

# Modelling of compression and extension of the continental lithosphere: towards rehabilitation of the necking-level model

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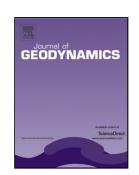
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5	MODELLING OF COMPRESSION AND EXTENSION OF THE CONTINENTAL
6	LITHOSPHERE: TOWARDS REHABILITATION OF THE NECKING-LEVEL MODEL
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23	isostasy.
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28	We present a dynamic model of continental lithosphere deformation under extension or
29	compression, focusing on the role of an effective mechanical parameter called "necking level"
30	or "necking depth", a widely used concept in basin modelling studies. Though it has generally
31	been assumed that "necking depth" depends strongly upon the rheological structure of the
32	lithosphere (especially the depth distribution of its strong layers), such a dependency has never
33	been demonstrated. Our model, which accommodates small deformations of a thin
34	inhomogeneous plate induced by in-plane as well as by mantle boundary forces (applied to the
35	model sides and base, respectively), shows that "necking depth" is a function of the horizontal
36	position and depends mainly on the relative thicknesses and strengths of the rigid layers in the
37	uppermost crust and below the Moho. Using different yield strength envelopes we
38	demonstrate that the final structure of the lithosphere formed as a result of deformation and its
39	consequent isostatic adjustment can be closely approximated by a model with a flat necking
40	level. In the process of extension and compression of the continental lithosphere all
41	boundaries, including the topographic surface and the Moho, deform. As a result, the total
42	disturbance of the isostatic equilibrium state (specified as a load) is only a part of the
43	topographic weight. Estimates of the correct load can be made using the depth to the necking
44	level inferred from lithosphere structure, composition and thermal state. The final topography
45	of lithospheric interfaces depends on both necking depth and effective flexural rigidity. Any
46	attempt to estimate simultaneously strain distribution, necking depth and effective flexural
47	rigidity, however, represents an ill-posed problem and is not possible without reliance upon
48	strong independent assumptions constraining lithosphere structure.

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#### 1. Introduction

	The topography of continents – both uplifted orogens and downwarped sedimentary basins
-	- results from a series of processes: tectonic deformations, erosion, sedimentation, isostatic
1	response of the lithosphere, etc. and, naturally, there is a long history of their quantitative
1	modelling. Numerical models typically incorporate complexities such as the rheological
(	effects of pressure, temperature and strain rate, compositional variations, inherited structures
í	and so forth. In such models the lithosphere is considered as a rheologically layered entity
,	with lateral heterogeneity [e.g. Mitrovica et al., 1989; Braun and Beaumont, 1989a; Bassi,
-	1991; Govers and Wortel, 1999 and many others]. These kinds of complex models have not
1	fully replaced simple kinematic ones postulating a relationship between horizontal shortening
(	or lengthening and the amplitude of vertical displacement of lithospheric boundaries [e.g.
İ	McKenzie, 1978; Weissel and Karner, 1989; Kooi et al., 1992; van der Beek et al., 1994;
,	Spadini et al., 1995; Cloetingh et al., 1995]. Indeed, although kinematic models often do not
l	have a fully appropriate physical background, they are still used in quantitative modelling
S	studies, for example in sedimentary basin analysis. These models are especially convenient
ł	because they permit formulation of effective algorithms for solving inverse problems, such as
1	reconstruction of the history of sedimentary basin formation using data on infill thickness, age
í	and lithology and on the structure of underlying crust. Using horizontally varying strain these
1	models are capable of reproducing complex tectonic structures forming in laterally
i	inhomogeneous lithosphere and compare well different geophysical and geological data.
	One of the earliest ways in which the lithosphere (or crust) was idealised in order to
f	facilitate modelling was a thin elastic plate. It was used for the first time by Vening Meinesz
[	[1931] and later by Gunn [1947] as a proxy for modelling the response to loading. This simple
1	model, reintroduced by Walcott (1970), is still widely in use today (e.g. Jordan and Watts,
2	2005; Leever et al., 2006; Pérez-Gussinyé et al., 2007). The key parameter characterising the

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rheology (or strength) of the lithosphere and, hence, its isostatic response to external loads is then the effective elastic thickness  $T_e$  (simply linked to the effective flexural rigidity of the plate). Of course,  $T_e$  is an "effective" parameter that serves as a proxy for what undoubtedly is a more complex lithospheric rheological structure. Several studies were made in which  $T_e$  was compared to how more complex, more realistic, numerical rheological models of lithosphere responded, in order to understand better the controls on T<sub>e</sub>. Burov and Diament [1995; 1996], for example, found that non-elastic effects and possible decoupling between layers in the lithosphere could play an important role in how a layered rheology was expressed as effective  $T_e$  value, especially in continental lithosphere. Thin elastic plate theory has provided a very successful way of modelling regional isostatic response, in which only vertical forces (surface load and buoyancy) are balanced, although sometimes horizontal (in-plane) forces have also been incorporated into the mechanical equilibrium equation [e.g. Cloetingh et al., 1985; Stephenson and Lambeck, 1985]. When dealing with active tectonic deformation in extensional or compressional processes, of course, the horizontal dynamics must be considered as well. Braun and Beaumont (1989b) found that the results of their numerical modelling, incorporating complex rheologies, could be interpreted as if extension occurred in two stages. The first stage included the deformation by external forces in the absence of isostatic rebound and the second one was the isostatic response of the lithosphere to that deformation. They hypothesized that within the lithosphere there exists a flat level that does not move vertically during the first stage. For this level they introduced the term "necking depth" – or  $z_n$ . Necking depth was suggested to depend on depth variations of lithospheric strength. Later, the necking depth was used as a mechanical parameter in numerous basin modelling studies (involving backstripping of sedimentary loads and forward modelling of thermal subsidence; cf. Cloetingh et al., 1995), in which  $z_n$  controlled the geometry of the rifted

100	lithosphere at the end of the active extensional period while $T_e$ controlled its response to
101	subsequent sedimentary and thermal loads.
102	Cloetingh et al. [1995] considered $z_n$ , like $T_e$ , to be a proxy for the actual, more complex,
103	rheology of the lithosphere and, accordingly, that insights into the rheology of the lithosphere
104	could be gained by looking at possible systematic relationships between $T_e$ and $z_n$ (given other
105	"known" parameters such as crustal and lithosphere thicknesses, heat flow, and tectonic age).
106	The results of this endeavour were somewhat ambiguous. On the basis of numerical
107	modelling, Govers and Wortel [1999] concluded that there is no one-to-one relationship
108	between depth to the necking level and strength distribution within the lithosphere.
109	However, the use of the necking level appeared to be successful for detailed analyses of the
110	structure and evolution of numerous sedimentary basins (for bibliography see Cloetingh et al.,
111	[1995]) and in explaining the formation of rift shoulders [e.g. Braun and Beaumont, 1989b
112	and many others]. Indeed, the necking-level model approximates well the numerical results
113	obtained adopting complex lithospheric rheologies [Mitrovica et al., 1989; Braun and
114	Beaumont, 1989a; Bassi, 1991; and others]. Accordingly, it is of interest to analyse further the
115	meaning of "necking level" in the context of more realistic lithospheric models, and to
116	investigate its possible relationship to other tectonic parameters such as crustal thickness, heat
117	flow or tectonic age, and, indeed, $T_e$ . Because of the inherent ambiguities in the complex
118	numerical approaches to this problem [cf. Govers and Wortel, 1999], we choose to apply an
119	analytical approach, reducing the number of free parameters and considering only several
120	archetypical yield strength envelopes [Ranalli and Murphy, 1987] characterizing different
121	lithospheric structures.
122	In the following part of the paper we focus on a dynamic description of continental
123	lithosphere deformation under extension or compression. We have adopted the two stage
124	scheme of Braun and Beaumont [1989b], mentioned above (deformation and consequent

isostatic rebound) and investigate the position of the level at which the first stage vertical displacement is equal to zero. Even though this level exists for both compressional and extensional deformations, we retain Braun and Beaumont's term "necking level" although they initially introduced it to describe extensional necking of the lithosphere only. We do simply this because the term is already well established in the geodynamics literature.

We present the general analysis of the problem and give an analytical solution for small deformations of a thin inhomogeneous elastic plate by forces applied to its side boundaries or to its bottom. This solution can be presented in the form of deformation around a necking surface  $z_n(x)$  which, in general, is not flat. In the last part of the paper we present and discuss some results of our numerical calculations and show that a model with a flat equivalent necking depth  $z_n = const$  provides a very close approximation to the exact solution after the isostatic adjustment stage. We then discuss which data are required to estimate the depth to the necking level and effective elastic rigidity of the lithosphere simultaneously.

#### 2. Kinematic necking-level model.

Let us now briefly recall the approach frequently used in modelling lithospheric deformation by intraplate forces [e.g. *Kooi et al.*, 1992; *van der Beek et al.*, 1994; *Spadini et al.*, 1995]. The lithosphere is assumed to be composed of one or several layers, such that: (a) U - the horizontal component of velocity or displacement vector within each layer does not depend upon the vertical coordinate z, and (b) the lithosphere deforms about some necking level  $z_n = const$ , which does not move vertically during intraplate deformation in the absence of isostatic rebound. In the particular case of one layered homogeneous lithosphere, the horizontal (U) and vertical (W) components of velocity or displacement vector are related by the equation:

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$$W(x,z,t) = -(z-z_n)\frac{\partial U(x,t)}{\partial x}$$
 (1)

(for the sake of simplicity, hereafter we consider only 2D problems with horizontal Ox axis and Oz axis directed upward). The deformation about the necking level is a first stage of the previously mentioned two-stage scheme. The second stage being the restoration of the isostatic balance which could have been disturbed during the first stage. It is implicitly assumed that the position of  $z_n$  depends upon the depth distribution of mechanical properties of the lithosphere, which in its turn is mostly determined by temperature profile and lithology [Ranalli and Murphy, 1987, Afonso and Ranalli, 2004]. Cloetingh et al. (1995) estimated  $z_n$  to vary from 4 to 35 km and made an attempt to relate its depth to the thermal age of the lithosphere, its thickness and strain rate at the stage of extension. Considering these results, Fernandez and Ranalli (1997) concluded that "the relationship between strength envelopes and kinematic level of necking is more complicated than previously thought". They classified the necking-level based model as a kinematic one with rheological constraints.

