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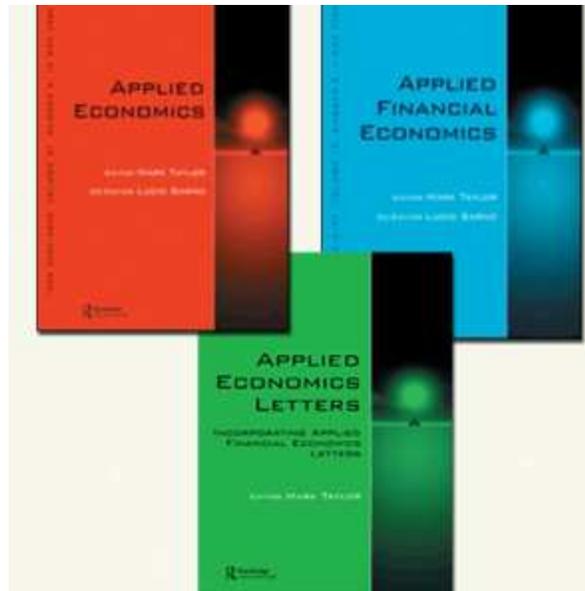
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Consumption and Housing Wealth Breakdown of the Effect of a Rise in Interest Rates

Manuel Leon Navarro¹ and Rafael Flores de Frutos²

¹*Centro Universitario Cardenal Cisneros, C/General Diaz Porlier 58, 28006,
Madrid, Spain.*

²*CUNEF, C/ Serrano Anguita, 8 - 28004, Madrid, Spain*

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Consumption and Housing Wealth

Abstract

In this article the effect on consumption is estimated of a fall in housing wealth and housing prices, resulting from an increase in interest rates. With the help of a dynamic multiequation, macroeconomic model, the consumer response function is broken down into two parts: a direct response, related to a rise in the cost of credit and another indirect one related to the deterioration of the property market. Estimating the theoretical model is done by means of a vectorial error-correction model.

Corresponding author:

mleon@cu-cisneros.es

I. Introduction

In the literature two theoretical approaches have been used to analyse the role of housing in the economy: (1) lifecycle models and (2) financial accelerator models.

In the ‘life cycle-permanent income’ models, Friedman (1957) and Ando and Modigliani (1963)¹, the individuals increase or reduce their wealth to maintain constant consumption. A windfall increase in wealth, whether residential or financial, will produce a permanent rise in consumption.

The financial accelerator models, Aoki *et al.* (2004) and Iacoviello (2005), are general equilibrium models in which housing is used as collateral for credits requested by families. An increase in their price leads to an increase in the collateral and therefore an increase in credit and activity.

The two theoretical approaches differ in several aspects: (1) In the lifecycle models income and wealth are used as explanatory variables in the consumption equation, whereas interest rates are excluded. In the financial accelerator models consumption mainly depends upon assets and their performance in an explicit way. Thus, interest rates and wealth play an important role in its behaviour. (2) In lifecycle models an increase in wealth has an effect on consumption, regardless of whether the effect is caused by an increase in the amount of wealth or the price. In the financial accelerator models it is the price of houses which has effects on consumption. (3) In lifecycle models the channel through which wealth affects consumption is not specified and it is implicitly assumed that agents are not restricted by either liquidity or credit. However, financial accelerator models assume that credit restrictions exist. Therefore, the way in which housing affects consumption is via the credit channel.

From an empirical viewpoint, works can be classified on the basis of the theoretical approach used. Thus, by using the lifecycle theory an equation has been specified in the form $C_t = f(Y_t, W_t)$ where C_t is consumption, Y_t is income and W_t is wealth. By means of this equation the effect exerted on consumption by an increase of wealth

¹A theoretical deduction of the lifecycle model in a context of general equilibrium of overlapping generations can be consulted in Gali (1990).

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3 is estimated. Although the lifecycle theory forecasts that the effect of wealth must
4 be the same for every type of wealth, in practice this equation has been estimated
5 for different types of wealth.
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10 Works which have estimated marginal propensity to consume housing wealth can
11 be classified among those estimating a long-term relationship, such as Case *et al.*
12 (2005) or Ludwing and Slok (2004) and those who analyse the short-term adjust-
13 ment, by using an error correction model (ECM) as Barata and Pacheco (2003) and
14 Catte *et al.* (2004). Though there are very diverse findings, the conclusion can be
15 drawn that in most of the works there exists a significant effect of housing wealth
16 on consumption.
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24 Most of the empirical works based on the financial accelerator model use the VAR
25 (Vector Autoregressive Model) methodology for studying the relationship between
26 consumption, housing and interest rates.
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30 Lastrapes (2002) estimates a VAR model for the American economy in which a
31 fall in interest rates gives rise to an increase in house prices and housing investment.
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34 Aoki *et al.* (2002) find that for the English economy, an interest rate rise produces
35 a drop in housing prices, residential investment and consumption of durable and
36 nondurable goods.
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40 Finally, Iacoviello (2005) estimates a VAR model for the American economy in
41 which a negative GDP and house price response is found in the face of an increase
42 in interest rates. Moreover, a positive shock in housing prices causes GDP to rise.
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46 There are two important differences between both empirical approaches: (1) In
47 works based on the lifecycle theory no specification is made of the reason for wealth
48 variation, whereas in works based on the financial accelerator model wealth varies
49 in the face of an interest rate shock. (2) In the case of lifecycle models the relevant
50 variable is housing wealth. This variable is a measurement of both the number of
51 dwellings and their price. In the case of financial accelerator models the relevant
52 variable is some measurement of housing prices.
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Finally, there exists a group of empirical works which do not specify a particular theoretical model and are concerned with the statistical properties of variables themselves. These works, which share the ideas of the lifecycle models, use a log-linear approach of agents' budgetary restriction to show that there exists a cointegration relationship between consumption, wealth and income. Subsequently, by using the previous cointegration relationship, a VEC model is specified. The prediction error variance is broken down in this model into permanent and transitory factors. Two important results are observed: (1) when there are imbalances in the cointegration relationship, the variable adjusted is wealth. And (2) Consumption is explained by permanent factors, so only permanent changes in wealth affect consumption.

Pichette and Tremblay (2003) analyse the Canadian case making a distinction between housing and financial wealth. This separation makes possible the conclusion that housing wealth is more important for explaining consumption since the prediction error variance of this wealth is made up of permanent factors. Fernandez-Corugedo *et al.* (2003) analyse the English case by separating durable and nondurable goods. Lettau and Ludvigson (2004) analyse the case of the American economy, Hamburg *et al.* (2008) analyse the German case and Chen (2006) the Swedish one.

Whatever the approach used, wealth seems to be an important explanatory variable for consumption.

In this paper we follow the financial accelerator approach where the variations in wealth come from a known source, a shock in the interest rate. As empirical findings and theoretical models show, a fall in interest rates might leads to a rise in house price, housing investment and a finally to a rise in consumption of durable and nondurable goods. Also, as pointed out in Iacoviello (2005), a fall in interest rate may lead to a rise in inflation that, by reducing real debt commitments, it may leads to a rise in consumption.

All these positive effects on consumption are not independent each others, i.e.: the final effect of a fall in interest rates has many components. A direct effect

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3 associated to a cheaper credit and some indirect effects associated to the rise in
4 housing investment, house prices and inflation, as well as the likely feedback reaction
5 of the Central Bank, omitted from the Iacoviello paper. Our objective is to evaluate
6 the relative importance of all these variables in the final response of consumption to
7 a rise in interest rates.
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13 In the present article the role of housing wealth in the Spanish economy is anal-
14 ysed. For that purpose, a theoretical macroeconomic framework, (adapted from that
15 used in Flores *et al.* (1998)) is proposed which, by using the relevant variables of the
16 financial accelerator model, enables the response functions of consumption, housing
17 wealth and the price of housing when faced with a permanent, unit increase in the
18 level of interest rates to be estimated.
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26 Moreover, with the help of this dynamic theoretical framework the final reaction
27 of consumption is identified and broken down into two: (1), the direct reaction,
28 related to the increase in the cost of credit and (2) the indirect reaction related to
29 variations in housing wealth and the fall in the price of houses. Finally, the above-
30 mentioned framework parameters and reactions are estimated from a vectorial error
31 correction model. This breakdown is the fundamental contribution of this article.
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38 Unlike works on the life-cycle, in this article housing wealth is considered as an
39 endogenous variable, which may have feedback relationships with the remaining
40 variables in the agent's set of information. Moreover, the model presented here
41 enables the total effect of housing work to be divided into two: (1) an effect brought
42 about by the increase in the stock of new housing and (2) an effect brought about
43 by the increase in its value. Regarding the financial accelerator models, our model
44 makes it possible to analyse through which channels an increase in interest rates
45 affect consumption, whilst making it possible to evaluate the importance both of the
46 price of housing and the stock of housing on consumption. In the empirical analysis
47 special attention has been devoted to the statistical properties of the data, that
48 is, orders of integration, existence of cointegration relationships, effects of possible
49 extreme values, presence of feedback, etc.
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3 All these properties, with no need to restrict any of them, have been incorporated
4 into the theoretical framework which admits a VAR-type stochastic multivariate
5 representation. This representation can be estimated consistently from the corre-
6 sponding empirical model. To identify the parameters of the theoretical framework,
7 it is only necessary to assume there is an asymmetry in the information used by
8 the different agents when determining the values corresponding to them. That is,
9 whereas private sector agents decide consumption levels, housing wealth and prices
10 in each period, being aware of the level of interest rates, the Central Bank determines
11 interest rates without knowing the exact values which the variables determined by
12 private agents will take.
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24 Once the reaction of the variables has been estimated, the conclusion is reached
25 that a permanent one percent rise in the interest rate produces a permanent fall
26 in consumption, in the growth of housing wealth and housing inflation. Moreover,
27 when the components of consumer response are analysed, it is seen that the final
28 long run effect of the interest rate on consumption (a 1.33% fall) can be broken
29 down into a 0.53% fall due to the direct effect occasioned by the increased cost of
30 credit, a 0.96% fall due to the drop in housing wealth, a 0.48% fall as a result of the
31 fall in housing prices and a 0.66% rise due to the feedback reaction of the Central
32 bank, that lowers rates when inflation falls. The expansion of the consumption and
33 the real state market, experienced by the Spanish economy since mid-nineties, could
34 be well explained by the continuous fall of interest rates (along with the low level of
35 indebtedness of Spanish families).
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48 The article is laid out in the following manner: in Section 2 the theoretical frame-
49 work is specified with which reactions of variables to interest rate shocks can be
50 identified. In Section 3 data and previous statistical findings are presented. In sec-
51 tion 4 the vectorial error correction model is constructed. In Section 5 there are
52 estimates of the response of variables to a permanent unit rise in interest rates. In
53 Section 6 the different components of the final consumer reaction to an interest rate
54 increase are estimated. And in Section 7 the main conclusions are presented.
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II. Theoretical Framework

In this section the theoretical model put forward in Flores *et al.* (1998) and Pereira and Flores (1999) is adapted for the aim of this article.

