



HAL
open science

Nonlinear dynamical systems with data and model uncertainties subjected to seismic loads

Christophe Desceliers, Christian Soize, S. Cambier

► **To cite this version:**

Christophe Desceliers, Christian Soize, S. Cambier. Nonlinear dynamical systems with data and model uncertainties subjected to seismic loads. 17th International Conference on Structural Mechanics in Reactor Technology, SMiRT 17, Aug 2003, Prague, Czech Republic. pp.Pages: 1-7. hal-00687878

HAL Id: hal-00687878

<https://hal.science/hal-00687878>

Submitted on 15 Apr 2012

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Nonlinear dynamical systems with data and model uncertainties subjected to seismic loads

Christophe Desceliers¹⁾, Christian Soize¹⁾, Simon Cambier²⁾

¹⁾ Laboratoire de Mécanique, Université de Marne-La-Vallée, 5, boulevard Descartes, 77454 Marne-La-Vallée Cedex 2, France

²⁾ R&D EDF, Analysis in Mechanics and Acoustics Dpt., 92141, Clamart cedex, France

ABSTRACT

This paper deals with data uncertainties and with model uncertainties of a nonlinear dynamical system subjected to seismic loads. The nonparametric probabilistic model of random uncertainties recently published and extended to nonlinear dynamical system analysis is used in order to model random uncertainties induced by the model errors which concern the linear part of the finite element model. The nonlinearities are due to restoring forces whose parameters are uncertain and are modeled by the parametric approach. Jayne's maximum entropy principle with the constraints defined by the available information allows the probabilistic model of such random variables to be constructed. Therefore, a nonparametric-parametric formulation is developed in order to model all the sources of uncertainties in such a nonlinear dynamical system. Finally, a numerical application for earthquake engineering analysis is proposed and concerned a reactor coolant system with data and model uncertainties subjected to seismic loads.

KEY WORDS: nonlinear structural dynamics, earthquake, random uncertainties.

INTRODUCTION

This paper deals with the transient response of a nonlinear dynamical system with random uncertainties. The source of random uncertainties is induced by the model uncertainties (or the model errors) and the data uncertainties (errors on the parameters of the model). For the problem under consideration, data uncertainties concern the local parameters of the finite element model and the parameters of the nonlinear forces. Usually, parametric approaches are used to model data uncertainties [1,2] for evaluating and analyzing the response of structures with uncertain parameters under seismic loads, like piping and equipment, power plant installations and industrial structures [3-7]. Nevertheless, such approaches do not allow model uncertainties to be taken into account. It should be noted that model uncertainties can only be modeled by using a nonparametric approach. Recently, a nonparametric model of random uncertainties has been introduced for linear dynamical system analysis [8,9]. This nonparametric model has also been extended to the transient response of nonlinear dynamical system [10] without having random uncertainties on the nonlinear part. This nonparametric model is constructed by the use of Jayne's entropy principle which consists in maximizing the probabilistic uncertainties with the constraints defined by the available information (for instance, related to algebraic properties of the finite element matrices). Nevertheless, this nonparametric formulation does not allow the uncertainties related to the nonlinear restoring forces to be modeled. This is the reason why a nonparametric-parametric formulation is proposed for analyzing nonlinear dynamical systems subjected to seismic loads with data uncertainties for the nonlinearities. An application to a multisupported reactor coolant system subjected to seismic loads is presented.

MEAN NONLINEAR DYNAMICAL SYSTEM

We consider a nonlinear dynamical system constituted of a damped structure subjected to m_s deterministic time-dependent dirichlet conditions corresponding to seismic loads applied to the supports of the structure. The nonlinearities are due to stops with high stiffness, installed with a given gap at given points of the structure. Let m_f be the number of degrees of freedom of the mean finite element model of this nonlinear dynamical system. Let \mathbf{z} be the \mathbb{R}^{m_f} -vector of the total displacements, including the displacements of the supports. We are interested in the transient response $t \mapsto \mathbf{z}(t)$ from $[0, T]$ into \mathbb{R}^{m_f} . Let $[\mathcal{M}]$, $[\mathcal{D}]$ and $[\mathcal{K}]$ be the mass, damping and stiffness matrices of the linear part of the mean finite element model. It is assumed that the structure with fixed supports has no rigid body modes. Consequently $[\mathcal{M}]$, $[\mathcal{D}]$ and $[\mathcal{K}]$ are positive-definite symmetric ($m_f \times m_f$) real matrices. The real-valued vector $\mathbf{z}(t)$ is rewritten as $\mathbf{z}(t) = (\mathbf{z}(t), \mathbf{z}_s(t))$ in which $\mathbf{z}_s(t) \in \mathbb{R}^{m_s}$ is the vector of the constrained

