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# Numerical study of the linear polarization resistance technique applied to reinforced concrete for corrosion assessment

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**RÉSUMÉ.** La technique de résistance de polarisation linéaire  $(R_p)$  est utilisée de plus en plus fréquemment pour évaluer la cinétique de corrosion des aciers dans le béton armé. Cependant, la technique souffre d'un manque de fiabilité. Afin de mieux appréhender la physique de la mesure, des simulations numériques ont été réalisées. Plusieurs dispositifs ont été simulés. Ces expériences numériques ont permis d'éprouver la robustesse du protocole RILEM dédié à la mesure de  $R_p$  in situ. Les résultats montrent que les mesures réalisées au moyen de sondes annulaires constituent un problème physique tridimensionnel qui doit être mieux pris en compte par le protocole RILEM. En particulier, la distribution non uniforme du courant polarisant constitue une source d'erreur importante dans la mesure où elle n'est pas considérée dans la recommandation RILEM. Enfin, les simulations ont révélé une forme de complexité supplémentaire induite par l'utilisation d'anneaux de garde pour le confinement du courant polarisant.

ABSTRACT. The linear polarization resistance (LPR) technique is increasingly being implemented to assess the corrosion rate of steel reinforcements in concrete. However, a lack of reliability is often observed experimentally. In order to improve the physical comprehension of the LPR technique, FEM simulations were performed. Several measurement devices using annular and rectangular probe geometries were simulated and the numerical experimentation allowed the relevance of RILEM recommendations for on-site measurements to be tested. It was shown that the LPR measurement using annular counterelectrodes with confining devices was a real three-dimensional physical problem and the non-uniform distribution of the polarizing current on the steel surface is actually a major source of error since it is not taken into account by the usual protocols. Moreover, it was found that some complexity was induced by the use of guard-rings.

MOTS-CLÉS : Corrosion, béton armé, résistance de polarisation linéaire, mesures in situ, simulation numérique

**KEYWORDS:** Corrosion, steel reinforced concrete, linear polarization resistance, on-site measurement, numerical simulation

## 1. Introduction

Corrosion is the main source of damage in reinforced concrete structures. Therefore, it is crucial for service life prediction to be able to assess the corrosion rate of steel. The Linear Polarization Resistance (LPR) technique theoretically provides the corrosion current density, and thus the corrosion rate of steel, by measuring the polarization resistance ( $R_p$ ). According to several assumptions, the corrosion current density  $j_{corr}$  [A.m<sup>-2</sup>] and the polarization resistance  $R_p$  [ $\Omega$ .m<sup>2</sup>] are linked by the Stern-Geary relation (Stern et al., 1957):

$$j_{corr} = \frac{B}{R_n}$$
 [1]

Where B [V] is a factor defined below, which depends on anodic and cathodic Tafel slopes.

Although the LPR technique is now widely used, a large dispersion is observed in  $R_p$  determination. The French research project 'Benchmark des poutres de la Rance' used common commercial devices and laboratory devices to assess the corrosion rate of corroded beams (Poupard et al., 2005). Results showed differences of a factor often higher than 20 between the devices tested. This lack of reliability may be explained in various ways. First, the technique is often implemented beyond the theoretical limits. It should be used only in cases of uniform corrosion induced, for example, by concrete carbonation (Stern et al., 1957) (Gulikers, 2005) (Song, 2000). Moreover, the polarization should be limited (lower than 20 mV / Ecorr) in order to remain in the linear polarization range (RILEM, 2004) (Nygaard et al., 2009). The second main issue is that the  $R_p$  calculation usually assumes uniform current density distribution on a specific surface of the corroding rebar, and consequently uniform polarization. Actually, according to the physical geometry, there is no reason for current density distribution and polarization to be uniform. Furthermore, current distribution is highly influenced by environmental and geometrical factors.

The modeling of corrosion propagation in reinforced concrete has been a field of intensive research, so scientific literature can be found easily. The main theoretical considerations are reviewed in (Warkus et al., 2006a) (Raupach, 2006) and a sample of applications is given in (Gulikers et al., 2006) (Warkus et al., 2006) (Nasser et al., 2010). Comparatively, there has been little work published specifically on LPR simulations. Resistance networks are often implemented to simulate the measurement. Wojtas used a 2D network to study the ability of a guard-ring to confine the current along the rebar axis, and showed that it was not possible to obtain a reliable Rp value for the full range of corrosion current (Wojtas, 2004). In (Feliu et al., 1995), the current distribution is considered in the rebar cross-sectional plane. It proves not to be uniform and, in cases of active corrosion, can lead to an overestimation of current corrosion by between 10% and 30% depending on the geometry. Kranc and Sagües considered radial symmetry of the problem and simulated the measurement according to a transient method (Kranc et al., 1993).

