

Divide and conquer? persistence of infectious agents in spatial metapopulations of hosts

Marieke Jesse, Hans Heesterbeek

▶ To cite this version:

Marieke Jesse, Hans Heesterbeek. Divide and conquer? persistence of infectious agents in spatial metapopulations of hosts. Journal of Theoretical Biology, 2011, 275 (1), pp.12. 10.1016/j.jtbi.2011.01.032. hal-00676094

HAL Id: hal-00676094

https://hal.science/hal-00676094

Submitted on 3 Mar 2012

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Author's Accepted Manuscript

Divide and conquer? persistence of infectious agents in spatial metapopulations of hosts

Marieke Jesse, Hans Heesterbeek

PII: S0022-5193(11)00044-0 DOI: doi:10.1016/j.jtbi.2011.01.032

Reference: YJTBI 6344

To appear in: Journal of Theoretical Biology

Received date: 12 July 2010 Revised date: 17 January 2011 Accepted date: 20 January 2011



www.elsevier.com/locate/yjtbi

Cite this article as: Marieke Jesse and Hans Heesterbeek, Divide and conquer? persistence of infectious agents in spatial metapopulations of hosts, *Journal of Theoretical Biology*, doi:10.1016/j.jtbi.2011.01.032

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting galley proof before it is published in its final citable form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

- Title: 1
- 2 Divide and conquer? Persistence of infectious agents in a spatial metapopulation
- 3 of hosts.
- 4 Authors:
- 5 Marieke Jesse (m.jesse@uu.nl) and Hans Heesterbeek (j.a.p.heesterbeek@uu.nl)
- 6
- 7 Theoretical Epidemiology, Faculty of Veterinary Medicine, Utrecht University,
- 8 Yalelaan 7, 3584 CL Utrecht, the Netherlands
- 9 Corresponding Author
- 10 ${\it Marieke Jesse}$
- all Theoretical Epidemiology, Faculty of Veterinary Medicine 11

18	Divide and conquer? Persistence of infectious agents in
19	spatial metapopulations of hosts.

20 Marieke Jesse*,a, Hans Heesterbeeka

21 a Theoretical Epidemiology, Faculty of Veterinary Medicine, Utrecht University, the Netherlands

23 Abstract

Persistence of an infectious agent in a population is an important issue in epidemiology. It is assumed that spatially fragmenting a population of hosts increases the probability of persistence of an infectious agent and that movement of hosts between the patches is vital for that. The influence of migration on persistence is however often studied in mean-field models, whereas in reality the actual distance travelled can be limited and influence the movement dynamics. We use a stochastic model, where within- and between-patch dynamics are coupled and movement is modelled explicitly, to show that explicit consideration of movement distance makes the relation between persistence of infectious agents and the metapopulation structure of its hosts less straightforward than previously thought. We show that the probability of persistence is largest at an intermediate movement distance of the host and that spatially fragmenting a population of hosts is not necessarily beneficial for persistence.

- 24 Key words: stochastic model, migration, movement distance, patch
- 25 neighbourhood, lattice

26 Introduction

- 27 Once an infectious disease invades a population, it can go extinct immediately,
- 28 fade out after an epidemic or persist in the population. In homogeneously mixing
- 29 populations, infectious agents tend to die out when the host population size is

^{*}Corresponding author

30	below a critical community size (Bartlett, 1957; Grenfell & Harwood, 1997),
31	related to the demographic processes that regulate the inflow of new susceptible $$
32	hosts in the population (Anderson & May, 1992). However, populations are
33	often structured in space and then the situation becomes much more subtle.
34	Examples are humans living in cities and towns (Hall et al., 2007), cattle on
35	farms (Le Menach et al., 2005; Kao et al., 2007) or wildlife populations, for
36	example the water voles in the U.K. (Telfer et al., 2001), the badgers in the
37	U.K. (Rogers et al., 1998) or the great gerbils in Kazakhstan (Davis et al.,
38	2007a). These populations live in a set of spatially separated patches of suitable
39	habitat, connected to each other by migration of the individuals (e.g. travel of
40	humans between cities, purchasing and selling of cattle and juvenile migration of
41	wildlife). Each patch moreover, has its own dynamics influenced by the incoming
42	and outgoing migrants and by the local conditions. Such a population is called
43	a (spatial) metapopulation (Hanski, 1999; Leibold et al., 2004). The patch size
44	measured is the size of the inhabiting population of interest and ranges from
45	very large (e.g. cities, farms), to very small (for example wildlife often lives in
46	small (family)groups).
47	The structure of such metapopulations for a given species is distinct from sin-
48	gle homogeneously mixing populations, resulting in differences in dynamics and
49	persistence of the species itself, and other species it interacts with. For exam-
50	ple, infectious disease agents both influence and are influenced by the structure
51	and migration of their host (Grenfell & Harwood, 1997). Hanski (1999) showed
52	that, if the total population size is below the critical community size, then spa-
53	tially fragmenting this population has a positive influence on the ability of an
54	infectious agent to persist and that notably movement of hosts between patches
55	is crucial. The latter aspect has received substantial attention in the literature
56	(e.g. Swinton et al., 1998; Keeling, 2000; Park et al., 2002; Hagenaars et al.,
57	2004; Lindholm & Britton, 2007).
58	However, there is a much broader range of aspects that influence and con-
59	trol persistence in a metapopulation (Swinton et al., 1998): (i) demographic
60	aspects: birth and death; (ii) epidemic aspects: length of infectious period and

