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Numerical and Experimental Study of the Interaction Between Two Marine Current Turbines

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Abstract—The understanding of interaction effects between marine energy converters represents the next step in the research process that should eventually lead to the deployment of such devices. Although some *a priori* considerations have been suggested recently, very few real condition studies have been carried out concerning this issue.

We therefore ran trials on 1/30th scale models of three-bladed marine current turbine prototypes in a flume tank. Our work focuses on the case where a turbine is placed at different locations in the wake of a first device. The interaction effects in terms of performance and wake of the second turbine are examined and compared to the results obtained on single-device configurations. Besides, we are currently developing a three-dimensional code based on a vortex method, which will be used in the near future to model more complex layouts.

The experimental study shows that the second turbine is deeply affected by the presence of an upstream device and that a compromise between individual device performance and inter-device spacing is necessary. Numerical results show good agreement with the experiment and are promising for the future modelling of turbine farms.

Index Terms—Marine current turbine, Array, Interaction effects, Vortex method, Laser Doppler Velocimetry

I. INTRODUCTION

A new level has been recently reached in the deployment of marine energy converters with the launching of several large-scale projects. For instance, India plans to install a 250MW tidal farm on its west coast, with a first implantation of fifty AK1000 (*Atlantis Resources*) turbines of 1MW each between 2012 and 2013 [1]. A few month later, the Scottish Government announced its approval for a 10MW tidal power array project on Scotland's west coast. It would consist of ten HS1000 (*Hammerfest Strøm*) turbines that should be installed from 2013 to 2015 [2]. *Marine Current Turbines Ltd* also announced in March 2011 that it had submitted a consent application to install in 2015 a 10MW tidal farm off the Anglesey coast, in Wales [3]. Some a priori studies have already been carried out to evaluate the potential retrievable power in specific areas, for instance the Race of Alderney, off the Cap de la Hague in France [4].

The behaviour of single marine energy converters such as marine current turbines is now globally well understood thanks to experimental and numerical studies [5]–[7]. However, as the size of such arrays is expected to grow with time, the issue of interaction effects between turbines, most importantly negative ones, has to be addressed. Some *a priori* considerations and suggestions have been presented in recent studies [8], [9] about different parameters of a marine current turbines array layout. As regards interaction effects, numerical studies on vertical axis tidal turbines have been carried out, such as [10] about the torque fluctuation.

The aim of the present paper is to give an idea of the interaction characteristics between two horizontal axis current turbines in real condition configurations. It complements a previous experimental study [7] carried on different but similar blade geometries and additional rotation speeds. We also wish to validate our three-dimensional code on a single device configuration, before extending it to multi-devices cases in the future. The main point is to be able to model more complex turbines array layouts, which cannot be set up in flume tanks.

The first part of this paper is thus dedicated to the characterization of a single marine current turbine behaviour and to the validation of the numerical software on these cases. The second part presents experimental trials on two-device configurations and uses the results on single device configurations as a comparison. Conclusions can then be drawn on the interaction effects between two marine current turbines. We eventually conclude and give an outlook on both our numerical and experimental future work.

II. SINGLE-DEVICE CONFIGURATION

Trials have been performed at the French Research Institute for Exploitation of the Sea (IFREMER) on a $1/30^{\text{th}}$ scale model of a three-bladed turbine prototype, in a $18 \times 4 \times 2m$ wave and current flume tank. The prototype consists of a rotor, which is 0.7m in diameter, and a 0.7m long axial hub (cf. figure 1). The blockage ratio is then less than 5%. The turbine blades are designed from a NACA63418 profile.

Force and moment on the turbine are measured thanks to six-component load cells, while velocity measurements are obtained thanks to a two component Laser Doppler Velocimetry (LDV) system. The experimental setup is presented in details in [7]. In this section, we present experimental trials concerning the wake behind the turbine and the performance of the device. Corresponding numerical results are shown in order to validate our numerical tool.

