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Resistance to fire of walls constituted by hollow blocks: Experiments and thermal modeling

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Abstract

The thermo-mechanical behavior of masonry walls is investigated from both experimental and theoretical points of view. Fire tests have been performed in order to evaluate the thermo-mechanical resistance of masonry wall submitted to a vertical load (13 ton/m) and exposed to temperatures ranging from 20 to 1200 °C. As a result we measure the temperature evolution inside the wall and evaluate the vertical and lateral displacements of this wall during heating for a period of 6 h. These results are affected significantly by phase-change phenomena which appeared as a plateau around °C in temperature–time curves. A theoretical model was then developed to describe the experimental results taking in to account convection, conduction and radiation phenomena inside the wall. In addition, liquid water migration using an enthalpic method is considered.

Keywords: Wall heat conduction; Phase-change phenomenon; Firewall tests; Fire resistant masonry; Wall heat convection; Wall heat radiation

1. Introduction

Recently the development of construction materials for bearing walls in buildings has made remarkable progress. The use of masonry walls seems to have many benefits [1,3,6–9,12], the first of which is the fact that a single element can fulfil several functions including structure, fire protection, thermal and sound insulation, weather protection and sub-division of space. The second major advantage is related to the durability of materials which may remain in service for many years. From an architectural point of view, masonry offers advantages in terms of great flexibility of plan form. The advantages of masonry wall construction are therefore considerable, but, as with all materials, they must be able to withstand fire. The resistance to fire of masonry wall [11,13–16] includes not only the capacity of constitutive blocks alone, but also the one

of its main constituent materials i.e. aggregate, cement and water. The contribution of the aggregates and cement to fire resistance of structure were discussed earlier [18]. Although there is much research concerning the effect of cement and aggregate on the resistance to fire of masonry walls, there is a need to pay attention to the role of the water content [5,17]. The present work is devoted to the study of this effect on the thermal response of masonry walls subjected to fire. This paper is in two parts:

- The experimental part, which is principally devoted to the temperature and displacement measurement within the masonry wall exposed to temperatures ranging from 20 to 1200 °C [2].
- The theoretical study, which establishes a thermal model taking into account heat transfer through the wall by convection, radiation and conduction.

This model also accounts for the liquid water migration inside the wall using an enthalpic method: specific heat variation in a small interval of temperature around the

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Nomenclature

c	specific heat (J/(kg K))	T	temperature (°C)
c_{eq}	equivalent specific heat (J/(kg K))	T_0	initial temperature (°C)
e	thickness of the partition (m)	$T_{furnace}$	temperature of the furnace (°C)
e_i	thickness of the sub-partition i ($i = 1, 2, 3$) (m)	T_{iso}	normalized temperature-curve (°C)
E_v	energy absorbed (J)	δT	interval of temperature (°C)
h_i	convection coefficient ($i = 1, 2, 3, 4$) (W/(m ² K))	w	water content
K	intrinsic permeability (m ²)	$\alpha_A(x)$	the interpolation function
L	latent heat of water vaporisation (J/kg)	ϕ	porosity
m_l	mass of liquid water (kg)	λ	thermal conductivity (W/(m °C))
q_{ra}	radiation heat flow (W/m ²)	ρ	mass density (kg/m ³)
q_{conv}	convection heat flow (W/m ²)	ρ_d	mass density at dry state (kg/m ³)
q_{cond}	conduction heat flow (W/m ²)	ε_i	emissivity coefficient ($i = 1, 2, 3$)
S_0	equivalent area heat (J/m ² K)	σ	Stephan Boltzman constant ($\sigma = 5.67 \times 10^{-8}$)
t	time (min)		

temperature of ebullition (100 °C) for modeling the water evaporation.

2. Experimental tests

2.1. Introduction

This Section presents the experimental results including the temperature and the displacements of a masonry wall subjected to high temperatures. These results are discussed to obtain qualitative information on the thermo-mechanical behavior of the wall, in particular the phase-change effect. Moreover, it will form the basis for a quantitative interpretation of the global thermal model developed in Sections 3 and 4.

2.2. Materials

2.2.1. Blocks

The form of blocks used to construct the wall is presented in Fig. 1. The apparent compressive strength of the block is 4 MPa. It is obtained by compacting the aggregates with mortar using a particular mold to produce the hollow blocks. The measured porosity and intrinsic permeability are equal to $\phi = 21\%$ and $K = 2 \times 10^{-12}$ m², respectively. This type of block is widely used in the majority of building construction in France.

2.2.2. Wall geometry and boundary conditions

The geometry of the wall used is presented in Fig. 2, where the vertical and horizontal sections are presented also. This wall is constructed by assembling the hollow blocks described above.

