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# Volume Assessment of the Cerebrospinal Fluid Spaces for Computer Aided Diagnosis

A. Lebret, E. Petit, B. Durning, J. Hodel, A. Rahmouni and P. Decq October 25, 2011

#### Abstract

The present work aims to provide support in the diagnosis of hydrocephalus, which requires an assessment to the volumes of the cerebrospinal fluid (CSF) within its total, ventricular and subarachnoid spaces. In this paper we describe a fully automatic method to estimate the CSF volumes from a new 3D whole body MR imaging sequence. The method was developed using image properties as well as anatomical and geometrical features, completed with a topological assumption on the CSF shape. Experiments on phantoms and clinical data were performed and evaluated by comparing our assessments of volumes with those derived from a segmentation controlled by expert physicians. Then we show that a robust distinction between pathological cases and healthy adult people can be achieved by a linear discriminant analysis on volumes of the ventricular and intracranial subarachnoid spaces. We also find that healthy adults maintain a proportional relationship between these volumes.

 $\label{lem:computer} \mbox{Keywords: cerebrospinal fluid, hydrocephalus, 3D segmentation, topology preservation, computer-aided diagnosis}$ 

#### 1 Introduction

Hydrocephalus is caused by an abnormal accumulation of the cerebrospinal fluid (CSF) into cerebral ventricles and/or subarachnoid cisterns of the brain (see [23] for more details). Obviously the measurement of mechanical features such as CSF pressures or volumes may be of great interest for assisted diagnosis and therapeutic [21, 16].

As MRI is a reference technique for the CSF imaging, a new sequence that significantly highlights the CSF, has recently been developed for intracranial images [9] and is also tested for whole body images. Due to the poor dynamic of the luminance perception of the human visual system, such images appear to be binary but in fact they are not (see Fig. 3, 4), and furthermore they are disturbed by noise and artifacts.

For now, the volume assessment of the CSF spaces is achieved by expert physicians by extracting the total volume through thresholding and interactive removal of noise and unwanted structures. Next, this volume is separated into its ventricular, spinal and intracranial subarachnoid spaces. This leads to a functional parameter calculated by the ratio between the ventricular CSF space volume and the intracranial subarachnoid one. This ratio could be efficient to discriminate healthy adults from patients affected by an hydrocephalus. However, it should be pointed out that most of the previous steps used to be manually performed and that the overlapping of ratio ranges between healthy people and patients may result to misclassification.

In order to solve these problems, we first propose to fully automate the above segmentation and separation steps, and then to refine the classification by applying a linear discriminant analysis to the ventricular and intracranial subarachnoid CSF volumes. We also show that healthy adults maintain a proportional relationship between these volumes.

To solve the segmentation and separation problems, we do not only use image properties, but also anatomical and geometrical features as well as a topological assumption about the CSF shape. The topological assumption becomes necessary because of both, the complex geometry of the CSF shape as shown in Fig. 1 (left), and the numerous image artifacts (especially motion artifacts), which can lead to changes in its topology. Benefits of associating topological constraints to medical image segmentation methods are shown in [29]. These constraints may prevent from any change in the topology of the anatomical structures to be extracted, such as unwanted created connections and/or holes. From a topological point of view, each anatomical structure including the CSF may be considered as a simple object such as a filled or a hollow sphere [1, 20, 25]. Several works have successfully added such constraints to their approach in order to preserve the topology of anatomical objects throughout the segmentation process (deformable surface with an energy minimization goal [18, 22], level set [8], fast marching [1], discrete deformable model [20], morphological operators [5, 25], statistical an topological atlases registration approach [2]).

Here, from a topological point of view, the CSF space is considered as a filled sphere as shown in Fig. 1 (right). This property, used as a refinement constraint, brings both accuracy and robustness to our segmentation method.

The paper is organized as follows. Section 2 describes the segmentation methodology for the whole CSF. The separation of the CSF volume into its ventricular, intracranial and spinal subarachnoid sub-volumes is presented in section 3. In section 4, we report experiments on phantoms and clinical dataset. Concluding remarks are given in section 5.