61	the specifics of the transmission process; (iii) spatial aspects: movement distance
62	of the host and frequency of migration or length of stay in patches. Notably the
63	interaction between these aspects appears to be important, and is not well un-
64	derstood. Indeed, seemingly new phenomena arise from analysis of real systems
65	(Davis et al., 2007b, 2008). In this theoretical paper we aim to contribute to
66	this debate and explore the question: how does the interaction between all the
67	aspects mentioned shape persistence of an infectious disease agent in a spatially
68	structured host population with movement modelled explicitly?
69	For studying persistence in a metapopulation often a mean-field approxima-
70	tion is used (Gog et al., 2002; McCallum & Dobson, 2002; Jesse et al., 2008),
71	but here we introduce a (preferred) movement distance of the host: hosts are
72	only allowed to migrate to patches within this movement distance. The set of
73	patches that can be reached by individual hosts migrating out of a given patch
74	within one time step is seen as the neighbourhood of that patch. The effect of
75	the neighbourhood of a patch on persistence has been studied both in an eco-
76	logical setting (Durrett & Levin, 1994; Hanski & Ovaskainen, 2000; Vuilleumier
77	et al., 2007) and in an epidemiological context (Levin & Durrett, 1996; Rhodes
78	& Anderson, 1996).
79	Keeling (2000) pointed out that there are two ways of coupling between
80	subpopulations. The first is based on movement rate of individuals between
81	subpopulations, which is the coupling we use in the present paper. The second
82	is by using a parameter that describes how much the global average affects
83	the dynamics of a subpopulation. Keeling used the latter way of coupling and
84	concluded that persistence is maximized at intermediate levels of coupling (in
85	the second interpretation), but expects the qualitative behaviour of both ways
86	of coupling to be similar. In this paper we show that using a movement rate and
87	in addition a movement distance indeed results in persistence being maximized $$
88	at intermediate levels of coupling.
89	Here, we take a much broader view by regarding an epidemiological model
90	with demography, explicit modelling of movement (distance and frequency of
91	movement) and coupling of between- and within-patch dynamics. Among other

results, we show that there can be an optimum for persistence at intermediate neighbourhood size. We explore the reasons behind this and how persistence of an infectious agent is influenced by the demographic, epidemic and spatial parameters. Moreover, we show that, in contrast to what was generally believed, a metapopulation is not necessarily more beneficial for the persistence of an infectious agent compared to a single homogeneously mixing population.

98 Methods

99 Model

The model describes a host population divided into subpopulations, each inhabiting a patch with suitable habitat (details in Jesse et al., 2008). In contrast to Jesse et al. (2008) we now consider a spatially explicit metapopulation, where patches are structured in space, in our case on a regular square lattice. At least initially there are no unoccupied patches and the patches are identical in the sense that all parameter values are the same for all subpopulations. An overview of the parameters and their default values used in the numerically studied cases is given in Table 1.

In each patch there is homogeneously mixing and SIR-type dynamics occurs, with hosts being in one of the three following states: susceptible (S), infectious (I) or recovered/immune to the infection (R). The infectious disease is transmitted directly and hosts do not lose immunity, but eventually die and are replaced by susceptibles. Births are locally density dependent, meaning that they depend on the number of hosts present in that patch.

Parameter	Value	Definition
\overline{P}	100	number of patches
K	10	carrying capacity
b	0.2	birth rate per week
μ	0.01	natural mortality rate per week
m	[0, 1]	movement rate per week
β	10	transmission rate per week
γ	0.5	recovery rate per week

Table 1: Definition and default values of the model parameters for numerically studied cases.

Random variable	Distribution	Parameter	Definition
$\mathbf{B}(N_x,t)$	Poisson	$\max[0; bN_x(t)(1-\frac{N_x(t)}{K})]$	# births
$\mathbf{D}(Z_x,t)$	Binomial	μ	# deaths
$\mathbf{Inf}(S_x,t)$	Binomial	$1 - exp(-\frac{\beta I_x(t)}{N_x(t)})$	# infecteds
$\mathbf{Rec}(I_x,t)$	Binomial	γ	# recovereds
$\mathbf{M}_{\mathrm{out}}(Z_x,t)$	Binomial	m	# emigrants
$\mathbf{M}_{\mathrm{in},Z}(x,t)$	Multinomial	1/P	# immigrants

Table 2: The random variables with their distribution and parameters. The state is given explicitly or by Z with $Z \in \{S, I, R\}$.

The model is stochastic and discrete in time, one time step denotes one week, where $S_x(t)$, $I_x(t)$ and $R_x(t)$ denote the number of hosts per infectious state in patch x at time t. The total number of hosts in patch x at time t is given by $N_x(t)$. Events occur successively in the interval [t, t+1) in the order of birth, death, infection, recovery and migration. Of course, ordering the events is artificial, but it is necessary in a discrete model so that in the bookkeeping individual-level events, such as dying or recovering, are taken into account in a consistent way. The complete set of stochastic difference equations is given by:

$$S_x(t+1) = S_x(t) - \mathbf{D}(S_x,t) - \mathbf{Inf}(S_x,t) + \mathbf{B}(N_x,t) - \mathbf{M}_{\text{out}}(S_x,t) + \mathbf{M}_{\text{in},S}(x,t)$$

$$I_x(t+1) = I_x(t) - \mathbf{D}(I_x,t) + \mathbf{Inf}(S_x,t) - \mathbf{Rec}(I_x,t) - \mathbf{M}_{\text{out}}(I_x,t) + \mathbf{M}_{\text{in},I}(x,t)$$

$$R_x(t+1) = R_x(t) - \mathbf{D}(R_x,t) + \mathbf{Rec}(I_x,t) - \mathbf{M}_{\text{out}}(R_x,t) + \mathbf{M}_{\text{in},R}(x,t)$$

The random variables and their distributions (Table 2) are calculated with the number of hosts at that point in the time interval, using the order of the events; for example, the number of newly infected hosts at time interval [t, t+1)depends on the number of infectious hosts at time t-1 minus the number of infectious hosts that died at time t.

127 Structure

128

129

130

131

132

114115

116

117

118119

120

121

Above we described the dynamics within each patch, but these patches are connected to each other via migration of the hosts, which we also model explicitly. Where in Jesse et al. (2008) a mean-field approximation was used, here a finite spatially explicit structure is looked at. The patches to which a host can migrate, are given by the adjacency matrix A. This adjacency matrix describes

the connections between the patches of the metapopulation: if $A_{ij} = 1$ it is possible to move from patch i to patch j, otherwise $A_{ij} = 0$. We view the metapopulation of patches as being arranged spatially in a finite regular lattice where a node is a patch and where an edge indicates a connection in the above sense. The network is non-directed, which means that if movement is possible from patch i to patch j, then it is also possible from patch j to patch i, i.e. $A_{ij} = A_{ji}$.