Two types of agents are considered in this economy, Private sector and Central Bank agents.

It is assumed that private agents in each period determine the consumption levels (C_t), housing wealth (W_t), and price of housing (PV_t).

With the aim of facilitating the theoretical model-empirical model integration, we shall assume that private agents determine the vector $z_t = (c_t, \nabla w_t, \nabla pv_t)'^2$ where the small letter variables denote the logarithm of the levels of the corresponding capital letter variables, with $\nabla = 1 - B$ and B the rational lag operator.

What is more, it is assumed that the Central Bank determines the interest rate levels (r_t)³ in each period. Both private agents and the Central Bank are aware, at the beginning of the period, of past values for all the variables. Nonetheless, whereas private agents fix c_t , ∇w_t and ∇pv_t , when aware of the interest level for the period, the Central Bank determines the interest rate without knowing the values of c_t , ∇w_t and ∇pv_t .

This assumption is crucial to be able to identify the relevant parameters in the theoretical model. The assumption does not seem to be excessively restrictive given the information provided by central banks to the rest of the economic agents nowadays.

The choice of the relevant variables making up the agents' set of information data in this model is similar to that made in typical financial accelerator models.

Representation of Private Agents' behaviour in mathematical form

The set of information available to private agents (Ω_{z_t}) made up of past values of z_t as well as past and present values of r_t , that is:

²In fact it is not necessary to assume that agents choose ∇w_t or ∇pv_t instead of w_t or pv_t .

The reason for maintaining this assumption is our wish to work with a vector z_t of integrated variables of order 1, I(1), since both w_t and pv_t are I(2).

³In the case of interest rate the small letter denotes $r_t = Ln(1 + R_t)$

$$\Omega_{zt} = \{z_{t-j}, r_{t-j}, r_t\}, j = 1, 2, 3, \dots$$

In each period, private agents determine the level of c_t , ∇w_t and ∇pv_t using the information of Ω_{zt} . This means that z_t depends upon the present and past values of r_t as well as the past ones of z_t ⁴, that is:

$$\begin{aligned} z_t &= \nu_z(B)r_t + \epsilon_{zt} \\ \pi_z(B)\epsilon_{zt} &= \alpha_{zt} \end{aligned} \quad (1)$$

Where $\nu_z(B) = (\nu_c(B), \nu_w(B), \nu_{pv}(B))'$ it is a (3x1) vector of stable transfer functions. Each of them registers the unidirectional reaction of the corresponding variable, to a transitory unit variation (impulse) in the interest rate. Each of them has the form $\nu_j(B) = \nu_{j0} + \nu_{j1}B + \nu_{j2}B^2 + \dots$ for $j = c, w, pv$. $\epsilon_{zt} = (\epsilon_{ct}, \epsilon_{wt}, \epsilon_{pvt})'$ it is a vector of random variables which follows a multivariate VAR-type stochastic process. $\pi_z(B) = I - \pi_1B - \pi_2B^2 - \dots$ Is a polynomial (3x3) matrix the determinant of which may have roots on the unit circle⁵, that is, the variables of the vector z_t may not be stationary. Finally, $\alpha_{zt} = (\alpha_{ct}, \alpha_{wt}, \alpha_{pvt})'$ is a white noise vector, with contemporary covariance matrixes Σ_z .

Mathematical representation of the Central Bank's behaviour

The set of information for the Central Bank (Ω_{rt}) is made up of the past values of r_t and only for the past ones of z_t , that is:

$$\Omega_{rt} = \{r_{t-j}, z_{t-j}\}, j = 1, 2, 3, \dots$$

⁴The evolution of the variables c_t , ∇w_t and ∇pv_t is interpreted as the result of the optimization problem of the theoretical financial accelerator models, in which private agents have to decide between two goods, to consume or buy housing, when the relative price of both goods is pv_t .

⁵The reason for not making any assumption on the transfer function and on $\pi_z(B)$ is that the proposed model allows variables not to be stationary. The data will determine whether such a polynome has unit roots or not.

In each period the Central Bank determines r_t using the information set of Ω_{rt} . This means that r_t depends on the past values of r_t and z_t ⁶.

$$\begin{aligned} r_t &= \nu_r(B)z_t + \epsilon_{rt} \\ \pi_r(B)\epsilon_{rt} &= \alpha_{rt} \end{aligned} \quad (2)$$

Where $\nu_r(B) = (\nu_{rc}(B), \nu_{rw}(B), \nu_{rpv}(B))$ it is a (1x3) transfer functions vector. Moreover, ϵ_{rt} is a random scale variable following a general ARIMA(p,d,q) type univariate process; $\pi_r(B)$ is a scale polynome the roots of which may be on the unit circle and α_{rt} is a scale white noise, with variance σ_r^2 and independent of the elements of α_{zt} .

It is important to highlight that the restriction $\nu_{rc}(0) = \nu_{rw}(0) = \nu_{rpv}(0) = 0$ in equation (2) a result of the assumption made on the set of information from the Central Bank, as well as the assumption of independence between α_{rt} and α_{zt} , constitute sufficient restrictions to identify the parameters of the reaction functions of the variables of the vector z_t , to an impulse in the interest rate.

Complete theoretical model in VAR form

The model (1) and (2) can be written in matrix form as:

$$\begin{bmatrix} \pi_z(B) & -\pi_z(B)\nu_z(B) \\ -\pi_r(B)\nu_r(B) & \pi_r(B) \end{bmatrix} \begin{bmatrix} z_t \\ r_t \end{bmatrix} = \begin{bmatrix} \alpha_{zt} \\ \alpha_{rt} \end{bmatrix} = \quad (3)$$

In compact notation:

$$\begin{aligned} \Pi_y(B)y_t &= \alpha_{yt} \\ \Sigma &= \begin{bmatrix} \Sigma_z & 0 \\ 0 & \sigma_r^2 \end{bmatrix} \end{aligned} \quad (4)$$

⁶It is assumed that the monetary policy of this economy is to determine the interest rate instead of money supply.

Where Σ is the contemporary matrix of variances and covariances of the error term.

The multivariate model proposed in (3) is not normalised in the sense of Alavi Jenkins and Alavi (1981) since:

$$\Pi_y(0) = V = \begin{bmatrix} I & -\nu_{z0} \\ 0 & 1 \end{bmatrix} \quad (5)$$

Where $\nu_{z0} = (\nu_{c0}, \nu_{w0}, \nu_{p0})'$ is the vector of contemporaneous effects of r_t on z_t .

The model can be normalised by premultiplying (3) by V^{-1} :

$$\Pi_y^*(B)y_t = \alpha_{yt}^* \quad (6)$$

where

$$\Pi_y^*(B) = V^{-1}\Pi_y(B)$$

$$\alpha_{yt}^* = V^{-1}\alpha_{yt}$$

and the covariance matrix of α_{yt}^* is:

$$\Sigma^* = V^{-1}\Sigma(V^{-1})^T = \begin{bmatrix} \Sigma_z + \nu_{z0}\nu'_{z0}\sigma_r^2 & \nu_{z0}\sigma_r^2 \\ \nu'_{z0}\sigma_r^2 & \sigma_r^2 \end{bmatrix} \quad (7)$$

The model (6) with covariance matrix (7) is a normalised VAR model.

Impulse response functions

Using (3) the vector z_t can be written as:

$$z_t = \Psi_r(B)\alpha_{rt} + \Psi_z(B)\alpha_{zt} \quad (8)$$

where:

$$\Psi_r(B) = [I - \nu_z(B)\nu_r(B)]^{-1}\nu_z(B)\pi_r(B)^{-1} = \Phi_{r0} + \Phi_{r1}B + \Phi_{r2}B^2 + \dots \quad (9)$$

$$\Psi_z(B) = [I - \nu_z(B)\nu_r(B)]^{-1}\pi_z(B)^{-1} = I + \Phi_{z1}B + \Phi_{z2}B^2 + \dots \quad (10)$$

The matrix $\Psi_r(B)$ is a polynomial 3x1 matrix:

$$\Psi_r(B) = \begin{pmatrix} \Psi_{rc}(B) \\ \Psi_{rw}(B) \\ \Psi_{rpv}(B) \end{pmatrix} \quad (11)$$

The sequence of coefficients associated with the polynomials $\Psi_{ri}(B)$ of equation (9) are interpreted as the reaction function of the variables of vector z_t to an impulse in α_{rt} , that is $\partial z_{t+j}/\partial \alpha_{rt-j}$ for $j = 0, 1, 2, \dots$. This function measures the effects of a shock in r_t , on the variables of z_t . Estimating this function is the key for describing the effects of interest rate on consumption, house prices and housing wealth.

It is important to note that in order to analyse the effects of interest rates it is not necessary to specify a whole structural model, all that is needed is the model represented by (3) and (4). Nonetheless, if the intention is to calculate the effect that, a shock in any of the variables determined by the private sector, may have on the rest of the variables, it will be necessary to make extra assumptions, tending towards the complete diagonalisation of the matrix Σ_z .

Breakdown of consumption reaction

By developing in detail the expression of the model (3) it can be observed how this system takes the form of system (12):

$$\begin{bmatrix} \pi_{11}(B) & \pi_{12}(B) & \pi_{13}(B) & \pi_{14}(B) \\ \pi_{21}(B) & \pi_{22}(B) & \pi_{23}(B) & \pi_{24}(B) \\ \pi_{31}(B) & \pi_{32}(B) & \pi_{33}(B) & \pi_{34}(B) \\ -\pi_r(B)\nu_{rc}(B) & -\pi_r(B)\nu_{rw}(B) & -\pi_r(B)\nu_{rpv}(B) & \pi_r(B) \end{bmatrix} \begin{bmatrix} c_t \\ \nabla w_t \\ \nabla pv_t \\ r_t \end{bmatrix} = \begin{bmatrix} \alpha_{ct} \\ \alpha_{wt} \\ \alpha_{pvt} \\ \alpha_{rt} \end{bmatrix} \quad (12)$$

With

$$\pi_{14}(B) = -[\pi_{11}(B)\nu_c(B) + \pi_{12}(B)\nu_w(B) + \pi_{13}(B)\nu_{pv}(B)]$$

$$\pi_{24}(B) = -[\pi_{21}(B)\nu_c(B) + \pi_{22}(B)\nu_w(B) + \pi_{23}(B)\nu_{pv}(B)]$$

$$\pi_{34}(B) = -[\pi_{31}(B)\nu_c(B) + \pi_{32}(B)\nu_w(B) + \pi_{33}(B)\nu_{pv}(B)]$$

Given (12), the final response of consumption to a shock in r_t can be written as⁷:

$$\Psi_{rc}(B) = \Gamma_c(B) + \Theta_w(B) + \Theta_{pv}(B) + \Upsilon_{cw}(B) + \Upsilon_{cpv}(B) \quad (13)$$

Equation (13) shows that the final reaction of consumption, $\Psi_{rc}(B)$, can be broken down into: (1) A direct effect of interest rates on consumption, represented by $\Gamma_c(B)$, (2) an indirect effect coming from variations in W and PV , given by $\Theta_w(B) + \Theta_{pv}(B)$ and (3) a feedback effect, given by $\Upsilon_{cw}(B) + \Upsilon_{cpv}(B)$, due to the reaction of the Central Bank.