Moreover, kinematic considerations presented in Appendix A show that this relationship cannot be found by a purely kinematic approach and calls either for additional assumptions (for example, of local isostatic equilibrium giving a 2D analogue of the *McKenzie* [1978] model or the presence of a flat necking level, etc.) or for consideration of forces and strain-stress relationships, i.e. for a dynamic approach.

#### 3. Dynamic model.

#### 3.1 Statement of the problem

The rheology of the medium (i.e. the equations coupling the stress and the strain and/or strain rate tensors) must be assigned when constructing a dynamic model. The rheology of the lithosphere depends upon several factors including rock compositions, temperature, pressure,

stress distribution and magnitude, strain rate [e.g. Goetze and Evans, 1979; Ranalli and 173 Murphy, 1987; Kohlsted et al., 1995; Afonso and Ranalli, 2004]. In recent years, various yield 174 strength envelopes accounting for these factors were proposed. They mostly vary by the 175 assumption of what has been adopted as a constant: the strain rate [e.g. Ranalli and Murphy; 176 177 1987; Carter and Tsenn, 1987; Cloetingh & Banda, 1992], external forces [Kusznir, 1991] or some combination [Ershov and Stepheson, 2006]. Fig.1 shows five typical yield strength 178 envelopes for different thermal regime and lithospheric structure accounting for heat 179 generation in the upper crust and for a strain rate  $\dot{\varepsilon} = 10^{-14} \ s^{-1}$ . Following Turcotte and 180 the steady-state continental lithosphere isotherm is *Shubert* [2002] 181  $T(z) = T_s + q_m \cdot z/k + (1 - \exp(-z/h_r)) \cdot \rho$   $Q_{rad}h_r^2/k$ , where  $T_s$  is the surface temperature,  $\rho$ 182 is the average crustal density,  $Q_{rad}$  is the radioactive heat generation per rock mass unit at the 183 top of the crust, k is a thermal conductivity,  $q_m$  is heat flow at the base of the lithosphere,  $h_r$  -184 characterize the decrease of the radioactive heat generation with depth. For all envelopes, 185  $T_s = 270\,K$ ,  $k = 3.35\,W/m \cdot grad\,K$ ,  $\rho = 3 \cdot 10^3\,kg/m^3$ ,  $Q_{rad} = 8.8 \cdot 10^{-10}\,W/kg$ . For all the 186 models,  $h_r = 10 \text{ km}$ , except for the model «Hot» where  $h_r = 7.1 \text{ km}$ . Other parameters are given 187 in Table 1. Resulting strength envelopes «Shield», «Collisional» and «Hot» are close to 188 models S1, C1 and H1 of Ranalli and Murphy [1987] and «Normal» and «Alpine» are close to 189 those of Cloetingh et al [1995]. 190 To construct these envelopes, we used the linear Coulomb frictional law [Sibson, 1974] 191 which is mostly constrained by experimental data obtained for conditions corresponding to the 192 upper crust. For higher pressure and temperature it overestimates the strength of rocks [see 193 experimental data compiled in Ranalli and Murphy, 1987 and Kohlstedt et al., 1995]. To 194 account for this effect, we limited the strength of the upper mantle to 1 GPa. We use these 195

strength profiles to characterize the relative position and thickness of "rigid" and "compliant" layers within the different types of the lithosphere.

According to numerous geological and geophysical studies, discontinuities generally accommodate compression or extension of rigid layers, hence elastic or plastic deformations are comparatively small. However, when a rigid layer contains numerous discontinuities, an equivalent continuous medium can be used for a generalized description of the macroscale deformations, although the choice of the stress-strain relationships is still open. Below we use linear stress-strain relationships to investigate the problem of lithosphere extension - compression. For a Newtonian compressible stratified medium the problem can be investigated using the equations obtained in *Mikhailov et al.* [1996; 1999].

Simple constitutive laws have been successfully applied to model many geodynamic processes. An impressive collection of such results can be found, for example, in *Turcotte and Schubert* [2002]. In our case, a simple model permits investigation of the main characteristics, and their dependence on rheology, of extensional and compressional structures of the lithosphere. In particular, the topography of the necking surface in our model is close to that of *Govers and Wortel* [1999], which was found using a dynamic numerical modelling techniques and more realistic rheologies. Thus, the complex rheological behaviours, transient effects, and so on, incorporated in many numerical models can be considered to produce second order effects. Our results simply demonstrate the validity of the necking level model, which has indeed been successfully used for modelling many sedimentary basins [see *Cloetingh et al.*, 1995 for an overview].

#### 3.2 Effective elastic model.

Let us use a heterogeneous pure elastic model to consider relatively fast deformations of the lithosphere by intraplate forces. Such a model provides an analogue (effective) description

and it is used below to specify large scale irreversible deformations including sliding along
faults. The effective elastic models are widely used to describe deformation in non-elastic
media [e.g. Lomakin, 1976; Ranalli, 1994; Burov and Diament, 1995; 1996]. To investigate
the mechanical response to the loading due to extension or compression one may consider the
problem of isostatic equilibrium of a thin elastic plate floating on a non-viscous substratum
[Turcotte and Shubert, 2002]. Since deformations by intraplate forces are supposed to be
irreversible and non-elastic, they can be considered separately from the associated isostatic
response. As before, these processes will be referred as stage (a) and stage (b). For both
stages, the purely elastic model only provides an approximation of the real, more complicated,
processes, its parameters are effective and cannot be determined in laboratory (for stage (b)
this question was studied in detail by Burov and Diament [1995, 1996)]). Moreover,
parameters in problems (a) and (b) describe different physical mechanisms of deformation and
as a result have different values. Fortunately, as it is shown below, the solution of problem (a)
depends only on the relative distribution of the effective Young's modulus with depth and to
characterize the depths of compliant and rigid layers we used the yield stress envelopes (Fig.
1). In problem (b), the behaviour of the lithosphere can be specified by the flexural rigidity
estimated from a combined analysis of gravity and topography.
In our model inhomogeneous mechanical properties of the lithosphere have to be assigned
at the onset of deformation. Such inhomogeneity can be intrinsic (e.g. vertical rheological
stratification of the lithosphere) or formed after intraplate forces are applied, as a result of
faulting or rock damage. Subsequently, the mechanical properties of the lithosphere change
only as a result of material displacements; accordingly, all transient effects resulting, for
example, from time varying temperatures are ignored.
Let us first consider problem (a). We adopt the following notations: $E(x,z)$ - apparent
Young's modulus, $\nu$ - Poisson's ratio assumed to be equal to 0.5 in order to obtain formulas

246 similar to (1), U(x,z) and W(x,z) are the horizontal and vertical components of the displacement vector. For the sake of simplicity, we assume that at t = 0 the lithosphere was in 247 local isostatic equilibrium (equation A3 in Appendix A) and the initial topography of the top 248 of the lithosphere ( $z_{l0}$ ), the Moho ( $z_{Moho0}$ ) and the asthenosphere ( $z_{a0}$ ) were flat. 249 In Appendix B we solve the problem of a deformation of the lithosphere by intraplate forces 250 considering only small deformations of a thin plate. This implies that we have assumed (1) 251 that L - equal to the characteristic scale of variations of E(x,z) and U(x,z) along horizontal 252 axis Ox - is much larger than H- the characteristic scale of variations of E(x,z) and the 253 vertical component W(x,z) along vertical axis Oz (this yields a small parameter 254  $\varepsilon = H/L \ll 1$ ); and (2) that - magnitudes of displacements are also small, i.e. characteristic 255 scales for the horizontal and vertical components of displacements are of the order of 256  $u_0 = \varepsilon^2 L$ ,  $w_0 = \varepsilon^2 H$ . 257 We then proceed to use dimensionless values by introducing characteristic scales and 258 expand all components of displacement and stress in power series of the squared small 259 parameter ( $\varepsilon^2$ ). 260 Assuming further that the distribution of apparent Young's modulus can be presented 261 as  $E(x,z) = E_I(x)F_I(z)$  where  $F_I(z)$  is a non-dimensional function that can be associated 262 with the yield strength profile, we arrive at an analytical solution, which, in the first expansion 263 terms, is analogous to a 2D state of plane stress [e.g. Turcotte and Schubert, 2002, section 264 3.5). But to find the displacement fields and position of the necking surface, it is necessary to 265 analyse the equations for the second order terms that strongly depend on vertical stratification 266 of the model. 267 From the obtained equations, it follows that the first term of the expansion of the 268

horizontal component of displacement  $U_1$  does not depend on the vertical coordinate z, i.e.

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 $U_1 = U_1(x)$ . As a result, the vertical component of displacement is related to the horizontal strain through an unknown function  $f_1(x)$ , which can be presented in a form close to equation (1):

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$$W_1 = -z \frac{\partial U_1}{\partial x} + f_1(x) = -(z - z_n(x)) \frac{\partial U_1}{\partial x}, \qquad (2)$$

- where  $z_n(x)$  is the position of the necking surface.
- In Appendix B we obtain equation for  $z_n(x)$  by considering second order terms of the expansion (equation B9). To express this equation in a more useful form for our analysis, let us introduce the depth:

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$$d_{I}(x) = \int_{z_{a0}}^{z_{l0}} E(x,z) \cdot z dz / \int_{z_{a0}}^{z_{l0}} E(x,z) \cdot dz.$$
 (3)

By analogy with the centre of mass this depth can be identified as *the centre of rigidity* of every vertical section. Then, introducing n-th central moment  $(n \ge 2)$  in respect to the centre of rigidity as:

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$$c_n(x) = \int_{z_{a0}}^{z_{l0}} E(x,z) \cdot (z - d_I(x))^n dz / \int_{z_{a0}}^{z_{l0}} E(x,z) \cdot dz$$
 (4)

one transforms equation for the necking surface (B9) to the form:

$$c_2 \frac{\partial^2 (z_n - d_1)\varepsilon_{xI}}{\partial x^2} - \frac{c_3}{2} \frac{\partial^2 \varepsilon_{xI}}{\partial x^2} - \varepsilon_{xI}^2 (z_n - d_1) = 0.$$
 (5)

- where  $\varepsilon_{xI} = \frac{\partial U_I}{\partial x}$  is the main component of the strain in *x*-direction.
- During the first stage the model has to be somehow fixed relative to the vertical axis Oz by assigning an asymptotic value to  $z_n(x)$  at the model side boundaries or at  $x \to \pm \infty$ .

