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Optimal Design of Rotary Transfer Machines with Turrets

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Abstract: A problem of design of rotary transfer machines with turrets is considered. Operations are partitioned into groups which are performed by spindle heads or by turrets. Constraints related to the design of spindle heads, turrets, and working positions, as well as precedence constraints related to operations, are given. The problem consists in minimizing the estimated cost of the transfer machine, while reaching a given cycle time and satisfying all constraints. The proposed method to solve the problem is based on its reduction to a constrained shortest path problem. An industrial example is presented.

Keywords: Computer-aided design, machining, optimization, graph theory.

1. INTRODUCTION

Transfer machines with rotary table are widely used in mechanical industry (Dashenko *et al.*, 2003; Hitomi, 1996). Designing such machines is a very complex problem due to manufacturing and design constraints and to the large number of possible decisions.

This paper deals with a problem of the optimal design of a transfer machine with rotary table (see Fig.1). In this type of machine a part is machined sequentially on m working positions by multi-spindle heads or turrets. At the k-th working position, a subset N_k , k=1,...,m of operations of the given set **N** of all operations is performed. One additional position is usually used for loading and unloading the parts.

Each set N_k is uniquely partitioned into n_k ($n_k \le 2$) subsets (N_{kj} , $j=1,...,n_k$) of operations which correspond to differents sides of the part and are executed in parallel. In turn, a subset N_{kj} are divided into b_{kj} blocks (N_{kjl} , $l=1,...,b_{kj}$) of operations. Several blocks are executed sequentially by turret or one block is performed by spindle head. We consider the rotary transfer machine with vertical and horizontal spindle heads or turrets. In such a machine there is only one vertical spindle heads or turrets. However, there are several horizontal spindle heads or turret per position. The rotary transfer machine (Fig. 1) has one vertical spindle head common for position 1 and 3, and one horizontal spindle head on position 4.

At the preliminary design stage, the following decisions must be made: the partitioning of the given set of operations into positions and blocks and the choice of cutting modes for each spindle head and turret. In this paper, we focus on mathematical aspects of the preliminary design stage. Similar design problems for transfer machines with spindle heads are considered in (Dolgui et al., 2003; 2005; 2008, 2008a, 2008b, 2008c, 2009a, 2009b). Close problems of assembly line balancing are discussed in (Baybars, 1986; Ghosh and Gadnon, 1989; Erel and Sarin, 1998, Scholl and Klein, 1998; Scholl, 1999; Rekiek et al., 2002; Dolgui and Proth, 2010). Problems of designing assembly lines with equipment selection are investigated in (Bard and Feo, 1991; Askin and Zhou, 1998; Bukchin and Tzur, 2000). Process planning problems are considered in (Halevi, 2003).

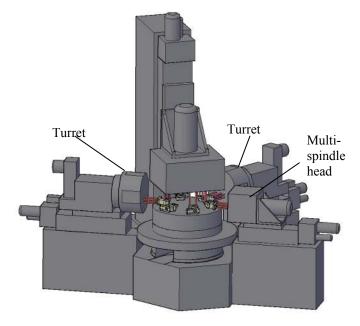


Fig. 1. A rotary transfer machine with turrets.

The paper is organized as follows. Section 2 presents the statement of the problem. Section 3 deals with our optimization method. An industrial example is presented in Section 4, and concluding remarks are given in Section 5.

2. PROBLEM STATEMENT

It is assumed that cutting modes (the feed per revolution and the cutting speed) for each operation are uniquely defined by the accepted feed per minute of the corresponding spindle head or turret. On the other hand, the execution time of a block of operations is defined by the length of its working stroke and its feed per minute. Both parameters depend on executed operations and their feasible cutting modes.