Of particular interest is the movement distance of the hosts, measured as path length in the lattice. For movement distance d, a host can migrate along at maximum d edges in the regular lattice of patches. The host can, with equal probability, migrate to all patches that can be reached within this number of edges. This movement distance can be seen as the capacity of the host to migrate to patches at that distance. When the movement distance equals 1, hosts can only migrate to their nearest neighbours and when the movement distance is large enough, hosts can move to every patch. The matrix M gives the patches to which a host can move within a movement distance d and has entries such that, for $i \neq j$:

$$M_{ij} = \begin{cases} 1 & \text{if patch } i \text{ and } j \text{ are connected, i.e. } (\sum_d A^d)_{ij} > 0 \\ 0 & \text{otherwise} \end{cases}$$

- and $M_{ii} = 0$, preventing hosts from migrating back immediately to the patch
- they just left (i.e. no loops of length 1 are allowed). The matrix M is calculated
- by means of $\sum_d A^d$, where A^d_{ij} gives the number of paths of length d from patch
- 143 i to patch j.
- 144 Simulations
- 145 The model is stochastic and hence there can be large variation between runs of
- 146 the model, even though the set of parameter values is identical. The stochastic
- 147 difference equations were simulated for a range of parameter values. The pro-
- gram is written in R (package 2.10.1, www.cran.r-project.org). At time t = 1 one
- 149 infectious host is introduced into one patch in an otherwise completely suscepti-
- 150 ble metapopulation. For the results the location of this (index) patch, where the

151	first infectious host is introduced, does not matter. This coincides with findings $% \left(1\right) =\left(1\right) \left(1\right$
152	of Pautasso & Jeger (2008), when they studied a model with $SI\text{-type}$ dynamics
153	on a directed network, where each node represents an individual.
154	After introduction of this one infectious host in the metapopulation, there
155	are four possible situations: the infectious agent may (i) not spread at all in
156	the initial patch, (ii) spread in the initial patch, but not between patches (iii)
157	spread within and between patches and then fade out or (iv) spread within and
158	between patches and (quasi)persist in the metapopulation (Jesse et al., 2008).
159	Here, we are interested in the fourth case, persistence in the metapopulation.
160	We defined the infectious agent to be persistent in a simulation if it is still
161	present in the population after twice the expected life span of the host. The
162	expected life span of a host is $1/\mu,$ therefore the simulations were run for $2/\mu$
163	time steps. The choice of twice the expected life span is arbitrary, but within
164	this number of time steps the infectious agent has survived two generations of
165	hosts, and has spread between the patches.
166	The results obtained are from 1000 simulations. This number of simulations
167	per data point was chosen such that variation between several runs of $1000\ \mathrm{sim}$
168	ulations for the same set of parameter values is small. Therefore, increasing the
169	number of simulations smoothens the graphs depicting our results, but does not
170	alter or add to conclusions we draw.
171	The default parameter values are shown in Table 1. The default death rate
172	equals 0.01 , meaning that the life span of a host is on average 100 weeks, i.e. a
173	host lives around two years. And the default recovery rate equals 0.5 , so that
174	a host is infectious for on average two weeks. The metapopulation consists of
175	100 patches, all with carrying capacity 10. This carrying capacity is chosen
176	such that persistence of the infectious agent in a single patch is not possible.
177	In a single homogeneously mixing population of size 1500 around 90% of the
178	simulations will result in a persisting infection for the default parameter values.
179	The metapopulation is arranged on a square 10×10 lattice, with reflective
180	boundaries. These boundaries can be considered as natural boundaries such as

water or mountains, which cannot be crossed by the host.

181

207

208

182 Results and Conclusions 183 In this section we will first present the influence of the spatial aspects on persis-184 tence of infectious agents in the metapopulation. Then the demographical and 185 epidemiological aspects will be presented. 186 Spatial aspect In Figure 1a, the influence of the spatial aspects on persistence of the infectious 187 188 agent are explored. In this figure, contour lines show the fractions of simulations 189 with persisting infection as functions of the migration rate and the movement 190 distance of the host. Fixing the movement distance and then increasing the 191 migration rate resulted in a higher fraction of simulations with persisting in-192 fection. A higher migration rate means that hosts spend a shorter time in one 193 patch and thus change patches more frequently. By changing patches more fre-194 quently, hosts increase the number of contacts with other hosts and therefore 195 have a higher probability of finding sufficient susceptible hosts to infect while 196 they are still infectious. 197 Fixing the migration rate and increasing the movement distance shows a 198 maximum in the fraction of simulations with persisting infection at intermediate 199 movement distance. This result is also shown in Figure 1b for four different 200 migration rates. Clearly there is a peak at intermediate movement distance, 201 except for relatively low migration rates (a migration rate of 0.2 means that a 202 host moves once every 5 weeks). The default infectious period is two weeks, so 203 at low migration rates the host spends, on average, most of its entire infectious 204 period within one patch. Since the patch size is too low for persistence, there is 205 only a very small fraction of simulations showing persistence. 206 Effect of movement distance on patch level

As already shown, varying only the movement distance already results in dis-

similarities between the fraction of simulations with persisting infection. In

order to understand where these dissimilarities come from, we focus on the dif-

209

210	ferences that occur on patch level. Because the infectious hosts are the key for
211	persistence of the infectious agent in the metapopulation, we focused on some
212	properties of patches with respect to infectious hosts that might be influenced
213	by the movement distance:
214	i) the total number of time steps (not necessarily consecutive) that a patch
215	contains at least one infectious host;
01.0	
216	ii) the number of times that a patch gets infected, i.e. how often are there
217	transitions from no infectious host in a patch to at least one infectious host
218	in that patch;
219	iii) the total number of infectious hosts per patch, i.e. the sum of the number
220	of infectious hosts at each time step in a patch;
221	iv) the number of consecutive time steps a patch contains an infectious host.
222	Only simulations with persisting infection were taken into account when calcu-
223	lating the above measures. The results are presented as box-and-whisker-plots
224	in Figure 2.
225	It is immediately clear that the medians for movement distance 6 and 14 are
226	approximately the same for all four measures, but that the range differs: the
227	variation between patches for intermediate movement distance is larger than
228	for large movement distance. Movement distance 14 corresponds to a situation
229	where the patches are almost fully connected and the system starts behaving
230	like one single homogeneously mixing population.
231	On average a patch contains 35 out of the 200 time steps (17.5% of the time)
232	at least one infectious host for low movement distance (Fig. 2a). The average
233	number for the other movement distances is slightly higher. The number of
234	transitions from no infectious hosts in a patch to at least one is the lowest
235	for the low movement distance (median 15 times, Fig. 2b). This might be
236	due to (infectious) hosts returning more often back to a patch they visited
237	just a few time steps ago (fewer patches to choose from). On average the

