be deduced through a Fourier transform of the frequency domain hydrodynamic coefficients (added mass and damping coefficient) for which dedicated computer codes like WAMIT [3], DIODORE, AQUADYN [4],..., can be used. In the present time-domain linear formulation, the free motion $\zeta(t)$ of the device may be calculated by integrating (1) for a given history of the wave excitation forcing term $F_{ex}(t)$, and given

initial conditions $\zeta(0)$ and $\dot{\zeta}(0)$. Once the impulse response function $K(t)$ has been determined, it can be further approximated by a sum of exponential functions by using Prony's method as described in [5]. This allows replacing the integro-differential form (1) by a system of ordinary differential equations (ODE) like (2) , generally better suited to the numerical simulation,

$$
\begin{cases}\n(M + \mu_{\infty})\ddot{\zeta}(t) + \sum_{i=0}^{N} I_i(t) + B\dot{\zeta}(t) + k\zeta(t) = F_{\text{ex}}(t) \\
I_i(t) = \beta_i I_i(t) + \alpha_i \dot{\zeta}(t)\n\end{cases} (2)
$$

The device as described up to now is a linear mechanical oscillator. The mean power \hat{P} extracted by the PTO over a time range *T* is given by

$$
\hat{P} = \frac{B}{T} \int_0^T \dot{\zeta}^2(\tau) d\tau \tag{3}
$$

The power of the incident wave train \hat{P}_i is classically expressed in kW per meter of the wave front (generally considering incident waves as a 2D train of long crested irregular waves). Then if we reduce \hat{P} (Eq. (3)) the power extracted by the device, by the power of incident waves to quantify the efficiency of the system, the result will be expressed in meters of the wave crest; it is the so-called *capture width* of the device. Further dividing this capture width by the width of the device itself, we obtain a nondimensional number which is called *capture width ratio* (sometimes shortened into *capture ratio*. This ratio will be used here to quantify the energetic efficiency of the device.

This device is basically a linear mechanical oscillator, with a natural circular frequency ω_0 depending on the spring coefficient *k*, on the proper mass and the added mass of the body. When it is left uncontrolled, the designer must choose the natural frequency to make the device the most possible efficient for the site where it will be deployed.

One condition for maximizing converted energy in harmonic regime is the phase condition imposing the oscillating velocity of the body to be in phase with the excitation force on the body phase control. This happens exactly when the wave frequency equals the natural frequency of the body. In order to maximize the extracted power, an optimum amplitude condition must also be satisfied. Basically, if the amplitude of the motion is uncon-

Fig. 1 The generic device: working principle

strained, this condition states that the resistive load *B* of the PTO should equal the hydrodynamic damping coefficient at the incident wave frequency. It is therefore easy to understand that in random sea, an uncontrolled device can't be optimally efficient at any time.

A device is said to be controlled if it can adapt itself to the incident wavetrain, wave after wave. The control can be either continuous or discrete (see Falnes [6] for a recent review about this topic).

Continuous control is achieved by acting on the mechanical parameters of the PTO in order to respect the two above conditions. A lot of work has been done about this topic; see, e.g., $[7,5,8]$.

In the present study, we have used instead another approach to Wave Energy Converters (WECs) control, called latching control. Unlike the previously continuous one, this method is discrete. It consists of locking (latching) the motion of the body at the moment when its velocity vanishes, and waiting for the wave force having reached the most favorable phase to release the body. The body then starts moving from this initial position to the next velocity vanishing position where it is latched again, and so on. Instead of being a smooth, continuous function of time, the position of the body is a succession of ramps of transient motions separated by stages of rest. The action control upon the system is therefore binary: either the body is latched, either it is free to move, which explains the meaning of the term "discrete" used in this context. The instant of latching is imposed by the dynamics of the body (i.e., vanishing velocity); thus, the control variable here is the duration of the latching phase, or equivalently the instant of release. A lot of work has been done by U.A. Korde about it with WEC where energy absorption and latching are achieved by means of pneumatic cylinders with open/close valves; see [9,10]. Here, latching is applied externally on the heave motion of the buoy, as proposed by Budal and Falnes [11] and investigated by Greenhow and White [12] and by Babarit, Duclos, and Clement $[13]$.