If the ranges $[s_1(p), s_2(p)]$ and $[\delta_1(p), \delta_2(p)]$ of feasible values of feeds per revolution and spindle speeds are known, and if each operation $p \in \mathbb{N}$ is performed by a separate tool, then

 $\mathbf{X}(\mathbf{N})=[X(N), X(N)]$

is the set of feasible values of feeds per minute for the block N of operations, where:

$$X(N) = \max \{ x_1(p) | p \in N \},\$$

 $X(N) = \min \{ x_2(p) \mid p \in N \},\$

 $x_r(p) = s_r(p)\delta(p), r=1,2.$

For a fixed value of the feed per minute $x \in X(N)$ and any $p \in \mathbf{N}$, the feed per revolution is equal to

 $s(p,x) = min [s_2(p), x/\delta_1(p)]$

and the spindle speed is equal to $\delta(p,x) = x/s(p,x)$.

Let $P = \langle P_1, ..., P_k, ..., P_m \rangle$ is a design decision with $P_k = (P_{k11}, ..., P_{k1b_{k1}}, P_{k21}, ..., P_{k2b_{k2}})$ and $P_{kl} = (N_{kjl}, X_{kjl})$. The execution time $t^b(N_{kjl}, X_{kjl})$ of the set N_{kjl} of operations with the feed per minute X_{kjl} is equal to

$$t^{b}(N_{kjl},X_{kjl})=L(N_{kjl})/X_{kjl}+\tau^{b}$$

where $L(N_{kjl}) = max\{\lambda(p) \mid p \in N_{kjl}\}, \lambda(p)$ is the given length of the working stroke for operation $p \in \mathbf{N}$, and τ^{b} is an additional time for advance and disengagement of tools.

The execution time of all the sets N_{kjl} of operations, $l=1,2,...,b_{kj}$, at the k-th working position (k=1,...,m) is equal

to
$$t^{p}(P_{k}) = \tau^{p} + max \{ \tau^{g}(b_{kj}-1) + \sum_{l=1}^{b_{kj}} t^{b}(N_{kjl}, X_{kjl}) | j=1, \dots, n_{k} \},$$

where τ^{g} and τ^{p} are additional times for turret rotation and table rotation.

Then the cycle time for design decision P is defined as follows:

$$T(P) = max \{t^{p}(P_{k}) \mid k=1,...,m\}.$$

We assume that the given productivity is provided, if the cycle time T(P) does not exceed the maximum value T_0 of the cycle time.

A number of known technological factors (such as fixed sequences of operations for machining part elements, the presence of roughing, semi-finishing and finishing operations, etc.) determines an order relation on the set **N**, which defines possible sequences of operations. These precedence constraints can be specified by a directed graph $G^{OR}=(\mathbf{N},D^{OR})$ where an arc $(p,q)\in D^{OR}$ if and only if the operation *p* has to be executed before the operation *q*. Let Pred(p) be the set of immediate predecessors of the operation *p* in the graph G^{OR} .

The required precision (tolerance) of mutual disposition of machined part elements as well as a number of additional factors imply the necessity to perform some pairs of operations from **N** at the same working position, by the same turret or even by the same spindle head for each pair. Such inclusion constraints can be given by undirected graphs $G^{SB} = (\mathbf{N}, E^{SB}), G^{ST} = (\mathbf{N}, E^{ST}), \text{ and } G^{SP} = (\mathbf{N}, E^{SP})$ where the edge $(p,q) \in E^{SB}$ $((p,q) \in E^{ST}, (p,q) \in E^{SP})$ if and only if the operations *p* and *q* must be executed in the same block (turret, position).

At the same time, the possibility to perform operations from **N** at the same working position or by the same spindle head is also defined by a number of constructional and technological constraints, for instance, mutual influence of combining operations, possibility of tool location in spindle head, turret, etc. These exclusion constraints can also be defined by undirected graphs $G^{DB} = (\mathbf{N}, E^{DB}), G^{DT} = (\mathbf{N}, E^{DT}),$ and $G^{DP} = (\mathbf{N}, E^{DP})$ where the edge $(p,q) \in E^{DB}$ $((p,q) \in E^{DT}), (p,q) \in E^{DP})$ if and only if the operations p and q cannot be executed in the same block (turret, position).