They studied the effect of guard ring and counter-electrode size with respect to cover depth and the accuracy of the results for local or uniform corrosion. The study indicated that the measurement was successful only in cases of uniform corrosion with an electrode size larger than the cover depth. In order to take account of the effect on polarized length of some parameters influencing the measurement (such as concrete resistivity), Tang and Fu used a 2D FEM model of a new linear device and developed a specific formula to interpret the measurement (Tang et al., 2006). The combination of this new device with the formula gives results comparable to other commercial devices but much faster. A more complete study is reported in (Janusz, 1993) with a 2D and 3D FEM model in the steady state. Several parameters, such as corrosion intensity, probe dimensions, cover depth and concrete resistivity, were investigated by focusing on potential and current mapping. However, no major measurement improvements were proposed from the numerous simulations carried out.

Despite the simulation works presented above, some questions remain as to the quantitative effects of the factors that most influence LPR measurements. In this field, the research presented below aimed to perform FEM experiments to analyze the effects of probe geometry on the polarizing current distribution for a complete 3D model, and to quantify errors on  $R_p$  and  $j_{corr}$  measurements.

# 2. Theoretical background

# 2.1. Corrosion

Corrosion of steel in concrete creates anodic zones on the steel surface, where the steel is oxidized, and cathodic zones where dioxygen is reduced. In cases of local or macrocell corrosion (generally induced by chlorides), the anodes and cathodes are significant distances apart. If corrosion is caused by carbonation, the anodes and cathodes are infinitely close and their locations change randomly with time. This is referred to as microcell corrosion. In that case, anodic and cathodic potentials are equal to the corrosion potential  $E_{corr}$  and anodic and cathodic current densities are equivalent. The corresponding current density is the corrosion current density  $j_{corr}$ . A shift  $\Delta E$  from the equilibrium potential  $E_{corr}$  results in a current density  $\Delta j$ . The relation between  $\Delta E$  and  $\Delta j$  defines the polarization behavior and can be modeled by the Butler-Volmer nonlinear equation involving anodic and cathodic Tafel slopes ( $b_a$ and  $b_c$ , respectively, expressed in Volt per decade) (Stern et al., 1957) (Warkus et al., 2006b):

$$\Delta j = j_{corr} \left[ \exp \left( \frac{\ln(10)}{b_a} \Delta E \right) - \exp \left( -\frac{\ln(10)}{b_c} \Delta E \right) \right]$$
 [2]

Where ln(10) is referred to as the natural logarithm of 10 (= 2.303). This relation is valid only in cases of microcell corrosion and if the charge transfer controls the

reaction (no diffusion control is taken into account). It excludes very dense or saturated concrete, in which oxygen diffusion may be limited. The expression can be modified to encompass the latter cases (Warkus et al., 2006a), but it is not the purpose of this study.

Close to the corrosion potential, the first-order expansion of the Butler-Volmer equation leads to Eq.3, which defines the constant *B* presented in Eq.1:

$$\Delta j = j_{corr} \frac{\ln(10)(b_a + b_c)}{b_a b_c} \Delta E = \frac{j_{corr} \Delta E}{B}$$

The polarization resistance  $R_p$  is defined as the slope of the linear part of the polarization curve close to the corrosion potential  $E_{corr}$ :

$$R_{p} = \frac{\Delta E}{\Delta j}\Big|_{E=E_{corr}} = \frac{B}{j_{corr}} = \frac{1}{j_{corr}} \cdot \frac{b_{a}b_{c}}{\ln(10)(b_{a} + b_{c})}$$
 [4]

This relation provides the basic concept of  $R_p$  measurement. Either  $\Delta E$  is imposed and the response  $\Delta j$  is measured, or  $\Delta j$  is imposed and the response  $\Delta E$  is measured.

## 2.2. Measurement of the polarization resistance

The LPR measurement in reinforced concrete involves three electrodes:

- the counter-electrode (CE) applying a polarizing current, which is usually controlled according to the steel potential or current density,
- the working electrode (WE) which is the steel rebar to be analyzed,
- the reference electrode located on the concrete surface to monitor the response of the electrochemical system to the perturbation induced by CE.