DOFs at the supports and where $\mathbf{z}(t) \in \mathbb{R}^m$ is the vector of the m unconstrained DOFs with $m = m_f - m_s$. The block splitting of matrices $[\mathcal{M}]$, $[\mathcal{D}]$ and $[\mathcal{K}]$ relative to $\mathbf{z}(t) = (\mathbf{z}(t), \mathbf{z}_s(t))$ are introduced,

$$[\mathcal{M}] = \begin{bmatrix} [\mathbb{M}] & [\mathbb{M}_{I_s}] \\ [\mathbb{M}_{I_s}]^T & [\mathbb{M}_s] \end{bmatrix}, \quad [\mathcal{D}] = \begin{bmatrix} [\mathbb{D}] & [\mathbb{D}_{I_s}] \\ [\mathbb{D}_{I_s}]^T & [\mathbb{D}_s] \end{bmatrix}, \quad [\mathcal{K}] = \begin{bmatrix} [\mathbb{K}] & [\mathbb{K}_{I_s}] \\ [\mathbb{K}_{I_s}]^T & [\mathbb{K}_s] \end{bmatrix}. \quad (1)$$

Since $[\mathcal{M}]$, $[\mathcal{D}]$ and $[\mathcal{K}]$ are positive-definite matrices, then $[\mathbb{M}]$, $[\mathbb{D}]$ and $[\mathbb{K}]$ are also positive-definite symmetric ($m \times m$) real matrices. Consequently, the inverse matrix $[\mathbb{K}]^{-1}$ exists and the ($m \times m_s$) real matrix $[\mathbb{R}] = -[\mathbb{K}]^{-1}[\mathbb{K}_{I_s}]$ and the relative unconstrained DOFs vector $\mathbf{y}(t) = \mathbf{z}(t) - [\mathbb{R}]\mathbf{z}_s(t)$ belonging to \mathbb{R}^m can be defined. Let $\{\omega_\alpha\}_{0 < \alpha \leq n}$ be the eigenfrequencies of the corresponding structural modes $\{\varphi_\alpha\}_{0 < \alpha \leq n}$ such that $[\mathbb{K}]\varphi_\alpha = \omega_\alpha^2[\mathbb{M}]\varphi_\alpha$. Let $\mathbf{y}^n(t)$ be the projection of $\mathbf{y}(t)$ on the subspace of \mathbb{R}^m spanned by $\{\varphi_\alpha\}_{0 < \alpha \leq n}$ with $n \ll m$ such that $\mathbf{y}^n(t) = [\Phi_n]\mathbf{q}^n(t)$, in which $[\Phi_n]$ is the ($m \times n$) real matrix whose columns are vectors $\{\varphi_\alpha\}_{0 < \alpha \leq n}$ and where $\mathbf{q}^n(t)$ is the vector of the generalized coordinates belonging to \mathbb{R}^n . Let the positive-definite symmetric ($n \times n$) real matrices $[\underline{M}_n]$, $[\underline{D}_n]$ and $[\underline{K}_n]$ be the generalized mass, damping and stiffness matrices of the nonlinear dynamical system such that

$$[\underline{M}_n] = [\Phi_n]^T [\mathbb{M}] [\Phi_n], \quad [\underline{D}_n] = [\Phi_n]^T [\mathbb{D}] [\Phi_n], \quad [\underline{K}_n] = [\Phi_n]^T [\mathbb{K}] [\Phi_n]. \quad (2)$$

It can be shown that generalized coordinates $\mathbf{q}^n(t)$ is a solution of the reduced matrix model of the nonlinear dynamical system,

$$[\underline{M}_n] \ddot{\mathbf{q}}^n(t) + [\underline{D}_n] \dot{\mathbf{q}}^n(t) + [\underline{K}_n] \mathbf{q}^n(t) + \mathbf{F}_c^n(t, \mathbf{q}^n(t), \dot{\mathbf{q}}^n(t); \mathbf{w}) = \mathbf{F}^n(t), \quad t \in [0, T], \quad (3)$$

with the initial conditions,

$$\mathbf{q}^n(0) = \dot{\mathbf{q}}^n(0) = 0, \quad (4)$$

in which $\mathbf{F}^n(t) \in \mathbb{R}^m$ and $\mathbf{F}_c^n(t, \mathbf{q}, \dot{\mathbf{q}}; \mathbf{w}) \in \mathbb{R}^m$ are such that

$$\mathbf{F}^n(t) = -[\Phi_n]^T ([\mathbb{M}] [\mathbb{R}] + [\mathbb{M}_{I_s}]) \ddot{\mathbf{z}}_s(t) - [\Phi_n]^T ([\mathbb{D}] [\mathbb{R}] + [\mathbb{D}_{I_s}]) \dot{\mathbf{z}}_s(t), \quad (5)$$

$$\mathbf{F}_c^n(t, \mathbf{p}, \mathbf{q}; \mathbf{w}) = [\Phi_n]^T \mathbb{f}_c(t, [\Phi_n] \mathbf{p} + [\mathbb{R}] \mathbf{z}_s(t), [\Phi_n] \mathbf{q} + [\mathbb{R}] \dot{\mathbf{z}}_s(t); \mathbf{w}), \quad (6)$$

where $\mathbb{f}_c(t, \mathbf{z}(t), \dot{\mathbf{z}}(t); \mathbf{w})$ is the nonlinear forces induced by the stops whose parameters are represented by vector $\mathbf{w} = (\underline{w}_1, \dots, \underline{w}_\nu) \in \mathbb{R}^\nu$. Hereinafter, it is assumed that the nonlinear dynamical problem defined by Eqs. (3) and (4) has a unique solution $t \mapsto \mathbf{q}^n(t)$ from $[0, T]$ into \mathbb{R}^n .