## 2 Segmentation of the whole CSF

The total CSF volume is segmented by using image properties with the hypothesis that its shape is topologically equivalent to a filled sphere as shown in Fig. 1 (right). The segmentation is performed as follows:

- 1. Extract an inner object  $(C_{inner})$  that is within the whole CSF as close as possible to its actual borders and has the same topology.
- 2. Extract an outer object of the CSF ( $C_{\text{lim}}$ ) that includes the whole CSF but do not necessarily have the same topology.
- 3. Homotopically thicken  $C_{\text{inner}}$  preserving its topology as long as it remains within  $C_{\text{lim}}$ . The transformation is guided by a priority function based on a distance criterion.

Note that obtaining both, inner and outer objects, as close as possible to the object of interest, allows to speed up significantly the processing time.

#### 2.1 Extraction of an inner object of the CSF

An inner object is extracted by applying the moment-preserving thresholding described in [33] on the initial image followed by a larger connected component extraction (Fig. 4–b).

#### 2.1.1 Moment-preserving thresholding

This method is suited to "binary nature" images with a low contrast. When the histogram presents an excessive overlapping between classes, the moment-preserving method becomes more efficient than conventional clustering-based or entropy-based methods.

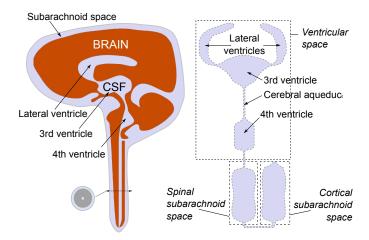


Figure 1: The CSF around the brain is considered as topologically equivalent to a filled sphere (right). In an axial cross-section of the spinal chord, the CSF has a disk topology (left).

The moment preservation assumes that statistical moments on original and thresholded images are identical. Let  $F = \{f_{ijk}\}$  be a 3D image of L intensity levels. For each intensity level z, its associated normalized histogram is given by p(z) and the statistical moment M of order m for m=1,2,3 is defined as:  $M_m = \sum_{z=0}^{L-1} p(z) z^m$ .

The resulting thresholded image  $G = \{g_{ijk}\}$  may be considered to be composed of two

gray levels  $z_0$  and  $z_1$  ( $z_0 < z_1$ ). The optimal threshold  $T_{\text{inner}}$  is obtained such that first three moments for F, the mean  $M_1$ , the variance  $M_2$  and the skewness  $M_3$ , are equals to those for Gwhen  $g_{ijk} = z_0$  (resp.  $g_{ijk} = z_1$ ) if  $f_{ijk} \leq T_{\text{inner}}$  (resp.  $f_{ijk} > T_{\text{inner}}$ ). Let  $P_0$  and  $P_1$  be the percentages of voxels of G on both sides of  $T_{\text{inner}}$ , the statistical moment

 $B_m$  of order m is:  $B_m = \sum_{l=0}^{1} P_l z_l^m$ . Moments preservation leads to solve the system:

$$\sum_{l=0}^{1} P_l z_l^m = \sum_{z=0}^{L-1} p(z) z^m, \tag{1}$$

with the constraint  $P_0 + P_1 = 1$  for m = 1, 2, 3. Equation (1) has four unknowns  $z_0, z_1, P_0$  and  $P_1$ , whose solution can be found in [33] and leads to a value for  $T_{\text{inner}}$  that is given by:

$$P_0 = \frac{1}{L} \sum_{z=1}^{T_{\text{inner}}} p(z).$$
 (2)

Figure 2 shows an histogram with the threshold  $T_{\rm inner}$  (= 38) obtained from the momentpreserving method, which allows to retrieve the inner CSF.  $T_{\rm lim}$  (= 13) is the threshold using the triangle thresholding, which is presented in Section 2.2 and allows to retrieve the outer object of the CSF. For comparison, the Otsu threshold  $T_{\text{Otsu}}$  (= 53) is also shown.

In Tab. 1, the results obtained by the other thresholding methods reviewed in [31], for the histogram on Fig. 2, are also presented for comparison to that of the moment-preserving and result in more distant threshold values.