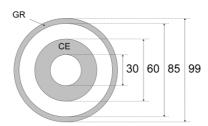
Several steady-state or transient techniques may be used to determine Rp. In the aim of controlling the steel surface polarized by the current injected through CE, some commercial devices use a complementary electrode referred to as a guard ring (GR). The purpose of the GR is to confine the polarizing current in a specific area. As mentioned above, comparative studies involving different devices have shown high dispersion in LPR measurements performed at the same points (Poupard et al., 2005) (Gepraegs et al., 2005) (Liu et al., 2003). Part of the dispersion may be explained by the sensitivity of the measurement to concrete resistivity and other environmental factors but some authors point out problems related to the confining device. Simulations using 2D resistance networks have shown that GR fails to confine the current over the full range of corrosion rates (Wojtas, 2004). Recently, the current distribution along the rebar was experimentally investigated for local corrosion (Nygaard et al., 2009). By focusing on the confinement techniques, it was shown that current injected from GR often compromised the measurement.

# 3. Modeling and simulation of LPR measurement

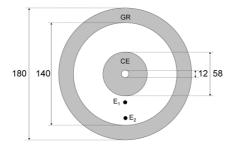
The purpose of this paper is to study the effects of probe geometry on  $R_p$  and  $j_{corr}$ measurement through FEM simulations. Only uniform corrosion and steady-state measurements were considered here to assess the three-dimensional distribution of polarizing and confining currents. Simulations were performed using the "DC conductive media" module of the commercial FEM code COMSOL Multiphysics®.

#### 3.1. Geometrical models

Three probe geometries were investigated: the two annular probes (including CE and GR) presented in Fig.1 and Fig.2 and one simple rectangular counter-electrode presented in Fig.3. The two annular probes had quite similar counter-electrodes but their guard-rings were of different sizes. The probe with the smaller GR is noted G<sub>1</sub> (Fig.1) and the probe with the larger GR is noted G<sub>2</sub> (Fig.2). A first simulation involving only the counter-electrode of G<sub>1</sub> was performed. This particular simulation case will be referred to as G<sub>1CE</sub>. For G<sub>2</sub>, GR current was controlled by means of two complementary reference electrodes E1 and E2 located between CE and GR. GR current was adjusted so as to achieve the same potentials E<sub>1</sub> and E<sub>2</sub>. It was possible to place the E<sub>1</sub>-E<sub>2</sub> axis either perpendicular or parallel to the rebar axis. Both configurations were simulated. The rectangular probe is noted G<sub>3</sub>.



**Figure 1.** Probe dimensions  $G_1$  (mm)



**Figure 2.** Probe Geometry  $G_2$  (mm)

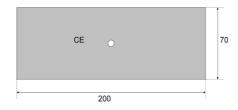
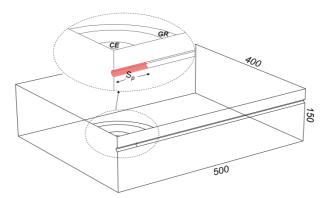


Figure 3. Probe dimensions G<sub>3</sub> (mm)

To simulate the LPR measurement, a 3D geometrical model was set up, corresponding to a concrete slab with a steel bar of 10 mm diameter embedded at a depth of 3 cm and an LPR probe located on the top surface. Fig.4 presents one of the three geometrical models involved in this study. Only a quarter of the geometry was needed for the computation thanks to problem symmetries.



**Figure 4.** Example of geometrical model involving G<sub>2</sub> (mm)

The numerical convergence was preliminary studied and achieved by refining progressively the meshing in order to make negligible current losses due to numerical approximations. It was checked by comparing integrated current densities injected in the specimen (by CE and GR) and the integrated current density on the entire rebar surface. Since the problem is conservative, all the injected current (CE+GR) has to be distributed on the rebar surface. This was achieved by mesh refinement, performed semi-automatically by the FEM code. The numbers of nodes and elements are presented in Table 1.

Probe geometry	$G_1$	$G_2$	$\mathrm{G}_3$
Elements	69696	75157	69787
Nodes	15298	16516	15392

Table 1. Mesh information

#### 3.2. Electrokinetics equations, boundary conditions and parameters

Concrete is assumed to be a homogeneous medium having a uniform electrical resistivity  $\rho$  [ $\Omega$ .m]. In the concrete volume, the equations governing electrical phenomena are Ohm's law (Eq.5), linking the local current density j [A.m<sup>-2</sup>] and the potential gradient  $\nabla \varphi$  [V.m<sup>-1</sup>], and charge conservation (Eq.6).

$$j = -\frac{1}{\rho} \nabla \varphi \qquad [5] \qquad \nabla \cdot j = 0 \qquad [6]$$

The steel-concrete boundary is modeled according to the Butler-Volmer equation (Eq.2) implemented in the code. Concerning CE and GR, different conditions were imposed depending on the geometry.