The horizontal and vertical joints are filled by a mortar which has the same mechanical characteristics as the blocks. The top and bottom edges of the wall are filled by a mortar of thickness equal to 30 mm and 20 mm, respectively.

2.3. Furnace and mechanical apparatus

A vertical furnace with dimensions of ($3 \times 3 \times 1.4$ m) is used. It has 12×224 kW gas-fired burners. The temperature evolution inside the furnace is controlled by the thermocouple type K and follows the normalized temperature-curve (ISO) [2], given by Eq. (1):

$$T_{furnace} = T_{iso} = T_0 + 345 \log_{10}(8t + 1) \quad (1)$$

where T_0 is the initial temperature, t the time in minutes. The maximal temperature which can be measured by the thermocouples is 1250 °C with an accuracy of ± 10 °C.

In the normalized temperature-curve (ISO) [2], the temperature reaches 900 °C at 40 min and reaches 1200 °C at 6 h.

A uniform vertical load (357 kN) is applied on the wall using the mechanical apparatus presented in Fig. 3. It is composed principally of a portal frame metallic beam and two jacks (V1 and V2) which apply the vertical load on the wall by means of a metallic frame. It is servo-controlled by a servo-mechanism which commands an autonomous hydraulic plant. The capacity of each jack is ± 500 kN and the force applied can be controlled with an accuracy of ± 2 kN. The vertical space between this frame and lateral parts of the wall is filled with a rock wool.

2.4. Temperature measurement

The temperature evolution inside the wall is measured using thermocouples fixed inside three blocks (see Fig. 4a). The position of thermocouples in each block is indicated in Fig. 4b. The position of the blocks is chosen according to the French regulation (CSTB) [2].

2.5. Displacement measurement

The vertical and horizontal displacements were measured using the LVDT transducers, which have a measurement

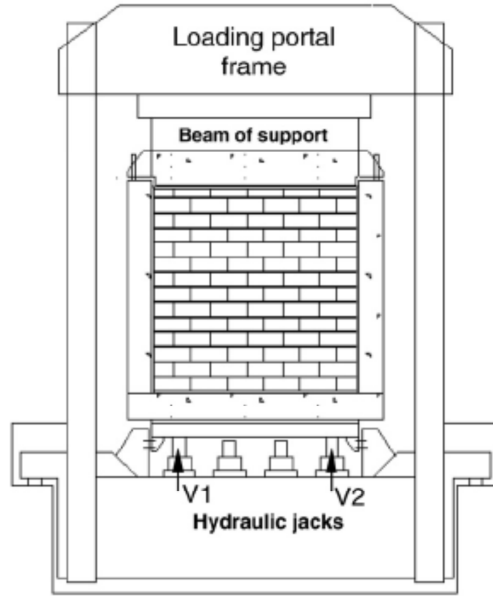


Fig. 3. Mechanical testing apparatus.

ear part ranging from 0 to 25 min, followed by the second part where the displacement is quasi-constant until 45 min.

We remark that the displacements of points (2, 4 and 6) situated in the median axis of the wall is more important than those corresponding to the points (3 and 7) which are near the bottom edge of wall. These last measurements are near the rigid metallic frame.

2.6.2.2. Vertical displacement. The average vertical displacement measured by the two LVDT transducers is reported in Fig. 8. We can point out a linear part of dis-

placement between 0 and 30 min followed by a plateau until 90 min. Then the displacement is increasing. The plateau observed from 30 to 90 min can be related to the same features as the one on temperature-time curves (see the curve corresponding to point 4 in Fig. 6) which can be interpreted as follows: thermal expansion of the constitutive material creates vertical and lateral deformations of the wall. These deformations take a constant value when the temperature of a great part of the wall becomes constant during the evaporation of liquid water inside the material.

3. Thermal modeling

The thermal transfer across different parts of the wall is studied using a simplified one-dimensional model which takes into account: convection, radiation and conduction. The energy absorbed to evaporate the interstitial water is also taken into account in this model. The model is based on a finite difference scheme, each partition of the wall being divided into three sub-partitions.