The indirect effect has two components:

2.1) The unidirectional effect through the residential wealth, defined as

$$\Theta_w(B) = -\frac{\pi_{12}(B)}{\pi_{11}(B)}\nu_w(B)$$

$\Theta_w(B)$ Arises as the combination of two effects: the effect of r_t on the residential wealth, represented by $\nu_w(B)$, and the effect of the residential wealth on consumption represented by $\frac{\pi_{12}(B)}{\pi_{11}(B)}$. And

2.2) The unidirectional effect through pv_t (price of housing or collateral effect), defined as

$$\Theta_{pv}(B) = -\frac{\pi_{13}(B)}{\pi_{11}(B)}\nu_{pv}(B)$$

$\Theta_{pv}(B)$ also arises as the combination of two effects: the effect of r_t on pv_t represented by $\nu_{pv}(B)$ and the effect of pv_t on consumption, given by $\frac{\pi_{13}(B)}{\pi_{11}(B)}$.

Also, the feedback effect has two components:

⁷The mathematical proof can be found in the algebraic appendix attached to article

3.1) A feedback effect coming from the reaction of the Central Bank to changes in w_t , given by:

$$\Upsilon_{cw}(B) = \frac{\nu_c(B)\nu_w(B)\nu_{rw}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]}$$

and

3.2) The feedback effect due to the reaction of the Central Bank to changes in pv_t , represented by

$$\Upsilon_{cp}(B) = \frac{\nu_c(B)\nu_{pv}(B)\nu_{rpv}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]}$$

Estimation Strategy

The model proposed in (6) and (7) is the VAR model on the levels of the variables which can be estimated directly from the data.

By matching the matrix of variances and covariances as estimated from the error term of the VAR model, to expression (7), V can be estimated. Once V has been estimated, the remaining parameters of the model proposed in (3) and (4) can be uniquely estimated from the estimates of (6). Finally, the impulse response function and its components can be estimated by using (9) and (13) respectively.

III. Empirical analysis

Data

Annual data on the Spanish economy, for the period 1974-2002⁸, has been used.

The variables are:

- C : ‘Domestic Consumption’. This series is built up by the INE, according to the SEC-95 methodology which standardises the annual accounts of EU countries. The data are obtained from the Economics ministry, on the web

⁸The time periods for which the data used are available vary, consumption from 1971 to 2004, housing wealth and housing prices from 1971 to 2002 and the interest rate from 1974 to 2004. Whenever possible, the greater number of data will be used.

(<http://serviciosweb.meh.es/APPS/DGPE/BDSICE/Busquedas/busquedas.aspx>).

The series is measured in real terms (1995 euros)⁹.

- W : ‘Stock of Real Net Housing Wealth’ (millions of 1995 euros). These data are estimates made by the IVIE and BBVA.
(<http://www.ivie.es/banco/stock.php> y
<http://w3.grupobbva.com/TLFB/TLFB-01/-detalle-bases-datos5-CAS.htm>)
- PV : ‘Implicit Deflator of Housing Wealth’, measured as the ratio between nominal and real stock. Both series are obtained from IVIE and BBVA.
- R : ‘MIBOR 1-Month’, obtained from the Bank of Spain
(<http://www.bde.es/infoest/htmls/capit18.htm>).¹⁰.

Univariate analysis and integration orders

In graphs (1), (2), (3) and (4) the series c_t , w_t , pv_t and r_t are presented. The series are clearly nonstationary. Table (1) shows the augmented Dickey-Fuller test (ADF) for the first differences of these variables.

The findings suggest that the ∇c_t and ∇r_t series are stationary, $I(0)$, since the value of the statistic, -3.08 and -4.32, is less than the critical value at 95% confidence. The ∇pv_t series is clearly nonstationary since the value of the statistic, for any number of lags is lower than the critical value. The ∇w_t series is nonstationary since its statistic for $p=3$ is -2.27, less than the critical value of the tables. However, since with other values of p the result is ambiguous, the graphs of ∇pv_t and ∇w_t are presented in (5) and (6). In both graphs it can be seen that the variables ∇pv_t and ∇w_t are nonstationary since they show a negative trend.

In Table (2) the estimates of the univariate ARMA models for the stationary series are presented.

⁹The data with SEC-95 methodology are available up to 1980. Previous data are provided with the growth rate of the National Private Consumption variable.

¹⁰This is a monthly series, analysed by means of the geometrical mean of $(1 + R_t)$

It is important to stress the lack of moving average (MA) operators in the univariate models for $\nabla^2 w_t$ and $\nabla^2 pv_t$. The appearance of MA terms close to invertability would indicate a possible overdifferentiation problems.

The ADF test and the univariate models indicate that the series c_t and r_t are integrated of order 1, I(1). The ADF test, the graphic analysis and the estimation of the univariate models show sufficient evidence in favour of the series w_t and pv_t being I(2).

IV. Empirical VAR Model

Choice of VAR order

In Table (3) the statistic of the likelihood ratio for the different orders of VAR is shown. Due to the fact that the value of the statistic for order 3 is 26.02 higher than the critical value at 90% confidence the null hypothesis that all coefficients of VAR (3) are 0 can be rejected. Thus, the LR test suggests a VAR(3) as the most suitable model.

Additionally, the residual crossed correlation functions, corresponding to a VAR(2) and a VAR (3) are calculated. These functions are presented in graphs (8) and (7).

Some residuals crossed correlations of VAR(2) have significant values which disappear when a VAR(3) is chosen.

Cointegration

In this section possible cointegration relationships are analysed. Assuming that there exists a constant both in the VAR and in the cointegration relationship, Johansen's Test (1991) Johansen (1991) showed two cointegrating equations:

$$\nabla w_t \underset{(0.02)}{-0.16} \nabla pv_t \underset{(0.02)}{+0.06} r_t = \zeta \hat{1}_t \quad (14)$$

$$c_t - 7.61 \nabla pv_t + 1.04 r_t = \zeta_2^{\hat{}}_t \quad (15)$$

(2.03) (2.42)

The relationships $\zeta_1^{\hat{}}_t$ and $\zeta_2^{\hat{}}_t$ are shown in graphs (9) and (10). These show that $\zeta_1^{\hat{}}_t$ can be considered as a cointegration relationship but $\zeta_2^{\hat{}}_t$ cannot, since it shows a clear positive trend.

Due to the great sensitivity of the Johansen's Test to degrees of freedom and for the purpose of making the findings more robust, the methodology of Engle and Granger (1987) is proposed to detect possible cointegration relationships. This methodology is less powerful than the Johansen's Test but less sensitive both to the choice of the order in the multivariate model and to degrees of freedom.

In Table (4) the ADF test for the residual of the regression of each nonstationary variable with the remaining ones is presented. If residuals are stationary, the regression shows a cointegration relationship.

From Table (4) the conclusion can be drawn that there exists a cointegration relationship between ∇w_t and the other variables¹¹. To analyse which variables should be included in the cointegration relationship, in table (5) the ADF test for the residuals of the regression of ∇w_t is presented with the other variables excluded one by one.

From table (5) it can be concluded that c_t should not be in the relationship. The OLS estimation of this relationship is presented in equation (16).

$$\nabla w_t = 0.021 + 0.13 \nabla pv_t - 0.05 r_t + \xi_{1t} \quad (16)$$

(0.002) (0.01) (0.02)

The cointegration relationship estimated in (16) is presented in graph (11).

This relationship is almost identical to (14) obtained by the Johansen method. Because both methods have the same cointegration relationship, it is concluded that this relationship exists and is the only one.

¹¹It could also be concluded that there is a relationship of ∇pv_t with the other variables but later analysis showed that it was the same relationship as with ∇w_t but normalised in another way

The latter is a stationary relationship between the growth rate of housing wealth, the growth rate of house prices and the interest rate. This relationship can be interpreted as the supply of housing in that economy, where new housebuilding, as calculated by the growth rate of housing wealth, positively depends on the increase in house prices and negatively on the interest rate.

VEC Model

By using the cointegration relationship shown in (16) an equation-by-equation specification is given of the corresponding VEC model. The estimation takes place in two stages. In the first the cointegration relationship, $ecm_t = \nabla w_t - 0.13\nabla pv_t + 0.05r_t$ is estimated and, subsequently, the remaining parameters are jointly estimated. The findings appear in Table (6).

The covariance matrix is presented in (17) and the instant correlations matrix is presented in (18). The confidence bands for the instant correlations at 95% are $\pm 2 * SD = \pm 2/\sqrt{n} = \pm 0.38$.

$$\Sigma_u = \begin{pmatrix} 0.00013144710 & 0.00000601234 & 0.00011080650 & -0.00005728316 \\ 0.00000601234 & 0.00000157181 & 0.00000745951 & -0.00001053496 \\ 0.00011080650 & 0.00000745951 & 0.00051477440 & 0.00000739939 \\ -0.00005728316 & -0.00001053496 & 0.00000739939 & 0.00045522570 \end{pmatrix} \quad (17)$$

$$\rho(0) = \begin{pmatrix} 1.00 & 0.42 & 0.43 & -0.23 \\ 0.42 & 1.00 & 0.26 & -0.39 \\ 0.43 & 0.26 & 1.00 & 0.02 \\ -0.23 & -0.39 & 0.02 & 1.00 \end{pmatrix} \quad (18)$$

The residuals graph is presented in (12) and the functions of residuals crossed correlations in graph (13). In none of them can significant correlations be seen, so these findings suggest that model (6) adequately represents the dynamic correlations structure among the variables.