Regarding G<sub>1</sub>, GR and CE were set at the same potential (Dirichlet condition) to achieve confinement; this potential was fixed at 10 mV beyond  $E_{corr}$ . Regarding  $G_2$ , Neumann conditions were imposed at the locations of CE and GR to set the polarizing and confining currents respectively. The injected polarizing current I<sub>CE</sub> was chosen so as to achieve a polarization of about +10 mV at the center of CE and GR current was adjusted so that the potential difference between E<sub>1</sub> and E<sub>2</sub> was zero. Finally, the Dirichlet condition was imposed on the G<sub>3</sub> counter-electrode, corresponding to 10 mV beyond  $E_{corr}$ . The polarization value was chosen to ensure that the linearity range of the polarization curve was respected so that no effects other than the geometry influenced the measurement.

Other boundary conditions were modeled as an electrical insulation, which is equivalent to a Neumann condition where the normal current is set to zero. Table 2 summarizes all the simulation parameters.

Concrete resistivity $\rho$	Concrete cover	Corrosion rate $j_{corr}$	$E_{\it corr}$	Anodic Tafel slope $\boldsymbol{b}_{\boldsymbol{y}}$	Cathodic Tafel slope $\boldsymbol{b}_c$	<b>B</b> (mV)
200 Ωm	3 cm	1.5 μA/cm <sup>2</sup>	-707 mV/SHE	60 mV/dec	120 mV/dec	17.37

**Table 2.** Simulation parameters

## 4. Numerical results and discussion

#### 4.1. Conventions

Numerical experiments allowed us to work with 2 different values of LPR. The actual value, noted  $R_p$ , was defined according to Eq.4 and was computed exactly from simulation parameters. An apparent value of LPR, noted  $R_{pa}$ , was computed by applying the measurement protocol recommended for on-site devices (Eq.7). If the protocol is correct,  $R_{pa}$  and  $R_p$  should be similar.

$$R_{pa} = \frac{\Delta E}{\Delta i_a}$$
 [7 
$$\Delta i_a = \frac{I_{CE}}{S_p}$$
 [8]

In Eq.7,  $\Delta i_a$  is an average current density assuming the rebar to be uniformly polarized. It is calculated by dividing the current injected through the counter-electrode  $I_{CE}$  by  $S_p$  (Eq.8), which is the assumed steel polarized surface defined according to RILEM recommendations [5]. The polarization  $\Delta E$  involved in the calculation was taken on the steel surface under the center of the probe in order to avoid the effect of the ohmic drop caused by concrete resistivity and thus to focus the analysis exclusively on geometrical effects.

Finally, a local value of current density  $(\Delta i_l)$  was introduced, corresponding to the current density polarizing the point of the rebar where  $\Delta E$  was collected (under the center of the probe). It was directly provided by the numerical simulation that gave the current density actually polarizing each point of the rebar. If the current distribution on the steel surface under CE is uniform, then  $\Delta i_a$  and  $\Delta i_l$  should be similar.

#### 4.2. Current distribution

Figures 5 to 9 show current density streamlines resulting from each simulation case implemented in this study. The result in terms of current density streamlines of the first simulation  $G_{1CE}$  is shown in Fig.5. It can be observed that much of the injected current does not polarize the target zone  $S_p$  since many current lines spread out of this area. The numerical experiment allows the amount of current  $I_{Sp}$  actually collected by the target zone to be calculated quite exactly. It is computed by integrating local current densities acting on  $S_p$ . Table 3 presents a comparison between the injected current  $I_{CE}$  and the collected current  $I_{Sp}$ . Observations made on the streamlines are confirmed by the fact that only 33% of  $I_{CE}$  is collected on  $S_p$ .

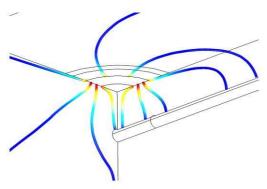


Figure 5. Current density streamlines :  $G_{1\text{CE}}$ 

When a guard ring is used (Fig.6), the current injected by CE appears more confined, especially in the rebar longitudinal plane. However, in the rebar transversal plane, some current lines from CE do not end on the target zone, indicating a slight under-confinement. Table 3 confirms this observation since 92 % of  $I_{CE}$  is collected on  $S_p$ .