3.1. Energy equation

The method to construct the system of equations is to apply the energy balance to each sub-partition of the wall. The temperature is assumed to vary quadratically within each partition (Fig. 9). An interpolation function within each partition describes the temperature variation from the temperature of three nodes ((1), (2) and (3) (see Fig. 9) for a partition 1, for example). The general form of the energy balance for each sub-partition i can be written as follows [4]:

$$e_i \cdot \rho \cdot c \cdot \frac{dT}{dt} = q_{\tau z} + q_{\text{conv}} + q_{\text{cond}} - L \frac{dE_v}{dt} \quad (2)$$

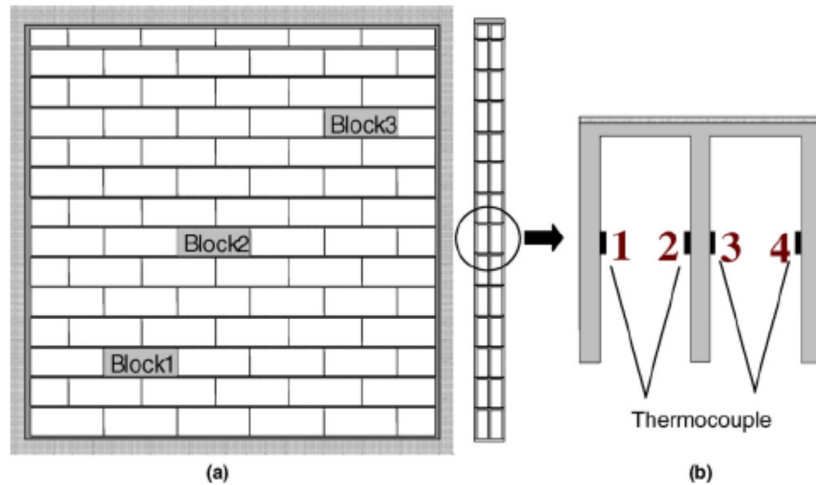


Fig. 4. Position of thermocouples in each block in the wall.

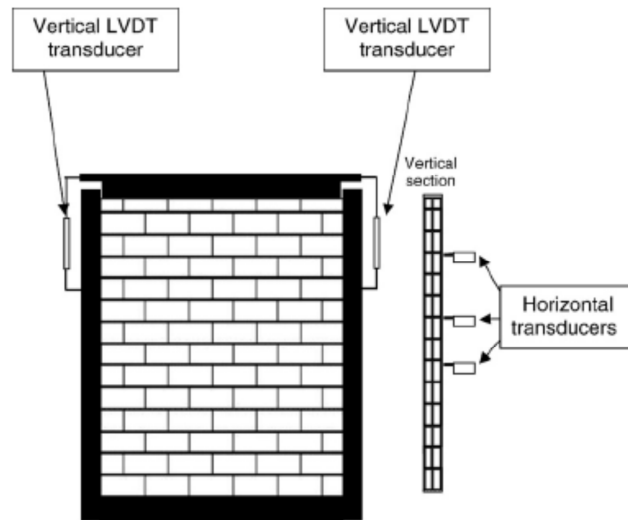


Fig. 5. Horizontal and vertical displacements measurement.

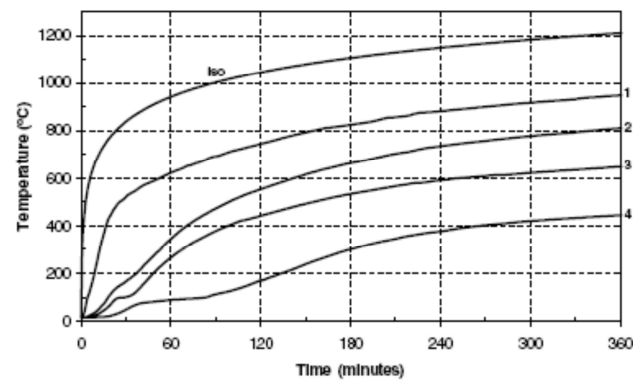


Fig. 6. Temperature evolution as function of time measured at several points as defined in Fig. 4.

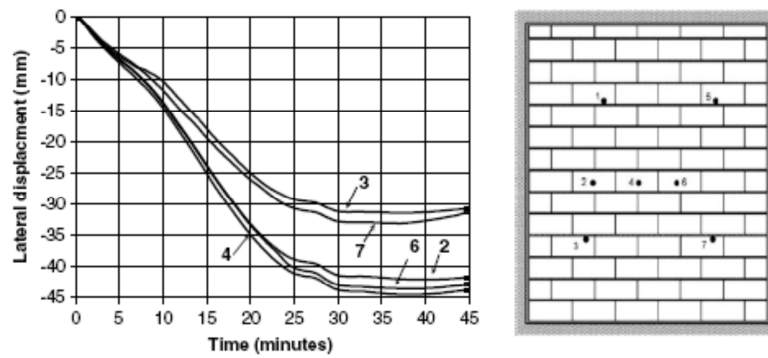


Fig. 7. Result of lateral displacement measurement in several points of the wall (1–7) obtained using horizontal transducers as defined in Fig. 5.