A. Description of the parameters

A marine current turbine may be subject to various parameters that can influence its behaviour, amongst others:

- The current velocity \mathbf{U}_∞ which we consider to be uniform and such that

$$\mathbf{U}_{\infty} = U_{\infty} \mathbf{e}_x \tag{1}$$

• The Tip Speed Ratio (TSR):

$$TSR = \frac{\Phi R}{U_{\infty}} \tag{2}$$

where R = D/2 denotes the rotor radius and Φ the rotation speed of the turbine.

• The ambient turbulence intensity rate (TI) defined by

$$TI = 100 \frac{\sqrt{\sigma_u^2 + \sigma_v^2 + \sigma_w^2}}{\sqrt{\bar{u}^2 + \bar{v}^2 + \bar{w}^2}}$$
(3)

where u, v and w are respectively the x, y and z velocity components, \bar{q} denotes the mean value and σ_q the standard deviation of quantity q.

These parameters, as well as the flume tank and turbine geometries are summarized on figure 1.



Figure 1. Description of the single configuration parameters. The origin O(0;0;0) is chosen at the rotor centre.

In our study, we consider an incoming velocity of 0.8m/s, a TSR between 0 and 10, and ambient TI of 5% and 25%. The

turbulence in the flow is induced by the current generator of the flume tank. Without the use of a honeycomb, a turbulence intensity rate of 25% is measured, which can be reduced to 5% by placing honeycomb grids at the beginning of the flume. These sources of turbulence imply an homogeneous turbulence structure.

B. Characterization of the wake

The general aspect of the wake behind a marine current turbine can be estimated by drawing velocity and turbulence maps of the downstream flow. Such maps can provide useful information to characterize the impact of the turbine on its close environment.

The LDV measurements are performed on a grid whose nodes (X_i, Y_i) are arranged as follows:

- $X_1 = 1.2D$ and $X_i = i \times D$ for i = 2, ..., 10.
- $Y_i = -1.2 + (i 1) \times 0.1$ m for i = 1, ..., 25, with two additional positions $Y_{26} = -Y_{27} = R = 0.35$ m;

The measurement on each node lasts 100 seconds with an observed data rate between 7 and 17Hz.

The downstream turbulence TI_{down} is evaluated as a turbulence intensity rate in the xOy plan:

$$TI_{down} = 100 \frac{\sqrt{\sigma_u^2 + \sigma_v^2}}{\sqrt{\bar{u}^2 + \bar{v}^2}} \tag{4}$$

As for the axial velocity, we consider u/U_{∞} , which represents the percentage of velocity recovered behind the turbine in comparison to the upstream velocity U_{∞} .

Figure 2 shows axial velocity and turbulence maps for different upstream ambient TI with a turbine at TSR=3.67. They point out that a higher ambient TI rate reduces the wake length in terms of velocity and turbulence. Indeed, figure 2(b) shows that at a distance of seven diameters behind the turbine in a 25% ambient TI, the axial velocity profile tends to recover its uniformity and about 90% of its intensity. On the other hand, the profile at the same location for an ambient 5% TI (figure 2(a)) remains very wake-shape like, with only 65% of U_∞ recovered at the centre. Even 10 diameters behind the turbine, the profile is still non-uniform and below the oncoming velocity, with about 75% recovered at the centre. The same behaviour can be observed with the downstream turbulence. Indeed, with a 5% ambient TI, figure 2(c) shows that 10 diameters behind the turbine, the downstream TI remains higher than 5%. On the contrary, it goes back to 25% in the case of an upstream 25% TI (figure 2(d)).

These experiments have been performed in the same conditions as in [7] but with a lower TSR to be able to compared them with our numerical computations. As a matter of fact, as stated in section II-C, computations with too high TSR are not valid because of our particles emission model. Another significant difference is that we have used new blades that are not patented, with a shorter chord, so as not to be limited by confidentiality restrictions.