STOCHASTIC NONLINEAR DYNAMICAL SYSTEM WITH DATA AND MODEL UNCERTAINTIES

The nonparametric approach consists in substituting the mean generalized mass, damping and stiffness matrices $[\underline{M}_n]$, $[\underline{D}_n]$ and $[\underline{K}_n]$ of the mean reduced matrix model by the random matrices $[\mathbf{M}_n]$, $[\mathbf{D}_n]$ and $[\mathbf{K}_n]$. For the problem under consideration, the parametric approach consists in substituting parameter mean values \mathbf{w} of the nonlinear forces by the \mathbb{R}^ν -valued random variable \mathbf{W} . Consequently, the m unconstrained DOFs and the m unconstrained relative DOFs are represented by the \mathbb{R}^m -valued stochastic processes $\mathbf{Z}^n(t)$ and $\mathbf{Y}^n(t)$ indexed by $[0, T]$, respectively, such that

$$\mathbf{Z}^n(t) = \mathbf{Y}^n(t) + [\mathbb{R}] \mathbf{z}_s, \quad \mathbf{Y}^n(t) = [\Phi_n] \mathbf{Q}^n(t), \quad (7)$$

where the \mathbb{R}^n -valued stochastic process $\mathbf{Q}(t)$ indexed by $[0, T]$ is the unique second-order solution of the following stochastic nonlinear dynamical system,

$$[\mathbf{M}_n] \ddot{\mathbf{Q}}^n(t) + [\mathbf{D}_n] \dot{\mathbf{Q}}^n(t) + [\mathbf{K}_n] \mathbf{Q}^n(t) + \mathbf{F}_c^n(t, \mathbf{Q}^n(t), \dot{\mathbf{Q}}^n(t); \mathbf{W}) = \mathbf{F}^n(t), \quad t \in [0, T], \quad (8)$$

with the initial conditions,

$$\mathbf{Q}^n(0) = \dot{\mathbf{Q}}^n(0) = 0, \quad \text{a.s.} \quad (9)$$

Random matrices $[\mathbf{M}_n]$, $[\mathbf{D}_n]$ and $[\mathbf{K}_n]$ and random vector $\mathbf{W} = (W_1, \dots, W_\nu)$ are second-order random variables subjected to the following constraints defined by the available information,

$$[\mathbf{M}_n], [\mathbf{D}_n], [\mathbf{K}_n] \in \text{Mat}_{\mathbb{R}}^+(n) \quad \text{a.s.} \quad , \quad (10)$$

$$E\{[\mathbf{M}_n]\} = [\underline{\mathbf{M}}_n] \quad , \quad E\{[\mathbf{D}_n]\} = [\underline{\mathbf{D}}_n] \quad , \quad E\{[\mathbf{K}_n]\} = [\underline{\mathbf{K}}_n] \quad , \quad (11)$$

$$E\{\|[\mathbf{M}_n]^{-1}\|_F^2\} < +\infty \quad , \quad E\{\|[\mathbf{D}_n]^{-1}\|_F^2\} < +\infty \quad , \quad E\{\|[\mathbf{K}_n]^{-1}\|_F^2\} < +\infty \quad , \quad (12)$$

$$W_1 \in \mathcal{D}_1, \dots, W_\nu \in \mathcal{D}_\nu \quad , \quad \text{a.s.} \quad , \quad (13)$$

$$E\{\mathbf{W}\} = \underline{\mathbf{w}} \quad , \quad (14)$$

in which E denotes the mathematical expectation and where $\|[\mathbf{A}]\|_F = (\text{tr}\{[\mathbf{A}][\mathbf{A}]^T\})^{1/2}$. In Eq. (10), $\text{Mat}_{\mathbb{R}}^+(n)$ is the set of all the positive-definite symmetric $(n \times n)$ real matrices and in Eq. (13), for all $1 \leq \ell \leq \nu$, \mathcal{D}_ℓ is a subset of \mathbb{R} .