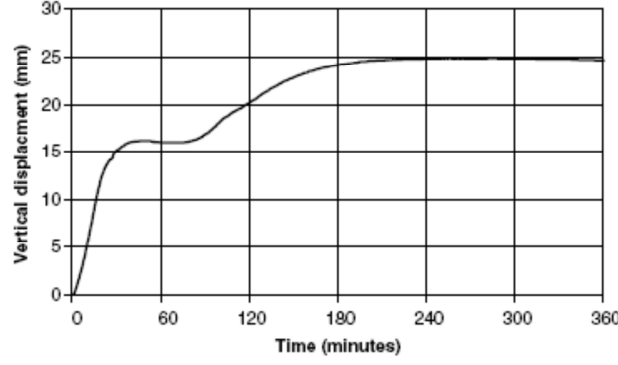


Fig. 8. Result of vertical displacement measurement obtained by vertical transducers as defined in Fig. 5.

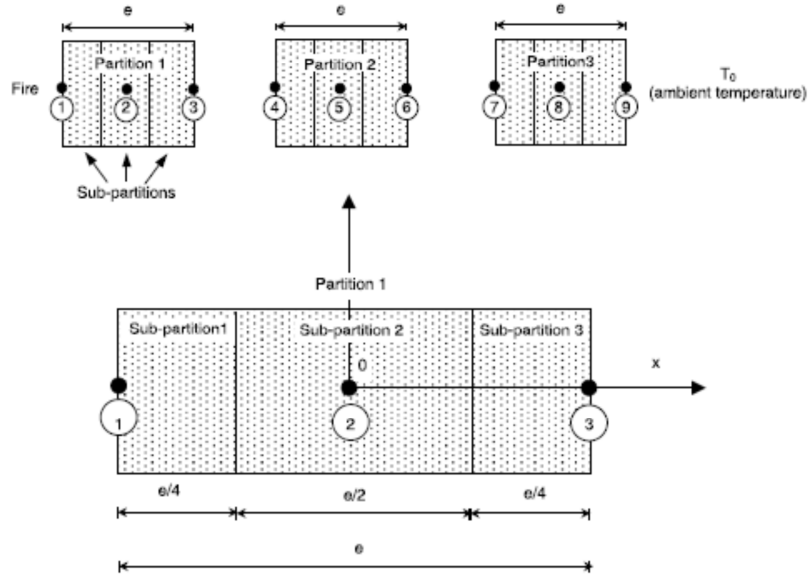


Fig. 9. Definition of partitions and sub-partitions of the wall.

where e_i is the thickness of sub-partition i , ρ the density, c a specific heat of the constitutive material. q_{ra} : radiation heat flow, q_{conv} : convection heat flow, q_{cond} : conduction heat flow and E_v is the energy absorbed to evaporate the interstitial water. In order to simplify the model, the phase-change phenomenon (physically occurring at exactly 100 °C under atmospheric pressure) is simulated by a continuous phenomenon during a temperature interval of δT around 100 °C. With this assumption, the energy absorbed during the evaporation can be written:

$$E_v = \int_{100-\delta T}^{100+\delta T} L \frac{dm_i}{dt} \int_{100-\delta T}^{100+\delta T} S_0 \frac{dT}{dt} dt \quad (3)$$

where L is the latent heat of water vaporization, m_i : mass of liquid water by unit of volume ($m_i = w \cdot e_i \cdot \rho$), w is the water

content and S_0 is the heat absorbed by evaporation for an increasing of temperature of 1 °C, given by:

$$S_0 = \frac{L \cdot w \cdot e_i \cdot \rho}{2 \cdot \delta T} \quad (4)$$

The computation were made with $\delta T = 5^\circ\text{C}$.

From Eq. (3) we can write:

$$\frac{dE_v}{dt} = S_0 \frac{dT}{dt} \quad (5)$$

Introducing Eq. (5) into Eq. (2) leads to:

$$e_i \cdot \rho \cdot [c + c_{eq}] \frac{dT}{dt} = q_{ra} + q_{conv} + q_{cond} \quad (6)$$

$$\text{where: } c_{eq} = \frac{S_0}{e_i \cdot \rho} \quad (7)$$

Combining Eqs. (4) and (7) allows to calculate c_{eq} . It can be written:

$$c_{eq} = \frac{L \cdot w}{2 \cdot \delta T} \quad (8)$$

Finally the energy balance for each sub-partition i can be written under the following global form:

$$e_i \cdot \rho \cdot c_i \frac{dT}{dt} = q_{ra} + q_{conv} + q_{cond} \quad (9)$$

where $c_i = c + c_{eq}$.

3.1.1. Energy balance for the first partition

Fig. 9 represent the first partition of the wall with a thickness equal to e . The thickness of central sub-partition is equal to $(e/2)$, the other sub-partitions have a thickness equal to $(e/4)$. At each sub-partition is attributed one node and the first partition can be therefore represented by three nodes (see Fig. 9).