The model in Table (6) once expressed as a nonstationary VAR on the variables of the vector z_t turns out to be the estimated version of the normalised model (6). The covariance matrix shown in (17) is precisely the estimated version of (7). From this covariance matrix, V can be estimated.

$$V = \begin{pmatrix} 1 & 0 & 0 & 0.126 \\ 0 & 1 & 0 & 0.023 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (19)$$

Premultiplying by V the VAR version of the model in Table (6) the orthogonalised model deduced from equation (3), along with the diagonal covariance matrix deduced in equation (4) can be obtained. This orthogonalised model, in its VEC version, is presented in Table (7) along with the instant correlations which are presented in matrix (20).

$$\rho(0) = \begin{pmatrix} 1.00 & 0.36 & 0.44 & 0.00 \\ 0.36 & 1.00 & 0.28 & -0.02 \\ 0.44 & 0.28 & 1.00 & 0.01 \\ 0.00 & -0.02 & 0.01 & 1.00 \end{pmatrix} \quad (20)$$

This model shows the presence of dynamic relationships among all the variables. In the second equation it is observed that when a shock in interest rates takes place, the residential wealth growth rate responds immediately. Nevertheless, the growth rate of housing prices takes two years to react. As can be seen in the third equation, the maladjustments in the cointegration relationship affect the growth rate of housing price rises which adapt to achieve the new equilibrium. The fourth equation of the VEC model shows that the interest rate is not strictly exogenous since it is affected by housing prices. If we assume that housing inflation may be a leading indicator of general inflation, equation 4 would reflect the reaction of

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2
3 the Central Bank in the face of variations in the latter. Finally, the first equation
4
5 indicates that consumption does not contribute to the balance of the new situation,
6
7 since it does not affect either housing wealth or housing prices, but it is affected by
8
9 their evolution and that of interest rates.

10
11 Therefore, faced with an increase in interest rates, an imbalance occurs between
12
13 ∇w_t and ∇pv_t . This imbalance is corrected with an immediate fall of ∇w_t (as in
14
15 empirical life cycle models) and after two years, with a fall in ∇p_t . The interest rate
16
17 rises, as well as the fall in ∇w_t and ∇pv_t , gives rise to a new equilibrium among the
18
19 variables in the real estate sector ,with consumption levels below the initial ones.
20
21 This effect is eased as a consequence of the Central Bank's reaction in reducing
22
23 interest rates when there is a fall in ∇pv_t .
24
25

26 27 **V. Reaction functions to the interest rate**

28
29 On the basis of the orthogonalised model (3), the estimate of which is presented in
30
31 table (7), the reaction function to the normalised impulse, proposed in equation (8)
32
33 is calculated. The reaction function to the step change, that is, the reaction function
34
35 to a permanent unit rise in interest rates, is presented in table (8).
36
37

38
39 As is observed in graph (14)¹² as well as in table (8) a permanent increase in
40
41 interest rates does not generate any instant effect on the growth rate of housing
42
43 prices. In fact, there is a two-year dead period until housing inflation begins to
44
45 react. In the third period a 0.07 percentage point fall in the increase in housing
46
47 prices occurs and from that time onwards, there is a steady drop during 7 periods
48
49 of as much as 0.9 percentage points, where it stays permanently. The fall in housing
50
51 prices is steady, and after 25 years stands at 19.27 %. These findings imply that
52
53 house prices are very sensitive to interest rates, thus supporting the theories pointing
54
55 to financial conditions as the determining components of house prices. Thus, the
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57
58
59
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¹² The bands of confidence of the reactions at 95% are sketched in by discontinuous lines. In the appendix the method used to calculate it is described and the findings presented.

1
2
3 rise in the price of housing since the mid-nineties could be partly accounted for by
4
5 the steady fall in interest rates.
6

7
8 As can be seen in graph (15), as well as in table (8), a permanent rise in interest
9
10 rates produces an immediate fall of 0.02 percentage points in the growth rate of
11
12 housing wealth (pp). Such a rate, interpreted as new housing starts, continues
13
14 to fall till it reaches 0.15 pp, which is permanent in the long term. Unlike what
15
16 happened with housing inflation, where the reaction was prolonged steadily over
17
18 a period of time, the reaction of housing wealth is produced over a small number
19
20 of periods. Thus, in 3 years, there is a 70% reaction and in 4 years nearly 90%,
21
22 showing a highly rapid adjustment. The drop in housing wealth, after 25 years,
23
24 is around 3.53%. These findings indicate that building is very sensitive to interest
25
26 rates, possibly because builders have to finance the product until it is sold and this
27
28 takes on average two years to complete.
29

30
31 As can be observed in graph (17), as well as in table (8), a permanent interest
32
33 rate increase gives rise to a transitory fall in the consumption growth rate, since its
34
35 reaction peters out over time (16 years). A rate increase produces an immediate
36
37 0.13% fall. This fall increases over the following period and after a brief rally at 5
38
39 years, the fall in the growth rate of consumption declines to 0.

40
41 Consumption, as can be seen in graph (16), falls immediately by 0.13%. The
42
43 fall in consumption grows steadily till it reaches 1.33%, in the long term. As far
44
45 as the speed of reaction is concerned, it can be seen that in 5 years 68% of the
46
47 consumption reaction takes place and in 7 years 93%, showing a relatively quick
48
49 adjustment. Finally, it is important to note that albeit in the long run the effect
50
51 may be a 1.33% fall, the fact that the rate only increases by 0.66% means that the
52
53 effect of consumption of a one point interest rise is 1.98%. Such a fall is similar to
54
55 the drop in consumption in the 1993 crisis where it stood at 2% .
56

57
58 The previous findings are compatible with the following economic explanation.
59
60 In immediate fashion the interest rate reduces consumption by making credit more
expensive. What is more, an increase in rates reduces housing wealth immediately

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2
3 since it makes financing dearer for builders. In two years there is a fall in the
4 growth rate in housing prices, due to the fall in demand. The fall in the growth rate
5 in house prices puts the brake on new housebuilding even more, on the supply side.
6
7 The behaviour of housing wealth and housing prices has effects on consumption
8 by reducing it further. However, as the price of housing (and inflation) falls, the
9 Central Bank begins to reduce interest rates, thus generating a positive effect on
10 consumption. As the periods go by, both the negative effects and the positive ones
11 run out till, finally, the total drop in consumption is 1.33%.

12
13 It is important to note that the nature of the reactions to permanent rate changes
14 is due to the integration orders of the variables. Thus, since r_t is I(1) a permanent
15 increase of r_t has permanent effects on c_t and transitory ones on ∇c_t . Since both w_t
16 and pv_t are I(2), a permanent increase in r_t has permanent effects on ∇w_t as well
17 as on ∇pv_t .

31 VI. Estimation of the components of consumption reaction

32
33 In this section an analysis is made of the effect of the interest rate on consumer
34 reaction, by separating its different components. Thus, the effect of the interest rate
35 subdivides into a direct effect brought on by the rise in the cost of credit and an
36 indirect effect resulting from variations in housing wealth and its price. This analysis
37 makes it possible to reach the conclusion as to what the most important factors in
38 the fall in consumption are.

39 From estimates of $\nu_c(B)$, $\nu_w(B)$ and $\nu_p(B)$ it can be obtained estimates of $\Gamma_c(B)$,
40 $\Theta_w(B)$, $\Theta_p(B)$ and $\Upsilon_{cp}(B)$ (see the algebraic appendix attached to this article).
41 Table (9) shows these findings. It is important to note that, because $\nu_{rw} = 0$ then
42 $\Upsilon_{cw}(B) = 0$ too, that is, it is not detected any response of the Central Bank to
43 changes in wealth.

44 As it can be seen in table (9), the effect exerted by the interest rate upon long-
45 term consumption can be separated into: (1) a 0.53% drop due to the direct effect,
46 (2) a 0.96% fall due to the role of housing wealth, (3) a 0.48% fall as a result of the

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2
3 unidirectional effect of housing prices and (4) a 0.66% rise due to the feedback effect
4 also generated by housing prices.
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6

7
8 In more detailed form, it can be observed that if the interest rate shows a per-
9 manent 1% rise there is an immediate, direct 0.13% drop in consumption. In the
10 following two periods the direct fall in consumption grows steadily till it reaches
11 0.43%. This fall represents 80% of the fall generated by the interest rate, in direct
12 form, on consumption and shows how much of the effect is produced in the first two
13 years.
14
15
16
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18

19
20 From the third year onwards, the fall in consumption begins, due to the real
21 estate market. Thus, in that same year, there is a 0.17% drop in consumption as a
22 consequence of housing wealth and house prices that show a 0.17% and 0.06% fall,
23 respectively. In the following periods the falls continue. In the long term, after 10
24 years, the housing wealth drop is a 0.84% and that of house prices 0.42%.
25
26
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30 The unidirectional effect is partially offset by the feedback effect. During the first
31 four years there was no feedback effect since housing prices did not react. Nonethe-
32 less, as housing prices began to fall, the Central Bank could reduce interest rates
33 thus bringing about an increase of consumption. In the fifth period this increase was
34 0.05%, an effect which continues to grow steadily till it produces a 0.66 percentage
35 point rise in long-term consumption.
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38
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42 Of the negative effects on consumption the one caused by housing wealth is the
43 most important. The collateral effect, as a consequence of the rise in house prices,
44 is half the previous one.
45
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49

50 **VII. Conclusions**

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52
53 Using data on the Spanish economy, the effect of a permanent increase in the interest
54 rate on consumption, housing wealth and housing prices has been estimated.
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57 For this purpose a theoretical model is proposed which would enable the reaction
58 of the variables to be identified without restricting any of their statistical properties.
59 Such a theoretical model, moreover, allows consumer reaction to be split into four
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3 components: (1) the direct reaction, related to the rise in the cost of consumer
4 credit, (2) the component stemming from the variations in housing wealth, (3) the
5 one due to variations in housing prices and (4) the feedback effect coming from the
6 reaction of the Central Bank.
7
8

9
10
11 From a qualitative viewpoint, a permanent rise in interest rates has a permanent
12 negative effect on consumption, the growth rate of housing wealth and the growth
13 rate of housing prices. All of these findings are in line with most of the previous
14 works. Specifically, a permanent one percentage point increase in rates gives rise to:
15
16

17
18 (1) A permanent drop in the growth rate of wealth of 0.15 percentage points.
19
20 (2) A permanent fall of 0.9 percentage points in the growth rate of housing prices.
21
22 This finding would partially account for the increase in housing prices in Spain from
23 the mid-nineties. (3) A permanent drop in consumption of 1.33 percentage points.
24
25 Of these, 0.53 points are a result of the direct effect of rates on consumption, by
26 making credit more expensive, 0.96 points to housing wealth effect, 0.48 points to
27 the unidirectional effect of house prices by reducing collateral and, -0.66 points from
28 the feedback effect, a positive one on consumption, which brings with it a reduction
29 in rates decided by the Central Bank as a response to an easing in prices.
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38 In the long run, the most important component of the consumption final response
39 is that of housing wealth, followed by the direct component and the price component.
40
41 In the short run, the direct component, as would be expected, dominates the others.
42
43
44

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46
47
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Appendix

Appendix 1. Bands of confidence for the response functions

Bands of confidence are obtained by means of the bootstrap method. By using this method with 100 iterations the sample distribution of responses is obtained. The confidence bands at 95% are obtained in accordance with the criteria of Efron and Tibshirani (2003).