#### Retrieval of the inner object 2.1.2

Since G contains several thresholded objects, a connected component labeling is performed to extract the three largest connected components (the inner object  $C_{\text{inner}}$  and both eyeballs  $E_1$  and

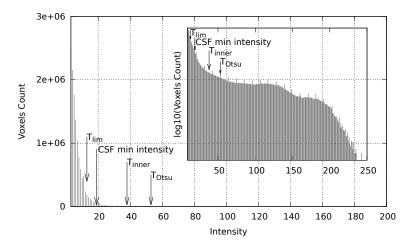


Figure 2: Image histogram sample from the clinical dataset and its zooming (vertical log scale) at the upper-right corner.

Table 1: Threshold values obtained on the histogram from Fig. 2 using various methods also reviewed in [31].

Method	${f Threshold}$
Attribute Huang [10]	1
Cluster Kittler [12]	5
Cluster Ridler [24]	52
Entropy Kapur [11]	43
Entropy Li [15]	4
Entropy Sahoo [26]	43
Entropy Shanbag [32]	241
Entropy_Yen [35]	53

 $E_2$ ).  $E_1$  and  $E_2$  are retained to determine a region of interest in Section 3.1. If  $C_{\text{inner}}$  has holes, then  $T_{\text{inner}}$  is automatically adjusted by increasing its value until the topological assumption is satisfied ( $E_1$  and  $E_2$  are not affected by this operation due to their intensity). By extracting the largest components (Fig. 4–b), residual noise as well as other small objects such as salivary ducts are also removed.

## 2.2 Thresholding of an outer object of the CSF

To extract an outer object of the CSF, another histogram-based thresholding method is carried out on the initial image as described in [36]. It is followed by a largest connected component extraction to retrieve an outer object of the CSF  $(C_{\text{lim}})$ .

The triangle thresholding algorithm in [36] is suitable for bimodal images for which the object to extract has a small amplitude and a large variance relatively to the background. Let p(z) be the histogram function for gray levels z. Maximum and minimum values,  $p_{\max}$  and  $p_{\min}$ , are determined from p(z) with their z values,  $z_{\min}$  and  $z_{\max}$ , and the points  $(z_{\min}, p_{\min})$  and  $(z_{\max}, p_{\max})$  are connected by a line segment  $\delta$ . Let  $d_e(a, b)$  be the Euclidean distance between two points a and b. For each point a = (z, p(z)), we can define the minimum distance from the

line segment  $\delta$  such that:  $d_{\min}(z, p(z)) = \min_{b \in \delta} \{d_{e}(a, b)\}$ . The optimal threshold  $T_{\lim}$  is obtained such that:

$$T_{\lim} = \underset{z}{\operatorname{argmax}} \{ d_{\min}(z, p(z)) \}. \tag{3}$$

 $C_{lim}$  is the object obtained as the largest connected component of the thresholded image.

### 2.3 Homotopic thickening of the inner object

An homotopic thickening is carried out on the inner object  $C_{inner}$ . The thickening is guided by a priority function  $\Psi$  that is related to  $C_{lim}$  and based on a distance criterion.

#### 2.3.1 Priority function

The priority function  $\Psi = \{\psi_{ijk}\}$  controls the order in which voxels are processed and eventually added to  $C_{\text{inner}}$ . This function uses an Euclidean distance map denoted by  $D = \{d_{ijk}\}$ , which is calculated by the linear algorithm proposed in [27]. The value  $\psi_{ijk}$  of each voxel (i, j, k) in the outer object  $C_{\text{lim}}$  is its distance to the nearest non-zero voxel of  $C_{\text{inner}}$  such that:

$$\psi_{ijk} = \begin{cases} d_{ijk} & \text{if } (i,j,k) \in C_{\lim} \\ +\infty & \text{otherwise.} \end{cases}$$
 (4)

#### 2.3.2 Guided homotopic thickening

Guided by the previous priority function  $\Psi$ , an homotopic thickening is applied to the inner object  $C_{\text{inner}}$  by adding simple points.