The distribution of temperature in each partition is supposed to have a parabolic form as follows:

$$T(x) = \alpha_1(x)T_1 + \alpha_2(x)T_2 + \alpha_3(x)T_3 \quad (10)$$

The temporal derivative of Eq. (10) can be written:

$$\dot{T}(x) = \alpha_1(x)\dot{T}_1 + \alpha_2(x)\dot{T}_2 + \alpha_3(x)\dot{T}_3 \quad (11)$$

where T_1 , T_2 , T_3 are the nodal temperatures in points 1, 2 and 3, respectively and $\alpha_1(x)$, $\alpha_2(x)$ and $\alpha_3(x)$ are the interpolation functions which are given by:

$$\begin{aligned} \alpha_1(x) &= x \left(x - \frac{e}{2} \right) \times \frac{2}{e^2}, \\ \alpha_2(x) &= \left(x - \frac{e}{2} \right) \left(x + \frac{e}{2} \right) \times \left(-\frac{4}{e^2} \right), \\ \alpha_3(x) &= x \left(x + \frac{e}{2} \right) \times \frac{2}{e^2} \end{aligned} \quad (12)$$

3.1.1.1. Energy balance for the sub-partition (1). The energy balance of the sub-partition (1) can be written:

$$\int_{-e/2}^{-e/4} (\rho \cdot c_1 \cdot \dot{T}) dx = q_{(furnace-1)} + \lambda \frac{\partial T}{\partial x} \Big|_{x=-e/4} \quad (13)$$

Using Eq. (11) allows one to write the left term of Eq. (13) as follows:

$$\int_{-e/2}^{-e/4} (\rho \cdot c_1 \cdot \dot{T}) dx = \rho \cdot c_1 \cdot (\dot{T}_1 \cdot a_{11} + \dot{T}_2 \cdot a_{12} + \dot{T}_3 \cdot a_{13}) \quad (14)$$

where $a_{11} = \frac{e}{6}$, $a_{12} = \frac{5}{48}e$ and $a_{13} = -\frac{1}{48}e$. The other terms of Eq. (13) are defined:

$$q_{ra} = e_1 \sigma (T_{furnace}^4 - T_1^4) \quad (15)$$

where e_1 is the emissivity coefficient between the furnace and the node (1), σ is the Stephan Boltzman constant ($\sigma = 5.67 \times 10^{-8}$), $T_{furnace}$ and T_1 are the temperature of the furnace and at node (1), respectively.

$$q_{conv} = h_1 (T_{furnace} - T_1) \quad (16)$$

where h_1 is the convection coefficient between the furnace and the node (1).

$$\frac{\partial T}{\partial x} \Big|_{x=-e/4} = T_1 c_{11} + T_2 c_{12} + T_3 c_{13} \quad (17)$$

where $c_{11} = \frac{\partial \alpha_1}{\partial x} \Big|_{x=-e/4}$, $c_{12} = \frac{\partial \alpha_2}{\partial x} \Big|_{x=-e/4}$ and $c_{13} = \frac{\partial \alpha_3}{\partial x} \Big|_{x=-e/4}$.

The final form of the energy balance for the sub-partition (1) can be then written:

$$\begin{aligned} \dot{T}_1 \cdot a_{11} + \dot{T}_2 \cdot a_{12} + \dot{T}_3 \cdot a_{13} \\ = \frac{1}{\rho \cdot c_1} [h_1 (T_{furnace} - T_1) + \sigma (T_{furnace}^4 - T_1^4) \\ + \lambda (T_1 c_{11} + T_2 c_{12} + T_3 c_{13})] \end{aligned} \quad (18)$$

where λ is the conduction coefficient.

3.1.1.2. Energy balance for the sub-partition (2). The energy balance for the sub-partition (2) can be written:

$$\int_{-e/4}^{e/4} (\rho \cdot c_2 \cdot \dot{T}) dx = -\lambda \frac{\partial T}{\partial x} \Big|_{x=-e/4} + \lambda \frac{\partial T}{\partial x} \Big|_{x=e/4} \quad (19)$$

Similarly to the development done for sub-partition (1) Eq. (19) becomes:

$$\begin{aligned} \dot{T}_1 \cdot a_{21} + \dot{T}_2 \cdot a_{22} + \dot{T}_3 \cdot a_{23} \\ = \frac{1}{\rho \cdot c_2} [-\lambda (T_1 c_{21} + T_2 c_{22} + T_3 c_{23}) \\ + \lambda (T_1 c_{21} + T_2 c_{22} + T_3 c_{23})] \end{aligned} \quad (20)$$

where $a_{21} = \frac{1}{48}e$, $a_{22} = \frac{11}{24}e$, $a_{23} = \frac{1}{48}e$.