Let $Z_1(t), \dots, Z_n(t)$ be the coordinates of $\mathbf{Z}^n(t)$. Let $S_j(\xi, \omega)$ be the random normalized response spectrum of stochastic transient response $Z_j^n(t)$ with (ξ, ω) belonging to $J_\xi \times J_\omega \subset \mathbb{R}^2$ where $J_\xi = [0, 1]$ and $J_\omega = [\omega_{min}, \omega_{max}]$. We then have

$$S_j(\xi, \omega) = \frac{\omega^2}{g} \max_{t \in [0, T]} |X_j(t)| \quad , \quad (15)$$

in which g is a normalization constant (for instance, the gravity acceleration) and where $X_j(t)$ is the solution of the linear dynamical system,

$$\ddot{X}_j + 2\xi\omega\dot{X}_j + \omega^2 X_j = -Z_j^n \quad , \quad t \in [0, T] \quad (16)$$

$$X_j(0) = \dot{X}_j(0) = 0 \quad . \quad (17)$$

Normalized response spectrum $S_j(\xi, \omega)$ is a random variable whose mean values $m_{1j}(\xi, \omega)$, second-order moment $m_{2j}(\xi, \omega)$, variance $V_j(\xi, \omega)$ and standard deviation $\sigma_j(\xi, \omega)$ are estimated by the Monte-Carlo numerical simulation. The stochastic convergence of the probabilistic model is studied with respect to n and with respect to the number n_s of samples for the Monte-Carlo numerical simulation, by introducing the norm $\|\|\|\ddot{Z}_j^n\|\|\|$ defined as

$$\|\|\|\ddot{Z}_j^n\|\|\|^2 = E\left\{\int_0^T \ddot{Z}_j^n(t)^2 dt\right\} \quad . \quad (18)$$

This norm is estimated by $\|\|\|\ddot{Z}_j^n\|\|\| \simeq \text{Conv}_j(n_s, n)$ with

$$\text{Conv}_j(n_s, n)^2 = \frac{1}{n_s} \sum_{k=1}^{n_s} \int_0^T \ddot{Z}_j^n(t, \theta_k)^2 dt \quad , \quad (19)$$

where $\theta_1, \dots, \theta_{n_s}$ denotes the n_s samples for the Monte-Carlo numerical simulation.

Let $dB(\xi, \omega)$ be the random variable such that $dB_j(\xi, \omega) = \log_{10}(S_j(\xi, \omega))$. The confidence region associated with the probability level P_c is delimited by the upper envelope $dB_j^+(\xi, \omega)$ and the lower envelope $dB_j^-(\xi, \omega)$ such that $\text{Proba}\{dB_j^-(\xi, \omega) < dB_j(\xi, \omega) \leq dB_j^+(\xi, \omega)\} \geq P_c$ in which dB_j^+ and dB_j^- are constructed by using the Tchebychev inequality and which are such that $dB_j^-(\xi, \omega) = 2dB_j^0(\xi, \omega) - dB_j^+(\xi, \omega)$ and $dB_j^+(\xi, \omega) = \log_{10}(m_{1j}(\xi, \omega) + a_j(\xi, \omega))$ in which $dB_j^0(\xi, \omega) = \log_{10}(m_{1j}(\xi, \omega))$ and $a_j(\xi, \omega) = \sigma_j(\xi, \omega)/(\sqrt{1 - P_c})$.

The probability model of random matrices $[\mathbf{M}_n]$, $[\mathbf{D}_n]$ and $[\mathbf{K}_n]$ are defined in references [8-10]. The probability model of random variable \mathbf{W} is constructed by using Jayne's maximum entropy principle with the constraints defined by Eqs. (13) and (14). If \mathcal{D}_ℓ is a bounded interval of \mathbb{R} such that $\mathcal{D}_\ell = [a_\ell, b_\ell]$ then it can be shown that, for all $1 \leq \ell \leq \nu$, the probability density function $p_{W_\ell}(w)$ of random variable W_ℓ is written as

$$p_{W_\ell}(w) = \mathbb{1}_{[a_\ell, b_\ell]}(w) \frac{k_\ell}{\alpha_\ell(k_\ell)} e^{-k_\ell w} \quad , \quad (20)$$

in which $\mathbb{1}_B(w)$ is the indicatrix function of the set B and where the positive real k_ℓ is such that $(\underline{w}_\ell k_\ell - 1)\alpha_\ell(k_\ell) - k_\ell\beta_\ell(k_\ell) = 0$ in which $\alpha_\ell(k) = e^{-a_\ell k} - e^{-b_\ell k}$ and $\beta_\ell(k) = a_\ell e^{-a_\ell k} - b_\ell e^{-b_\ell k}$. If there exists a real a_ℓ such that $\mathcal{D}_\ell = [a_\ell, +\infty[$, then it can be shown that

$$p_{W_\ell}(w) = \mathbb{1}_{[a_\ell, +\infty[}(w) \frac{e^{-(w-a_\ell)/(\underline{w}_\ell - a_\ell)}}{\underline{w}_\ell - a_\ell} \quad . \quad (21)$$