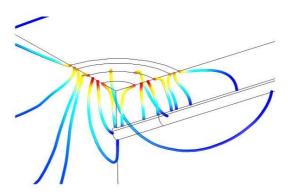


Figure 6. Current density streamlines : G<sub>1</sub>

Simulation case	Comment	<b>Ι</b> <sub>CF</sub> (μΑ)	<b>Ι</b> <sub>3σ</sub> (μΑ)	I <sub>M</sub> / I <sub>CE</sub> (%)
$G_{1CE}$	CE only	8.04	2.65	33
$G_1$	CE + GR	4.87	4.48	92
$\mathrm{G}_{2por}$	E <sub>1</sub> -E <sub>2</sub> axis parallel	4.88	6.64	136
$G_{a_{Der}}$	E <sub>1</sub> -E <sub>2</sub> axis perpendicular	4.88	4.68	96
$G_3$	Rectangular CE	19.28	10.96	57

**Table 3.** Current injected by CE and actually collected by the surface  $S_p$ 

For the probe  $G_2$ , two simulations were carried out according to the  $E_1$ - $E_2$  axis orientation. When the  $E_1$ - $E_2$  axis was parallel to the rebar axis (noted  $G_{2par}$ ), good confinement was observed in the rebar direction (Fig.7). As is often represented in the literature by two-dimensional illustrations, streamlines from CE extended approximately to the middle of the space between CE and GR. However, in the plane perpendicular to the rebar, some current lines from GR ended on  $S_p$ , resulting in over-confinement. The consequence was that the steel surface  $S_p$  considered for  $R_{pa}$  calculation collected more current than assumed, about 36% as indicated in table 3. In contrast, in the case where the  $E_1$ - $E_2$  axis was perpendicular to the rebar (noted  $G_{2per}$ ), a few current lines injected by CE were lost (Fig.8), meaning that the injected current was slightly under-confined (about 4 % as indicated in table 3).

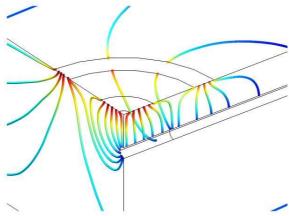


Figure 7. Current density streamlines :  $G_{2par}$ 

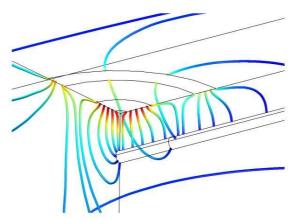


Figure 8. Current density streamlines: G<sub>2per</sub>

Therefore, a first conclusion can be drawn here about the significance of E<sub>1</sub>-E<sub>2</sub> positioning regarding the effectiveness of the confining device. Moreover, the global confinements achieved for cases G<sub>1</sub> and G<sub>2per</sub> were similar, 92 % and 96 % respectively. These values express slight under-confinements and could be considered as satisfactory, but the developments below will show that this condition is actually not sufficient.

The use of annular probes to assess the corrosion rate of linear steel bars leads to complex three-dimensional effects in the current density distribution. Fig. 9 shows the current distribution related to probe G<sub>3</sub>, which was simply rectangular. Since there was no confinement device, some current density streamlines naturally spread all over the concrete volume. Table 3 shows that only 57 % of the injected current was collected by the steel located under the probe. However, a greater longitudinal uniformity can be observed in the current streamlines starting from the central part of the probe, expressing a simpler current distribution compared to annular probes.

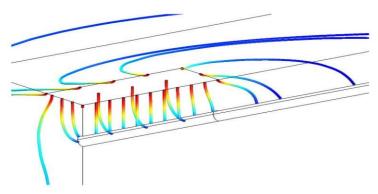


Figure 9. Current density streamlines: G3

Table 4 summarizes  $R_{pa}$  and  $j_{corr}$  (=  $B / R_{pa}$ ) values deduced from each simulated probe by applying the recommended protocol and the true  $R_p$  (1.16 ohm.m<sup>2</sup>) and  $j_{corr}$ (1.5 µA/cm<sup>2</sup>) values, which were kept for each simulation case. The table also presents the local current density  $\Delta i_l$  actually polarizing the point where the potential shift  $\Delta E$  is considered (top of the rebar under the centre of the probe) for each case and the average current density  $\Delta i_a$  resulting from the application of RILEM recommendations.