  The final result (after isostatic rebound) does not depend on this asymptotic value. Indeed, any

  shift of the asymptote only produces an additional constant in the total perturbation of the

290	initial isostatic balance (see below); thus, during the isostatic adjustment stage the lithosphere
291	will return to the same place independent of its flexural rigidity. We place the asymptotic
292	value at the centre of rigidity $d_I$ whose depth is different for different yield strength envelopes
293	used in this study.
294	From equation (5) it follows that in the general case when $\varepsilon_{xl} \neq const$ , the necking surface
295	$z_n(x)$ is not flat. Furthermore, this equation is non-linear relative to $z_n(x)$ ; thus, when
296	approaching the final solution, corresponding to some $\varepsilon_{xl}(x)$ after two steps (i.e. deforming
297	first to $\varepsilon_{xl}(x)/2$ and then to the same value again) one finds that $z_n(x)$ is different at the
298	first and the second steps. All this is in good agreement with the results of the numerical
299	modelling of Govers and Wortel [1999]. Note that, in the particular case of a horizontally
300	homogeneous plate, $E(x, z) = E(z)$ ; thus (equation (B6c) of the Appendix B) $\varepsilon_{x1} = a = const$ .
301	In this specific case, when $a > 0$ (extension), equation (5) has the solution: $z_n = d_1 = const.$
302	When $a < 0$ (compression), in addition to $z_n = d_1 = const$ , a periodic solution corresponding
303	to a loss in stability exists as well (if the compressional force is big enough). In this particular
304	case the necking level does not exist.
305	Our solution allows calculating the necking surface depth (equation 5) as well as the
306	position of the top and the base of the lithosphere when the distribution of strength (apparent
307	Young's modulus) and intraplate force $F_{pl} = \frac{4}{3} \bar{e}(x) \frac{\partial U_I(x)}{\partial x}$ , where $\bar{e}(x) = \int_{z_a(x)}^{z_l(x)} E(x,z) dz$ ,
308	(equation B6c of Appendix B) are known.
309	For applications of the model to actual observations it is important that, instead of $F_{\it pl}$ and
310	the distribution of $\overline{e}(x)$ (which are difficult to assign a priori), the horizontal component of
311	the strain tensor $\varepsilon_{x1}(x)$ can be assigned. This function is related to the final topographies of
312	the lithospheric interfaces and can be found by modelling real data. Moreover, when assigning

 $\varepsilon_{x1}(x)$ , in addition to the deformation by in-plane forces, our solution also describes the deformation by force applied to the base of the lithosphere (by mantle drag). See Appendix B for more details.

Let us consider now the isostatic response stage (problem (b)). If at t=0 the lithosphere was in local isostatic equilibrium, then the disturbance of the equilibrium state due to a deformation by external forces (referred below as a load) at time t is

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$$q(x,t) = g\left[\int_{z_{a}}^{z_{l}(x,t)} \rho(x,z,t)dz + (z_{a}(x,t) - z_{a0}) \cdot \rho_{a} - \int_{z_{a0}}^{l_{0}} \rho(x,z,0)dz\right], \tag{6}$$

where g is the gravity acceleration,  $\rho_a$  is the asthenosphere density,  $z_{l0}$ ,  $z_{a0}$ ,  $z_l(x)$  and  $z_a(x)$  are the topography of the top of the lithosphere and the asthenosphere before and after deformation. Using the definition of the free mantle (floating) level (A2) and considering that, under assumed conditions,  $\varepsilon_{x1}$  is independent from the coordinate z, one obtains:

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$$q(x,t) = \rho_a g(z_n(x) - z_{fin}) \varepsilon_{x1} / (1 + \varepsilon_{x1}). \tag{7}$$

This means that the load due to an extensional or compressional deformation varies in direct proportion with the spacing between the necking and the floating (free mantle) levels and does not depend on the density distribution within the lithosphere.

To describe the isostatic response we use a model of a thin homogeneous elastic plate [e.g. *Turcotte and Schubert*, 2002]:

$$D_s \frac{d^4 \omega}{dx^4} + \rho_a g \omega = q(x)$$
 (8),

where  $D_s$  is the flexural rigidity of the lithosphere,  $\omega(x)$  - the magnitude of elastic flexure under the load q(x) calculated from equation (7). For dependence of the flexural rigidity on the rheology of the lithosphere see *Burov and Diament* [1995, 1996].

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#### 4. Results and discussion.

Now we present and discuss some results of our model. As mentioned above, in order to arrive at our analytical solution we assumed for stage (a) that the distribution of the apparent Young's modulus at t=0 can be approximated as  $E(x,z)=E_I(x)F_I(z)$  where  $F_I(z)$  is a non-dimensional function, which can be associated with the yield strength profile. In this case the depth to the centre of rigidity  $d_I$  and all central moments  $c_n$  are constant.

4.1. The necking surface  $z_n(x)$  is almost flat in the area of main deformation; thus  $z_n(x)$  can be replaced by an equivalent flat necking level  $z_n^{eqv}$ .

According to equations (4)-(5), the depth to the necking surface as well as the disturbance of the isostatic equilibrium (specified by value of load q) depend on the relative depth distribution of the mechanical properties of the lithosphere, but not on their absolute values. The yield stress envelopes (Fig. 1) characterize the distribution of rigid and compliant layers and can be used to assign thicknesses and relative strengths of rigid layers at the top of the crust and below the Moho (i.e. function  $F_I(z)$ ) within the lithosphere. We computed the depth to the necking surface shown in Fig. 2 for the five types of lithosphere (Fig.1) with the horizontal component of strain tensor specified as

352 
$$\varepsilon_{xI} = a_0 exp(-b_0 x^2) + \varepsilon_x^0, \tag{9}$$

where parameter  $a_0$  governs the amplitude of extension or compression;  $b_0$  determines the final width of the tectonic structures as well as (through equation B6c) the horizontal gradients of mechanical properties of the lithosphere at the periphery of the tectonic structure. The coordinate origin is at the centre of the model. Fig. 2A and 2B show the position of the necking surface for narrow ( $b_0=3.2 \text{ km}^{-2}$ ) and wide ( $b_0=0.8 \text{ km}^{-2}$ ) areas of extension, respectively, when the asymptotic value for  $z_n(x)$  is assigned as the centre of rigidity d1. (The

choice of asymptotic value does not affect the final result after isostatic rebound, as explained above). All curves  $z_n(x)$  are nearly flat beneath the area of main deformations. Their forms become more complicated only at the periphery of the tectonic structure where  $\varepsilon_{xI}$  is close to its asymptotic value  $\varepsilon_x^0$  (the same behaviour was obtained by *Govers and Wortel*, 1999). As a consequence, the solution of the elastic problem with the necking surface  $z_n(x)$  provided by (2)-(8) can be closely approximated by a solution with an equivalent flat necking level  $z_n^{eqv} = const$ . Replacement of  $z_n(x)$  by a constant value affects both the vertical component of displacement  $W_I$  (equation 2) and the load (7). Therefore, the depth of this equivalent level is close to but not equal to the depth of the necking surface at the centre of the considered structure.

It is important to emphasise that the complex geometry of  $z_n(x)$  and of all lithospheric boundaries at the periphery of the area of main deformation almost completely vanish after isostatic adjustment. Therefore, the model with a flat necking level approximates considerably better the final geometry after isostatic rebound than after the extension of the first stage. This can be understood in terms of the main deformation occurring in a weaker zone (pre-existing or formed during deformation), while the surrounding non-deformed areas are stronger. Deformation in the transition zone, where the mechanical properties of the lithosphere rapidly change, is actually more complicated than predicted by the model with a flat necking level. The solid curve on Fig. 3A shows the topography of the top of the lithosphere having an "Alpine" yield strength profile and extended around the exact necking level calculated from equation (5). The graph marked by filled circles corresponds to a flat necking level at 19.8 km depth, which provides the best fit for the final result after isostatic rebound. Basin shoulders, during extension, relative to  $z_n(x)$  move upward and, therefore, it

is more diff	ficult to match	the results	of the firs	t stage	(before	isostatic	rebound)	by the	model
with a flat n	ecking level.								

The more complicated necking  $z_n(x)$  manifested in the geometry of all other interfaces produces a more complicated perturbation of isostatic equilibrium in comparison to the model with flat necking level (Figure 3 B). Finally, after isostatic rebound, the topographies of the top of the lithosphere as well as all other boundaries (not shown) become almost identical (Figure 3 C).

Note that at the borders of the extensional basin, all of the lithosphere moves upward and, accordingly, the necking surface  $z_n(x)$  for the "Alpine" lithosphere is situated above the top of the model (curve A1 on Fig. 2). The same behaviour was found in *Govers and Wortel* [1999] even on their figures when necking level came out of the limits of the crust, it was fixed at the nearest crustal boundary.

Thus we conclude that even if the topography of the necking surface significantly changes close to the edges of the tectonic structure (where  $\varepsilon_x$  approaches zero on Fig. 2 A, B), the equivalent constant necking level provides a close final solution everywhere. For all tested cases, the difference in topography of all boundaries calculated for  $z_n(x)$  and  $z_n^{eqv}$  after isostatic rebound never exceeds 1% of displacement in the centre of the structure.

4.2. The depth to the necking level mainly depends on the relative thickness of the rigid layers in the upper crust and below the Moho.

According to formulae (3)-(4), when a depth distribution of mechanical properties in the lithosphere has odd symmetry about the centre of rigidity  $d_1$ , parameter  $c_3$  is equal to zero. In this particular case the necking surface is flat and situated at the depth  $z_n = d_1$ . Hence, the topography of the necking surface depends on asymmetry of the function E(x,z) about

the centre of rigidity  $d_1$ , i.e. it mainly depends on the relative thickness and "strength" of rigid layers in the upper crust and below the Moho and only slightly depends on the mechanical properties of the middle part of the crust. As a result, the necking levels for a one-layered and a two-layered crustal model are very close, especially within the region of main deformation.

Fig.2 A, B presents the shape of the necking surface for the five different yield strength profiles shown in Fig. 1. This figure reveals the dependence of this shape with the crustal thickness and the thermal state of the lithosphere. Comparison of these curves with the corresponding strength diagrams suggests that the thicker and deeper the "strong" layer is below the Moho - the deeper the centre of rigidity is. As a consequence, the deeper the equivalent flat necking level  $z_n^{egv}$  is.