238 total number of infectious hosts per patch is about 1.5 times larger for low 239 movement distance (median of 120) than for the other two movement distances 240 (Fig. 2c). Because the number of infected patches at each time step is equal 241 for all movement distances, the number of infectious hosts in each patch must 242 be higher for low movement distance than for the other movement distances. 243 Again, this is probably caused by hosts returning more often to a patch they just 244 visited at low maximum movement distances. Finally in Figure 2d the median 245number of consecutive time steps a patch is inhabited by infectious hosts is 246 shown. Basically, this is just the total number of time steps a patch is infected 247divided by the number of transitions from having no infectious host in a patch 248 to having at least one. Here, the low movement distance shows that a patch 249 contains at least one infectious host for a longer uninterrupted number of time 250 steps. 251 With the four measures we looked at, we can conclude that at low movement 252 distance, patches are on average longer infected and contain over the whole time 253 period more infectious hosts than at large movement distance. This implies that the infectious agent remains within the same area at low movement distance 254 255until that area runs too low on available susceptible hosts. At large movement 256 distance on the other hand, the infectious agent is more scattered throughout the 257 whole metapopulation, patches get (re)infected more often, but it is for a short 258 period of time and with only a few infectious hosts. Hence, at low movement 259 distance the spreading of the infectious agent occurs more locally and gradually 260 becomes more global when the movement distance increases. 261 Demographical and epidemiological aspects 262 As mentioned earlier, persistence of an infectious agent is also influenced by 263 demographical and epidemiological aspects. The fraction of simulations with 264 persisting infection is therefore studied as function of each of the four parameters 265 controlling these aspects: birth rate, death rate, transmission rate and recovery 266 rate. The fraction is shown in Figure 3 for three different movement distances, 267 namely 2,6 and 14, and for a single homogeneously mixing population.

268	This single homogeneously mixing population consists of one patch with a
269	carrying capacity K of 1000 hosts; the total size of the metapopulation and the
270	single population are therefore equal. Moreover, this figure shows how a change
271	in a relevant parameter influences the fraction of simulations with persisting
272	infection. For all parameters, the fraction of simulations with persisting infection
273	is the highest for intermediate movement distance, corresponding to the previous
274	result that there is a maximum in the fraction of simulations with persisting
275	infection at this movement distance.
276	The natural death rate (i.e. not related to the infection) determines the
277	life span of a host and influences also, because of the density-dependent birth
278	rate, the population turnover: a lower death rate implies a longer life span and
279	therefore a slower population turnover; i.e. a slower inflow of new susceptible
280	hosts. The life span is used to define when an infectious agent is persistent
281	in our set up, so varying the death rate means that the number of time steps
282	before an infectious agent is called persistent varies as well. Increasing the death
283	rate, i.e. increasing population turnover, has a positive effect on the fraction
284	of simulations with persisting infection (Fig. 3a). At a low death rate, while
285	the speed by which the infectious agent spreads through the whole population
286	remains equal, it takes longer for new susceptible hosts to arise. This time gap is
287	more difficult to bridge in a single homogeneously mixing population, where all
288	susceptible hosts are immediately available for contact to the infectious agent.
289	Therefore, a low death rate is more beneficial for persistence in a metapopulation α
290	than in a single homogeneously mixing population.
291	The birth rate in this model is density dependent; a high birth rate implies
292	that each subpopulation is around carrying capacity and dead hosts are replaced
293	by susceptible new-borns quickly. Hence, increasing the birth rate also increases
294	the fraction of simulations with persisting infection (Fig. 3b). At low birth rate,
295	a single homogeneously mixing population is more beneficial for the infectious
296	agent, because the few susceptible hosts that are born per unit of time are found

297

298

299 and are immediately available for contact with infectious hosts in case of a single 300 homogeneously mixing population. This could mean that the infectious agent 301 'burns through' the available susceptibles too fast to allow persistence. It is 302 then advantageous for the infectious agent to be in the metapopulation: not all 303 susceptible hosts are immediately available for contact, allowing the infectious 304 agent to persist in the population for a longer time (i.e. the risk of fade out is 305 spread). 306 In Figure 3c the fraction of simulations with persisting infection is shown for 307 various transmission rates. For low transmission rates the fraction of simulations 308 with persisting infection is higher in a metapopulation than in a single homoge-309 neously mixing population, but the opposite holds at high transmission rates. 310 In a single homogeneously mixing population an infectious host has immediate access to all susceptible hosts. At high transmission rate, this availability of all 311 312 susceptibles in a single homogeneously mixing population is beneficial for the 313 infectious agent, because even when there are only a few susceptibles left, there 314 is a high probability that they will be contacted. In a metapopulation on the 315 other hand, an infectious host needs time to travel to patches where the few 316 susceptibles remain, and before successful contact has been made this infectious 317 host may have died or recovered. At low transmission rate, the above situations 318 are reversed. 319 The recovery rate determines the infectious period of a host and Figure 3d 320 shows that the fraction of simulations with persisting infection as a function of 321 recovery rate is hardly influenced by the movement distance of the host. When 322 the recovery rate is large, the infectious period is short and, on average, fewer 323 infectious hosts leave the patch during the infectious period, making it more 324 difficult for the infectious agent to spread to other patches. The movement 325 distance does not have a large influence on this, because the ability to spread is 326 here, in the first instance, mostly determined by the chance to leave the patch 327 at all. 328 Furthermore, a short infectious period results in a population of many re-329 covered hosts. In Figure 3d, the fraction of simulations with persisting infection

330	coincides for both the single homogeneously mixing population and a metapop-
331	ulation where hosts have an intermediate movement distance. However, this
332	fraction is very much influenced by the migration rate of the host (not shown).
333	Persistence of the infectious agent is more difficult at low migration rate, because $% \left(1\right) =\left(1\right) \left($
334	the infectious host does not change patches frequently enough to sustain the in-
335	fectious agent. A high migration rate in a metapopulation performs slightly
336	better than a single homogeneously mixing population, because running out of
337	susceptible hosts happens faster in a single population than in a metapopulation.
338	Finally, both the shape of the lattice and the number of patches do not
339	qualitatively change the results (not shown). Reshaping the lattice, for example $$
340	into 4×25 with the same total population size as the 10×10 case, still gives
341	a peak at the same intermediate movement distance of 6. Interestingly, the
342	mean distance of one patch to any other patch is for the 4 \times 25 lattice 9.2
343	steps and for the 10×10 lattice 6.6. Increasing the number of patches to, for
344	example, a 12×12 lattice also gives a peak at intermediate movement distance.
345	The latter peak occurs at a slightly higher movement distance compared to the
346	above cases, however, the 12×12 case is not directly comparable, because both
347	the total population size and the mean distance from one patch to any other
348	is larger. Thus the size of the lattice does not appear to essentially change the
349	results.
350	Balance
351	Persistence of an infectious agent in a metapopulation results from a balance
352	between the spatial, demographical and epidemiological components. We stud-
353	ied the components in isolation above, but now look at their combined effect
354	(Fig. 4).
355	Each panel in this figure shows curves leading to the same fraction of simu-
356	lations with persisting infection ('isopersistence level') as function of the death
357	and the transmission rate. The isopersistence levels are shown for low, interme-
358	diate and high movement distance in a metapopulation and for a single homo-
359	geneously mixing population and for the four parameter combinations low/high