The studied problem is to determine:

- a) the number *m* of working positions;
- b) the partitioning of the given set N of operations into
- subsets N_{kjl} , $k=1,...,m, j=1,...,n_k, l=1,...,b_{kj}$;
- c) the feed per minute X_{kjl} for each block N_{kjl} , $l=1,\ldots,n_k$.

Let C_1 , C_2 , C_3 , and C_4 be the relative costs for one working position, one turret, one block of a turret, and one block of a spindle head, respectively. Then the cost of equipment $C(N_{kj})$ for execution of set of operations N_{kj} can be estimated as

$$C(N_{kj}) = sign(b_{kj} - 1)(C_2 + C_3 b_{kj}) + (1 - sign(b_{kj} - 1))C_4$$

where sign(x)=1 if x > 0 and 0 otherwise.

Later we assume also that subsets N_{k1} and N_{k2} correspond to operations for machining of horizontal and lateral sides of a part, respectively, and \mathbf{N}^1 is set of operations for machining of the horizontal side of a part.

Therefore, the mathematical model of the considered design problem can be formulated as follows:

$$Min \ Q(P) = C_1 m + \sum_{k=1}^{m} \sum_{j=1}^{n_k} C(N_{kj})$$
(1)

subject to:

$$T(P) \le T_0; \tag{2}$$

$$\bigcup_{k=1}^{m} \bigcup_{j=1}^{n_k} \bigcup_{l=1}^{b_{kj}} N_{kjl} = \mathbf{N}$$
(3)

 $N_{k'j''} \cap N_{k''j'''} = \emptyset; k', k'' = 1, \dots, m; j', j'' = 1, \dots, n_k;$

$$l', l''=1,...,b_{kj}; j'\neq j''$$
 (4)

 $\bigcup_{l=1}^{b_{kj}} \bigcup_{p \in N_{kjl}} Pred(p) \subseteq \bigcup_{k'=1}^{k-1} \bigcup_{j'=1}^{n_{k'}} \bigcup_{l'=1}^{b_{k'j'}} N_{k'j'l'} \bigcup_{j'=1}^{j-1} \bigcup_{l'=1}^{b_{kj'}} N_{kj'l'};$

$$k=1,\ldots,m; j=1,\ldots,n_k \tag{5}$$

$$\bigcup_{j=1}^{n_k} \bigcup_{l=1}^{o_{kj}} N_{kjl} \cap \{p,q\} | \neq 1, (p,q) \in E^{SP}; k=1,...,m;$$
(6)

$$\bigcup_{l=1}^{b_{kj}} N_{kjl} \cap \{p,q\} | \neq 1, (p,q) \in E^{ST}, k=1,...,m, j=1,...,n_k \quad (7)$$

$$|\bigcup_{l=1}^{b_{kj}} N_{kjl} \cap \{p,q\} | \neq 1, (p,q) \in E^{ST}, k=1,...,m, j=1,...,n_k \quad (8)$$

$$|N_{kjl} \cap \{p,q\}| \neq 1, (p,q) \in E^{SB}; k=1,...,m; j=1,...,n_k;$$

$$l=1,\ldots,b_{kj} \tag{9}$$

$$|\bigcup_{j=1}^{n_k} \bigcup_{l=1}^{o_{kj}} N_{kjl} \cap \{p,q\} | \neq 2, (p,q) \in E^{DP}; k=1,...,m$$
(10)

$$|\bigcup_{l=1}^{b_{kj}} N_{kjl} \cap \{p,q\} | \neq 2, (p,q) \in E^{DT}; k=1,...,m; j=1,...,n_k(11)$$

$$N_{kjl} \cap \{p,q\} | \neq 2, (p,q) \in E^{DB}; k=1,...,m; j=1,...,n_k;$$

 $l=1,...,b_{kj}$ (12)

$$\sum_{k=1}^{m} sign(b_{k1}-1) \le 1; (b_{k1} \le 1) \lor (sign(b_{k1}-1)b_{k2}); k=1,...,m \quad (13)$$

$$X_{kjl} \in X(N_{kjl}); k=1,...,m; j=1,...,n_k; l=1,...,b_{kj}$$
 (14)