Appendix 2. Algebraic Appendix

Breakdown of Effects: Proof

From Matrices Inversion lemma:

$$(A - gh')^{-1} = \left(I + A^{-1} \frac{gh'}{1 - h'A^{-1}g} \right) A^{-1}$$

Making $A = I$, $g = \nu_z(B)$ and $h' = \nu_r(B)$:

$$[I - \nu_z(B)\nu_r(B)]^{-1} = I + \frac{\nu_z(B)\nu_r(B)}{1 - \nu_r(B)\nu_z(B)} \quad (1)$$

where

$$\nu_z(B)\nu_r(B) = \begin{pmatrix} \nu_c(B) \\ \nu_w(B) \\ \nu_{pv}(B) \end{pmatrix} \cdot (\nu_{rc}(B), \nu_{rw}(B), \nu_{rpv}(B)) =$$

$$\begin{pmatrix} \nu_c(B)\nu_{rc}(B) & \nu_c(B)\nu_{rw}(B) & \nu_c(B)\nu_{rpv}(B) \\ \nu_w(B)\nu_{rc}(B) & \nu_w(B)\nu_{rw}(B) & \nu_w(B)\nu_{rpv}(B) \\ \nu_{pv}(B)\nu_{rc}(B) & \nu_{pv}(B)\nu_{rw}(B) & \nu_{pv}(B)\nu_{rpv}(B) \end{pmatrix}$$

and

$$\nu_r(B)\nu_z(B) = (\nu_{rc}(B), \nu_{rw}(B), \nu_{rpv}(B)) \cdot \begin{pmatrix} \nu_c(B) \\ \nu_w(B) \\ \nu_{pv}(B) \end{pmatrix} = \\ \nu_{rc}(B)\nu_c(B) + \nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)$$

Thus,

$$1 - \nu_r(B)\nu_z(B) = 1 - [\nu_{rc}(B)\nu_c(B) + \nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]$$

and

$$\frac{\nu_z(B)\nu_r(B)}{1 - \nu_r(B)\nu_z(B)} = \begin{pmatrix} \frac{\nu_c(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_w(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_{pv}(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \end{pmatrix}$$

Then:

$$I + \frac{\nu_z(B)\nu_r(B)}{1 - \nu_r(B)\nu_z(B)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \begin{pmatrix} \frac{\nu_c(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_w(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_{pv}(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \end{pmatrix} = \\ \begin{pmatrix} 1 + \frac{\nu_c(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_w(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & 1 + \frac{\nu_w(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \\ \frac{\nu_{pv}(B)\nu_{rc}(B)}{1 - \nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rw}(B)}{1 - \nu_r(B)\nu_z(B)} & 1 + \frac{\nu_{pv}(B)\nu_{rpv}(B)}{1 - \nu_r(B)\nu_z(B)} \end{pmatrix}$$

Since:

$$1 + \frac{\nu_i(B)\nu_{ri}(B)}{1 - \nu_r(B)\nu_z(B)} = \frac{[1 - \nu_r(B)\nu_z(B)] + \nu_i(B)\nu_{ri}(B)}{1 - \nu_r(B)\nu_z(B)}$$

A detailed form of (1) becomes:

$$\begin{pmatrix} \frac{[1-\nu_r(B)\nu_z(B)]+\nu_c(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_c(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_c(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \\ \frac{\nu_w(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{[1-\nu_r(B)\nu_z(B)]+\nu_w(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \\ \frac{\nu_{pv}(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{[1-\nu_r(B)\nu_z(B)]+\nu_{pv}(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \end{pmatrix} \quad (2)$$

The first row of the expression:

$$\Psi_r(B) = [I - \nu_z(B)\nu_r(B)]^{-1}\nu_z(B)\pi_r(B)^{-1} =$$

$$\begin{pmatrix} \frac{[1-\nu_r(B)\nu_z(B)]+\nu_c(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_c(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_c(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \\ \frac{\nu_w(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{[1-\nu_r(B)\nu_z(B)]+\nu_w(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_w(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \\ \frac{\nu_{pv}(B)\nu_{rc}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{\nu_{pv}(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} & \frac{[1-\nu_r(B)\nu_z(B)]+\nu_{pv}(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \end{pmatrix} \cdot \begin{pmatrix} \nu_c(B) \\ \nu_w(B) \\ \nu_{pv}(B) \end{pmatrix} \cdot \pi_r(B) \quad (3)$$

is

$$\begin{aligned} \Psi_{rc}(B) &= \left[\frac{[1-\nu_r(B)\nu_z(B)]+\nu_c(B)\nu_{rc}(B)\nu_c(B)}{1-\nu_r(B)\nu_z(B)} \right] \pi_r(B)^{-1} + \\ &+ \left[\frac{\nu_c(B)\nu_w(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} + \frac{\nu_c(B)\nu_{pv}(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \right] \pi_r(B)^{-1} \end{aligned}$$

If $\nu_{rc}(B) = 0$:

$$\Psi_{rc}(B) = \left[\nu_c(B) + \frac{\nu_c(B)\nu_w(B)\nu_{rw}(B)}{1-\nu_r(B)\nu_z(B)} + \frac{\nu_c(B)\nu_{pv}(B)\nu_{rpv}(B)}{1-\nu_r(B)\nu_z(B)} \right] \pi_r(B)^{-1} \quad (4)$$

where

$$1 - \nu_r(B)\nu_z(B) = 1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]$$

since $\nu_{rc}(B) = 0$, (4) becomes:

$$\begin{aligned} \Psi_{rc}(B) = & \nu_c(B)\pi_r(B)^{-1} + \left[\frac{\nu_c(B)\nu_w(B)\nu_{rw}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]} \right] \pi_r(B)^{-1} + \\ & + \left[\frac{\nu_c(B)\nu_{pv}(B)\nu_{rpv}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]} \right] \pi_r(B)^{-1} \end{aligned} \quad (5)$$

Equation (5) shows that $\Psi_{rc}(B)$ can be broken down into two components: (1) An unidirectional response from interest rate to consumption, represented by $\nu_c(B)$, and (2) the sum of two feedback effects:

i. the feedback effect due to the residential wealth:

$$\frac{\nu_c(B)\nu_w(B)\nu_{rw}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]}$$

ii. the feedback effect due to the housing price:

$$\frac{\nu_c(B)\nu_{pv}(B)\nu_{rpv}(B)}{1 - [\nu_{rw}(B)\nu_w(B) + \nu_{rpv}(B)\nu_{pv}(B)]}$$

If we represent the residential wealth feedback effect by $\Upsilon_{cw}(B)$ and the housing price feedback effect by $\Upsilon_{cpv}(B)$ then the reaction of consumption to the interest rate can be written as (6).

$$\Psi_{rc}(B) = \nu_c(B) + \Upsilon_{cw}(B) + \Upsilon_{cpv}(B) \quad (6)$$

Moreover, it was pointed out in section (II) that the direct effect of the interest rate on consumption can be obtained from the structural model and takes the form:

$$\Gamma_c(B) = \left[\nu_c(B) + \frac{\pi_{12}(B)}{\pi_{11}(B)}\nu_w(B) + \frac{\pi_{13}(B)}{\pi_{11}(B)}\nu_{pv}(B) \right] \quad (7)$$

Then,

$$\nu_c(B) = \Gamma_c(B) + \Theta_w(B) + \Theta_p(B) \quad (8)$$

Where

$$\Theta_w(B) = -\frac{\pi_{12}(B)}{\pi_{11}(B)}\nu_w(B)$$

is the unidirectional indirect effect of interest rates on consumption, throughout housing, because $\Theta_w(B)$ is the combination of two effects: (1) the effect of interest rate on residential wealth, represented by $\nu_w(B)$ and (2) the effect of housing prices on consumption, represented by $\frac{\pi_{12}(B)}{\pi_{11}(B)}$.

And

$$\Theta_{pv}(B) = -\frac{\pi_{13}(B)}{\pi_{11}(B)}\nu_{pv}(B)$$

is the unidirectional indirect effect of interest rate on consumption through housing prices, because $\Theta_{pv}(B)$ is the combination of two effects: (1) the effect of interest rate on housing price represented by $\nu_{pv}(B)$ and (2) the effect of housing prices on consumption, represented by $\frac{\pi_{13}(B)}{\pi_{11}(B)}$.

Finally, (9) is obtained by substituting (8) in (6):

$$\Psi_{rc}(B) = [\Gamma_c(B) + \Theta_w(B) + \Theta_p(B) + \Upsilon_{cw}(B) + \Upsilon_{cpv}(B)]\pi_r(B)^{-1} \quad (9)$$

Identification of the polynomials in the CRF

The theoretical model presented in Section (II) can be written in its most detailed form as:

$$\begin{bmatrix} \pi_{11}(B) & \pi_{12}(B) & \pi_{13}(B) & -\pi_{11}(B)\nu_c(B) - \pi_{12}(B)\nu_w(B) - \pi_{13}(B)\nu_{pv}(B) \\ \pi_{21}(B) & \pi_{22}(B) & \pi_{23}(B) & -\pi_{21}(B)\nu_c(B) - \pi_{22}(B)\nu_w(B) - \pi_{23}(B)\nu_{pv}(B) \\ \pi_{31}(B) & \pi_{32}(B) & \pi_{33}(B) & -\pi_{31}(B)\nu_c(B) - \pi_{32}(B)\nu_w(B) - \pi_{33}(B)\nu_{pv}(B) \\ -\pi_r(B)\nu_{rc}(B) & -\pi_r(B)\nu_{rw}(B) & -\pi_r(B)\nu_{rpv}(B) & \pi_r(B) \end{bmatrix} \begin{bmatrix} c_t \\ \nabla w_t \\ \nabla pv_t \\ r_t \end{bmatrix} = \begin{bmatrix} \alpha_{ct} \\ \alpha_{wt} \\ \alpha_{pvt} \\ \alpha_{rt} \end{bmatrix} \quad (10)$$

From an estimated VEC model and using (11)

$$VY_t = VD + V(I_k + \Pi + \Gamma_1)Y_{t-1} + V(\Gamma_2 - \Gamma_1)Y_{t-1} - V\Gamma_2Y_{t-3} + V\epsilon_t \quad (11)$$

It can be estimated the orthogonalized VAR model in (10):

$$\begin{pmatrix} (1 - 1.47B)\nabla & -2.31B^2\nabla & -0.19B\nabla & (0.126 + 0.126B)\nabla \\ 0.00 & (1 - 0.352B - 0.226B^2)\nabla & -0.01B\nabla & (0.023 + 0.03B + 0.03B^2)\nabla \\ 0.00 & -5.84B & 1 - 0.24B & -0.29B \\ 0.00 & 0.00 & -0.38B\nabla & 1 - B \end{pmatrix} \cdot \begin{pmatrix} c_t \\ \nabla w_t \\ \nabla pv_t \\ r_t \end{pmatrix} = \begin{pmatrix} 0.015 \\ 0 \\ -0.12 \\ 0 \end{pmatrix} + \begin{pmatrix} \epsilon_{c_t} \\ \epsilon_{w_t} \\ \epsilon_{pv_t} \\ \epsilon_{r_t} \end{pmatrix} \quad (12)$$

That is, the estimated version of the theoretical model proposed in (3).