It is easy to calculate the position of the centre of rigidity when the lithosphere consists of *n*-layers each having a constant strength  $F(z) = F_i$ , when  $z_{i-1} \le z \le z_i$ . It is equal to:

$$d_1 = \sum_i z_i^{mid} \frac{F_i \Delta z_i}{T_{str}},$$

calculations of Govers and Wortel [1999].

where  $\Delta z_i = z_i - z_{i-1}$  is the thickness of the *i*-th layer,  $z_i^{mid} = (z_i + z_{i-1})/2$  is the depth to its central part and  $T_{str} = \sum_k F_k \Delta z_k$  is total (integrated) strength of the lithosphere. In other words, the depth to  $d_1$  and consequently to  $z_n^{egv}$ , is equal to the weighted average of all layer's  $z_i^{mid}$ . In particular, when the lithosphere contains two equally rigid layers with a negligibly small strength for all other layers the necking level is situated just in between them. If one of these layers is thicker and stronger than the others, the necking level shifts closer to the stronger layer. This result coincides with the guess of *Spadini et al* [1995] and with the numerical

The depth to the necking surface slightly depends on the amount of strain. If parameter  $a_0$  in equation (9) varies within two orders of magnitude, the depth to the necking surface

beneath the area of main deformation moves less than 10%. Pro	bably, the strong dependence
of the depth to the necking surface with the extensional ratio	$\beta(x)$ found for very small
values of $\beta(x)$ in Govers and Wortel (1999) can be explained by	y the difficulty to numerically
integrate a finite element solution for a very small extensional r	ratio. In their calculations for
$\beta(x) > 1.05$ the depth to the necking surface was more stable an	nd changed in the same range
of 10%.	

4.3 The depth to the equivalent necking level  $z_n^{egv}$  depends on the horizontal gradients of mechanical properties of the lithosphere and falls in the range from  $d_1$  to  $d_1+c_3/2c_2$  (see equations (3)-(4)).

Parameter  $b_0$  in equation (9) controls the horizontal gradients of strain  $\varepsilon_x$ , which through equation (B6c) is related to the horizontal gradients of the vertically averaged apparent Young's modulus  $\overline{e}(x)$ . The smaller is  $b_0$  the smaller are these gradients.

Fig. 2B shows the necking surface for the same previously studied five models, but for smaller  $b_0$  value. Under the assumed mode of deformation (9) it results in a wider area of extension and smaller gradients of  $\varepsilon_x$  and  $\bar{e}(x)$  (the horizontal component of the strain tensor  $\varepsilon_x$  is shown at the top of the plots). As follows from equation (5), when the width of a structure tends to infinity (i.e.  $b_0 \to 0$  in equation (9)) the second derivatives in equation (5) tend to zero, in turn, tending to move  $z_n(x)$  to the centre of rigidity  $d_1$ . On the contrary, when a width of a structure tends to zero, the term in brackets in equation (5) tends to zero faster than the second derivatives and  $z_n(x)$  becomes flat and equal to  $d_1 + c_3/2c_2$ . As a result, the depth to the equivalent necking level  $z_n^{egv}$  depends on the horizontal gradients of mechanical

parameters and falls in the interval  $[d_1, d_1 + c_3/2c_2]$ . These intervals are shown in Fig. 1 by arrows starting at  $d_1$  and ending at  $d_1 + c_3/2c_2$ .

It is important to note that, although the equivalent necking depth can be located anywhere within these depth intervals since these intervals are quite narrow (see Fig. 1), the necking level depth can be used to characterize the rheological properties of the lithosphere. Fig. 4 shows the shape of the lithosphere upper and lower boundaries, as well as crustal thickness and depth to the necking surface computed for the "Normal" lithosphere model (Fig. 1). As a result of extension and consequent isostatic rebound, uplifts (shoulders) are formed at the both sides of an extensional basin. The height of shoulders depends on horizontal gradient of mechanical properties at the periphery of tectonic structure. For the same maximum extension ratio, the lower gradient results in the wider structure and both the depth to the necking level and the amplitude of the elastic flexure depend on the width of this gradient zone.

4.4. The simultaneous estimation of the strain distribution  $\varepsilon_x(x)$ , depth to the equivalent necking level  $z_n^{eqv}$  and effective flexural rigidity of the lithosphere  $D_s$  is an ill-posed inverse problem.

Let us now investigate how to determine simultaneously the strain distribution, depth to the equivalent necking level and effective elastic rigidity. If it is assumed that the shape of the upper and lower crustal boundaries  $z_l(x)$  and  $z_{Moho}(x)$  after deformation are known from geophysical data, then we get:

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$$z_{l}(x) = z_{l0} - (z_{l0} - z_{n}^{eqv}) \varepsilon_{x} / (1 + \varepsilon_{x}); \ z_{Moho}(x) = z_{Moho,0} - (z_{Moho,0} - z_{n}^{eqv}) \varepsilon_{x} / (1 + \varepsilon_{x}) \ (10),$$

where functions with index "0" denote the topography before deformation and  $\varepsilon_x(x)$  is the horizontal component of the strain tensor. The crustal thickness  $H(x) = z_{Moho}(x) - z_l(x)$  does

475	not depend on the depth to $z_n^{eqv}$ , thus the function $\varepsilon_x/(1+\varepsilon_x)$ can be estimated from crustal
476	thickness before and after deformation. For sedimentary basins an alternative approach is to
477	use subsidence curves to estimate the extensional ratio $\beta(x) = 1 + \varepsilon_x(x)$ [McKenzie, 1978].
478	Thus, since $\varepsilon_x(x)$ is known (probably with some error), the problem reduces to a
479	simultaneous estimate of $z_n^{eqv}$ and the flexural rigidity $D_s$ from the topography of $z_l(x)$ and
480	$z_{Moho}(x)$ . Equations (7)-(8) reveal that this problem has a unique solution. However, the
481	problem is ill-posed. Solid lines in Fig. 5 show the topographies of the top of the crust and of
482	the Moho in the area of extension (the horizontal component of the strain $\varepsilon_x$ is shown at the
483	top of the figure) for the "Shield" model (Fig. 1) when $D_s$ is equal to $10^{22} \ N \cdot m$ . A very close
484	estimate with slightly different strain (shown by crosses) was obtained for $D_s = 5 \cdot 10^{22} \ N \cdot m$ .
485	In this case $z_n^{eqv} = 21$ km, while for the first solution $z_n^{eqv} = 50$ km. In both cases $z_l(x)$ and the
486	Moho topography are almost identical and would not be distinguishable with seismic imagery.
487	This example suggests that there is a trade-off between $z_n^{eqv}$ and $D_s$ and, as a result
488	they cannot be simultaneously estimated. To resolve the problem, independent data must be
489	used. Probably this explains why no clear dependence of the necking level depth on thermal
490	age and thickness of the lithosphere was previously inferred [Cloetingh et al., 1995].
491	
492	4.5. The depth to $z_n^{eqv}$ can be estimated from seismic, seismological or geothermal data.
493	Let us now investigate how to estimate $z_n^{eqv}$ . For this, we assume that the lithosphere
494	has two uniform rigid layers: in the upper crust and below the Moho with thicknesses $H_1$ and
495	$H_2$ respectively. We note A, the strength ratio (expressed as effective Young's modulus) of

the two rigid layers. Fig. 6 shows the computed depth to  $z_n^{eqv}$  versus the thickness of the rigid

layer below the Moho for three different values of A (line 1-3 on Fig.6). In addition, Fig. 6

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also shows two curves: curve 4 corresponds to the necking depth computed as the distance between the middle of the upper and lower rigid layers  $(H_1/2 + H_{Moho} + H_2/2)/2$  and curve 5 shows the half depth to the base of the lower rigid layer -  $(H_{Moho} + H_2)/2$ . As soon as A is not too large (e.g. less then 5) the depth to  $z_n^{eqv}$  can be reasonably approximated with these simple relationships. However, in the presence of a very stiff and thick layer in the upper mantle (see curve 3 for A=10) this does not hold. This approximation can be applied to almost all extensional and compressional structures since values of A>3, and  $H_2/H_1>4$  seem unrealistic for the lithosphere of any tectonically active region (see Fig. 1).

Estimates of the relative thicknesses of the rigid layers  $H_1$  and  $H_2$  and of their relative strengths A depend on the assumed geotherm and the composition and rheological parameters of lithospheric rocks.

4.6. The load resulting from lithospheric extension or compression does not equal the topographic weight;

To estimate the flexural rigidity  $D_s$  from equations (7)-(8) one has to specify the load that causes the flexure. Where  $D_s$  is estimated from gravity data it is generally assumed that this load is equal to the weight of topography after tectonic deformation but before isostatic adjustment ( $z_l(x)$ ) [see e.g. Forsyth, 1985]. According to equations (7), (10) the load can be expressed as:  $q(x) = K[\rho_c g(z_l(x) - z_{l0})]$ , where  $K = [(z_{l0} - z_{Moho,0})/(z_{l0} - z_n^{eqv})]$   $\cdot (z_{fm} - z_{Moho,0}) / (z_{fm} - z_{Moho,0})$ ,  $\rho_c$  is the average density of the crust, g is the acceleration of gravity,  $z_{fm}$  is the free mantle level,  $z_{l,0}$  and  $z_{Moho,0}$  are the topographies of the top of the crust and of the Moho before deformation (supposed to be flat for the sake of simplicity). Thus, the load is equal to the weight of the topography only in the specific case  $z_n^{eqv} = z_{Moho,0}$ .

Fig. 1 shows the depth interval in which the equivalent necking level is situated. For all types
of strength profiles except "Shield" this interval is situated within the crust; hence, $K < 1$ .
Accordingly, all estimates made under the assumption $K=1$ underestimate the flexural rigidity.
This is consistent with Forsyth [1985] who explained abnormally low values of $D_s$ estimated
for orogenic belts using topography only (through isostatic admittance) in terms of neglected
subsurface loads.