If the additional constraint $E\{(W_\ell - a_\ell)^{-2}\} < +\infty$ is introduced, then the probability density function $p_{W_\ell}(w)$ is such that

$$p_{W_\ell}(w) = \mathbb{1}_{[a_\ell, +\infty[}(w) \times C_{W_\ell} \times (w - a_\ell)^{(1-\delta_\ell^2)/(\delta_\ell^2)} \times e^{-(w-a_\ell)/((w_\ell-a_\ell)\delta_\ell^2)} \quad , \quad (22)$$

in which

$$C_{W_\ell} = (\underline{w}_\ell \delta_\ell^2 - a_\ell \delta_\ell^2)^{-\frac{1}{\delta_\ell^2}} / \Gamma\left(\frac{1}{\delta_\ell^2}\right) \quad , \quad (23)$$

where the real parameter $\delta_\ell > 0$ allows the dispersion of random variable W_ℓ to be fixed. Let σ_ℓ be the standard deviation of random variable W_ℓ . It can be shown that $\delta_\ell = \sigma_\ell / |\underline{w}_\ell - a_\ell|$.

REACTOR COOLANT SYSTEM WITH DATA AND MODEL UNCERTAINTIES

The structure under consideration is a typical four loops reactor coolant system [11]. Each loop is constituted of a reactor vessel, a reactor coolant pump and a steam generator (see Fig. 1). These three elements are connected to each other by three primary coolant pipes: a hot leg which links the reactor vessel with the steam generator, a cold leg which links the reactor vessel with a reactor coolant pump and an intermediate leg which links the reactor coolant pump with the steam generator. The structure is multisupported with 36 supports. Its supports are constituted of anchors located under the reactor coolant pumps, the steam generators and the reactor vessel. Due to seismic loads, the displacement field of all the 36 supports are constrained by time-dependent Dirichlet conditions (mesh nodes 1 of Fig. 1).

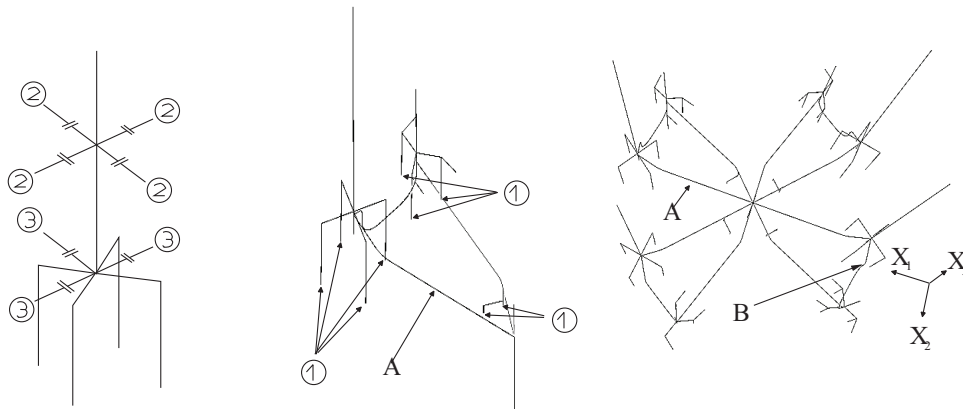


Fig. 1. Finite element mesh of a steam generator (figure on the left), of one loop (figure on the middle) and of the four loops reactor coolant system (figure on the right).

The vibrations of each steam generator are limited by three elastic stops located at their connection point with the intermediate leg and the hot leg (mesh nodes 3 of Fig. 1) and by four elastic stops located at the middle of each steam generator (mesh nodes 2 of Fig. 1). These elastic stops induce nonlinear restoring forces. Furthermore, each elastic stop is subjected to seismic load and consequently, at each stop, the displacement is constrained by a time-dependent Dirichlet condition. The mean finite element model of the reactor coolant system is composed of beam finite elements. Let j_B be the DOF number corresponding to the vertical translation of the node B which is close to three stops (see Fig.1). Let j_A be the DOF number corresponding to the vertical translation of the node A (see Fig. 1).

Figure 2 shows the normalized response spectra of the mean reduced matrix model of the nonlinear dynamical system for DOF number j_A (Fig 2 on the left) and for DOF number j_B (Fig. 2 on the right). The dispersions of random matrices $[\mathbf{M}_n]$, $[\mathbf{D}_n]$ or $[\mathbf{K}_n]$ are controlled by parameters δ_M , δ_D and δ_K . The stochastic convergence analysis is performed for $n \geq 5$ which yields $n_0 = 5$. Consequently, parameters δ_M , δ_D and δ_K are such that

$$0 < \delta_M, \delta_D, \delta_K < 0.9258 = \sqrt{\frac{n_0 + 1}{n_0 + 5}} \quad . \quad (24)$$