From (12), estimates of:

$$\begin{aligned} -\pi_{11}(B)\nu_c(B) - \pi_{12}(B)\nu_w(B) - \pi_{13}(B)\nu_{pv}(B) &= a(B) \\ -\pi_{21}(B)\nu_c(B) - \pi_{22}(B)\nu_w(B) - \pi_{23}(B)\nu_{pv}(B) &= b(B) \\ -\pi_{31}(B)\nu_c(B) - \pi_{32}(B)\nu_w(B) - \pi_{33}(B)\nu_{pv}(B) &= c(B) \end{aligned} \quad (13)$$

and $\pi_{ij}(B)$ polynomials in (10) can be obtained directly.

The system (13) can be solved using a computer program of numerical and symbolic calculus, yielding estimates of $\nu_w(B)$, $\nu_{pv}(B)$ and $\nu_c(B)$:

$$\nu_c(B) = \frac{-0.126 - 0.087B + 0.10B^2 - 0.09B^3 - 0.10B^4 + 0.02B^5}{1 - 1.06B + 0.08B^2 + 0.14B^3 - 0.025B^4} \quad (14)$$

$$\nu_w(B) = \frac{-0.023 - 0.024B - 0.02B^2 + 0.007B^3}{1 - 0.59B - 0.19B^2 + 0.054B^3} \quad (15)$$

$$\nu_{pv}(B) = \frac{0.16B - 0.28B^2 - 0.24B^3}{1 - 0.59B - 0.19B^2 + 0.054B^3} \quad (16)$$

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Appendix 3. Data

The data are presented in table (11)

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Table 1. ADF Test for the ∇ series

ADF ^a	p=1	p=2	p=3	p=4
∇c_t	-3.08	-2.72	-2.58	-4.39
∇w_t	-4.54	-4.59	-2.27	-3.09
∇pv_t	-1.50	-1.98	-1.61	-2.01
∇r_t	-4.32	-3.68	-3.47	-2.02

^aNote: $H_0 : \rho = 1$ in the model $\nabla^2 z_t = \mu + \rho \nabla z_{t-1} + \sum_{j=1}^p \gamma_j \nabla^2 z_{t-j} + u_t$. The critical value at 95% is -2.96 (MacKinnon). For r_t , $\mu = 0$ and the critical value at 95% is -1.95 (MacKinnon)

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Table 2. Univariate Model

variable ^a	ϕ	μ	σ_a %	Q(4)
∇c_t	0.61 (0.12)	0.024 (0.007)	1.59	3.23
$\nabla^2 w_t$	0.56 (0.15)	-	0.21	2.11
$\nabla^2 pv_t$	-	-	3.87	3.85
∇r_t	-	-	2.3	2.46

^aNote: The specification of the univariate model for the stationary series (z_t) is $(1 - \phi)[z_t - \mu] = a_t$. The SD are presented in brackets. σ_a , is the typical residual deviation and Q(4) is the Ljung-Box statistic for 4 lags.

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Table 3. likelihood ratio for selecting the order of VAR

Orden ^a	0	1	2	3	4
Ratio de Verosimilitud (LR)	NA	159.6518	37.79070	26.02069	22.95179

^aThe statistic LR is computed in the following way $LR = (T - m)(\log|\Omega_{l-1}| - \log|\Omega_l|)$ where l is the order of the test. LR is distributed as a chi-squared with 16 degrees of freedom. The critical values for a chi-squared with 16 degrees of freedom are 23.54 at 90% and 26.3 at 95%

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Table 4. Engle-Granger Approach for cointegration

Dependent var	p=0	p=1	p=2	p=3	p=4
c_t	-2.85	-2.95	-2.53	-2.33	-2.50
∇w_t	-4.06	-2.65	-4.47	-3.93	-2.59
∇pv_t	-4.03	-2.48	-4.1	-3.26	-2.29
r_t	-3.13	-2.75	-2.99	-2.58	-2.33

The critical value(95 %) is -4.11 (Phillips and Ouliaris (1990))

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Table 5. Engle-Granger Approach for cointegration with ∇w_t

Excluded variable	p=0	p=1	p=2	p=3	p=4
c_t	-4.60	-2.89	-5.25	-4.49	-2.99
∇pv_t	-2.40	-1.73	-2.40	-2.51	-3.06
r_t	-3.25	-2.42	-2.01	-1.40	-2.13

The critical value (95 %) is -3.77 (Phillips and Ouliaris (1990))

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Table 6. Estimation of the VEC model

dependent variable	equations ^a			
	∇c_t	$\nabla^2 w_t$	$\nabla^2 pv_t$	∇r_t
μ	0.015 (0.004)		-0.12 (0.02)	
ecm_{t-1}			5.84 (1.16)	
∇c_{t-1}	0.47 (0.10)			
$\nabla^2 w_{t-1}$		0.35 (0.14)		
$\nabla^2 pv_{t-1}$	0.14 (0.07)			0.38 (0.13)
∇r_{t-1}	-0.16 (0.08)	-0.03 (0.01)		
∇c_{t-2}				
$\nabla^2 w_{t-2}$	2.31 (0.89)	0.23 (0.12)		
$\nabla^2 pv_{t-2}$				
∇r_{t-2}		-0.03 (0.01)		

^aThe table shows the estimated coefficients of the VEC model where each column represents an equation of the same. The SD are presented in brackets. The term *ecm* represents the cointegration relationship.

Table 7. VEC Orthogonalised Model

Dependent variable	ecuaciones			
	∇c_t	$\nabla^2 w_t$	$\nabla^2 pv_t$	∇r_t
μ	0.015		-0.12	
ecm_{t-1}			5.84	
∇c_{t-1}	0.47			
$\nabla^2 w_{t-1}$		0.35		
$\nabla^2 pv_{t-1}$	0.19	0.01		0.38
∇r_{t-1}	-0.16	-0.03		
∇c_{t-2}				
$\nabla^2 w_{t-2}$	2.31	0.23		
$\nabla^2 pv_{t-2}$				
∇r_{t-2}		-0.03		
∇r_t	-0.13	-0.02		

Table 8. Reaction to a permanent interest rate shock

years	∇c_t	∇w_t	∇pv_t^a	∇r_t	ecm_t	c_t	w_t	pv_t	r_t
1	-0.13	-0.02	0.00	1.00	0.03	-0.13	-0.02	0.00	1.00
2	-0.22	-0.06	0.00	0.00	-0.01	-0.35	-0.08	0.00	1.00
3	-0.16	-0.11	-0.07	0.00	-0.05	-0.50	-0.20	-0.07	1.00
4	-0.17	-0.14	-0.37	-0.03	-0.04	-0.68	-0.33	-0.44	0.97
5	-0.23	-0.16	-0.60	-0.11	-0.03	-0.91	-0.49	-1.04	0.86
6	-0.18	-0.16	-0.80	-0.09	-0.02	-1.09	-0.65	-1.84	0.77
7	-0.15	-0.17	-0.93	-0.08	-0.01	-1.24	-0.82	-2.77	0.69
8	-0.09	-0.16	-0.99	-0.05	0.00	-1.33	-0.98	-3.76	0.65
9	-0.05	-0.16	-1.00	-0.02	0.00	-1.38	-1.14	-4.76	0.62
10	-0.01	-0.15	-0.99	0.00	0.00	-1.39	-1.29	-5.75	0.62
11	0.01	-0.15	-0.96	0.01	0.00	-1.39	-1.45	-6.71	0.63
12	0.02	-0.15	-0.93	0.01	0.00	-1.37	-1.59	-7.64	0.64
13	0.02	-0.15	-0.91	0.01	0.00	-1.36	-1.74	-8.55	0.65
14	0.01	-0.15	-0.89	0.01	0.00	-1.34	-1.89	-9.44	0.66
15	0.01	-0.15	-0.89	0.01	0.00	-1.33	-2.04	-10.33	0.66
16	0.01	-0.15	-0.89	0.00	0.00	-1.33	-2.19	-11.21	0.66
17	0.00	-0.15	-0.89	0.00	0.00	-1.32	-2.34	-12.10	0.66
18	0.00	-0.15	-0.89	0.00	0.00	-1.32	-2.49	-12.99	0.66
19	0.00	-0.15	-0.89	0.00	0.00	-1.33	-2.64	-13.89	0.66
20	0.00	-0.15	-0.90	0.00	0.00	-1.33	-2.79	-14.78	0.66
21	0.00	-0.15	-0.90	0.00	0.00	-1.33	-2.93	-15.68	0.66
22	0.00	-0.15	-0.90	0.00	0.00	-1.33	-3.08	-16.58	0.66
23	0.00	-0.15	-0.90	0.00	0.00	-1.33	-3.23	-17.48	0.66
24	0.00	-0.15	-0.90	0.00	0.00	-1.33	-3.38	-18.38	0.66
25	0.00	-0.15	-0.90	0.00	0.00	-1.33	-3.53	-19.27	0.66

^aThe effect in the second period on ∇pv_t estimated is 0.16 but due to it being within the bands of confidence the idea of it being 0 cannot be rejected.