$$n_k \le 2; \ b_{kj} \le b_0 \tag{15}$$

$$m \le m_0. \tag{16}$$

The objective function (1) is the equipment cost; constraint (2) provides the required productivity rate; constraints (3-4) ensure the assignment of all the operations from N to one working position exactly; (5)-(12) provide precedence constraints, inclusion and exclusion constraints for blocks, turrets, and working positions; (13) ensure that at most one vertical turret will be designed; (14) choose feasible values of the feed per minute for each block of operations; (15 -16) are the constraints on the number of turrets and spindle heads, on the number of blocks in one turret, and on the number of working positions; m_0 and b_0 are the maximal number of

working positions and the number of blocks in one turret, respectively.

3. SOLUTION METHOD

 $\underline{t}(N_k) \le T_0$

It is easy to see that $P = \langle (N_{111}, X_{111}), ..., (N_{11b_{11}}, X_{11b_{11}}), (N_{121}, X_{121}), ..., (N_{12b_{12}}, X_{12b_{12}})..., (N_{m11}, X_{m11}), ..., (N_{m1b_{m1}}, X_{m1b_{m1}}), (N_{m21}, X_{m21}), ..., (N_{m2b_{m2}}, X_{m2b_{m2}}) \rangle$ is a solution of the problem (1) - (16) iff $P' = \langle (N_{111}, X(N_{111})), ..., (N_{11b_{11}}, X(N_{11b_{11}})), ((N_{121}, X(N_{121})), ..., (N_{12b_{12}}, X(N_{12b_{12}})), ..., (N_{m11}, X(N_{111})), ..., (N_{11b_{11}}, X(N_{m11})), ..., (N_{m11}, X(N_{m11})), ..., (N_{m1b_{m1}}, X(N_{m1b_{m1}})), (N_{m21}, X(N_{m21})), ..., (N_{m2b_{m2}}, X(N_{m2b_{m2}})) \rangle$ satisfies (1)-(16). Therefore, the optimization problem (1)-(16) may be reduced to a problem of finding a partition of N into subsets N_{kjl} , $k=1,...,m, j=1,...,n_k, l=1,...,b_{kj}$, such that

•
$$C_1m + \sum_{k=1}^{m} \sum_{j=1}^{n_k} C(N_{kj})$$
 is small as possible,

where $\underline{t}(N_k) = \tau^p + max\{(b_{kj} - 1)\tau^g + \sum_{l=1}^{b_{kj}} t^b(N_{kjl}, X(N_{kjl}))| j=1, \dots, n_k\}.$

In turn, such a problem may be transformed into the problem of finding a shortest constrained path in the following digraph.

Let **P** be a set of collections $P = \langle N_1, ..., N_k, ..., N_m \rangle$, satisfying the constraints (3)-(15). The set $v_k = \bigcup_{r=1}^k N_r$ can be considered as a state of the part after machining it at *k*-th working position. Let *V* be the set of all states of part for all *P* \in **P**, including also the states $v_0 = \emptyset$ and $v_N =$ **N**.

An arc (v',v'') is included into a digraph G=(V, D) if $v' \subset v''$ and the set $N''=v''\setminus v'$ can be partitioned into subsets $(N_{11}^{"}, ..., N_{1b_1}^{"}, N_{12}^{"}, ..., N_{1b_2}^{"})$ such that precedence, inclusion, and exclusion constraints are not violated as well as $\underline{t}(N'') \leq T_0$.

The arc (v',v'') represents the set $v'' \setminus v'$ of operations that are performed at one working position. Each arc (v',v'') is assigned the cost $c(v',v'')=C(v'' \setminus v')$.

Each design decision $P \in \mathbf{P}$ can be associated with a path $z(P)=(v_0=u_0,..., u_{k-1}, u_k,..., u_m=v_N)$ in the digraph *G* from the vertex v_0 to the vertex v_N where $u_k = \bigcup_{r=1}^k N_r$.