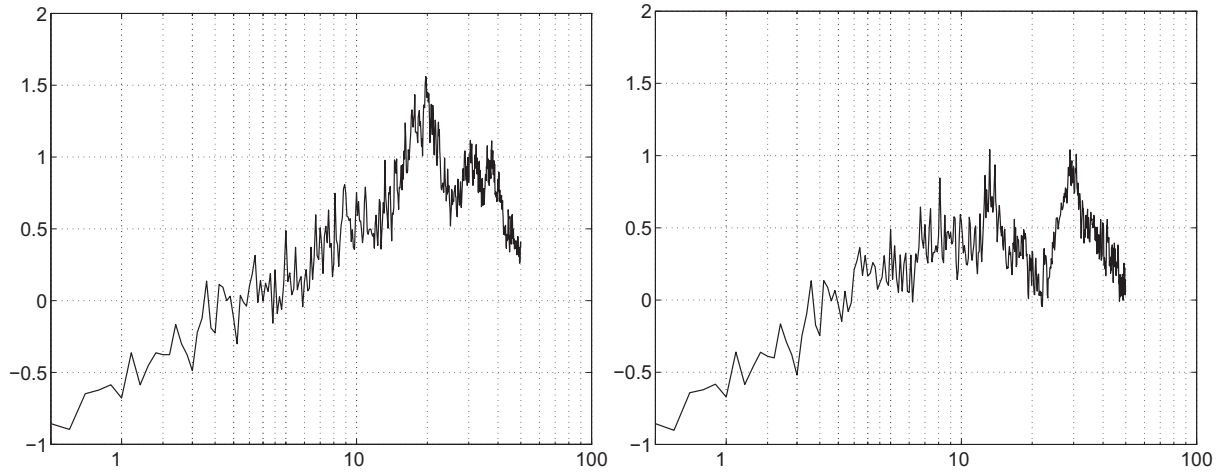


Fig. 2. Normalized response spectrum of the mean reduced matrix model of the nonlinear dynamical system for DOF number j_A (figure on the right) and for DOF number j_B (figure on the left). The horizontal axis in log scale correspond to the frequency (in Hz).

Data uncertainties are relative to the stiffnesses of the stops whose probabilistic models are defined by Eqs.(22) to (23). Parameters $\{W_\ell\}_{1 \leq \ell \leq \nu}$ correspond to the 28 stiffnesses of the 28 elastic stops. Therefore, each parameter belongs to $\mathcal{D}_\ell = [0, +\infty[$. Since the structure is multisupported and the number of nonlinear elastic stops is large, then the solution is very sensitive to the value of the time-step size Δt of the time integration scheme. Time-step size Δt has the same value for all $n \in \{5, 50, 150, 200\}$. For each sample θ_k , Eq. (8) is solved by using the Euler explicit step-by-step integration scheme with $\Delta t = 1/25000s$ and for a time duration $T = 15s$. The Monte-Carlo numerical simulation is performed with $n_s = 700$ samples. Figure 3 shows the graphs of the functions $n_s \mapsto \log_{10}\{\text{Conv}_{j_A}(n_s, n)\}$ for $n = \{5, 50, 150\}$ and for $\delta_M = \delta_D = \delta_K = 0.2$ and $\delta_1 = \dots = \delta_{28} = 0.2$. It can be seen that convergence with respect to n and n_s is obtained for $n = 50$ and $n_s = 60$.

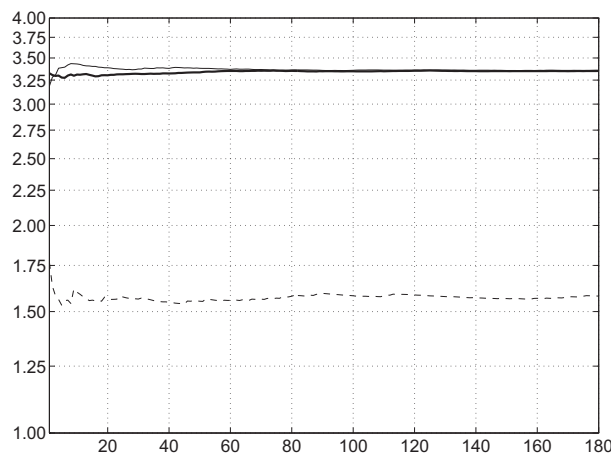


Fig. 3. Graph of function $n_s \mapsto \log_{10}\{\text{Conv}_{j_A}(n_s, n)\}$ for $n = 5$ (lower dotted line), $n = 50$ (upper thin solid line) and $n = 150$ (upper thick solid line).

Figures 4 to 6 show the confidence regions associated with the probability level $P_c = 0.95$ for $n_s = 700$, $n = 200$, $\xi = 0.001$. Figure 4 correspond to a nonparametric level and a parametric level of uncertainties equal to 0.2. Figure 5 show s the confidence regions with just a parametric level of uncertainties equal to 0.2 and with a very low nonparametric level of uncertainties equal to 0.00002 while Fig. 6 show the confidence regions whith just a non zero nonparametric level of uncertainties equal to 0.02.