360	migration rate and low/high birth rate. For all four subfigures the default re-
361	covery rate is used, because Figure 3d showed that for the various movement
362	distances differences in the fraction of simulations with persisting infection are
363	not strongly affected by the recovery rate. In order to compare situations we
364	used in Figure 4a,c an isopersistence level of 0.3 and in Figure 4b,d a level of
365	0.6. These levels are chosen with use of Figure 3d, where for migration rate 0.4
366	the fraction of simulations with persisting infection is around 0.3 at the peak
367	and for migration rate 0.8 around 0.6.
368	At low birth rate the total population size is smaller than at high birth rate,
369	because in the latter situation the population is close to carrying capacity. For
370	low birth rates both the panels with low and high migration rates (Fig. 4a-b)
371	show that in a single homogeneously mixing population the isopersistence level
372	is achieved at much lower transmission and death rates than in a metapopula-
373	tion. In that situation, a single homogeneously mixing population is thus more
374	beneficial for the infectious agent than a metapopulation, because at a low birth
375	rate susceptible hosts are not replenished at the same rate as at a high birth
376	rate; it takes more time before new susceptible hosts arise. When they do arise
377	it is more difficult for an infectious host in a metapopulation to successfully meet $% \left(1\right) =\left(1\right) \left($
378	this susceptible host, because the infectious host first has to move to a patch
379	with sufficient susceptible individuals within its infectious period. In a single
380	homogeneously mixing population the new susceptible hosts are immediately
381	available for contact.
382	At high birth and low migration rate (Fig. 4c), the isopersistence level for
383	the single homogeneously mixing population and the intermediate movement
384	distance almost coincide. At high transmission rate the isopersistence levels of
385	all situations coincide, because infectious hosts then have successful contacts
386	with more susceptible hosts per unit of time.
387	At both high birth and high migration rate (Fig. 4d), the differences between
388	the four cases are very small, especially at a large transmission rate all movement $% \left(1\right) =\left(1\right) +\left(1\right)$
389	distances coincide more or less with the single homogeneous mixing population

390

All panels in this figure show the same pattern as described in previous

- sections: persistence of an infectious agent in a metapopulation is easier accomplished at intermediate movement distance of the host.
 - Discussion

393

401

402

403

404

405

406

407

408

409

410

411

412

413

414

415

417

418

419

420

416

In this paper we showed that persistence of an infectious agent in a metapopulation results from of a balance between spatial, demographical and epidemiological parameters. We showed on lattices a robust non-linear relation between the fraction of simulations with persisting infection and movement distance of hosts, with this fraction being largest at an intermediate movement distance of the host. Furthermore we showed that dividing a single homogeneously mixing population into several smaller populations that are connected to each other, is

not necessarily beneficial for the persistence of the infectious agent.

The insight we obtain is based on simulations only. While an important part of relevant parameter space has been explored, there is considerable additional value in providing analytical proof of the observed qualitative phenomena, to obtain robustness of results and deeper understanding. There have been many approaches in the literature where authors have focussed on analytical results concerning infectious disease in spatial metapopulations, and even more concerning single-species populations, predator-prey systems, and notably hostparasitoid systems. Mostly these studies concentrate on stability analysis of the trivial equilibrium (i.e. invasion problems, see Jansen & Lloyd, 2000, and references given there) or on providing analytical expressions for the expected time to extinction from a quasi-steady state (see Nåsell, 1999; Hagenaars et al., 2004; Lindholm & Britton, 2007, and the references given there), as persistence in stochastic models is always temporary (Hanski, 1998; Lloyd-Smith et al., 2005). In discrete-time models it is not possible to determine the quasi-stationary distribution and other measures have to be used; for example, persistence time (Rhodes & Anderson, 1996) or a certain number of time steps the infectious disease is present in the metapopulation (Swinton et al., 1998; Vuilleumier et al., 2007; Jesse et al., 2008; Courcoul & Ezanno, 2010). We focus on persistence

(long-term quasi-stability), i.e. we look at the fraction of realisations of the

421 stochastic process persisting for a time beyond a certain minimum (set arbitrar-422 ily by twice the average life span of the host species). We noticed that increasing 423 this minimum did not qualitatively change the results. However, taking twice 424 the life span of the host as measure for persistence for hosts with very short life 425 spans, may lead to a time scale that is too short to speak of persistence. 426 In our system we merged a stochastic description with discrete spatial struc-427 ture, with on top of that non-uniform dispersal (due to a maximum movement 428 distance for hosts). This combination did not allow us to obtain analytical re-429 sults, nor does the set-up allow for easy simplified models with only two patches, 430 say, that might be amenable to direct analysis. We can, however, compare to 431 studies where discrete space was studied analytically with different choices for dispersal. Rohani et al. (1996) conclude that, in predator-prey type interac-432 433 tion with uniform dispersal, the equilibrium becomes unstable, compared to a 434 single homogeneous population, when there is a big difference in the dispersal 435 between the two species. We have identical dispersal for our two 'predator-prey 436 species' (infected and susceptible individuals, respectively). In our set-up we show, by simulation, differences in persistence, if dispersal is not uniform, but 437 438 constrained. In the discussion of Rohani et al. (1996), it is argued that the 439 equilibrium may destabilise when dispersal is not uniform. Similar equilibrium 440 (in)stability results are discussed analytically by White & White (2005) studying 441 coupled map lattices with integro-differential equations. They show in addition 442 that destabilising influences of dispersal can only occur in "exploiter-victim" 443 type of relationships. 444 In a much simpler model, Funk et al. (2005) study the dynamics of virus par-445 ticles in a spatial metapopulation of host cells. This is basically a one-species system because only the virus particles disperse. The dispersal mechanism, 446