Let **Z** be the set of all paths in *G* from v_0 to v_N . Then the path $z \in \mathbf{Z}$ defines a decision $P(z)=(u_1 \setminus u_0, \ldots, u_j \setminus u_{j-1}, \ldots, u_{m(z)} \setminus u_{m(z)-1})$ satisfying constraints (2)-(15) but maybe does not respect constraint (16).

Let us consider the following constrained shortest path problem:

$$Min \ Q(z) = \sum_{k=1}^{m(z)} C(u_k | u_{k-1});$$
(17)

$$z \in \mathbb{Z};$$
 (18)

$$m(z) \le m_0. \tag{19}$$

The following algorithm simultaneously generates the digraph *G* and solves the problem (17)-(19). Vertices from *V* can be easily enumerated in the non-decreasing order of their rank in *G*. In order to do this, we simply partite *V* into V_i in such a way that $v \in V_i$ if $|V_i|=i$, $i=0, 1, ..., |\mathbf{N}|$.

In this algorithm, $Cost_j(v)$ corresponds to a path with the minimal cost in digraph *G* from the vertex v_0 to the vertex v, which consists exactly of *j* arcs. Using $Pred_j(v)$, such a path can be easily found in digraph *G*. Since only one vertical turret is allowable it can be designed beforehand. To partite the set \mathbf{N}^1 we can use methods (Dolgui et al, 2008a).

Algorithm 1.

Step 0. Let $V_0 \leftarrow \{\emptyset\}$, $V_i \leftarrow \emptyset$, $i=1,...,\mathbf{N}$, $Cost_1(v_0)=0$, $Cost_k(v_0) \leftarrow \infty$, $k=2,...,m_0$.

Step 1. For $i=0,...,|\mathbf{N}|-1$ For each $v \in V_i$ such that $\min\{Cost_k(v)|k=1,...,m_0\} < \infty$ repeat Steps 2 and 3.

Step 2. By Algorithm 2 generate the set D(v) of arcs whose origin is the vertex v. Include into D(v) the arc \mathbf{N}^1 if $c(\mathbf{N}^1) < \infty$ and all the predecessors of \mathbf{N}^1 are in $v \cup \mathbf{N}^1$.

Step 3. For each arc $d \in D(v)$:

- *a*) let $w \leftarrow v \cup d$;
- b) if $w \notin V_{|w|}$ then add w to $V_{|w|}$ and let $Cost_r(w) \leftarrow \infty$, $r=1,...,m_0$;
- c) if $v = v_0$ then let $Cost_1(w) \leftarrow c(d)$, $Pred_1(w) \leftarrow v_0$, else for all $k=1,..., m_0$ -1 such that $Cost_k(w) < \infty$, : if $Cost_k(v) + C(d) < Cost_{k+1}(w)$ then let $Cost_{k+1}(w) \leftarrow Cost_k(v) + c(d)$,

$$Pred_{k+1}(w) \leftarrow v.$$
endif
endfor

endif

Step 4. If $V_{|N|}$ is empty then there is no a feasible solution else set min $\{Q(z)|z \in \mathbb{Z}\} \leftarrow \min \{Cost_k(v_N)| k=1, ..., m_0\}$.

Let J(v) be the set of operations that can be performed at one working position after the state v of the part taking into account the precedence constraints. The set J(v) can be partitioned into subsets $J_i(v)$, i=1,..., I(v) of operations that must be executed in the same working position (subsets $J_i(v)$ can consist of one operation only). The following algorithm generates the set D(v) of digraph G. In this algorithm, *last(d)* indicates the greatest index of subset $J_i(v)$ including in d.

Algorithm 2.

Step 1. Construct J(v) and partite J(v) into subsets $J_i(v)$, i=1,...,I(v). Let $D(v) \leftarrow \emptyset$.

Step 2. For i=1,..., I(v) let $d \leftarrow J_i(v)$, $last(d) \leftarrow i$, and compute c(d) by Algorithm 3. Add d to D(v) if $c(d) < \infty$ and stop otherwise.