Figure 2. Wake behind a turbine with TSR=3.67

C. Comparison with numerical results

A three-dimensional software is under development in the LOMC laboratory of Le Havre University, based on a Lagrangian vortex particle method [11]–[15]. The vortical flow is discretized into particles, which are small volumes of fluid carrying intrinsic physical quantities such as their position and vorticity. Those particles are emitted at the trailing edge of the obstacle according to the Kutta-Joukowski condition and then advected in a Lagrangian frame thanks to the Navier-Stokes equations for an incompressible flow. The details of the method we use are presented in [16]–[19]. Velocity maps can also be drawn from our numerical computations. Figure 3 presents an axial velocity map obtained from a numerical computation and shows that the general aspect of the wake is well reproduced. It should be pointed out that all of our computations are performed with a 0% ambient TI, with a Large Eddy Simulation (LES) turbulence model.



Figure 3. Axial velocity map from our simulation code with TSR=3.67, TI=0% and a turbulence model.

A closer look can be taken by considering a velocity profile at one particular distance behind the turbine. Figure 4 shows both experimental and numerical profiles 1.2 diameter behind the turbine. From these profiles we also estimated the mean value of the axial velocity $\bar{u}(x)$ at position x integrated on a $R^* = R + \delta r$ radius disc:

$$\bar{u}(x) = \frac{1}{{R^*}^2} \int_{-R^*}^{R^*} |y| u(x, y) \,\mathrm{d}y \tag{5}$$

Here we take $\delta r = 0.05 \text{m} \simeq 0.14 R$, which enlarges the integration interval to the two nearest experimental measurement nodes outside the rotor. In that manner, the whole velocity deficit is accounted for. The R^* radius disc thus represents the turbine's area of influence, which is slightly larger than the turbine's cross-section area. The numerical profile fits quite well with the experiment, even though the mean value seems to be slightly underestimated and the shape of the deficit is not accurately represented at the centre. This can be explained by our numerical turbulence model, which is not sophisticated enough at the present time and will be improved in the near future.

Now that the evaluation of the axial velocity mean value on the turbine's area of influence has been defined, we can examine the reduction of the velocity deficit as the distance from the turbine increases. The mean axial velocity deficit γ (in %) at a specific location x behind the turbine is defined as

$$\gamma(x) = 100(1 - \bar{u}(x))$$
(6)

We thus obtain figure 5, on which we see that with an ambient 5% TI, the experimental velocity deficit steadily decreases from nearly 40% at x < 2D down to 15% at x = 10D. On the other hand, with a 25% TI, the deficit decreases sharply in the close wake and then levels off around 8% from x = 5D. The relation between the velocity deficit (and therefore the velocity as well) and the distance from the turbine seems to be linear in the case of an ambient 5% TI. An equivalent numerical curve corresponding to the wake presented in figure 3 is also shown



Figure 4. Numerical (TI=0% with turbulence model) and experimental (TI=5%) axial velocity profile with TSR=3.67. Horizontal bars on the experimental curve represents the standard deviation and vertical bars represent the mean value of the axial velocity integrated on a $R + \delta r$ radius disc. The tips of the vertical bars represent the integration diameter for the estimation of the mean values (*i.e.* $2(R + \delta r)$).

in order to check that the wake dynamics is numerically well reproduced. A better turbulence model should enable us to compute more accurately and to distinguish the 5% and 25% TI configurations.



Figure 5. Mean velocity deficit behind the turbine for varying TI as values of 5% and 25% in the experiment, and a TI of 0% together with a turbulence model in the computation.

Another aspect of the behaviour of a marine current turbine can be deduced from the forces and moments on the turbine blades. More particularly, the axial moment or torque is used to determine the turbine power coefficient C_P that assesses its performance. Besides, the axial force can provide information about the fatigue of the machine and is used for the calculation of the thrust coefficient C_T .