3.1.1.3. Energy balance for sub-partition (3). The energy balance of this sub-partition can be written:

$$\int_{e/4}^{e/2} (\rho \cdot c \cdot \dot{T}) dx = q_{ra} + q_{conv} + \lambda \frac{\partial T}{\partial x} \Big|_{x=e/4} \quad (21)$$

$$\text{where } q_{ra} = e_2 \sigma (T_3^4 - T_4^4) \quad \text{and} \quad q_{conv} = -h_2 (T_3 - T_4) \quad (22)$$

with e_2 and h_2 are the emissivity and convection coefficients, respectively, and T_4 is the temperature on point (4) defined in Fig. 9. Similarly to the development done for the sub-partitions (1) and (2), the energy balance for the sub-partition (3) can be written as follows:

$$\begin{aligned} \dot{T}_1 \cdot a_{31} + \dot{T}_2 \cdot a_{32} + \dot{T}_3 \cdot a_{33} \\ = \frac{1}{\rho \cdot c_3} [-h_2 (T_3 - T_4) - \sigma (T_3^4 - T_4^4) \\ - \lambda (T_1 c_{31} + T_2 c_{32} + T_3 c_{33})] \end{aligned} \quad (23)$$

where $a_{31} = -\frac{1}{48}e$, $a_{32} = \frac{5}{48}e$, $a_{33} = \frac{1}{6}e$.

Finally the energy balance for partition (1) can be written under the matrix form below:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \times \begin{bmatrix} \dot{T}_1 \\ \dot{T}_2 \\ \dot{T}_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} \quad (24)$$

where

$$[a_{ij}] = \begin{bmatrix} 1/6 & 5/48 & -1/48 \\ 1/48 & 11/24 & 1/48 \\ -1/48 & 5/48 & 1/6 \end{bmatrix} \times e$$

and

$$b_1 = \frac{h_1(T_{\text{furnace}} - T_1) + \sigma(T_{\text{furnace}}^4 - T_1^4) + \lambda(T_1 c_{11} + T_2 c_{12} + T_3 c_{13})}{\rho \cdot c_1}$$

$$b_2 = \frac{\lambda(T_1 c_{21} + T_2 c_{22} + T_3 c_{23}) - \lambda(T_1 c_{11} + T_2 c_{12} + T_3 c_{13})}{\rho \cdot c_2}$$

$$b_3 = \frac{-h_2(T_3 - T_4) - \sigma(T_3^4 - T_4^4) - \lambda(T_1 c_{21} + T_2 c_{22} + T_3 c_{23})}{\rho \cdot c_3}$$

or

$$\begin{bmatrix} \dot{T}_1 \\ \dot{T}_2 \\ \dot{T}_3 \end{bmatrix} = [a_{ij}]^{-1} \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} \quad (25)$$

The development of calculation of the energy balance for the second Section A.1 and third Section A.2 partitions is given in the appendix.

3.2. Coupled model equations

The resulting Eqs. (24), (26) and (28) (given in the appendix) can be written under the following matrix form:

$$\begin{bmatrix} \dot{T}_1 & \dot{T}_2 & \dot{T}_3 & \dot{T}_4 & \dot{T}_5 & \dot{T}_6 & \dot{T}_7 & \dot{T}_8 & \dot{T}_9 \end{bmatrix}^T$$

$$= \begin{bmatrix} [a_{ij}]^{-1} & 0 & 0 \\ 0 & [a_{ij}]^{-1} & 0 \\ 0 & 0 & [a_{ij}]^{-1} \end{bmatrix}$$

$$\times [b_1 \ b_2 \ b_3 \ b_4 \ b_5 \ b_6 \ b_7 \ b_8 \ b_9]^T \quad (30)$$

4. Results and discussion

The physical parameters of the material used in the thermal model are reported in Table 1. The equivalent specific heat given by Eq. (8) has the value of $C_{\text{eq}} = 4954$ (J/kg °C). The convection and emissivity coefficients corresponding to

Table 1
Values of different physical parameters used within the model

Given parameter	Value	Unit
Thickness of the wall	0.017	m
Mass density of the material at dry state ρ_d	2000	kg/m ³
Latent heat of water vaporisation L	2.477×10^6	J/kg
Radiation coefficient σ	5.67×10^{-8}	–
Initial water content in the partitions w	2%	–
Specific heat of solid phase C	900	J/(kg K)
Initial temperature T_0	16	°C
Thermal conductivity of the material λ	2	W/(m °C)
Interval of temperature of phase change phenomenon	(100–5, 100 + 5)	–

Table 2
Values of convection and emissivity coefficients in each partition, used within the model