As expected, the average current density  $\Delta i_a$  was systematically different from the local current density  $\Delta i_l$ , due to the real three-dimensional nature of the physical problem. This resulted in a systematic mis-estimation of  $R_p$  since the local current corresponding to the shift  $\Delta E$  was not well approximated by the average current. Moreover, it was observed that the satisfactory global confinements achieved for G<sub>1</sub> and  $G_{2per}$  were not sufficient to correctly assess the value of  $R_p$  since the recommended protocol does not take the three-dimensional distribution of the polarizing current into account. This was particularly demonstrated by the fact that,

although the best confinement was achieved for  $G_{2per}$  (96 % versus 92 % for  $G_1$ ), the best estimation of  $R_p$  was obtained for the  $G_1$  configuration, only because of geometrical effects. The  $G_1$  simulation case provided an  $R_p$  value that was overestimated by +21 %, while  $R_p$  was overestimated by +32 % according to the  $G_{2per}$  configuration. Moreover, it is interesting to note that the  $G_3$  simulation resulted in an underestimation (-26 %), which was in the same error range as  $G_1$  and  $G_{2per}$ , whereas no confinement system was used. Regarding the  $G_2$  geometry, the significance of  $E_1$ - $E_2$  axis positioning was also highlighted for  $R_p$  estimation since, due to the strong over-confinement of 36 %, the  $G_{2par}$  simulation resulted in an overestimation of  $R_p$  by +71 % compared to +32 % for  $G_{2per}$ .

	$G_{\text{1CE}}$	$G_1$	$\mathrm{G}_{\scriptscriptstyle{2\mathrm{per}}}$	${\rm G_{2per}}$	$\mathrm{G}_{\scriptscriptstyle 3}$
$\Delta I_{I}(\mu A/cm^{2})$	0.22	0.26	0.27	0.21	0.23
Δ , (μA/cm²)	0.43	0.21	0.16	0.16	0.31
$R_{\infty}$ (ohm.m <sup>2</sup> )	0.57	1.40	1.98	1.53	0.85
$R_{p}$ (ohm.m <sup>2</sup> )			1.16		
Error on $R_p$ estimation (%)	-51	+ 21	+ 71	+ 32	-26
Estimated $j_{corr}(\mu A/cm^2)$	3.05	1.24	0.88	1.14	2.04
Actual value of $j_{corr}$ ( $\mu$ A/cm <sup>2</sup> )			1.5		
Error on $j_{corr}$ estimation (%)	+ 103.2	-17.3	-41.5	-24.3	+ 36.2

**Table 4.**  $R_p$  and  $j_{corr}$  estimations and errors

In terms of corrosion rate assessment, table 4 also shows  $j_{corr}$  estimations deduced from  $R_{pa}$  and B (17.37 mV) values according to Eq.1. The best estimate was achieved by the  $G_1$  configuration and actually corresponded to a significant underestimation of  $j_{corr}$  (about -17 %). Moreover, it can be observed that the  $G_{2per}$  configuration provided a better estimation of the corrosion rate than the  $G_3$  configuration whereas the relative error on  $R_p$  estimation was smaller for  $G_3$ . This result was simply due to the mathematical form of Eq.1, which gave stronger influence to  $R_p$  negative errors than to  $R_p$  positive errors. For example, it can be seen that, despite a strong over-estimation of  $R_p$  by +71 %, the  $G_{2par}$  configuration gave smaller errors on the  $j_{corr}$  estimation (about -41 %).

The simulation results show that, even in very favorable conditions (no ohmic drop effects, homogeneous materials, etc.), the recommended protocol for on-site LPR measurement failed to precisely assess the corrosion rate. This was mainly due to the actual non-uniform distribution of the polarizing current in both longitudinal

and orthoradial rebar directions, which is not considered by the usual protocols. Fig.10 presents the longitudinal distribution of the polarizing current density computed on the top of the rebar for the different configurations simulated. The dashed line symbolizes the average current  $(\Delta i_a)$  assumed to polarize the steel rebar uniformly according to RILEM recommendations.