In a much simpler model, Funk et al. (2005) study the dynamics of virus particles in a spatial metapopulation of host cells. This is basically a one-species system because only the virus particles disperse. The dispersal mechanism, however, is closer to ours, as dispersal is constrained to be to (eight) nearest neighbours only. The analytical results allow a large class of dispersal mechanisms to be studied. One of their results is that if dispersal is too fast the infection cannot be maintained. Webb et al. (2007) show, for a host-parasite system, that highly local systems, i.e. where dispersal is limited, have reduced

447 448

449

450

451

452

453

454

455

456

457

458

459

460

461

462

463

464

465

466

467 468

469

470

471 472

473

474

475

476

477

478 479

480

481

482

persistence of the infectious agent. Both these observations (Funk et al., 2005; Webb et al., 2007) are, although from very different models, in broad agreement with our finding of an optimal persistence for intermediate dispersal frequency and distance. This is in contrast to results by Hagenaars et al. (2004) who study persistence (measured as time to extinction from a quasi steady state and as mean outbreak duration) in a spatial and stochastic SIR set-up similar to ours. Their analytical and simulation results show a rather more monotone rise in persistence as a function of increasing between-patch contacts. However, there is an important difference with our model: their model has no actual dispersal within the metapopulation, the only migration comes from outside the system, and is essentially a model with two levels of contacts (within-patch and with individuals in other patches) for individuals that are otherwise fixed in their patch. Together, the above comparisons to related studies lead us to expect that our observation of non-monotone persistence as a function of coupling crucially depends on the physical migration between patches of individuals of at least two types in an "exploiter-victim" relationship, with constraints on the distance over which individuals can migrate within a time step. An important characteristic of a metapopulation is that the infectious hosts have to move to find susceptible hosts. At low movement distance infectious hosts encounter a lower number of susceptible hosts than the average host, because the number of susceptible hosts is depleted by the presence of other infectious hosts. These infectious hosts are competing with each other over the available susceptibles and thereby reduce the potential for each one of them to transmit the infectious disease to a susceptible (Rhodes & Anderson, 2008). At a relatively high migration rate, i.e. with a short sojourn time per patch, a host can meet more others than at a low migration rate. An infectious host will therefore have a larger number of contacts with susceptible hosts, because they visit more patches during their infectious period. Compared to a single homogeneously mixing population, hosts in metapopulations can have the advantage that they do not reach all susceptible hosts at the same time, which can improve

the probability of survival of the infectious agent.

483	As is also shown by Cross et al. (2005), the relation between migration
484	and recovery is very important for the ability of an infectious agent to persist,
485	because the infectious period determines the time an infectious host has to infect
486	susceptible hosts. And the migration rate is an important determinant of the
487	level of mixing.
488	Regarding movement we studied a wide range of migration rates: from mi-
489	grating almost never, to migrating every week. We also assumed that all indi-
490	viduals experience the same migration rate. In reality there is a lot of difference
491	in movement behaviour among species (Hawkes, 2009). Movement may, for ex-
492	ample, be restricted to mainly juveniles leaving their nest to settle elsewhere or
493	to foraging outside the own habitat patch. The first mechanism can be thought
494	of at low migration rates, although there are no age-classes defined in the model.
495	The latter one at high migration rates, where individuals leave their own patch,
496	visit another one and then return to their home patch again.
497	This situation could be even more resembled when the probability to move to
498	a certain patch depends on the distance of that patch with respect to the resident
499	patch. We assumed random dispersal, within the movement distance, but it
500	can also be argued that hosts may have a preference for nearby patches. The
501	influence of a dispersal function, favouring nearby patches, on the persistence
502	of the infectious agent should therefore be studied more carefully.
503	In this paper we defined the movement distance by the number of edges
504	crossed. Another option would have been using a radial movement distance,
505	where individuals can move to all patches within a certain radius around their
506	resident patch. However, using a radial movement distance instead, does not
507	affect the results. Durrett & Levin (1994) also concluded that the qualitative
508	behaviour is independent of the exact definition of movement distance when
509	they studied interacting particle systems for various definitions of movement
510	distance.
511	There have been studies of the effect of the neighbourhood of a patch on the
512	persistence of the infectious agent in a spatially structured population. In an
513	ecological context Vuilleumier et al. (2007) and in an epidemiological context

- 514 Rhodes & Anderson (1996) concluded that increasing the movement distance 515 maximises the probability of persistence. They considered patches as the unit 516 of study and had many unoccupied patches in the population. Another study 517 (Courcoul & Ezanno, 2010) did take within-patch dynamics into account, but 518 they also considered indirect transmission. The probability of infection of a sus-519 ceptible host in a patch depended then not only on the available infectious hosts 520 in the same patch, but also on the prevalence of the infection in neighbouring 521 patches. Courcoul & Ezanno (2010) varied the number of neighbouring patches 522 that influence the infection dynamics in a patch, but did not see a peak in the 523 fraction of simulations with persisting infection at an intermediate number of 524 neighbours. However, due to the different ways persistence can be defined, one 525 should be cautious in comparing the various studies. 526
 - The model used in this paper is as simple as possible. For example, it is not taken into account that infectious hosts might experience reduced mobility or death as a result of the infectious disease. Another assumption is continuous birth, as opposed to seasonal birth, where births occurs in a short period of a year, which is often the case in animal populations. Seasonal births reduces the probability of persistence of the infectious agent, because there are fewer infectious hosts between epidemics, which increases the probability of fade-out due to stochasticity (Grassly & Fraser, 2006). But, each year there is also a burst of new susceptible hosts into the population (Altizer et al., 2006), creating the possibility of a new epidemic. One of the next steps in exploring the balance of the various aspects (spatial, demographical and epidemiological) involved in the persistence of an infectious agent would be to include one or more of the above mentioned options.

539 Acknowledgements

527

528

529

530531

532

533

534

535

536

537

538

- 540 This research is supported by The Netherlands Organisation for Scientific Re-
- 541 search (NWO grant 918.56.620).