Given parameter	Value	Unit
Convection coefficients of different partitions	h_1	20
	h_2	15
	h_3	15
	h_4	14
Emissivity coefficients of different partitions	ε_1	0.02
	ε_2	0.06
	ε_3	0.07
	ε_4	0.04

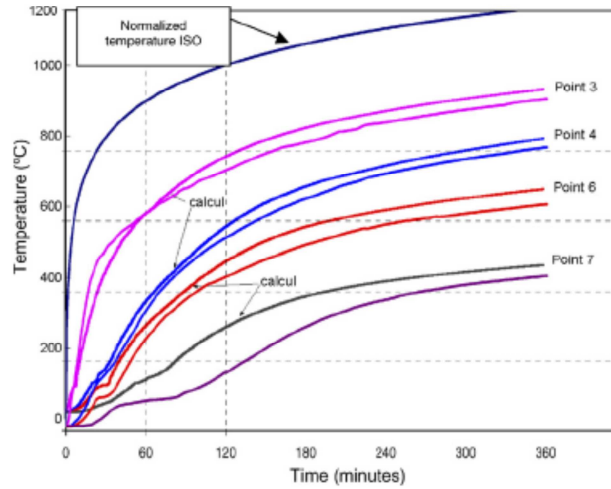


Fig. 10. Evolution of temperature through the wall as function of time. Comparison between experimental and theoretical predictions using thermal model.

the boundary conditions for the three partitions are reported in Table 2.

Fig. 10 allows the comparison between the experimental results (obtained by temperature measurement during the heating of masonry wall) with the theoretical curves simulated using the formulation previously described (Eq. (30)).

It can be seen that the theoretical model estimates correctly the temperatures at nodes (4) and (6) as defined in Fig. 9 corresponding to measurement points (2) and (3) defined in Fig. 4b. It can be seen that the plateau of phase-change phenomenon at these points is also reproduced correctly. Concerning the node (7), (defined in Fig. 9 and corresponding to measurement point (4) in Fig. 4b), the model over-estimates by 35% the temperature, compared to that measured experimentally between 60 and 240 min. This is probably due to the vapor re-condensation in the third partition which is not taken into account in this model. On the other hand, the model under-estimates by 4.5% the temperature in node (3) (defined in Fig. 9 and corresponding to measurement point (1) in Fig. 4b) between 0 and 100 min. This difference is probably due to the fact that the convection coefficient is supposed constant in the present model. In fact, the convection coefficient depends strongly on the temperature [10].

5. Conclusion

In the present study the experimental methodology used to characterize the thermo-mechanical behaviour of a masonry wall subjected to high temperature (until 1200 °C) has been shown. A vertical furnace has been used to apply this temperature with respect to the normalized ISO curve. The evolution of temperature inside the wall at different positions has been measured using thermocouples. During heating, the vertical and the lateral displacements of the wall were measured using LVDT transducers. The maximal values registered for the vertical and lateral displacements were almost 25 and 45 mm, respectively. The experimental results highlighted the phase-change effect, which appears under a form of plateau on temperature and displacements curves. A thermal model has been developed to take into account the different phenomena observed during the experiments. This model is based on continuous heat transfer by convection, radiation and conduction through the different sections of the wall. An enthalpic method is used to incorporate the energy absorption by liquid water evaporation under a form of equivalent specific heat around the temperature of ebullition of interstitial water (100 °C). This model gave results that showed reasonable agreement with those obtained experimentally.

Acknowledgements

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Appendix A

A.1. Energy balance for the second partition

Similarly to the development done in the partition (1) (see Section 3.1.1), the energy balance for the partition (2) can be written:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \times \begin{bmatrix} \dot{T}_4 \\ \dot{T}_5 \\ \dot{T}_6 \end{bmatrix} = \begin{bmatrix} b_4 \\ b_5 \\ b_6 \end{bmatrix} \quad (26)$$

where

$$\begin{aligned} b_4 &= [h_2(T_3 - T_4) + \sigma(T_3^4 - T_4^4) \\ &\quad + \lambda(T_4c_{11} + T_5c_{12} + T_6c_{13})]/\rho \cdot c_4 \\ b_5 &= [\lambda(T_4c_{21} + T_5c_{22} + T_6c_{23}) \\ &\quad - \lambda(T_4c_{11} + T_5c_{12} + T_6c_{13})]/\rho \cdot c_5 \\ b_6 &= [-h_3(T_6 - T_7) - \sigma(T_6^4 - T_7^4) \\ &\quad - \lambda(T_4c_{21} + T_5c_{22} + T_6c_{23})]/\rho \cdot c_6 \end{aligned}$$

Eq. (26) can be written as follows:

$$\begin{bmatrix} \dot{T}_4 \\ \dot{T}_5 \\ \dot{T}_6 \end{bmatrix} = [a_{ij}]^{-1} \begin{bmatrix} b_4 \\ b_5 \\ b_6 \end{bmatrix} \quad (27)$$