Fig. 2 Sea state occurrence frequency for the Yeu Island

2 Three Project Sites

Optimization of such a device consists of determining *B* and *k* (or equivalently the natural period T_0 since k is proportional to $1/T₀$) to obtain as large a yearly energy output as possible. For each wave condition (couple H_s , T_s) five different wave excitation time series (for five different set of random phases) of 1 h have been simulated. If for one of the five wave time series, $|\zeta(t)|$ reach a value bigger than *b* at least once, the device is turned into the survival condition and the energy produced is set equal to zero for this wave condition.

This optimization work was performed for three different sites: Yeu Island which is located in front of the french Atlantic coast near Nantes. The scatter diagram for this place giving the probability of occurrence of each sea state, see Fig. 2, was found on www.cetmef.equipement.gouv.fr, it has been established from field data collected by a wave measuring buoy.

The two others are located around the Reunion Island in the Indian Ocean: Saint Pierre is on the south coast of the island and P67 is a reference meteorological point located in open sea at latitude 21 deg and longitude 55.5 deg. Wave scatter diagrams for this two sites have been found in a report by Perrono [14]. The first one, Fig. 3, was obtained through some in situ measurements whereas the second one, Fig. 4, is the result of a wind-wave numerical model.

The first two sites have the same level of mean annual wave power per unit width but their scatter-diagrams (frequency occurrence for each couple H_s , T_s) are different. The wave power of the third site is lower. Figure 2 shows that the Yeu Island features two distinct prevailing sea states: the first one, $H_s = 1.0$ m, $T_s = 8$ s, is faintly energetic $(\approx 3 \text{ kW/m})$, mean power per meter wave front

Fig. 3 Sea state occurrence frequency for point 67

Fig. 4 Sea state occurrence frequency at St. Pierre

 $\hat{P}_i = 0.55 \times H_s^2 \times T_z$ in kW/m with $T_z = T_s/1.4$), whereas the second one, $H_s = 2.5$ m, $T_s = 8$ s, is far more energetic (≈ 20 kW/m). So we have considered two different dominant sea states for this place. At P67 and Saint Pierre sites, prevailing sea state powers are, respectively, about 16 kW/m and 8 kW/m. Table 1 sums up these prevailing sea states and the related power for each of the three sites considered herein.

3 Results

Results for the mean annual production are generally plotted here in terms of capture width ratio which is the common measure of the point absorber device efficiency in wave energy literature. When results are given in terms of energy, they are computed as the mean of five different time series, or in terms of mean power which is the energy defined above divided by the length of the time series.

3.1 The Optimal Natural Period. Let us first consider the evolution of capture width versus excitation period for various natural periods of the system. Results are plotted in Fig. 5 for the uncontrolled device and in Fig. 6 for the controlled one. In this section, the significant wave amplitude is constant and small 1 m, and the PTO damping coefficient is set to its optimal value for regular wave $(B_{\text{optimal}} = \text{Ca}(\omega_0))$. In this first series of simulations the amplitude of the vertical motion was not limited and so $|\zeta(t)|$ can be greater than *b*.

Capture widths of controlled devices are about twice greater than uncontrolled ones, and system bandwidth are also larger. In the controlled case, and for each value of the natural period T_0 , maximal capture width seems to occur for significant wave period T_s a bit larger than T_0 . When the device is left uncontrolled, the maximal capture width is reached when T_s is very close to T_0 . Figures 7 and 8 show that vertical motion amplitude increases with T_0 and confirm that amplitudes are larger when the device is controlled. Even for such a small wave amplitude (1 m) , when the natural frequency of the system is set to 10 s, the body response $|\zeta(t)|$ can overpass its limit value $b=5$ m.