The power coefficient is defined as the proportion of power \mathcal{P} retrieved by the turbine as compared to the maximum power

available from the incoming flow through the rotor area:

$$C_P = \frac{\mathcal{P}}{\frac{1}{2}\rho S U_\infty^3} = \frac{\mathcal{M}_x \Phi}{\frac{1}{2}\rho \pi R^2 U_\infty^3} = \frac{\mathcal{M}_x}{\frac{1}{2}\rho \pi R^3 U_\infty^2} \times TSR \quad (7)$$

where ρ is the density of the fluid, S is the cross-section area of the turbine and \mathcal{M}_x is the axial moment, also referred to as the turbine torque, defined as the x-component of the moment. Similarly, the thrust coefficient is defined as the axial force T acting upon the turbine as compared to the kinetic energy of the incoming flow through S:

$$C_T = \frac{T}{\frac{1}{2}\rho\pi R^2 U_\infty^2} \tag{8}$$

For a given current velocity of 0.8m/s, and an ambient TI of 5%, we present in figure 6 the evolution of power and thrust coefficients of a turbine function of its TSR. Figure 6(a) shows that approximately 40% of the total available power is retrieved by the turbine ($C_P \simeq 0.4$) when its TSR is between three and four. Once again, we compare these curves to results obtained from our numerical computations, which show very good agreement. However, our numerical particle emission model does not account for flow separation, which explains why for TSR higher than three, the C_P keeps increasing in the numerical computations while it should reach a peak and then decrease. The modelling of flow separation with our vortex method is currently being considered and should be implemented soon.

Other configurations and blades have been tested to validate our software in terms of C_P and C_T , in particular from [20], to examine the influence of the blades set angle and to check the convergence of our method. As pointed out, development is still necessary to improve the accuracy of our computations. More particularly, the turbulence model needs to be more sophisticated, which is why one of our first priority is to find an adequate model amongst those presented in [21], for instance. In order to assess correctly a turbine performance, the emission model of our numerical method also needs to be altered so as to account for flow separation. Once we have achieved those modifications, we will focus our attention on the modelling of multi-device configurations and we will be able to validate it thanks to the experimental results presented in the next section of this paper. The main interest of the fully-validated software will be to model with accuracy more complex layouts that cannot be set up in experimental trial facilities.

III. MARINE CURRENT TURBINES INTERACTION

A. General considerations

Studies concerning the layout of marine current turbines arrays are still few. However, general guidelines and *a priori* considerations can be found in recent literature [8], [9]. Two kinds of arrays have to be distinguished, first generation and second generation arrays, so called because of the probable progressive row by row growth of these farms. First generation arrays designate the youngest farms, made up of a single or two rows, designed to avoid any interaction effect between the turbines. On the contrary, second generation arrays refer



Figure 6. Evaluation of Power (C_P) and Thrust (C_T) coefficients, with a 5% ambient TI in the experiment. The corresponding evolution for our computations has been obtained with a TI of 0% with a turbulence model. The numerical points represent the mean values computed over $\Delta t = 2s$ and the vertical bars represent the standard deviation with respect to this mean value.

to older and bigger arrays in which such interactions cannot be avoided [8].

It is then clear that those two designations have a chronological meaning. As a matter of fact, at an early age of their implantation, arrays will be made up of one or two rows of turbines, the second row being placed downstream the first one and shifted so that the wakes of the upstream devices will not interact with the turbines of the second row. The early extensions of such arrays will be performed by adding new devices into the one or two existing rows, but a time will come when the only way to enlarge first generation arrays will consist in adding rows. From then on, interactions between turbines will no longer be avoidable. Figure 7 illustrates such a layout.

Several parameters, besides the depth of the array in the flow that we consider to be far enough from both the free surface and the sea bed in order to neglect their interaction,



Figure 7. Schematic top view of a marine current turbines array.

are characteristic of an array layout:

- The distance a_1 between two successive "even" rows;
- The distance a_2 between two successive "odd" rows;
- The distance *a*₃ between an upstream even row and the very next (odd) row;
- The distance b_1 between two adjacent turbines of a same row;
- The *y*-offset *b*₂ between two successive current perpendicular lines of turbines.