A.2. Energy balance for the third partition

Similarly to the development done in the previous partitions, the energy balance for partition (3) can be written:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \times \begin{bmatrix} \dot{T}_7 \\ \dot{T}_8 \\ \dot{T}_9 \end{bmatrix} = \begin{bmatrix} b_7 \\ b_8 \\ b_9 \end{bmatrix} \quad (28)$$

where

$$\begin{aligned} b_7 &= [h_3(T_6 - T_7) + \sigma(T_6^4 - T_7^4) \\ &\quad + \lambda(T_7c_{11} + T_8c_{12} + T_9c_{13})]/\rho \cdot c_7 \\ b_8 &= [\lambda(T_7c_{21} + T_8c_{22} + T_9c_{23}) \\ &\quad - \lambda(T_7c_{11} + T_8c_{12} + T_9c_{13})]/\rho \cdot c_8 \\ b_9 &= [-h_4(T_9 - T_0) - \sigma(T_9^4 - T_0^4) \\ &\quad - \lambda(T_7c_{21} + T_8c_{22} + T_9c_{23})]/\rho \cdot c_9 \end{aligned}$$

Eq. (28) can be written as follows:

$$\begin{bmatrix} \dot{T}_7 \\ \dot{T}_8 \\ \dot{T}_9 \end{bmatrix} = [a_{ij}]^{-1} \begin{bmatrix} b_7 \\ b_8 \\ b_9 \end{bmatrix} \quad (29)$$

References

- [1] A.W. Hendry, F.M. Khalaf, *Masonry Wall Construction*, Spon Press, London, 2000.
- [2] CSTB, Arrêté du 3 août 1999 relatif à la résistance au feu des produits, éléments de construction et d'ouvrages. chapitre 1^{er}, *Journal Officiel de la république française*, 11 septembre, 1999, p. 13638.

- [3] A.W. Hendry, Masonry walls: materials and construction, *Construction and Building Materials* (2001) 323–330.
- [4] F. Al Nahhas, Comportement Thermo-Mécanique des Murs en Maçonnerie de Blocs Creux en Béton sous l'Action d'un Feu Conventionnel, Thèse de doctorat de l'Université de Marne La Vallée, (2004).
- [5] F. Al Nahhas, R. Ami Saada, P. Delmotte, G. Bonnet, Modélisation Thermo-hydrigue des milieux poreux soumis à de hautes températures, XXIIèmes Rencontres Universitaires de Génie Civil (AUGC 04), 3–4 Juin, 8p., Marne La Vallée, France, 2004.
- [6] Masonry 2007. Department of the Environment, London (1997).
- [7] K. Thomas, Masonry walls, Butterworth-Heinemann, Oxford, 1996.
- [8] A.M. Sowden, The Maintenance of Brick and Stone Masonry Structures, E. and F.N. Spon, London, 1990.
- [9] A.W. Hendry (Ed.), Reinforced and Pre-stressed Masonry Structures, Longman Scientific and Technical, Harlow, 1991.
- [10] Y. Bayazitoglu, M. Özisik Necati, Elements of Heat Transfer, McGraw-Hill, New York, 1988.
- [11] A. Nadjai, M. O'Garra, F.A. Ali, D. Laverty, A numerical model for the behaviour of masonry under elevated temperature, *Fire and Materials* 27 (2003) 163–182.
- [12] BS 5628, Code of Practice for Use of Masonry. Pt 1. Structural Use of Unreinforced Masonry, British Standards Institution, London, 1992.
- [13] CP 121, Code of Practice for Walling. Pt 1: Brick and Block Masonry, British Standards Institution, London, 1973.
- [14] Eurocode No. 6, Design of Masonry Structures. Pt 10: Structural Fire Design, Commission of European Communities, Brussels, 1990.
- [15] Building Regulations. Technical Booklet E. Fire Safety. Department of the Environment for Northern Ireland, June, 1994.
- [16] N. Gnanakrishnan, R. Lawther, Some aspects of the fire performance of single leaf masonry construction. 2 International Symposium on Fire Engineering for Building Structures and Safety, Melbourne, 89/16, The Institution of Engineers, Australia, 1989, pp. 93–99.
- [17] F. Al Nahhas, R. Ami Saada, G. Bonnet, P. Delmotte, Heat and mass transfer coupling in porous media under high temperatures: modelisation and parametric study, *Computer Methods in Applied Mechanics and Engineering*, Submitted for publication.
- [18] C.R. Cruz, M. Gillen, Thermal expansion of Portland cement, mortar and concrete at high temperatures, *Fire and Materials* 4 (1980).