When the necking surface is situated within the crust, then, during extension or compression, the topographies of the upper surface and of the Moho and other density interfaces increase in amplitude simultaneously but in opposite directions, thus partly isostatically compensating each other. When necking depth coincides with free mantle depth (which can occur for the lithosphere having "Hot" or "Alpine" yield strength profiles), the weight of the topography is completely compensated by displacement of the subsurface density interfaces. In this case, the tectonic structure keeps its initial local isostatic equilibrium state independent of the flexural rigidity of the lithosphere. *Fernandez and Ranalli* [1997] named this depth as "neutral necking".

Fig. 7 demonstrates the topography of lithospheric interfaces formed as a result of compression of the lithosphere having the "Normal" yield strength profile (Fig. 1). The zoomed in area shows flexural subsidence at the periphery of the compressional belt. In this specific case the load (7) is 20% less than the weight of the topography before isostatic adjustment. This presumably changes the morphology of admittance and coherence functions routinely used to estimate the flexural rigidity of the lithosphere in such areas. It may also be relevant to the geodynamics of foreland basin formation [e.g. *Mikhailov et al.*, 1999].

Our study suggests that for structures formed by extension or compression (for example post-rift basins and foredeeps) the ratio between subsurface and surface loads (equal

545	to K-1) can be found a priori using the estimate of the depth to the necking level we discussed
546	above.

#### 5. Conclusions.

- We investigated the deformation of the continental lithosphere using a model incorporating small deformations of a thin inhomogeneous plate by boundary forces: in-plane forces applied to its side boundaries and/or mantle forces applied to its base. Our results demonstrate that the necking level model is valid at least for a first order description of the geodynamics of regional tectonic structures such as sedimentary basins, continental rifts, orogenic belts and passive continental margins. According to this model:
- 1. The vertical component of displacement W can be expressed as  $W = -(z z_n(x))\varepsilon_x$ ; where  $\varepsilon_x$  is the horizontal component of strain, which does not depend on the vertical coordinate z; and  $z_n(x)$  is the necking surface, where there is no vertical displacement before isostatic response takes place.
- 2. Beneath the area of the most significant deformation, the necking surface is almost flat. Thus  $z_n(x)$  can be replaced by a constant  $z_n^{eqv}$ . The depth to this constant equivalent necking level depends on the strength distribution within the lithosphere.
- 3. The depth to  $z_n^{eqv}$  depends mainly on the relative thickness and strength of the rigid layers in the uppermost crust and below the Moho.
- 4. The simultaneous estimation of distribution of strain, equivalent depth to the necking level and effective flexural rigidity is an ill-posed problem. It may be solved when  $z_n^{eqv}$  is estimated *a priori* from independent data on the structure, composition and thermal state of the lithosphere (e.g., yield strength diagrams), seismic or seismological data.

568	5. The load on the lithosphere in extensional or compressional areas must include both
569	topographic weight and subsurface loads. In the absence of "geological loads" due to lateral
570	heterogeneity in the lithosphere the total load can be evaluated using estimates of the depth to
571	the necking level.
572	
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577	contribution XXX.
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580 Appendix A:

More general considerations.

Let us consider a general model of the formation of regional tectonic structures under extension or compression. We assume that the lithosphere deforms by in-plane (far field) forces and/or forces applied to its base resulting from mantle dynamics. We introduce the Cartesian coordinates xOz with the axis Oz directed upwards and denote the horizontal and vertical components of the velocity field initiated within the lithosphere by tectonic forces as U and W respectively. We suppose that U slightly depends upon the vertical coordinate z, so that in a first approximation  $U_{lith} = U(x,t)$  (the assumption is valid for a thin plate, see Appendix B). We then assume that within the lithosphere and sedimentary cover, the density  $(\rho)$  depends upon x and z coordinates and temperature (T), neglecting density/pressure dependency:

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$$\frac{d\rho(x,z,t)}{dt} = -\alpha \cdot \rho(x,z,0) \frac{dT(x,z,t)}{dt}$$
 (A1)

where  $\alpha$  is the thermal expansion coefficient. We assume also that the following initial conditions are known at t=0: spatial distribution of temperature - T(x,z,0), density which corresponds to this temperature -  $\rho(x,z,0)$ , and initial topographies of the top of the sedimentary cover -  $z_s(x,0)$ , the lithosphere -  $z_l(x,0)$  and the asthenosphere -  $z_a(x,0)$ . To reduce the length of the formulas we consider initial topographies to be constants:  $z_{s0}=z_s(x,0)$ ,  $z_{l0}=z_l(x,0)$  and  $z_{a0}=z_a(x,0)$ . Let us finally assume that before being deformed, the lithosphere was in a state of local isostatic equilibrium:

600 
$$\int_{z_a(x,t)}^{z_s(x,t)} \rho(x,z,t) dz = \rho_a \cdot (z_{fm} - z_a(x,t)), \quad \text{when } t = 0.$$
 (A2)

- Here  $z_{fm}$  corresponds to the so-called floating or free mantle level. Equation (A2) can be used as a mathematical definition of  $z_{fm}$ . Its physical meaning is as follows: it is a level to which the top of the asthenosphere would rise if rocks of every vertical column were compressed to
- The topography of any material boundary  $z_p(x,t)$  can be determined from the equation:

606 
$$\frac{\partial z_p}{\partial t} + U(x,t) \cdot \frac{\partial z_p}{\partial x} = W(x,z_p,t), \qquad (A3)$$

- assuming that at each instant of time this boundary marks the same material points. For the
- top of the sedimentary cover  $(z = z_s)$  the term  $\varphi(x,t)$  should be added to the right side of the
- equation (A3) to account for material brought by sedimentation or removed by erosion [e.g.
- 610 Mikhailov, 1983].
- The temperature distribution (T) is given by:

the density of the asthenosphere  $\rho_a$ .

612 
$$\frac{dT}{dt} = \nabla(\chi \nabla T) + \rho Q_{rad}(x, z, t), \qquad (A4)$$

- where  $\chi(x,z)$  is thermal diffusivity and  $Q_{rad}$  is radioactive heat generation per mass rock
- 614 unit.

604

615 Combining equations (A1) and (A4) with the equation of continuity yields:

616 
$$\frac{d\rho(x,z,t)}{dt} + \rho(x,z,t) \left( \frac{\partial U(x,t)}{\partial x} + \frac{\partial W(x,z,t)}{\partial z} \right) = 0.$$
 (A5)

The vertical component of the velocity vector - W(x,z,t) can be expressed as:

$$W(x,z,t) = -(z - z_{fin}) \frac{\partial U}{\partial x} + \int_{z_{a}(x)}^{z} \frac{\alpha}{1 - \alpha(T - T_{0})} (\nabla(\chi \nabla T) + \rho Q_{rad}) dz$$

$$-\frac{\rho_{s}}{\rho_{a}} \varphi(x,t) + f(x,t)$$
(A6)

where f(x,t) is an unknown function that depends on a number of factors including the mode of deformation and physical properties of the constituent lithospheric rocks. Thus, in

general, equations (A4) and (A6) can be used to determine the vertical component of the velocity vector and the topography of the boundaries if the following functions are available: 622 (a) horizontal component of velocity vector U(x,t), (b) rate of sedimentation and/or erosion 623  $\varphi(x,t)$ , (c) thermal diffusivity  $\chi(x,z)$ , (d) initial conditions, including temperature 624 T(x,z,0), density  $\rho(x,z,0)$ , and initial topographies  $z_{s0}$ ,  $z_{l0}$  and  $z_{a0}$ , and (e) a 625 supplementary condition to define the unknown function f(x,t). 626

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For many tectonic processes one can assume, as McKenzie [1978] did, that the duration of lithospheric deformation by external forces is considerably shorter than the time required to re-establish the thermal equilibrium in the lithosphere. If so, two stages of structure formation can be recognized. Rather short stage I, with a duration of several My, includes two substages introduced by [Braun and Beaumont, 1989b]: I.1 - deformation by external forces and I.2 isostatic rebound (if the equilibrium had been disturbed at stage 1<sup>a</sup>). Thus, for stage I equation (A6) takes a following form:

634 
$$W(x,z,t) = -(z - z_{fm}) \frac{\partial U}{\partial x} + f_1(x,t)$$
 (A7.1)

Stage II, that lasts up to 100 My, besides restoring thermal equilibrium, comprises 635 sedimentation and erosion and the isostatic movements associated with them: 636

637 
$$W(x,z,t) = \int_{z_a(x)}^{z} \frac{\alpha}{1 - \alpha(T - T_0)} (\nabla(\chi \nabla T) + \rho Q_{rad}) dz - \frac{\rho_s}{\rho_a} \varphi(x,t) + f_2(x,t) . (A7.2)$$

Unknown functions are encountered at both stages. In stage II, the function  $f_2(x,t)$  accounts for the contribution of the material reloading by sedimentation / erosion and into movements within the lithosphere and asthenosphere related to their intrinsic stress relaxation [e.g. Mikhailov et al, 1996]. Consideration of 2D or 3D dynamics at the second stage is beyond the scope of this paper. Below we consider only the first stage of the process - the initial deformation by external forces (stage I.1) and the consequent isostatic rebound (stage I.2).

To investigate the role of the function  $f_1(x,t)$  in equation (A7.1), let us suppose that at stage I the deformation rate was small and resulting tectonic structures wide enough to neglect the contribution of elasticity in the isostatic balance. Hence, the condition of the local isostatic equilibrium (equation 3 in the main text) can be used as the supplementary equation at any t > 0. Then, applying the operator  $\frac{\partial(\cdot)}{\partial t} + U(x,t)\frac{\partial(\cdot)}{\partial x}$  to the equation (A2) and combining the equations (A1)-(A6), one founds  $f_1(x,t) \equiv 0$  and yields to a 2D analogue of the *McKenzie* [1978] model.

When the isostatic equilibrium is not local, the function  $f_1(x,t)$  does not vanish and has to be determined or defined. For example, based on results of numerical modelling, *Braun and Beaumont* [1989] postulated that under extension the lithosphere deforms about a horizontal necking level  $z_n$  (in the absence of gravity, before the stage of the isostatic rebound, i.e. at stage I.1); thus actually they assigned  $f_1(x,t) = (z_n - z_{fin}) \partial U/\partial x$  plus isostatic rebound at stage I.2 (see problem (b) in Section 3.2 for detailed consideration). Another way to determine this function is to consider the actual mechanism of the lithosphere deformation.