Table 9. Consumption: Separation of effects

years	Ψ_{bc}	$\Gamma_c(B)$	$\Theta_w(B)$	$\Theta_p(B)$	Υ_{cp}
0	-0.13	-0.13	0.00	0.00	0.00
1	-0.35	-0.38	0.00	0.03	0.00
2	-0.48	-0.43	-0.05	0.01	-0.01
3	-0.67	-0.42	-0.17	-0.06	-0.01
4	-0.90	-0.44	-0.33	-0.14	0.01
5	-1.09	-0.45	-0.46	-0.22	0.05
6	-1.24	-0.47	-0.58	-0.28	0.09
7	-1.33	-0.49	-0.67	-0.33	0.15
8	-1.38	-0.50	-0.74	-0.36	0.23
9	-1.39	-0.51	-0.80	-0.39	0.31
10	-1.38	-0.51	-0.84	-0.42	0.39
11	-1.36	-0.52	-0.87	-0.43	0.46
12	-1.34	-0.52	-0.90	-0.45	0.52
13	-1.33	-0.53	-0.92	-0.46	0.57
14	-1.32	-0.53	-0.93	-0.46	0.60
15	-1.31	-0.53	-0.94	-0.47	0.63
16	-1.31	-0.53	-0.95	-0.47	0.64
17	-1.31	-0.53	-0.95	-0.48	0.65
18	-1.31	-0.53	-0.96	-0.48	0.66

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Table 10. Bands of confidence for the ERF of r_t

Years	c_t		∇w_t		∇pv_t		r_t	
	lower	higher	lower	higher	lower	higher	lower	higher
1	-0.29	0.09	-0.05	0.00	0.00	0.00	0.71	1.14
2	-0.75	0.05	-0.10	-0.03	0.00	0.27	0.71	1.14
3	-1.13	-0.02	-0.18	-0.07	-0.27	0.14	0.74	1.23
4	-1.49	-0.11	-0.22	-0.08	-0.75	-0.06	0.66	1.16
5	-1.92	-0.29	-0.25	-0.09	-1.12	-0.20	0.53	1.03
6	-2.29	-0.38	-0.26	-0.10	-1.42	-0.33	0.37	0.96
7	-2.57	-0.44	-0.25	-0.09	-1.60	-0.36	0.22	0.92
8	-2.83	-0.44	-0.25	-0.09	-1.68	-0.37	0.13	0.88
9	-2.96	-0.43	-0.24	-0.09	-1.67	-0.38	0.16	0.87
10	-3.00	-0.42	-0.24	-0.09	-1.67	-0.39	0.17	0.88
11	-2.97	-0.41	-0.23	-0.09	-1.64	-0.39	0.16	0.89
12	-2.97	-0.40	-0.23	-0.09	-1.57	-0.38	0.18	0.90
13	-2.95	-0.40	-0.23	-0.09	-1.51	-0.36	0.22	0.91
14	-2.93	-0.40	-0.23	-0.09	-1.48	-0.36	0.24	0.91
15	-2.92	-0.41	-0.23	-0.09	-1.47	-0.37	0.27	0.91
16	-2.92	-0.41	-0.23	-0.09	-1.46	-0.37	0.28	0.91
17	-2.92	-0.41	-0.23	-0.09	-1.45	-0.37	0.28	0.91
18	-2.92	-0.41	-0.23	-0.09	-1.46	-0.37	0.27	0.90
19	-2.92	-0.41	-0.23	-0.09	-1.47	-0.37	0.27	0.90
20	-2.92	-0.41	-0.23	-0.09	-1.48	-0.37	0.26	0.90
21	-2.93	-0.41	-0.23	-0.09	-1.48	-0.37	0.25	0.90
22	-2.93	-0.41	-0.23	-0.09	-1.48	-0.37	0.24	0.90
23	-2.93	-0.41	-0.23	-0.09	-1.48	-0.37	0.24	0.90
24	-2.93	-0.41	-0.23	-0.09	-1.48	-0.37	0.24	0.91
25	-2.93	-0.41	-0.23	-0.09	-1.48	-0.37	0.24	0.91

Table 11. Data

years	Consumption	Housing Wealth	Price of Housing	Interest reat
1974	171872	433701	10.03	1.118
1975	174965	454592	12.51	1.102
1976	184764	475290	14.90	1.127
1977	187535	495230	18.77	1.153
1978	189223	513513	23.29	1.211
1979	191683	530001	29.06	1.162
1980	192833	545863	34.07	1.157
1981	190890	561548	38.16	1.156
1982	190962	576650	43.00	1.159
1983	191710	590611	46.34	1.200
1984	191304	603446	49.82	1.143
1985	195670	616196	52.31	1.120
1986	202251	629329	58.84	1.117
1987	214272	643321	63.65	1.161
1988	224637	659351	69.50	1.115
1989	236673	675817	74.51	1.148
1990	244836	693521	80.35	1.150
1991	251768	710122	85.50	1.133
1992	257141	725552	88.77	1.133
1993	251899	739974	92.48	1.122
1994	254285	754068	95.40	1.079
1995	258645	769339	100.00	1.092
1996	264242	786508	102.86	1.076
1997	272621	803398	105.74	1.055
1998	284482	822513	108.26	1.043
1999	297733	843658	115.01	1.028
2000	309908	867001	126.11	1.042
2001	318641	890417	135.40	1.043
2002	327695	915236	144.63	1.033

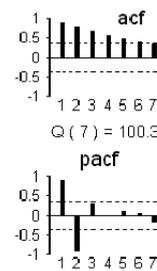
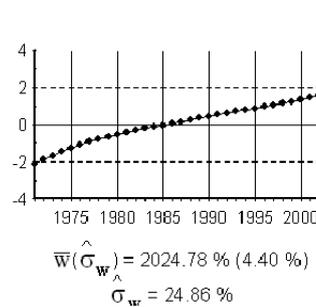
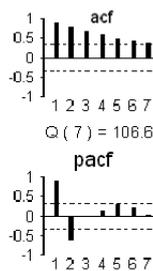
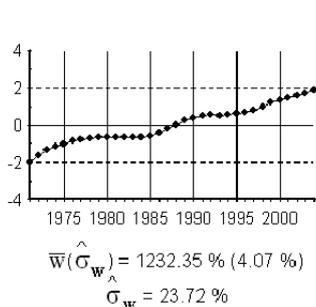


Figure 1. c_t

Figure 2. w_t

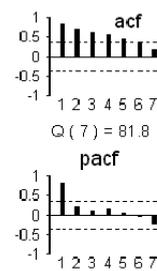
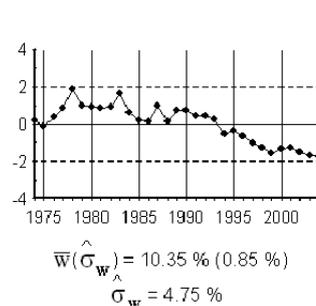
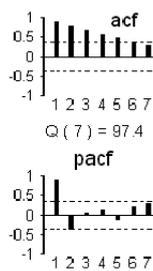
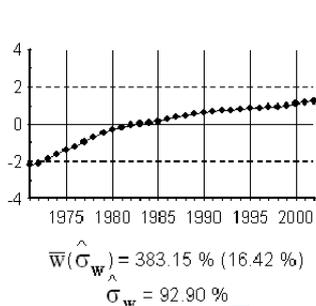


Figure 3. pv_t

Figure 4. r_t

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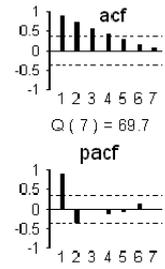
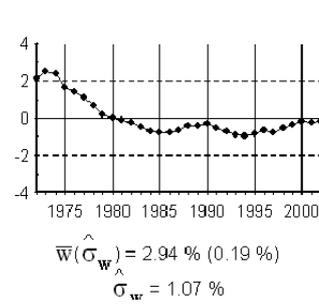
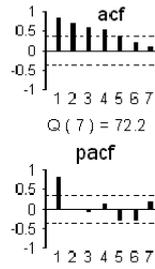
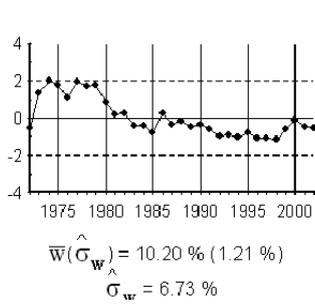


Figure 5. ∇pv_t

Figure 6. ∇w_t

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Crosscorrelations

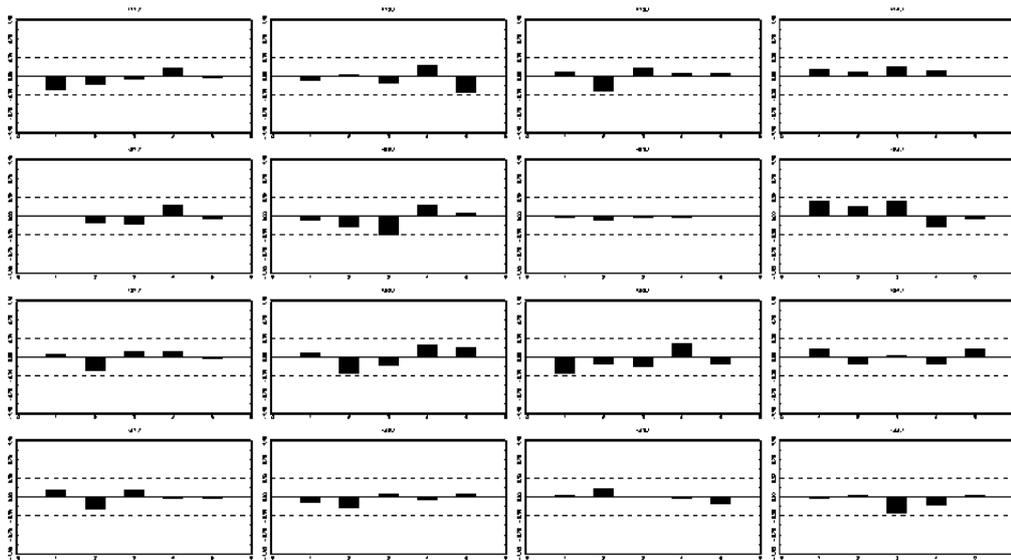


Figure 7. CCF of VAR(3)

Crosscorrelations

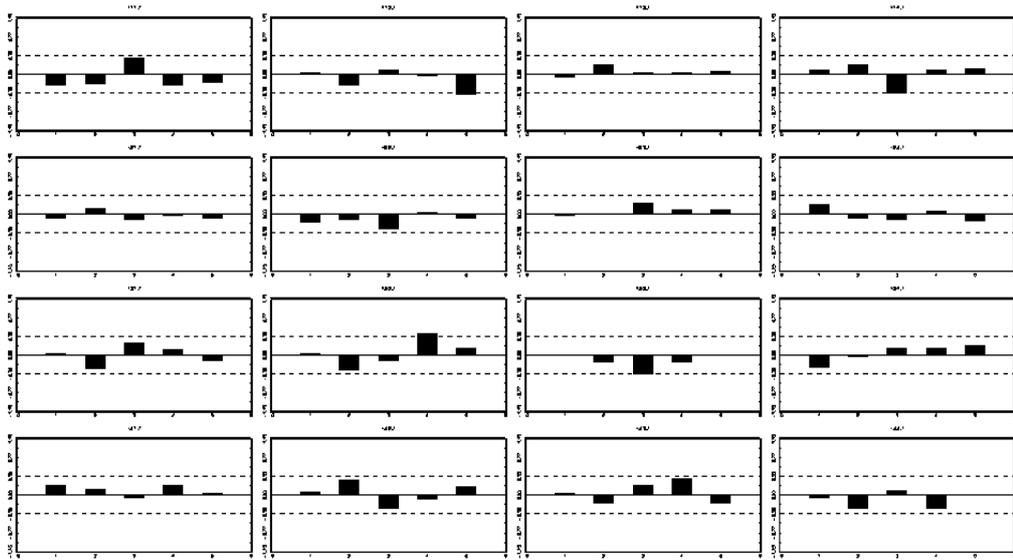


Figure 8. CCF of VAR(2)