Table 1 Prevailing sea states of the three sites

		Yeu Island	Point 67	St. Pierre	
Mean power (kW/m)	25.9		29.6	15.4	
Prevailing H_s (m)	10	2.5	2.0	1.5	
Prevailing Ts (s)	8		10	9	
Power of prevailing sea state Yearly number of hours	370	20 345	16 914	8 755	

Fig. 5 Capture width ratio versus T_s , varying T_0 , with B $=$ $Ca(\omega_0)$ (uncontrolled device)

Fig. 6 Capture width ratio versus T_s , varying T_0 , with B $=$ Ca (ω_0) (controlled device)

Fig. 7 Heave motion amplitude versus T_s , varying T_0 , with B $=$ $Ca(\omega_0)$ (uncontrolled device)

Fig. 8 Heave motion amplitude versus T_s , varying T_0 , with B $=$ **Ca** (ω_0) **(controlled device)**

3.2 The PTO Damping Coefficient. In this part, we will vary the PTO damping coefficient B to assess its influence on the capture width. In this section the natural period of the system will be kept equal to 9 s and the significant wave height of the tested sea states set to 1 m.

Again we can see here the benefit brought by the control on the capture width ratio, especially for the small values of *B*.

For a given sea state and a given T_0 , the capture width (or \hat{P}) according to *B* is a bell shaped curve. It is easy to understand that when $B=0$ (no PTO) and $B=\infty$ (PTO infinitely stiff), then no power will be output from the device $(\hat{P}=0)$; when *B* is small ζ tends to be high and oppositely when *B* is high ζ decreases. It is important to notice that the maximum that occurs for values of *B* are very different, whether the device is controlled or not. When the device is uncontrolled, all *B* give results very close to each others, and better results are obtained with $B = 100,000$ (Fig. 9). When the device is controlled, results are very different according to *B*, and the best results are obtained with smaller values of *B* in the range (20,000–30,000), that is close to $Ca(\omega_0)$ (Ca(2 π /9) $= 28,000$. For *B* between 200,000 and 300,000 results are similar whatever the devices are controlled or not.

This first study about damping coefficient does not permit us to conclude definitely on the optimal value of *B* because we didn't consider in this section any bound for the vertical motion; neither

Fig. 9 Capture width ratio versus T_s , varying B, with $T_0 = 9$ s $(uncontrolled$ device)

Fig. 10 Capture width ratio versus T_s , varying B, with $T_0 = 9$ s $(controlled device)$

the fact that for small damping coefficients, the motion amplitudes can be very large, especially when the device is controlled Fig. 10.

3.3 Optimization of the Device by Using the Prevailing Sea State. In this section, we are looking for the couple of mechanical parameters (B,T_0) maximizing energy production over a full year $(8760 h)$ working in the prevailing sea state of each site (let us be reminded that there are two distinct prevailing sea states for the Yeu Island site). Simulations were performed on both the controlled and uncontrolled devices at the three sites. Results are plotted in Figs. 11–18 and summarized in Table 2.

In Figs. 13–18 energy was set to zero for some couples (B, T_0) ; the reason is that, for these sets of parameters, the vertical motion should overpass its imposed limits $\pm b$ and therefore the real device would normally be put in survival condition. The conclusions are similar for all the three locations:

- (1) for the uncontrolled device $(T_0)_{\text{optimal}} = Ts$, whereas (T_0) _{optimal} $\leq T_s$ for the controlled one;
- (2) B_{optimal} is always smaller for the controlled device than for the uncontrolled device;
- (3) energy produced with the optimal couple (B, T_0) is always larger when the device is controlled.

We can observe that in some cases B_{optimal} is the smallest *B* (named B_{min}) for which the device does not reach the endstops *b* (see Figs. $13-16$). Figures 11 and 12 which correspond to a low energetic prevailing sea state show B_{optimal} bigger than B_{min} . This

Fig. 11 Influence of B and T_0 on annual energy production (uncontrolled device), $T_s = 8$ s, $H_s = 1$ m

Fig. 12 Influence of B and T_0 on annual energy production (controlled device), $T_s = 8$ s, $H_s = 1$ m

difference depends on the energy of the considered sea state, and the critical energy threshold seems to be lower when the device is controlled (see Figs. 17 and 18). This can be explained by a larger motion amplitude of this device in comparison with the uncontrolled device.