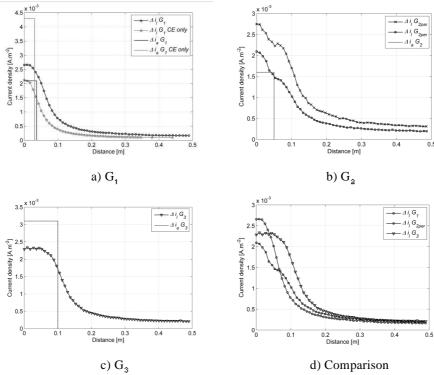
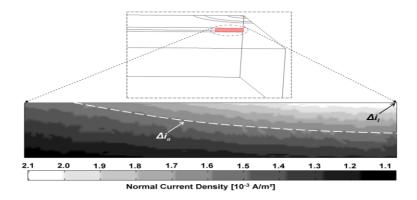


Figure 10. Longitudinal distribution of the current density polarizing the top of the

It can be observed for all the configurations that current density is maximal under the center of the probe and decreases strongly along the rebar axis, except for G<sub>3</sub> where some longitudinal uniformity is observed around the center of the probe as mentioned regarding Fig.9. In cases of high under-confinement (G<sub>1CE</sub>, G<sub>3</sub>), the average current density is significantly higher than the local value of polarizing current density under the center of the probe  $(\Delta i_l)$ . However, in cases of slight global under-confinement (G<sub>1</sub> and G<sub>2per</sub>), the local value of the polarizing current is still higher than the average current due to the non-uniform distribution. This result shows that global under-confinement may be partially compensated by the nonuniform distribution of the polarizing current density. On the other hand, the nonuniform distribution may enhance over-confinement effects (G<sub>2par</sub>).

Fig.11 was drawn to help the comprehension of the three-dimensional distribution of the polarizing current resulting from the numerical experimentation. The representation is limited to the extension of the polarized surface  $S_p$  involved in the calculation of the apparent polarization resistance  $R_{pa}$ . It can be clearly seen that the polarizing current distribution is not uniform in the longitudinal direction, nor in the orthoradial direction. Under the center of CE, the current density is about 0.21  $\mu$ A.cm<sup>-2</sup> at the top of the rebar while it is about 0.13  $\mu$ A.cm<sup>-2</sup> at the bottom, showing that the polarization is much greater on the top of the rebar. The white dotted line links the points where the current density equals the average current density  $\Delta i_a$ . It clearly shows that the current density  $(\Delta i_a)$  involved in  $R_p$  estimation is actually not the current density  $(\Delta i_l)$  polarizing the point of the rebar where the potential response is collected, i.e. under the center of the probe.



**Figure 11.** Distribution of the polarizing current density on  $S_p$  for G2per

# 5. Conclusion

The Linear Polarization Resistance (LPR) technique is being more and more frequently used to assess the corrosion rate of steel reinforcements in concrete. To explain the lack of reliability that is often observed experimentally, numerical simulations were performed in order to improve the physical comprehension of the LPR technique. Several measurement devices using annular and rectangular probe geometries were simulated and the numerical experimentation allowed the relevance of RILEM recommendations to be tested for on-site measurements. Interesting conclusions were drawn based on these numerical experiments.

By drawing polarizing and confining current density streamlines resulting from the simulations, it was shown that the LPR measurement using annular counter-electrodes with confining devices was a real three-dimensional physical problem. Moreover, it was found that some complexity was induced by the use of guard-rings. For example, if complementary reference electrodes (E<sub>1</sub> and E<sub>2</sub>) were used to control the confining current, unexpected effects were observed regarding their positioning

with respect to rebar axis. An optimal configuration was found by positioning the E<sub>1</sub>-E<sub>2</sub> axis perpendicular to the rebar axis, providing a slight global under-confinement. If the E<sub>1</sub>-E<sub>2</sub> axis was positioned parallel to the rebar axis, strong over-confinement

However, although the confining devices succeeded in limiting global current spreading in some geometrical configurations, the distribution of the polarizing current density at the steel surface was clearly not uniform in either the longitudinal or the orthoradial direction. The major consequence is that the assumption of an average current density uniformly polarizing the steel surface is not relevant, and the calculated LPR, deduced from this assumed current density, is wrong. Regarding the optimal configuration highlighted in this numerical study, although the global confinement was almost perfect, the polarization resistance, assessed according to RILEM recommendations, was still overestimated by more than 20 % and the corrosion rate was underestimated by about 17 %. This error generated by applying RILEM recommendations was due to the existence of a local maximum of the polarizing current distribution which was not taken into account by the protocol. This local current maximum effect compensates the under-confinement and enhances the over-confinement. To improve the RILEM protocol, efforts should be made towards a better estimation of the current density which actually polarizes the point of the rebar where the potential response is collected.