Some suggestions can be made concerning those parameters. In particular, it would be natural to consider that $b_2 = \frac{1}{2}b_1$, as it has been suggested in [8]. Similarly, parameters a_1 , a_2 and a_3 can be chosen such that $a_1 = a_2 = 2a_3$. However, the choice of a smaller a_3 would also make sense so as to benefit from potential "positive" interactions from the upstream turbines.

Our study focuses on the layout of second generation arrays issue, and more particularly on the characterization of the interaction effects between two marine current turbines placed one behind another. Hence parameter a_1 alone describes the configuration, and will then simply be referred to as a.

B. Experimental setup

The experimental setup is made up of two $1/30^{\text{th}}$ scale turbine models attached to one (for $a \le 5D$ configurations) or two (for a > 5D configurations) lengthwise girder(s) thanks to two poles of the same length. A photography of the setup with a = 4D is given in figure 8.

The girder is placed over the flume tank, parallel to the upstream current and at equal distance from the two sides. The downstream turbine is equipped with a six-component load cell and a two-component laser is attached to a footbridge over the flume. The laser can move along the footbridge that can itself be shifted backward and forward along the flume. The Laser Doppler Velocimetry (LDV) technique is used to measure axial and radial velocities at different locations on a grid behind the downstream turbine. This enables us to



Figure 8. Photography of the experimental setup with a = 4D. For a > 5D configurations, the lengthwise girder is split into two smaller girders and two additional transerse girders are used to support them (cf. figure 9).

draw maps such as those of figure 2 shown in section II-B. Schematic views of the complete setup are given in figure 9.



Figure 9. Schematic view of the experimental setup for configurations with a > 5D. The origin O(0; 0; 0) is chosen at the center of the downstream turbine rotor.

C. Wake interactions

We focus on a a = 4D configuration, with both TSR=3.67 and an upstream 5% ambient TI. This is motivated by the results obtained with a single turbine (cf. section II-B). As a matter of fact, when looking at figure 2(c), one can see that the turbulence intensity rate four diameters behind the turbine is in the order of 25%. We would thus like to compare this case to the single device configuration in a 25% ambient TI due to the current generation process in the flume tank without any "smoothing" techniques (e.g. using a honeycomb to reduce the ambient TI; for more detail, see [7]). If the downstream device in the a = 4D configuration behaves as if it were single, this would mean that there is no wake interactions *per se* and that the ambient TI rate represents the only affecting "input" parameters for the behaviour of interacting turbines.

In the single device configuration, figures 2(b) and 5 show that the velocity deficit behind a turbine in a 25% turbulent upstream flow tends to reduce rapidly. This represents a significant advantage with a view to place a second turbine in the wake of the first one. On the other hand, in the case of interacting turbines, axial velocity and turbulence maps behind the downstream turbine are drawn in figure 10. Since the downstream turbine is placed in an area where the mean turbulence intensity rate is close to 25%, the general aspect of its wake may look like the wake of a single turbine in a 25% ambient TI. Unfortunately, one can easily see that this is not the case, which indicates that there is a real interaction between the two turbines.

This suggests that the turbulence induced by the current generation process and the one induced by the turbine do not present the same characteristics. A complementary study will probably be carried out with two turbines in a 25% upstream ambient TI in order to determine whether the presence of the upstream turbine modifies the turbulence structure.



Figure 10. Wake behind the second turbine with a = 4D, upstream TI=5% and both TSR=3.67.