A point is simple if its addition to or its removal from a binary object C does not change the topology of the object and of the background. Therefore, removing simple points does not change the number of connected components and holes (cavities and/or tunnels) of C and its complement  $\overline{C}$ . It is shown in [3] that a simple point x is locally characterized by two topological numbers denoted by  $\mathcal{T}_n(x,C)$  and  $\mathcal{T}_{\bar{n}}(x,\overline{C})$  for  $(n,\bar{n}) \in \{(6,26),(26,6)\}$ , such that  $\mathcal{T}_n(x,C) = 1$  and  $\mathcal{T}_{\bar{n}}(x,\overline{C}) = 1$ . An efficient computation of  $\mathcal{T}_n(x,C)$  and  $\mathcal{T}_{\bar{n}}(x,\overline{C})$  that only involves the 26-neighborhood is also described in [3].

Let  $\partial \overline{C}_{\text{inner}}$  denotes the boundary of  $C_{\text{inner}}$  such that  $\partial \overline{C}_{\text{inner}} = \{x \in (\overline{C}_{\text{inner}} \cap C_{\text{lim}}) \mid N_n(x) \cap C_{\text{inner}} \neq \emptyset \}$ , where  $\overline{C}_{\text{inner}}$  is the complement of  $C_{\text{inner}}$  and  $N_n(x)$  is the n-neighborhood of x with  $n \in \{6, 26\}$ . The thickening process consists to add to  $C_{\text{inner}}$  simple points from  $\partial \overline{C}_{\text{inner}}$  as presented in Algorithm 1. It shows that boundary points (i.e. voxels) of  $\partial \overline{C}_{\text{inner}}$  are chosen iteratively, according to their priorities, and are incorporated into  $C_{\text{inner}}$  if they are simple. The resulting thickened object is illustrated in Fig. 3-d and 4-c, d.

## 3 Separation into CSF volumes

The separation of the CSF spaces is required to analyze the relationship between the ventricular and intracranial subarachnoid volumes. First, the spinal and intracranial regions are separated using geometrical and topological properties of the CSF at their interface. Second, to retrieve the ventricular space volume from that of the intracranial subarachnoid one, the cerebral aqueduct must be detected because we use it as a morphological reconstruction marker.

### Algorithm 1: Guided homotopic thickening

```
Input: C_{\text{inner}}, \Psi
Output: C_{\text{inner}}
Make a priority queue \mathcal{Q} from \partial \overline{C}_{\text{inner}} using \psi_{ijk} in the ascending order while \mathcal{Q} \neq \emptyset do
Poll x = (i, j, k) from \mathcal{Q};
if x is simple for C_{\text{inner}} then
C_{\text{inner}} \leftarrow C_{\text{inner}} \cup \{x\} ;
Add new points of \partial \overline{C}_{\text{inner}} around x to \mathcal{Q};
end if
end while
```

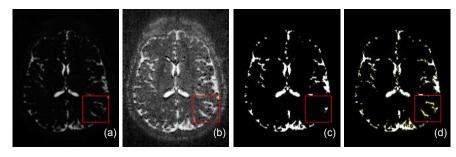


Figure 3: Segmentation process (axial cross-section), which is easily observed in the red square region. (a) original image; (b) contrast-enhanced original image; (c) inner object image; (d) homotopic thickened image.

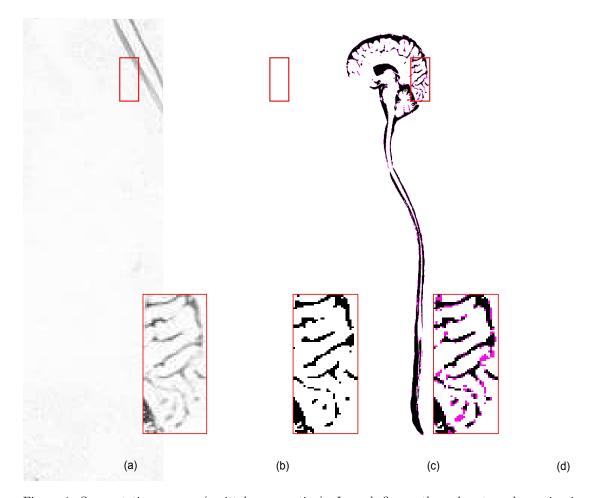


Figure 4: Segmentation process (sagittal cross-section). In each figure, the red rectangular region is zoomed in the bottom for more details. (a) original image; (b) inner object image; (c) homotopic thickened image; (d) 3D reconstruction after thickening. [inverted grayscale used to improve printing]