Step 3. For each $d \in D(v)$:

For k=last(d)+1,...,l(v): let $d' \leftarrow d \cup J_k(v)$, $last(d') \leftarrow k$ and compute c(d)by Algorithm 3; if $c(d') < \infty$ then add d' to D(v).

Step 4. Exclude dominated arcs from D(v).

Algorithm 3.

Step 1. Let $c(d) = C_1$, $d^1 = d \cap \mathbf{N}^1$ and $d^2 = d \setminus d^1$.

Step 2. If $d^1 = \emptyset$ then go to Step 3. Let $c(d) = \infty$ if the set d^1 of operations cannot be performed in one block else let $c(d) = c(d)+C_4$.

Step 3. Using methods (Dolgui et al, 2008a) partite the set d^2 of operations in the minimal number b_{k2} of blocks such that $\underline{t}(d^2) \leq T_0$. If $b_{k2} = 1$ then let $c(d) = c(d) + C_4$ else if $b_{k2} \leq b_0$ then let $c(d) = c(d) + C_2 + C_3 b_{k2}$ else let $c(d) = \infty$.

Several dominance rules can be applied for elements from D(v).

<u>**Rule 1**</u>. An arc d'dominates an arc d if $d \subseteq d'$ and c(d') = c(d).

<u>**Rule 2**</u>. An arc d'dominates an arc d if $d \subseteq d'$, c(d') = c(d), and $\underline{t}(d') = \underline{t}(d)$.

Using values $Cost_k(v)$, $k=1,..., m_0$, we can restore all the optimal paths in digraph G and evaluate them by means of other criteria.

Values of X_{kjl} can be defined in such a way that b_{kj}

$$\sum_{l=1}^{L(N_{kjl})/X_{kjl}} \leq T_k$$

where $T_{kj} = T_0 - \tau^p - (b_{kj} - 1)\tau^g - b_{kj}\tau^b$.

If "recommended" values $x_0(p)$ of feed per minute are known for each operation $p \in \mathbb{N}$ then X_{kjl} may be chosen as

$$\max \{ \sum_{l=1}^{b_{kj}} \sum_{p \in N_{kjl}} x_0(p) / \sum_{l=1}^{b_{kj}} |N_{kjl}|, \sum_{l=1}^{b_{kj}} L(N_{kjl}) / T_{kj} \}$$
for $k=1,...,m; j=1,...,n_k$.

4. AN INDUSTRIAL EXAMPLE

Eight holes are machined in the part (Fig. 2). Operations for machining the holes and their parameters are given in Table 1; $T_0=3$ min; $\tau^b=\tau^g=\tau^p=0.1$ min; $m_0=6$; $b_0=4$; $C_1=10$; $C_2=5$; $C_3=2$; $C_4=3$. Precedence constraints, exclusion constraints for blocks and positions are presented in Tables 2, 3 and 4, respectively. Inclusion constraints for blocks are given in Table 5. All the constraints were generated by decision support system (Dolgui et al, 2009a).



Fig.2. The part to be machined

Table 1. Operations and their parameters

р	$\lambda(p)$	$x_1(p) x_2(p)$	$x_0(p)$	р	$\lambda(p)$	$x_1(p)$	$x_2(p)$	$x_0(p)$
1	24	26.5 86.7	56.1	13	24	24.9	86.8	57.4
2	11	30.3 107	70	14	9	29.7	105.7	68.4
3	22	29.8 107.2	68.8	15	22	29.9	265.4	57.4
4	22	27.8 249.5	127.5	16	24	24.9	86.8	57.4
5	24	26.5 86.7	56.1	17	9	29.7	105.7	68.4
6	11	30.3 107	70	18	22	29.9	265.4	57.4
7	22	29.8 107.2	68.8	19	24	24.9	86.8	57.4
8	22	27.8 249.5	127.5	20	9	29.7	105.7	68.4
9	72	22.8 81.3	52.6	21	22	29.9	265.4	57.4
10	70	29.7 105.7	68.4	22	24	24.9	86.8	57.4
11	72	22.8 81.3	52.6	23	9	29.7	105.7	68.4
12	70	29.7 105.7	68.4	24	22	29.9	265.4	57.4