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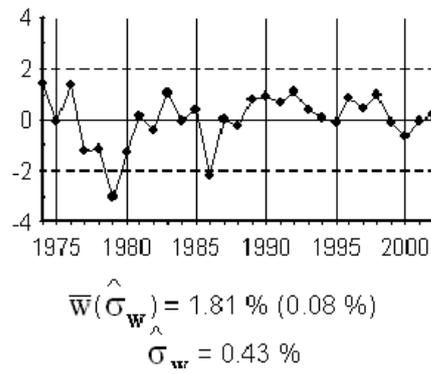


Figure 9. $\hat{\epsilon}_{2t}$

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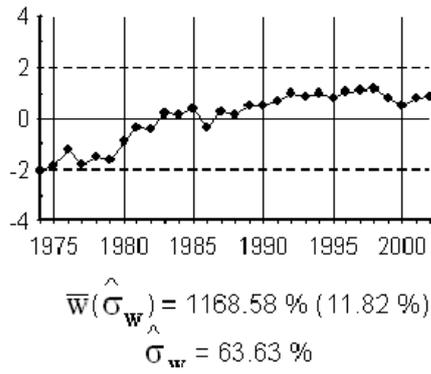
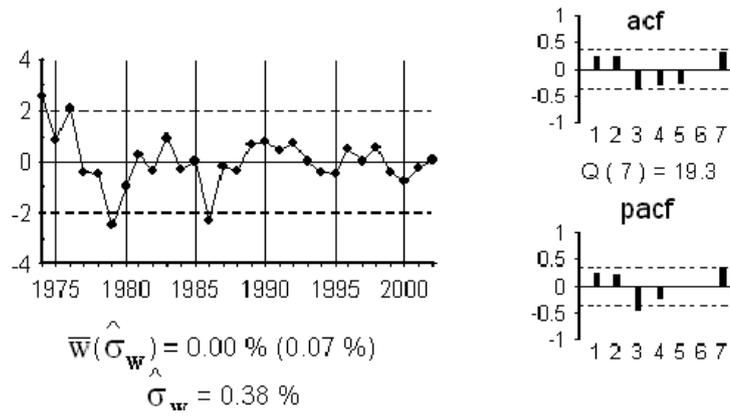


Figure 10. $\hat{\epsilon}_t$

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Figure 11. ecm_t

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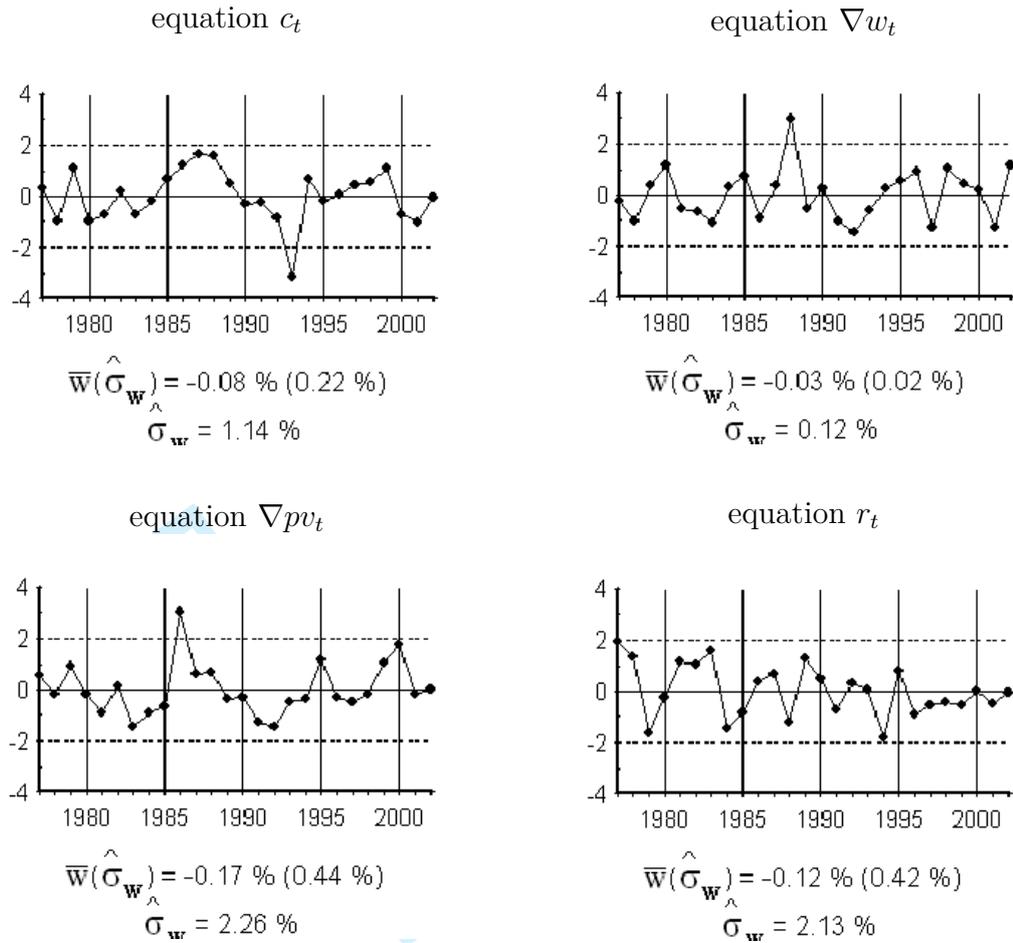


Figure 12. Residuals of the model

Crosscorrelations

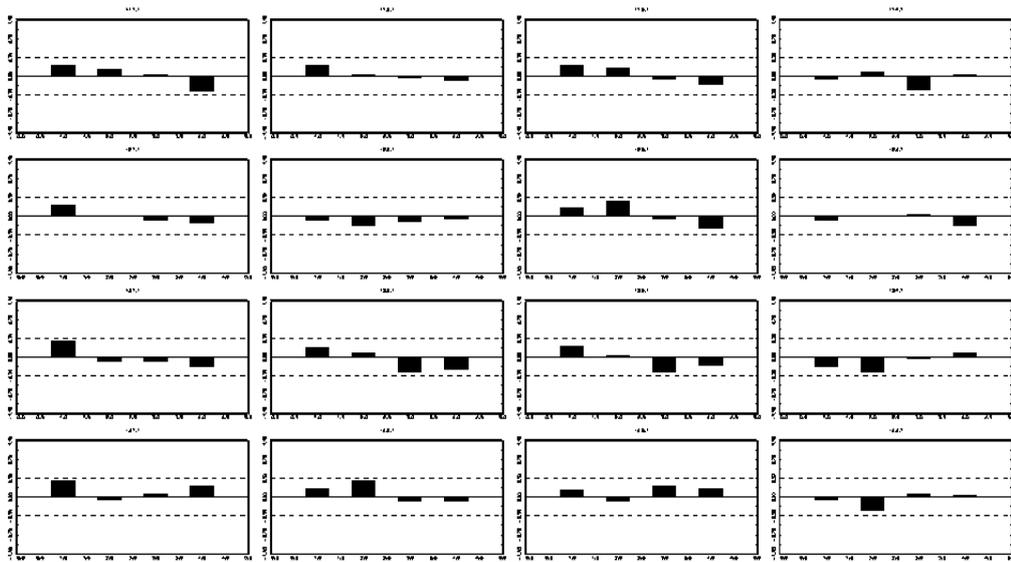


Figure 13. Residual CCF

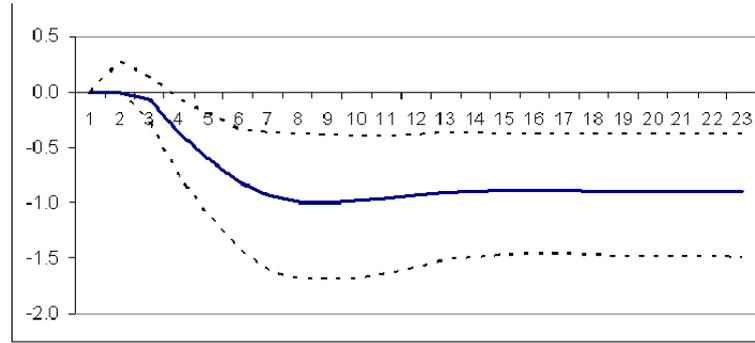


Figure 14. ∇pv_t in the face of a shock in r_t

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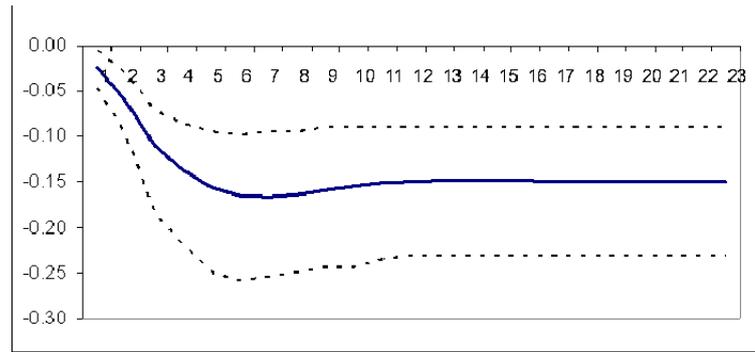


Figure 15. ∇w_t in the face of a shock in r_t

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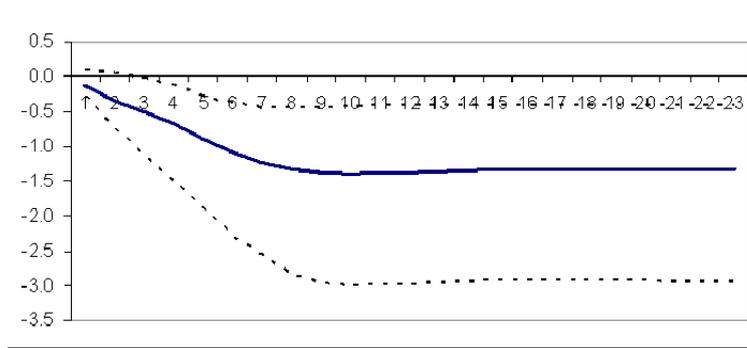


Figure 16. c_t in the face of a shock in r_t

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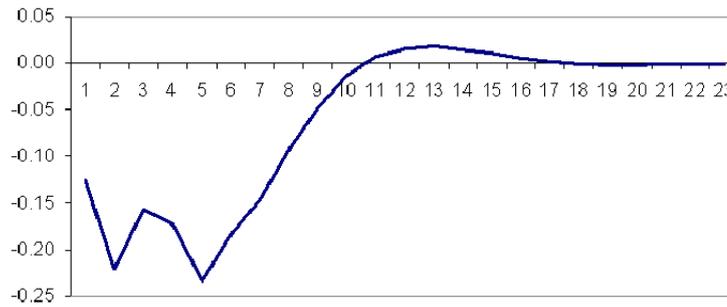


Figure 17. ∇c_t in the face of a shock in r_t

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