- 542 References
- 543 References
- 544 Altizer, S., Dobson, A., Hosseini, P., Hudson, P., Pascual, M., & Rohani, P.
- 545 (2006). Seasonality and the dynamics of infectious diseases. Ecol. Lett, 9,
- 546 467-484.
- 547 Anderson, R. M., & May, R. M. (1992). Infectious Diseases of Humans: Dy-
- 548 namics and Control. Oxford University Press, USA.
- 549 Bartlett, M. S. (1957). Measles periodicity and community size. J. R. Stat. Soc.
- 550 Ser. A Stat. Soc., 120, 48-70.
- 551 Courcoul, A., & Ezanno, P. (2010). Modelling the spread of bovine viral di-
- 552 arrhoea virus (bvdv) in a managed metapopulation of cattle herds. Vet.
- 553 Microbiol., 142, 119–128.
- 554 Cross, P. C., Lloyd-Smith, J. O., Johnson, P. L. F., & Getz, W. M. (2005).
- 555 Duelling timescales of host movement and disease recovery determine invasion
- of disease in structured populations. *Ecol. Lett.*, 8, 587–595.
- 557 Davis, S., Klassovskiy, N., Ageyev, V., Suleimenov, B., Atshabar, B.,
- 558 Klassovskaya, A., Bennett, M., Leirs, H., & Begon, M. (2007a). Plague
- 559 metapopulation dynamics in a natural reservoir: the burrow system as the
- unit of study. Epidemiol. Infect., 135, 740–748.
- 561 Davis, S., Leirs, H., Viljugrein, H., Stenseth, N. C., Bruyn, L. D., Klassovskiy,
- 562 N., Ageyev, V., & Begon, M. (2007b). Empirical assessment of a threshold
- model for sylvatic plague. J. R. Soc. Interface, 4, 649–657.
- Davis, S., Trapman, P., Leirs, H., Begon, M., & Heesterbeek, J. A. P. (2008).
- The abundance threshold for plague as a critical percolation phenomenon.
- 566 Nature, 454, 634–637.
- 567 Durrett, R., & Levin, S. A. (1994). Stochastic spatial models: A user's guide to
- ecological applications. Philos. Trans. R. Soc. B, 343, 329–350.

- 569 Funk, G. A., Jansen, V. A. A., Bonhoeffer, S., & Killingback, T. (2005). Spatial
- models of virus-immune dynamics. J. Theor. Biol., 233, 221–236.
- 571 Gog, J., Woodroffe, R., & Swinton, J. (2002). Disease in endangered metapop-
- ulations: the importance of alternative hosts. Proc. R. Soc. B, 269, 671–676.
- 573 Grassly, N. C., & Fraser, C. (2006). Seasonal infectious disease epidemiology.
- 574 Proc. R. Soc. B, 273, 2541–2550.
- 575 Grenfell, B., & Harwood, J. (1997). (Meta)population dynamics of infectious
- 576 diseases. *Trends Ecol. Evol.*, 12, 395–399.
- 577 Hagenaars, T. J., Donnelly, C. A., & Ferguson, N. M. (2004). Spatial het-
- erogeneity and the persistence of infectious diseases. J. Theor. Biol., 229,
- 579 349-359.
- 580 Hall, I. M., Egan, R., J., Barrass, I., Gani, R., & Leach, S. (2007). Comparison
- of smallpox outbreak control strategies using a spatial metapopulation model.
- 582 Epidemiol. Infect., 135, 1133–1144,
- Hanski, I. (1998). Metapopulation dynamics. Nature, 396, 41–49.
- 584 Hanski, I. (1999). Metapopulation Ecology. Oxford University Press.
- 585 Hanski, I., & Ovaskainen, O. (2000). The metapopulation capacity of a frag-
- mented landscape. Nature, 404, 755–758.
- 587 Hawkes, C. (2009). Linking movement behaviour, dispersal and population
- 588 processes: is individual variation a key? J. Anim. Ecol., 78, 894–906.
- 589 Jesse, M., Ezanno, P., Davis, S., & Heesterbeek, J. A. P. (2008). A fully cou-
- 590 pled, mechanistic model for infectious disease dynamics in a metapopulation:
- movement and epidemic duration. J. Theor. Biol., 254, 331–338.
- 592 Kao, R. R., Green, D. M., Johnson, J., & Kiss, I. Z. (2007). Disease dynamics
- 593 over very different time-scales: Foot-and-mouth disease and scrapie on the
- 594 network of livestock movements in the uk. J. R. Soc. Interface, 4, 907–916.

- 595 Keeling, M. J. (2000). Metapopulation moments: Coupling, stochasticity and
- 596 persistence. J. Anim. Ecol., 69, 725–736.
- 597 Le Menach, A., Legrand, J., Grais, R. F., Viboud, C., Valleron, A., & Flahault,
- 598 A. (2005). Modeling spatial and temporal transmission of foot-and-mouth
- disease in france: Identification of high-risk areas. Vet. Res., 36, 699–712.
- 600 Leibold, M. A., Holyoak, M., Mouquet, N., Amarasekare, P., Chase, J. M.,
- 601 Hoopes, M. F., Holt, R. D., Shurin, J. B., Law, R., Tilman, D., Loreau,
- 602 M., & Gonzalez, A. (2004). The metacommunity concept: a framework for
- 603 multi-scale community ecology. Ecol. Lett., 7, 601–613.
- 604 Levin, S. A., & Durrett, R. (1996). From individuals to epidemics. Philos.
- 605 Trans. R. Soc. B, 351, 1615–1621.
- 606 Lindholm, M., & Britton, T. (2007). Endemic persistence or disease extinction:
- The effect of separation into sub-communities. Theor. Popul. Biol., 72, 253–
- 608 263.
- 609 Lloyd-Smith, J. O., Cross, P. C., Briggs, C. J., Daugherty, M., Getz, W. M.,
- 610 Latto, J., Sanchez, M. S., Smith, A. B., & Swei, A. (2005). Should we expect
- 611 population thresholds for wildlife disease? Trends Ecol. Evol., 20, 511–519.
- 612 McCallum, H., & Dobson, A. (2002). Disease, habitat fragmentation and con-
- 613 servation. Proc. R. Soc. B, 269, 2041–2049.
- Nåsell, I. (1999). On the time to extinction in recurrent epidemics. J. R. Stat.
- 615 Soc. Series B. Stat. Methodol., 61, 309–330.
- 616 Park, A. W., Gubbins, S., & Gilligan, C. A. (2002). Extinction times for closed
- 617 epidemics: the effects of host spatial structure. Ecol. Lett., 5, 747–755.
- 618 Pautasso, M., & Jeger, M. J. (2008). Epidemic threshold and network structure:
- The interplay of probability of transmission and of persistence in small-size
- 620 directed networks. Ecol. Complex., 5, 1–8.