#### Appendix B:

#### Effective elastic model.

For the elastic problem, we used the following notations: E(x,z) - apparent (effective) Young's modulus,  $\nu$  - Poisson's ratio assumed to be equal to 1/2 to obtain formulas similar to (1 or A6), U(x,z) and W(x,z) - the horizontal and vertical components of the displacement vector. As above, we consider that at t=0 the lithosphere was in local isostatic equilibrium

- (A1) and the initial topographies of all density interfaces including the top of the lithosphere
- 667  $(z_{l0})$  and of the asthenosphere  $(z_{a0})$  were flat.
- To find a solution of any elastic problem, functions of displacements have to obey
- Hooke's Law, which under our assumptions can be written as follows:

670 
$$(\sigma_x - \sigma) = \frac{2}{3} E(x, z) \varepsilon_x, \qquad \varepsilon_x = -\varepsilon_z, \qquad \frac{E(x, z)}{3} \gamma_{xz} = \tau_{xz},$$

671 where:

672 
$$\varepsilon_x = \frac{\partial U}{\partial x}$$
,  $\varepsilon_z = \frac{\partial W}{\partial z}$ ,  $\gamma_{xz} = \frac{\partial U}{\partial z} + \frac{\partial W}{\partial x}$  are the components of strain tensor,

- 673  $\sigma_x$ ,  $\sigma_z$ ,  $\tau_{xz}$  components of stress tensor,
- 674  $\sigma = (\sigma_x + \sigma_z)/2$  mean normal stress,
- 675 Equilibrium equations must also be included:

676 
$$\frac{\partial \sigma_x}{\partial x} + \frac{\partial \tau_{xz}}{\partial z} = 0, \qquad \frac{\partial \tau_{xz}}{\partial x} + \frac{\partial \sigma_z}{\partial z} = 0.$$
 (B1)

- To describe lithospheric deformation by in-plane forces we set the following boundary
- 678 conditions:
- 679 (a) free surface condition at the top at  $z = z_1(x)$  and at the base at  $z = z_a(x)$  of the
- 680 lithosphere:

681 
$$\sigma_x \cos(nx) + \tau_{xz} \cos(nz) = 0, \quad \tau_{xz} \cos(nx) + \sigma_z \cos(nz) = 0.$$
 (B2)

(b) compressive or extensive external force at the side boundaries,

$$F_{pl} = \int_{z_{-}(x)}^{z_{l}(x)} \sigma_{x} dz.$$
 (B3)

- The problem was solved suggesting that deformations are small and the plate is thin.
- Then, using the assumptions listed in the section 3.2, introducing dimensionless values as

follows: 
$$x = \xi L$$
,  $z = \varsigma H$ ,  $U(x,z) = \varepsilon^2 L u(\xi,\varsigma)$ ,  $W(x,z) = \varepsilon^2 H w(\xi,\varsigma)$ ,  $E(x,z) = E_0 e(\xi,\varsigma)$ ,

687  $\sigma(x,z) = \varepsilon^2 E_0 s(\xi,\zeta)$  and replacing components of displacement by the components of

strain tensor, one can rearrange equations (B1)-(B2) as:

689 
$$\begin{cases} \varepsilon^{2} \frac{\partial}{\partial \xi} \left( \frac{2}{3} e \frac{\partial u}{\partial \xi} + s \right) + \frac{\partial}{\partial \zeta} \frac{e}{3} \left( \frac{\partial u}{\partial \zeta} + \varepsilon^{2} \frac{\partial w}{\partial \xi} \right) = 0 \\ \frac{\partial}{\partial \xi} \frac{e}{3} \left( \frac{\partial u}{\partial \zeta} + \varepsilon^{2} \frac{\partial w}{\partial \xi} \right) + \frac{\partial}{\partial \zeta} \left( s - \frac{2}{3} e \frac{\partial u}{\partial \xi} \right) = 0 \end{cases}$$
(B1')

$$\frac{\partial u}{\partial \xi} + \frac{\partial w}{\partial \zeta} = 0 \tag{B2}$$

- with the boundary conditions accounting for  $\frac{\partial z}{\partial x} = \varepsilon^2 \frac{\partial w}{\partial \xi}$  at the top and the bottom of the
- 692 lithosphere being:

693 
$$\begin{cases} \frac{e}{3} \left(\frac{\partial u}{\partial \zeta} + \varepsilon^2 \frac{\partial w}{\partial \xi}\right) - \varepsilon^4 \left(\frac{2}{3} e \frac{\partial u}{\partial \xi} + s\right) \frac{\partial w}{\partial \xi} = 0\\ \left(s - \frac{2}{3} e \frac{\partial u}{\partial \xi}\right) - \varepsilon^2 \frac{e}{3} \left(\frac{\partial u}{\partial \zeta} + \varepsilon^2 \frac{\partial w}{\partial \xi}\right) \frac{\partial w}{\partial \xi} = 0 \end{cases}$$
(B3')

Let us expand the components of displacement and the mean normal stress in a power

series of the squared small parameter ( $\varepsilon^2$ ). For example for the non-dimensional mean normal

696 stress *s*:

697 
$$s(\xi,\zeta) = s_1(\xi,\zeta) + \varepsilon^2 s_2(\xi,\zeta) + \varepsilon^4 s_3(\xi,\zeta) + \dots$$

- Substitute the expansion in terms of the small parameter in (A1')-(A3') and set equal to
- each other the terms of the same power of  $\varepsilon$ . As a result for the zero and second power of  $\varepsilon$
- one obtains:

701 
$$\frac{\partial}{\partial \zeta} \left( e^{\frac{\partial u_I}{\partial \zeta}} \right) = 0$$
 (B4a)

702 
$$\frac{\partial}{\partial \zeta} \left( s_1 - \frac{2}{3} e^{\frac{\partial u_1}{\partial \xi}} \right) + \frac{\partial}{\partial \xi} \left( \frac{e}{3} \frac{\partial u_1}{\partial \zeta} \right) = 0$$
 (B4b)

703 
$$\frac{\partial}{\partial \xi} \left( \frac{2}{3} e^{\frac{\partial u_I}{\partial \xi}} + s_I \right) + \frac{1}{3} \frac{\partial}{\partial \varsigma} e^{\left(\frac{\partial u_2}{\partial \varsigma} + \frac{\partial w_I}{\partial \xi}\right)} = 0$$
 (B4c)

704 
$$\frac{\partial}{\partial \xi} \left( s_2 - \frac{2}{3} e^{\frac{\partial u_2}{\partial \xi}} \right) + \frac{1}{3} \frac{\partial}{\partial \xi} e^{\frac{\partial u_2}{\partial \xi}} + \frac{\partial w_1}{\partial \xi} = 0$$
 (B4d)

Boundary conditions at  $\varsigma = \varsigma_1(\xi)$  and  $\varsigma = \varsigma_a(\xi)$  are as follows:

$$s_1 - \frac{2}{3}e^{\frac{\partial u_1}{\partial \xi}} = 0 \tag{B5a},$$

$$\frac{\partial u_1}{\partial \zeta} = 0 \,, \tag{B5b}$$

708 
$$\frac{\partial u_2}{\partial \zeta} + \frac{\partial w_1}{\partial \xi} = 0,$$
 (B5c)

$$s_2 - \frac{2}{3}e^{\frac{\partial u_2}{\partial \xi}} = 0,$$
 (B5d)

The solution of the system (B4) with the boundary conditions (B5) takes the form:

711 
$$u_1 = u_1(\xi),$$
 (B6a)

$$s_1 = \frac{2}{3}e^{\frac{\partial u_1}{\partial \xi}},\tag{B6b}$$

713 
$$\overline{e}(\xi)\frac{\partial u_1}{\partial \xi} = const$$
 (B6c)

714 
$$\frac{\partial u_2}{\partial \zeta} + \frac{\partial w_1}{\partial \xi} = 0$$
 (B6d)

$$s_2 = \frac{2}{3}e^{\frac{\partial u_2}{\partial \xi}}$$
 (B6e)

where  $\bar{e}(\xi) = \int_{z_a(\xi)}^{z_l(\xi)} E(\xi, \zeta) d\zeta$ . Equations (B6 a-c) are valid for arbitrary function  $e(\xi, \zeta)$ , but to

arrive at the solution (B6 d,e) it is necessary to suggest that the distribution of Young's

modulus can be presented in the form:  $e(\xi, \zeta) = \overline{e}(\xi) \cdot f(\zeta)$ , where  $f(\zeta)$  is a non-

dimensional function that can be associated with the normalized yield strength profile

- Integrating (B6d) taking into account the following relationship, which follows from the equation of continuity (B2′):
- 722  $w_1 = -\varsigma \frac{\partial u_1}{\partial \xi} + f_1(\xi) = -(\varsigma \varsigma_n(\xi)) \frac{\partial u_1}{\partial \xi},$  (B7)
- 723 gives the equation:

724 
$$u_2(\xi,\varsigma) = \frac{\varsigma^2}{2} \frac{\partial^2 u_1}{\partial \xi^2} - \varsigma \frac{\partial f_1}{\partial \xi} + f_2(\xi).$$

- Equation (B7) is presented in the form containing  $\zeta_n(\xi)$ , which specifies the position of the
- necking surface. The functions  $f_1$  and  $f_2$  can be determined from the following equations for
- the zero and the first moments (n = 0,1) which under the adopted boundary conditions can be
- 728 written in the form:

729 
$$\frac{\partial}{\partial \xi} \int_{\varsigma_a(\xi)}^{\varsigma,(\xi)} \frac{4}{3} e \frac{\partial u}{\partial \xi} \varsigma^n d\varsigma = 0.$$
 (B8)

- This expression was obtained integrating the first equation in (B1') and accounting for
- 731 the fact that when  $u_1 = u_1(\xi)$  an in-plane force (B2) can be presented as follows:

732 
$$F_{pl} = \frac{4}{3} \int_{\zeta_{a0}}^{\zeta_{10}} e(\xi, \zeta) \frac{\partial u}{\partial \xi} d\zeta$$
.  $/(1 + \varepsilon^2 \frac{\partial u_1}{\partial \xi}) + o(\varepsilon^4)$ . The function  $f_2$  can be expressed from

- the equation for the zero moment (equation (B8) when n = 0). Substituting  $f_2$  in the equation
- for the first moment (equation (B8) when n = 1) one obtains the following equation for the
- function  $f_1$  (here we return to dimensional values):