3.4 Optimization Based on the Whole Sea States Statistics. In this second approach we are seeking for the couple of mechanical parameters *B*,*T*⁰ maximizing energy production over a full working year when one takes into account all the possible sea

Fig. 13 Influence of B and T_0 on annual energy production (uncontrolled device), $T_s = 8$ s, $H_s = 2.5$ m

Fig. 14 Influence of ^B and ^T⁰ on annual energy production (controlled device), $T_s = 8$ s, $H_s = 2.5$ m

Fig. 15 Influence of B and T_0 on annual energy production (uncontrolled device), $T_s = 10$ s, $H_s = 2$ m

states weighted by their probability of occurrence, as given by the scatter diagram of each site. Figures 19–24 show the results of these simulations, and the first conclusions are similar:

- (1) (T_0) _{optimal} are smaller for the controlled device than for the uncontrolled device;
- (2) B_{optimal} are smaller for the controlled device than for the uncontrolled device;
- 3 the maximum capture width ratio is always better for the controlled device.

Fig. 16 Influence of B and T_0 on annual energy production (controlled device), $T_s = 10$ s, $H_s = 2$ m

Fig. 17 Influence of B and T_0 on annual energy production (uncontrolled device), $T_s = 9$ s, $H_s = 1.5$ m

Fig. 18 Influence of ^B and ^T⁰ on annual energy production (controlled device), $T_s = 9$ s, $H_s = 1.5$ m

Fig. 19 Influence of B and T_0 on annual energy production at Yeu Island (uncontrolled device)

Fig. 20 Influence of B and T_0 on annual energy production at Yeu Island (controlled device)

Fig. 21 Influence of B and T_0 on annual energy production at **P67** (uncontrolled device)

Fig. 22 Influence of B and T_0 on annual energy production at **P67** (controlled device)

Fig. 23 Influence of B and T_0 on annual energy production at **St. Pierre (uncontrolled device)**

Table 2 Result of the optimization of $(T0, B)$ based on prevailing sea states

	Prevailing H_s (m)	Prevailing T_s (s)	Uncontrolled		Controlled	
			T_0 (s)	B (N s/m)	T_0 (s)	B (N s/m)
Yeu (1)	1.0		8	100,000		50,000
Yeu (2)	2.5		8	150,000	h	50,000
Point 67	2.0	10	10	100,000	h	40,000
St. Pierre	1.5		Q	100,000	8	40,000

Fig. 24 Influence of B and T_0 on annual energy production at **St. Pierre (controlled device)**

The optimal couples (B, T_0) _{optimal} for each location and for the two optimization methods (by using only prevailing sea state or all sea states statistics) are summarized in Table 3 for the uncontrolled device and in Table 4 for the controlled device. We also report in the tables the energy produced over 1 year by the device working in all sea states (with their frequency occurrences) at each site, computed by using the couples (B, T_0) _{optimal} obtained by both methods.

Both methods provide values of $(T_0)_{\text{optimal}}$ very close to the prevailing *Ts* if the device is uncontrolled, and smaller otherwise. Values of B_{optimal} are very different and we can observe than those obtained by using all the sea states are always larger. This can be explained by the fact that the device must work in sea states where wave amplitude is larger than the prevailing amplitude, and for which it may be put in survival condition if the damping coefficient is too low.

Looking at energy production in Tables 3 and 4, we can see that devices tuned by using all sea state statistics for a given site allow us to produce more energy. As can be expected, the most efficient device is tuned that way, and controlled. The gain in energy output obtained by selecting the best optimization method can be as high as 400%.

Let's compare results obtained for St. Pierre with those obtained for the P67 site:

- (a) For the first place and for the uncontrolled device, the optimization method allows a small gain, 25%, versus 420% for the second place;
- (b) If the device is tuned by using only the prevailing sea state, the control results in a loss of efficiency of about 50%, but an increase of 100% for the other place.