D. Downstream performance

Another way to evaluate the interaction effects between two turbines is to examine the performance of the downstream turbine. The comparison with the performance of a single device gives an idea on how deeply a turbine is affected by the presence of an upstream device. The evolution of the downstream turbine C_P^{down} is plotted against its TSR on figure 11, for different a/D configurations, and with an upstream device TSR of three, which yields maximum individual energy. The evolution of the single device C_P^{single} function of its TSR, already shown in section II-C, is also plotted as a matter of comparison. It should be noted that the TSR of the downstream turbine is computed thanks to equation (2) where U_{∞} is the upstream velocity before the first device, and thus not the mean velocity at the location of the second device. This choice is motivated by the fact that in real conditions, one will not be able to access the actual velocity at the location of the downstream turbine. Our study of interaction effects between turbines is thus carried out considering only "measurable" upstream quantities. By doing so, we aim at drawing general conclusions about the behaviour of interacting turbines depending only on those input parameters. Similarly, the downstream turbine C_P^{down} is still computed from the upstream velocity U_{∞} . It is then important to understand that C_P^{down} is an abuse of notation since this quantity does not represent any power coefficient; it can only be an indicator of the power retrieved as compared to the upstream velocity U_{∞} .



Figure 11. C_P^{down} of the downstream device function of its TSR, with an upstream TSR of 3 and an ambient TI of 5%, compared to the C_P^{single} of a single turbine shown in section II-C.

The experiment shows that the maximum C_P^{down} for the downstream turbine is obtained with a downstream turbine TSR between three and four, except for the a = 4D configuration where the C_P^{down} is slightly better with TSR=2. One can also notice that the longer the distance between the two devices is, the better the evolution of the downstream turbine C_p^{down} fits with a single turbine C_P^{single} . This is clearly due to the fact that the velocity deficit generated by a turbine decreases as a function of the distance from the device (cf. figure 5).

This trend can be confirmed by plotting the value of the maximum C_P^{down} obtained for each a/D configuration. We

define η as the ratio of the maximum C_P^{down} of the downstream device to the maximum C_P^{up} of the upstream device, that is to say the one obtained with TSR=3 for a single device:

$$\eta = \frac{\max\left(C_P^{down}(TSR)\right)}{\max\left(C_P^{up}(TSR)\right)} = \frac{\max\left(C_P^{down}(TSR)\right)}{C_P^{single}(TSR=3)}$$
(9)

Figure 12 shows the evolution of η function of the distance a/D, for upstream device TSR of 3 and 4. As expected, the maximum C_P^{down} raises as a increases and reaches 80% of the maximum retrievable power for a single device when a/D = 10. It should be pointed out that the downstream device can retrieve more power when the upstream turbine has its TSR=3 rather than 4. These results indicate that a compromise between individual performance and inter-device spacing is necessary. Considering an implantation area of given shape and surface, the more distant two successive rows of turbines, the higher the individual power retrieved; but there is then less space for additional rows of devices, that is to say that fewer turbines can be implanted. Hence a complete compromise has to be made considering the implantation of marine current turbines farms.



Figure 12. Maximum C_P^{down} obtained on the downstream turbine function of the inter-device distance, for two different upstream TSR.

IV. CONCLUSIONS AND OUTLOOK

A first study about interaction effects between two horizontal axis marine current turbines has been successfully carried out. On single device configurations, we characterized the wake behind the turbine in terms of velocity deficit and turbulence intensity and we saw that a higher upstream ambient TI tends to reduce the wake influence length. The behaviour of a single turbine has already been examined in terms of performance, which lead us to determine that the range of TSR yielding the most power was between three and four for this type of geometry. These experimental data enabled us to validate our numerical tool both on the wake computation and on the performance evaluation. The comparison showed very promising results and we are confident that we will soon be able to model successfully multi-device configurations. Single configurations data have been used as a basis to carry out trials on two devices configurations. We have shown that wake interaction effects between the turbines exist and that the downstream turbine is thus deeply affected by the presence of an upstream device. A qualitative and quantitative characterization of the interaction has been presented concerning both the wake and the performance of the downstream turbine. It is clear that increasing inter-device spacing to retrieve higher individual power can only be done to the detriment of the total number of turbine rows in a given space. So a compromise between individual performance and the number of energy converters has to be made wisely when considering an array implantation.

Some of our prospects, which concern both the experimental and the numerical aspect, consist in modelling other kinds of turbine prototypes or in taking into account both wave and current effects on the behaviour of marine current turbines.

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