736 
$$\frac{\partial^2 f_1}{\partial x^2} - a_1(x) \frac{\partial^2 \varepsilon_{x1}}{\partial x^2} - a_2(x) \varepsilon_{x1} (f_1 - d_1(x) \varepsilon_{x1} - p_0) = 0,$$
 (B9)

737 where: 
$$a_1 = (d_3 - d_2 d_1) / [2(d_2 - d_1^2)], \quad a_2 = 1 / (d_2 - d_1^2), \quad \varepsilon_{x1} = \frac{\partial U_1}{\partial \xi}, \quad f_1 = \varepsilon_{x1} z_n(x),$$

738 
$$d_n(x) = \int_{z_{a0}}^{z_{t0}} E(x, z) \cdot z^n dz / \int_{z_{a0}}^{z_{t0}} E(x, z) dz \text{ and } p_0 \text{ is an unknown parameter that provides a}$$

739	vertical shift of the model as a whole. This shift is compensated at the isostatic rebound stage;
740	thus one can assign $p_0=0$ which yields an asymptotic value equal to $d_1$ .
741	
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833				

37

834	
835	Figure captions
836	
837	Fig.1. Strength diagrams for different types of lithosphere based on rock mechanics data
838	[Ranalli and Murphy, 1987]. The crust has a quartzite rheology, except in the model of
839	"Normal" lithosphere where the lower part of the crust has a diorite rheology (shown in
840	light gray). The underlying mantle has an olivine rheology. Thicknesses of the crust and
841	the lithosphere are listed in Table 1.
842	
843	Fig.2. a. Topography of the necking surface for a relatively narrow area of extension (the
844	horizontal component of the strain tensor is shown at the top of the figure) for the five
845	different models of the lithosphere shown in Fig. 1. All models are one-layered. Letter
846	index corresponds to the first letter in the name of the model in Fig. 1 (for example N1
847	stays for a one-layered "Normal" lithosphere). Asymtotic value for the necking level is
848	fixed at the centre of rigidity (equation (3)). b. The same for a relatively wide area of
849	extension.
850	
851	Fig.3. Comparison of extension relative to the necking level $z_n(x)$ calculated from our model
852	(solid line) and relative to the best fitting constant necking level (solid lines marked by
853	filled circles). A – topography of the top of the lithosphere after extension but before
854	isostatic rebound. B – the total disturbance of isostatic equilibrium (equation (7)) as a
855	result of deformation. C topography of the top of the lithosphere after extension and
856	consequent isostatic rebound.
857	

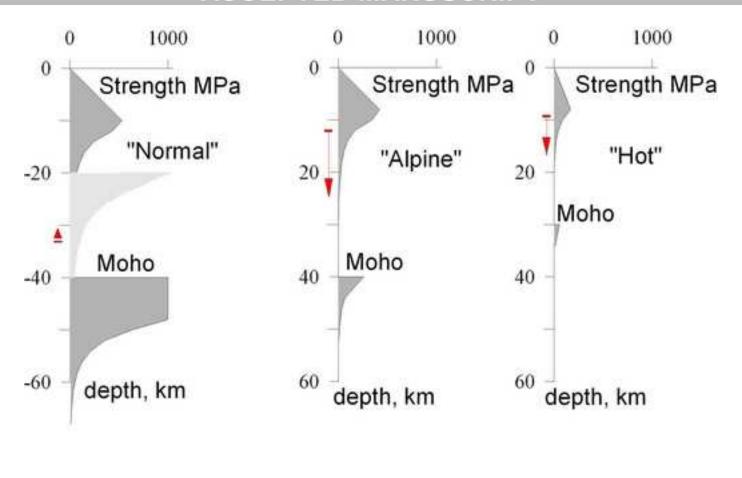
858	Fig.4. Topography of the top ( $Z_{lith}$ ) and the bottom ( $Z_a$ ) of the lithosphere and the crustal			
859	base ( $Z_{\it Moho}$ ) after extension and the isostatic rebound. The topography of the left half of			
860	an extensional basin and of a shoulder is shown in more detail. Solid line with circles			
861	shows position of the necking level.			
862				
863	Fig.5. Close solutions for two different values of effective elastic rigidity of the lithosphere.			
864	Solid lines show the topographies of the top of the crust and the Moho for extensional			
865	area when effective flexural rigidity $D_s$ is equal to $10^{22} \ N \cdot m$ . Lines with crosses are			
866	the solutions for equal to $D_s = 5 \cdot 10^{22} N \cdot m$ , extension for the both examples is shown at			
867	the top of the figure.			
868				
869	Fig.6. Depth to the equivalent necking level versus thickness of the rigid layer below the			
870	Moho. Model of the lithosphere has two rigid layers: in the upper crust (of the constant			
871	thickness $H_1 = 5$ km) and below the Moho (of the thickness $H_2$ which changes from 0			
872	to 25 km, shown on horizontal axis). The ratio of the "strength" of the lower rigid layer			
873	to the upper one A is 0.1 for the line 1, 1 for the line 2 and 10 for the line 3. Line 4			
874	shows the depth equidistant to the middle lines of the upper and lower layers			
875	$(H_1/2 + H_{\textit{Moho}} + H_2/2)/2$ . Line 5 shows the half-depth to the middle line of the lower			
876	layer $(H_{Moho} + H_2)/2$ .			
877				
878	Fig.7. Topography of the top ( $Z_{lith}$ ) and the bottom ( $Z_a$ ) of the lithosphere and the crustal			
879	base $(Z_{\textit{Moho}})$ after compression and the isostatic rebound. The topography of the left half			
880	of the compressional belt is shown in more detail. Solid line with circles shows position			

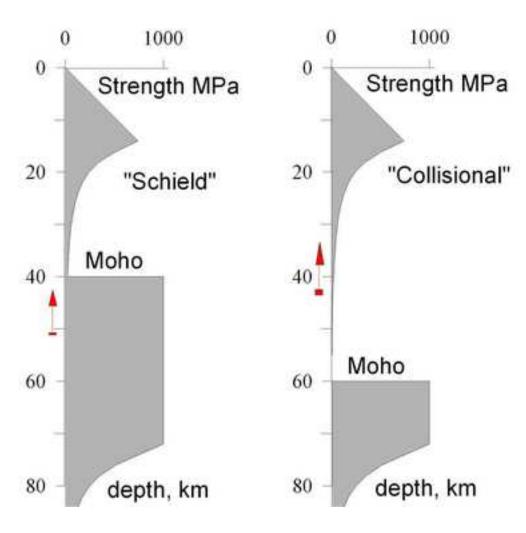
of the necking level.

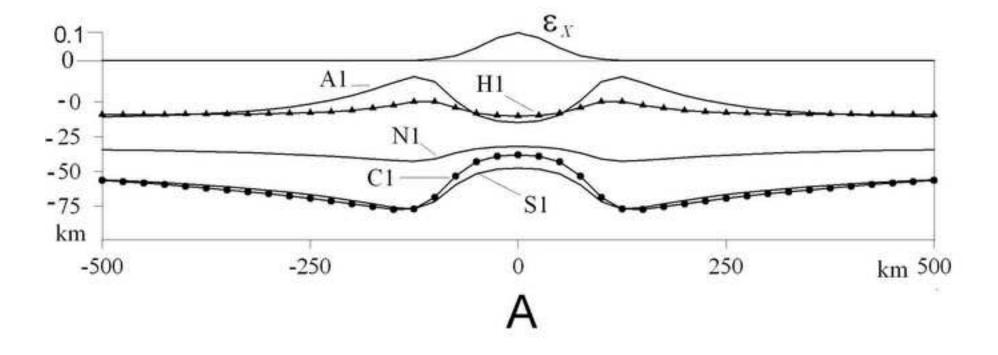
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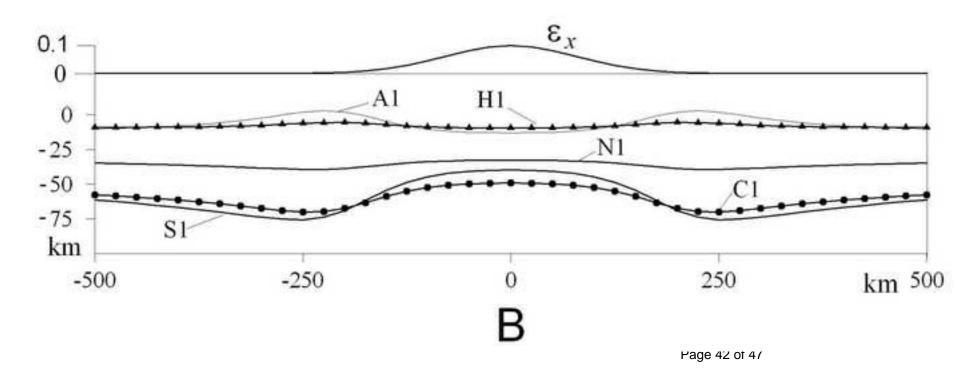
**Table 1**Parameters of the lithosphere used to calculate strength diagrams (Fig.1).