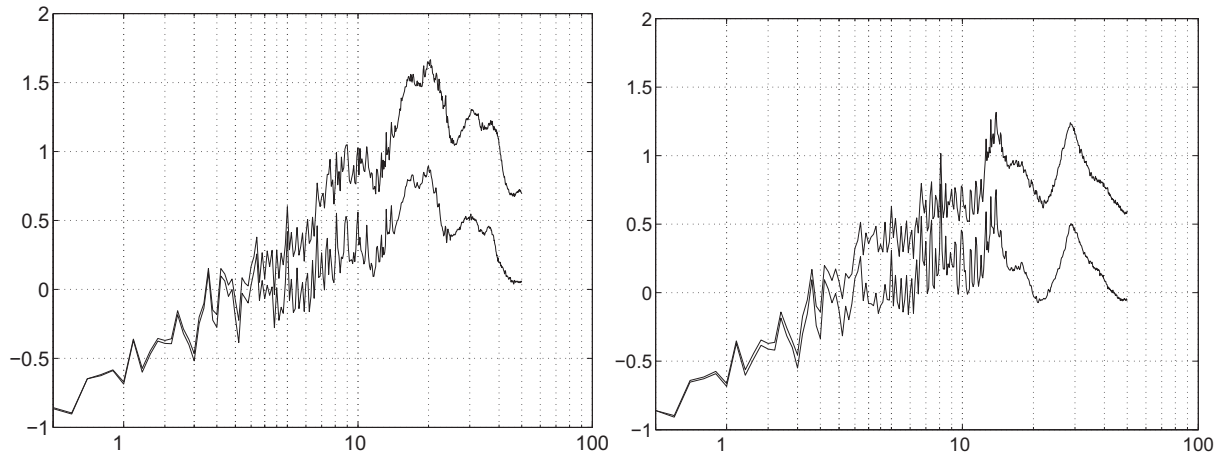


Figure 7. Confidence regions of DOF number j_A (figure on the right) and of DOF j_B (figure on the left) with a nonparametric and a parametric level of uncertainties equal to 0.2. The upper line corresponds to the upper envelope $dB_j^+(\xi, \nu)$ and the lower line corresponds to the lower envelope $dB_j^-(\xi, \nu)$. The frequency ν is represented on the horizontal axis in log scale (in Hz).

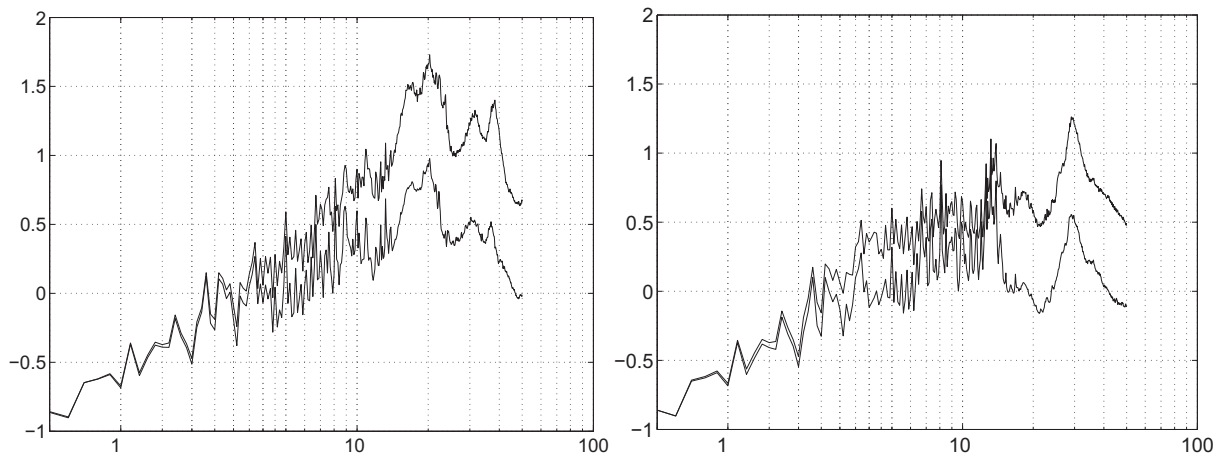


Figure 9. Confidence region of DOF number j_A (figure on the right) j_B and of DOF (figure on the left) with a nonparametric equal to 0.00002 and a parametric level of uncertainties equal to 0.2. The upper line corresponds to the upper envelope $dB_j^+(\xi, \nu)$ and the lower line corresponds to the lower envelope $dB_j^-(\xi, \nu)$. The frequency ν is represented on the horizontal axis in log scale (in Hz).