To understand these differences, we can look at Figs. 25 and 26 which show the optimized device working in all four situations at these two sites. We have plotted, for each sea state, the mean annual extracted power: Fig. 25 is related to St. Pierre while Fig. 26 to the P67 place. For the uncontrolled devices the results are plotted in the top figures, whereas results for the controlled device are plotted in the bottom figures: the left plots (a) and (c) correspond to the devices tuned by using only the prevailing sea state, and the right plots (b) and (d) at the devices tuned with the detailed method.

The first difference (previously quoted) between this two places can be explained by the B_{optimal} values. Indeed for P67 site B_{optimal} is equal to B_{min} (see Fig. 15) and so it is easy to understand that in a sea state a bit more energetic than the prevailing sea state, the device is put in survival condition. Figure $26(a)$ proves that the device is stopped very often. In this case the cumulated working time is very short $(2354 h)$. We can see in Fig. 26*(b)*, that the detailed optimization method, by providing a bigger B_{optimal} , enables the device to work more frequently and in more energetic sea states. For the St. Pierre site, the B_{optimal} is larger than B_{min} and the device will work in more energetic sea state than that used for the optimization. Figure $25(a)$ confirms this and in this case the device works over a long period of time (7350 h). So even if the other method of optimization gives a bigger value of B_{optimal} , the working time can be only a bit longer and so the production of energy can only be a bit higher.

Let's now turn to the second difference mentioned above: for the P67 site, whether the device is controlled or not, B_{optimal} is in both case equal to B_{min} . We can see by comparing Figs. 26*(a)* and $26(c)$ that the controlled device works a bit more often and that, for the same sea state, it produces more energy. For the St. Pierre site, if the device is controlled B_{optimal} is equal to B_{min} but if the device is uncontrolled B_{optimal} is upper to B_{min} . And so we can see in Figs. $25(a)$ and $25(c)$ that the uncontrolled device works more and for frequent and energetic sea states.

By comparing Figs. 25*(b)* and 25*(d)* or 26*(b)* and 26*(d)*, we can see the uncontrolled devices work during a longer period of time

		lable 3		Optimal production for the uncontrolled device				
	Optimization/prevailing sea states			Optimization/whole scatter diagram				
	T_0 (s)	B $(N \, s/m)$	Energy (MWh)	Working hours (h/year)	T_{0} (s)	B $(N \, s/m)$	Energy (MWh)	Working hours (h/year)
Yeu (1) Yeu (2)	8 8	100,000 150,000	138.1 266.4	4761 6031	9	350,000	562.2	8273
Point 67 St. Pierre	10 9	100,000 100,000	154.6 335.5	2354 7350	9 10	300,000 250,000	798.6 421.0	8562 8568

Table 3 Optimal production for the uncontrolled device

Table 4 Optimal production for the controlled device

Fig. 25 St. Pierre site: top row (a, b) uncontrolled device; bottom row; (c, d) controlled device; left column (a, c) **prevailing sea state optimization; right column** (b, d) **global optimization**

Fig. 26 P67 site: top row (a, b) uncontrolled device; bottom row (c, d) controlled device; left column (a, c) prevailing sea state optimization; right column (b, d) global optimization

than the controlled devices, but as for a same sea state, the power delivered by the controlled device is larger; finally a controlled device tuned by using all sea state statistics is far more efficient.

4 Conclusion

This study has shown that the tuning of a wave energy converter to a given site should necessarily be based on the detailed wave climate, accounting for sea states statistics of the site instead of being tuned for the dominant sea state, as it is often reported. This optimal tuning of the mechanical parameters is even more important than the control. We saw that a badly optimized device, even controlled, can be less efficient than a badly optimized and uncontrolled device. Finally a well optimized device, even uncontrolled, is always more efficient than a badly optimized one, controlled or not. Whatever the site considered, the best device in terms of annual energy production is the one which has been tuned by using detailed sea states statistics, and which works under wave to wave control.

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