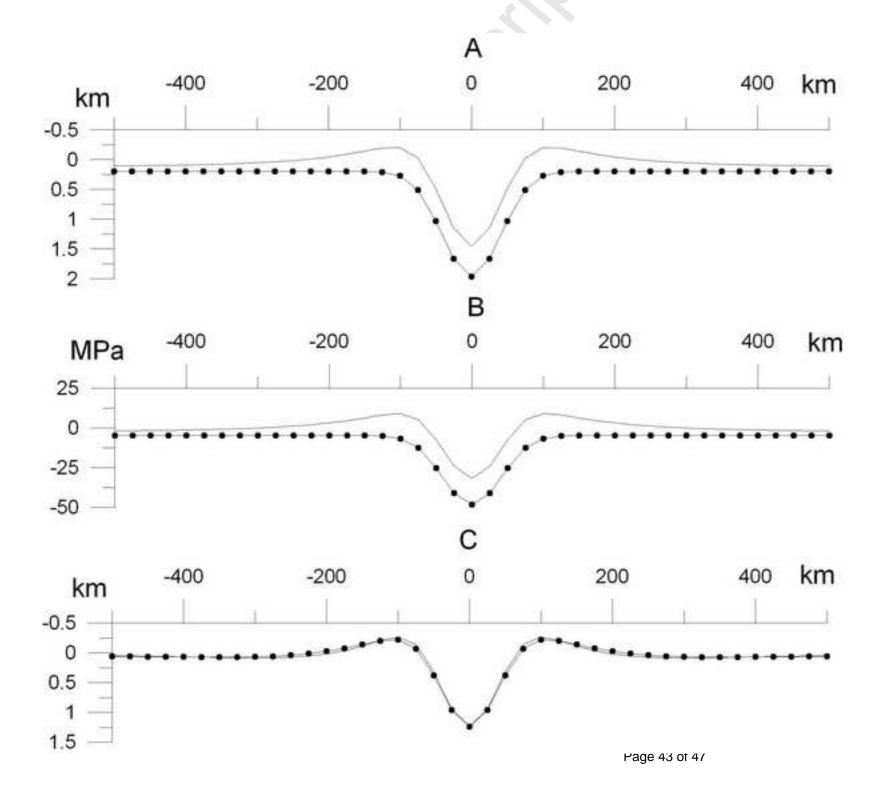
	Thickness of	Thickness of the	Heat flow at the base of
	the crust, (km)	lithosphere, (km)	the lithosphere, $mW/m^2$
"Normal"	40	100	41.9
"Alpine"	40	75	55.9
"Hot"	30	50	85.4
"Shield"	40	150	27.8
"Collisional"	60	150	27.8

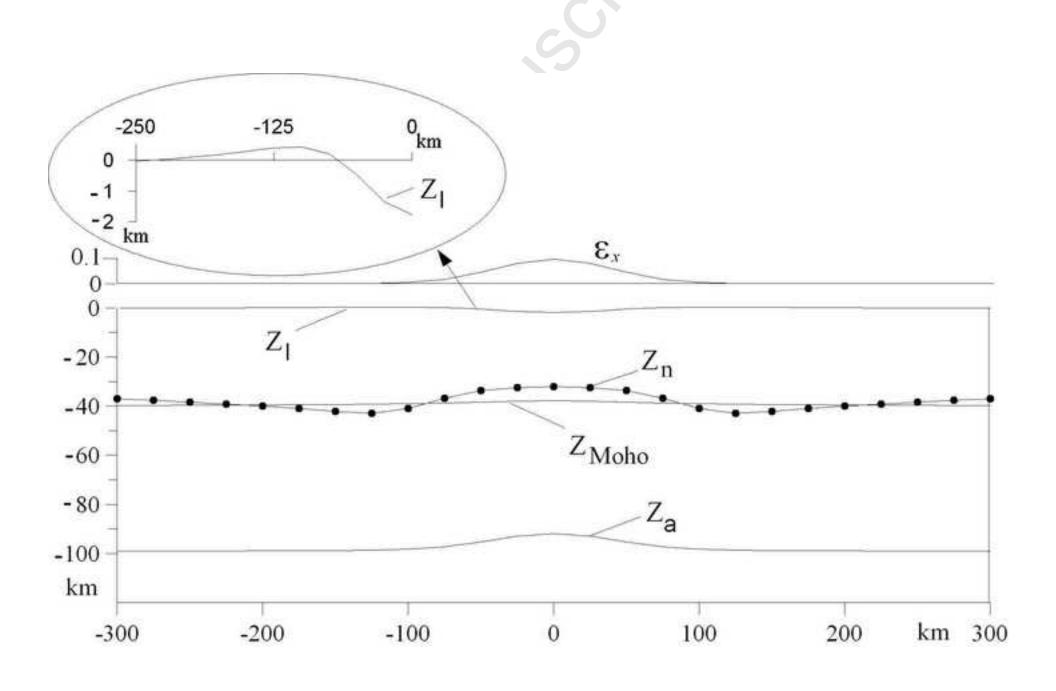


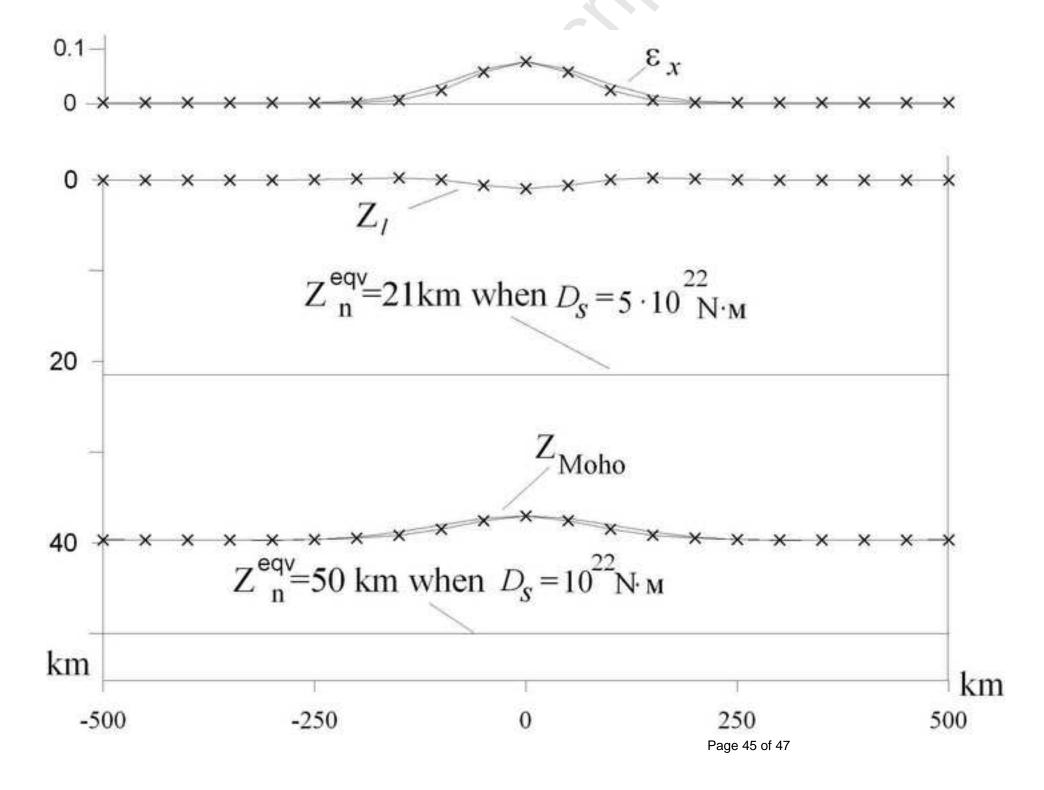


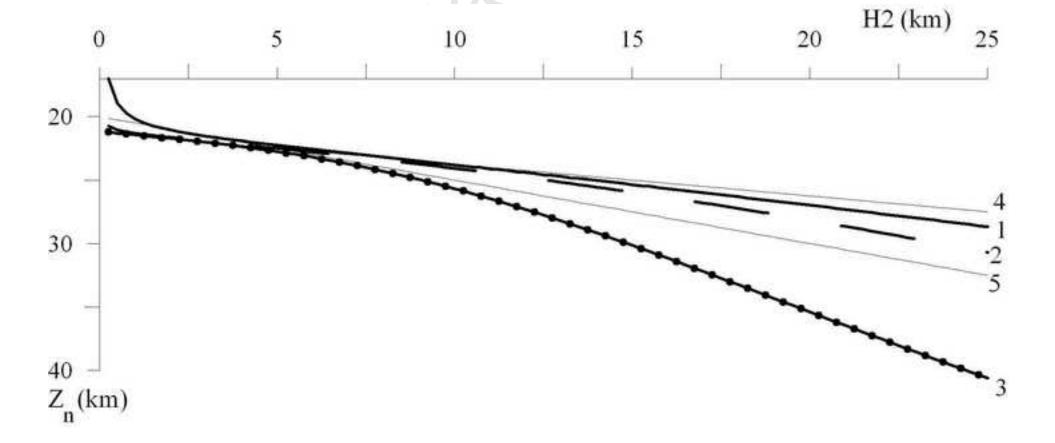


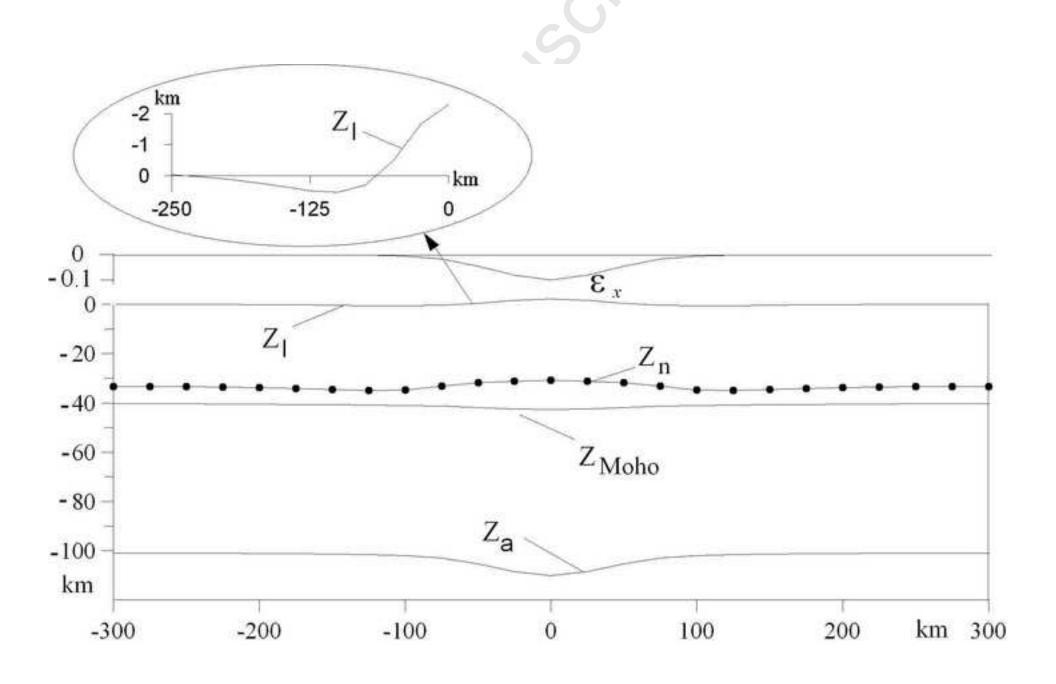












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