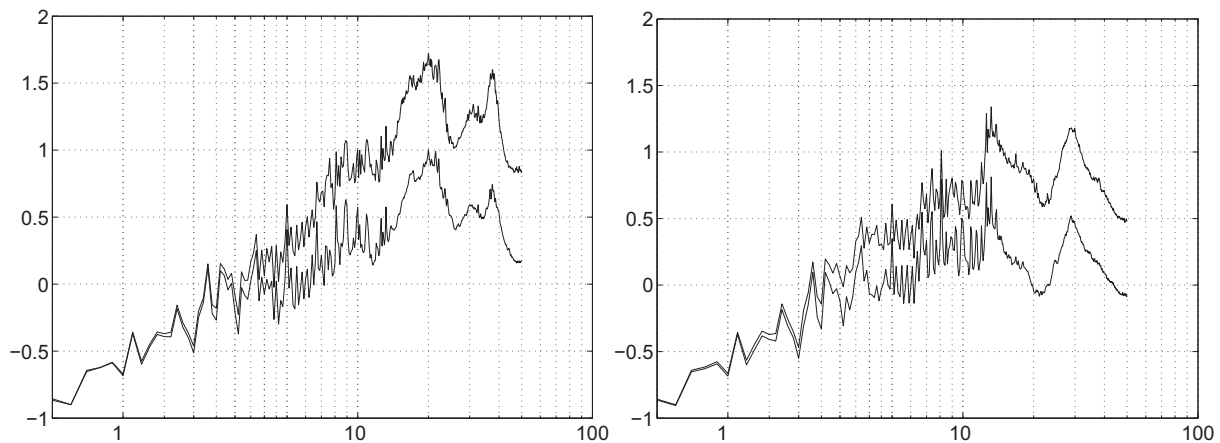


Figure 9. Confidence region of DOF number j_A (figure on the right) j_B and of DOF (figure on the left) with a nonparametric equal to 0.2 and a parametric level of uncertainties equal to 0. The upper line corresponds to the upper envelope $dB_j^+(\xi, \nu)$ and the lower line corresponds to the lower envelope $dB_j^-(\xi, \nu)$. The frequency ν is represented on the horizontal axis in log scale (in Hz).

CONCLUSIONS

A nonparametric-parametric probabilistic model of random uncertainties has been developed for nonlinear dynamical system in the time domain. A nonparametric probabilistic model of random uncertainties is used for

modeling the random uncertainties concerning the linear part of the system. The random uncertainties of the nonlinear part is modeled by the use of a parametric approach.

From the analysis of the normalized response spectra, it can be seen that a DOF not close to a stop (for instance DOF j_A) can be sensitive to the both data and model uncertainties. This result underlines that a local data uncertainty can be propagated in all the structure. However, the model uncertainties have not to be neglected even if the DOF under consideration is close to a stop with data uncertainties. For instance, DOF j_B is close to a stop with data uncertainties but the model uncertainties are clearly not negligible because the confidence regions of DOF j_B seem to be controlled by the nonparametric level of uncertainties. Consequently, it is necessary to model the uncertainties for such a nonlinear dynamical system in order to allow an efficient seismic capacity assessment of such a structure to be performed. For such a dynamical system, the nonparametric-parametric approach allows the level of uncertainties to be extended and is well adapted to this kind of problem.

REFERENCES

1. Ibrahim, R.A., "Structural dynamics with parameters uncertainties", *Applied Mechanics Reviews*, Vol. 40(5), 1987, pp 309-328.
2. Ghanem, R.G., Spanos, P.D., *Stochastic Finite Elements. A Spectral Approach*, Springer, Berlin, 1991.
3. Zhao, Y.G., Ono, T., Idota, H., "Response uncertainty and time-variant reliability analysis for hysteretic MDF structures", *Earth. Engng. Struct. Dyn.*, Vol. 28, 1999, pp 1187-1213.
4. de la Llera, J.C, Chopra, A.K., "Accidental torsion in buuildings due to stiffness uncertainty", *Earth. Engng. Struct. Dyn.*, Vol. 23(5), 1994, pp 117-136.
5. Shenton, H.W, Holloway, E.S., "Effect of stiffness variability on the response of isolated structures", *Earth. Engng. Struct. Dyn.*, Vol. 29, 2000, pp 19-36.
6. Labbé, P., Noe, H., "Stochastic approach for the seismic design of nuclear power plant equipments", *Nuclear Engineering and Design*, Vol. 180, 1991, pp 367-379.
7. Cambier, S., Guihot, P., Coffignal, G., "Computational methods for accounting of structural uncertainties, applications to dynamic behaviour prediction of piping systems", *Structural safety*, Vol. 24, 2002, pp 29-50.
8. Soize C., "A nonparametric model of random uncertainties for reduced matrix models in structural dynamics", *Probabilistic Engineering Mechanics*, Vol. 15(5), 2000, pp 277-294.
9. Soize C., "Maximim entropy approach for modeling random uncertainties in transient elastodynamics", *J. Acoust. Soc. Am.*, Vol. 109(5), 2001, pp 1979-1996.
10. Soize C., "Nonlinear dynamical systems with nonparametric model of random uncertainties", *Uncertainties in Engineering Mechanics*, Vol. 1(5), 2001, pp 1-38. <http://www.resonance-pub.com>.
11. Duval, C., Guyonvarh, V., Louche, V., Pigat, J., Waeckel, F, "Estimation methods for seismic behavior of a PWR primary system", *5th National colloque AFPS*, pp 19-21 1999.