These results also raise some questions about the relevance of the annular geometry of the probes usually used for on-site LPR measurement. For example, the rectangular counter-electrode experimented in this numerical study presented a more uniform current distribution along the rebar axis, indicating a probably easier interpretation although there was no confinement device. Lastly, to emphasize the true difficulty of real on-site LPR measurements, it has to be recalled that these results, highlighting some theoretical limits of the usual protocol, were achieved from numerical simulations carried out in very favorable conditions: stationary measurement, no ohmic drop, uniform corrosion, homogeneous materials, etc. This study focused on geometrical effects but complementary research is currently being conducted to understand the effects of the various other influential factors and thus to improve measurement protocols.

# 4. References

- Feliu S., González J.A., Andrade C., « Effect of Current Distribution on Corrosion Rate Measurements in Reinforced Concrete », Corrosion, vol. 51, n° 1, 1995, p. 79-86
- Gepraegs O.K., Hansson C.M., « A comparative evaluation of three commercial instruments for field measurements of reinforcing steel corrosion rates », Journal of ASTM International, vol. 2, n° 8, 2005, p. 1-16.
- Gulikers J., « Theoretical considerations on the supposed linear relationship between concrete resistivity and corrosion rate of steel reinforcement », Materials and Corrosion, vol. 56, n° 6, 2005, p. 393-403.

- Gulikers J., Raupach M., « Numerical models for the propagation period of reinforcement corrosion Comparison of a case study calculated by different researchers », *Materials and Corrosion*, vol. 57, n° 8, 2006, p. 618-627.
- Janusz F., in: Condition evaluation of concrete bridges relative to reinforcement corrosion -Vol.2: Method for measuring the corrosion rate of reinforcing steel, Strategic Highway Research Program, Washington DC, 1993.
- Kranc S.C., Sagües A.A., « Polarization current distribution and electrochemical impedance response of reinforced concrete when using guard ring electrodes », *Electrochimica Acta*, vol. 38, n° 14, 1993, p. 2055-2061.
- Liu Y., Weyers R.E., «Comparison of guarded and unguarded linear polarization CCD devices with weight loss measurements », *Cement and concrete research*, vol. 33, n° 7, 2003, p. 1093-1101.
- Nasser A., Clément A., Laurens S., Castel A., «Influence of steel-concrete interface condition on galvanic corrosion currents in carbonated concrete », *Corrosion Science*, vol. 52, n° 9, 2010, p. 2878-2890.
- Nygaard P.V., Geiker M.R., Elsener B., «Corrosion rate of steel in concrete: evaluation of confinement techniques for on-site corrosion rate measurements », *Materials and Structures*, vol. 42, n° 8, 2009, p. 1059-1076.
- Poupard O., L'Hostis V., Laurens S., Catinaud S., Petre-Lazar I., « Benchmark des Poutres de la Rance": Damage diagnosis of reinforced concrete beams after 40 years exposure in marine environment by non destructive tools », *Proceedings of the EUROCORR 2005 conference*, Lisbon, 4-8 September, 2005.
- Raupach M., « Models for the propagation phase of reinforcement corrosion an overview », *Materials and Corrosion*, vol. 57, n° 8, 2006, p. 605-613.
- RILEM Technical Committee 154 EMC (Andrade C., Alonso C., Gulikers J., Polder R., Cigna R., Vennesland O., Salta M, Raharinaivo A., Elsener B.), «Test methods for onsite corrosion rate measurement of steel reinforcement in concrete by means of the polarization resistance method », *Materials and Structures*, vol. 37, n° 273, 2004, p. 623-643.
- Song G., « Theoretical analysis of the measurement of polarisation resistance in reinforced concrete », Cement and Concrete Composites, vol. 22, n°, 2000, p. 407-415.
- Stern M., Geary A.L., «Electrochemical polarization», *Journal of the electrochemical society*, vol. 104, n° 1, 1957, p. 56-63.
- Tang L., Fu Y., « A rapid technique using Handheld instrument for mapping corrosion of steel in reinforced concrete », *Restoration of Buildings and Monuments*, vol. 15, n° 5/6, 2006, p. 387-400.
- Warkus J., Raupach M. and Gulikers G., «Numerical modelling of corrosion Theoretical backgrounds », *Materials and Corrosion*, vol. 57,  $n^{\circ}$  8, 2006a, p. 614-617.
- Warkus J., Raupach M., « Modelling of reinforcement corrosion Corrosion with extensive cathodes », *Materials and Corrosion*, vol. 57, n° 12, 2006b, p. 920-925.

Wojtas H., « Determination of corrosion rate of reinforcement with a modulated guard ring electrode; analysis of errors due to lateral current distribution », Corrosion Science, vol. 46, n° 7, 2004, p. 1621-1632.