Table 2. Precedence constraints

Operation	Direct	Operation	Direct
number	predecessors	number	predecessors
2	1	14	13
3	2	15	14
4	3	17	16
6	5	18	17
7	6	20	19
8	7	21	20
10	9	23	22
12	11	24	23

Table 3. Incompatibility of operations in blocks

Operation	Operations to	Operation	Operations to	
number	be not in the	number	be not in the	
number	same block	number	same block	
13	123567911	19	1 2 3 5 6 7 9 11	
14	123456789	20	12345678	
	10 11 12		9 10 11 12	
15	23467810	21	23467810	
	12		12	
16	123567911	22	123567911	
17	123456789	23	12345678	
	10 11 12		9 10 11 12	
18	23467810	24	23467810	
	12		12	

Table 4. Incompatibility of operations in positions

Operation number	Operations to be not in the same position	Operation number	Operations to be not in the same position
4	1	16	4 8 10 12 15
5	4	17	15
6	4	18	1 5 8 9 11 13 14
			16
8	125	19	4 8 10 12 15 18
9	48	20	15 18
10	159	21	1 5 8 9 11 13 14
			16 17 19
11	4810	22	4 8 10 12 15 18 21
12	15911	23	15 18 21
13	4 8 10 12	24	1 5 8 9 11 13 14
			16 17 19 20 22
15	134578911		
	13		

Table 5. Inclusion constraints for blocks

Operation number	Operations to be in the same block	Operation number	Operations to be in the same block
1	5	10	12
3	7	13	16 19 12
9	11		

Table 6. An optimal solution

Set N _{kjl}	Operations of N_{kjl}	$L(N_{kjl})$	X_{kjl}	$t^b(N_{kjl})$
N ₁₁₁	13 16 19 22	24	57.4	0.54
N ₁₂₁	15911	72	52.6	1.6
N ₁₂₂	26	11	52.6	0.33
N ₁₂₃	37	22	52.6	0.56
N ₂₁₁	14 17 20 22	24	57.4	0.54
N ₂₂₁	4 8 10 12	70	68.4	1.17
N ₃₁₁	15 18 21 24	24	57.4	0.54

An optimal solution is presented in Table 6. The designed transfer machine has one vertical spindle head common for

position 1, 2, 3 (N_{111} , N_{211} , N_{311}), one horizontal turret on position 1 (N_{121} , N_{122} , N_{123}), and one horizontal spindle head on position 2 (N_{221}). In Table 7 we show the results of application of different dominance rules.

Table	7.	Size	of	graph	G

Rule	Number of vertices	Number of arcs	Running time, sec
Rule 1	<u>26</u>	55	0.078
Rule 2	45	124	0.172
-	2214	47839	23.109

In Table 8 an optimal solution is depicted if turrets are not allowable. In this case the number of working positions is equal to 5, i.e. has increased in 2 working positions in comparison with the rotary table with turrets.

Table 8. An optimal solution without turrets

Set N _{kjl}	Operations of N_{kjl}	$L(N_{kjl})$	X_{kjl}	$t^b(N_{kjl})$
N ₁₂₁	15911	72	52.6	1.47
N ₂₂₁	261012	70	68.4	1.12
N ₃₁₁	13 16 19 22	24	57.4	0.54
N ₃₂₁	37	22	68.4	0.42
N_{411}	14 17 20 23	24	57.4	0.54
N_{421}	48	22	127.5	0.27
N_{511}	15 18 21 24	24	57.4	0.54

5. CONCLUSION

A problem of design of rotary transfer machines has been studied. The problem is to assign the manufacturing operations to positions in order to minimize the equipment cost. The initial problem has been reduced to a constrained shortest path problem. The advantage of the graph approach is to easy introduce additional constraints to the problem (1) – (16), for instance, constraints on the number of operations in one block or constraints on the total power, the total feed force in one block. These characteristics can be calculated by user's procedures.

The further research will concern the design of reconfigurable rotary transfer machines for machining different types of parts in batches.

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