- 621 Rhodes, C., & Anderson, R. (1996). Persistence and dynamics in lattice models
- 622 of epidemic spread. *J. Theor. Biol.*, 180, 125–133.
- 623 Rhodes, C. J., & Anderson, R. M. (2008). Contact rate calculation for a basic
- 624 epidemic model. *Math. Biosci.*, 216, 56 62.
- 625 Rogers, L., Delahay, R., Cheeseman, C., Langton, S., Smith, G. C., & Clifton-
- 626 Hadley, R. S. (1998). Movement of badgers (meles meles) in a high-density
- 627 population: Individual, population and disease effects. Proc. R. Soc. B, 265,
- 628 1269–1276.
- 629 Rohani, P., May, R. M., & Hassell, M. P. (1996). Metapopulations and equilib-
- rium stability: the effects of spatial structure. J. Theor. Biol., 181, 97–109.
- 631 Swinton, J., Harwood, J., Grenfell, B. T., & Gilligan, C. A. (1998). Persistence
- thresholds for phocine distemper virus infection in harbour seal phoca vitulina
- 633 metapopulations. J. Anim. Ecol., 67, 54–68.
- 634 Telfer, S., Holt, A., Donaldson, R., & Lambin, X. (2001). Metapopulation
- 635 processes and persistence in remnant water vole populations. Oikos, 95, 31–
- 636 42.
- 637 Vuilleumier, S., Wilcox, C., Cairns, B. J., & Possingham, H. P. (2007). How
- 638 patch configuration affects the impact of disturbances on metapopulation per-
- 639 sistence. Theor. Popul. Biol., 72, 77–85.
- 640 Webb, S. D., Keeling, M. J., & Boots, M. (2007). Host-parasite interactions
- between the local and the mean-field: how and when does spatial population
- 642 structure matter? J. Theor. Biol., 249, 140–152.
- 643 White, S. M., & White, K. A. J. (2005). Relating coupled map lattices to integro-
- difference equations: dispersal-driven instabilities in coupled map lattices. J.
- 645 Theor. Biol., 235, 463–475.

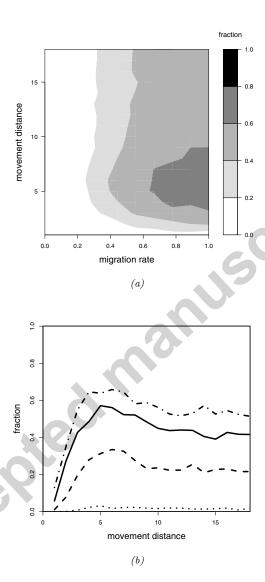


Figure 1: In a) the contour lines mark the area where the combination of the migration rate and the movement distance yield the same minimum fraction of simulations with persisting infection. In b) the fraction of simulations with persisting infection is shown with migration rate 0.2 (dotted line), 0.4 (dashed line), 0.6 (solid line) and 0.8 (dot-dashed line). The results are taken from 1000 simulations and the default parameter values are $P=100,~K=10,~\beta=10,~\gamma=0.5,~b=0.2$ and $\mu=0.01.$

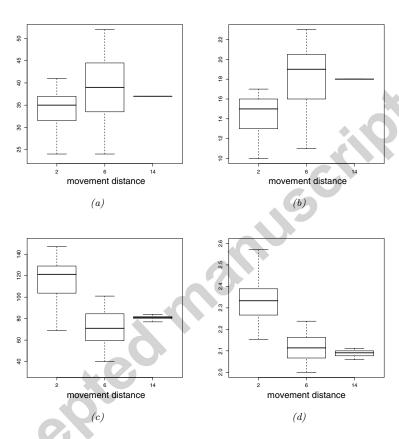


Figure 2: A box-and-whisker-plot, where the thick line denotes the median, the box encloses 50% of the observations and the whiskers show the 2.5 and 97.5 percentile. Panel a) shows the total number of time steps that a patch contains at least one infectious host is shown; panel b) the number of times that a patch gets infected, i.e. the number of transitions from no infectious host in a patch to at least one infectious host; panel c) the total number of infectious hosts per patch and panel d) the number of consecutive time steps a patch contains an infectious host. The results are from 1000 simulations with persisting infection, run till t=200. The default parameter values are P=100, K=10, $\beta=10$, $\gamma=0.5$, b=0.2 and $\mu=0.01$.

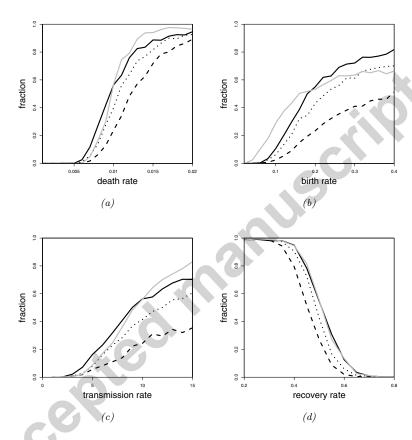


Figure 3: The fraction of simulations with persisting infection for a range of values of four demographical and epidemiological parameters. In each panel, the results (from 1000 simulations) are shown for the movement distance 2 (dashed line), 6 (solid line) and 14 (dotted line) and for a single homogeneously mixing population (grey line). A migration rate of 0.6 is used, and the default parameter values are $P=100,\,K=10,\,\beta=10,\,\gamma=0.5,\,b=0.2$ and $\mu=0.01.$

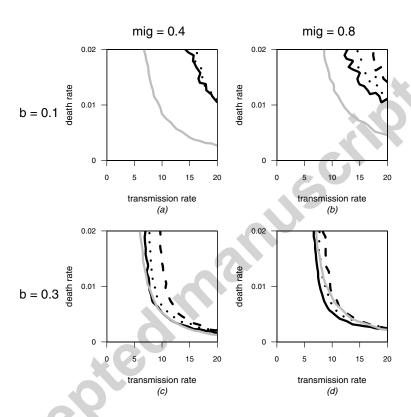


Figure 4: Curves for parameter combinations leading to the same fraction of simulations with persisting infection, where for panel a) and c) this fraction is 0.3 and for panels b) and d) the fraction is 0.6. The results are for movement distance 2 (dashed line), 6 (solid line) and 14 (dotted line) and for a single homogeneously mixing population (grey line). As migration rates 0.4 (panel a) and c) and 0.8 (panel b) and d) are used and birth rate 0.1 (panel a) and b)) and 0.3 (panel c) and d). The other parameters are set to the default values: P=100, K=10 and $\gamma=0.5$.