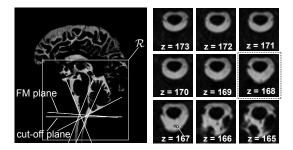


Figure 5: Separation of intracranial and spinal regions in the ROI  $\mathcal{R}$ . The resulting cut-off plane (z=168) is close to that goes through the foramen magnum (FM plane). The axial cross-sections around the cut-off plane are also illustrated (right).

#### 3.1 Separation of spinal and intracranial spaces

Expert physicians usually perform the disconnection of the spinal and intracranial spaces by tracking the foramen magnum (the hole in the bottom of the skull through which the spinal cord passes in order to be connected to the brain), which is even for an expert, difficult to detect on this type of images. The separation into spinal and intracranial spaces requires to locate the closest axial cross-section plane to that of the foramen magnum. Thus, the disconnection is achieved by browsing the 2D connected component on each axial plane from the spinal part, and by detecting any change in its topology (see the axial cross-section in Fig. 5). A region of interest (ROI) is first determined to reduce the processing time as well as to improve the robustness.

#### 3.1.1 Determination of the ROI

An ROI  $\mathcal{R}$  is used on one hand to locate the cutting axial cross-section, and on the other hand to retrieve the cerebral aqueduct in order to separate the intracranial space into its ventricular and subarachnoid spaces (Section 3.2). Apart from pathological cases, the eyeballs typically face the cerebral aqueduct in the axial plane. We consider the ROI forming a rectangular cuboid, each of whose edge is parallel to one of the i-, j-, k-axes of the image and such that:

- The ROI is located in the *i*-axis direction between the coronal plane that passes through the maximum posterior boundary of  $E_1$  and  $E_2$ , and the last coronal plane that still contains non-zero voxels.
- Let D be the larger diameter of  $E_1$  and  $E_2$ . The height of the ROI is set empirically to be 8D, such that the top face of the ROI is located with the distance 2D above the eyeballs and the bottom face is located with the distance 5D below the eyeballs. The height may be interactively resized to fit human variations.
- The depth is determined by the two sagittal planes between the medial boundaries of  $E_1$  and  $E_2$ .

#### 3.1.2 Determination of the cut-off plane

2D connected components are counted on each axial plane from the bottom to the top of the ROI  $\mathcal{R}$ . The first axial plane that shows a change in the topology of the connected components is the plane just above that of the searched cut-off (Fig. 5).

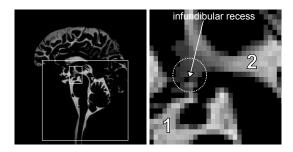


Figure 6: Proximity of the interpeduncular cistern (1) to the infundibular recess of the third ventricle (2). The small rectangular part in the left figure is zoomed in the right figure.

#### 3.2 Intracranial volumes separation

The process to extract the ventricular space may fail because of some subarachnoid regions that are very close to the third and fourth ventricles. Figure 6 shows, for instance, the proximity between the interpeduncular cistern and the infundibular recess of the third ventricle.

To overcome this problem we first detect a specific tubular object. The cerebral aqueduct is a thin tubular structure (diameter: 1 to 3 mm; length:  $\sim$ 14 mm) located in the median sagittal plane, which connects the third and fourth ventricles. It is also the longest tubular structure with the highest intensity range in the most median sagittal planes of the ROI  $\mathcal{R}$ . Its enhancement is performed by a vessel segmentation method (see [14]). Finally, ventricles are recovered by a morphological reconstruction [34] using the cerebral aqueduct as a marker.

#### 3.2.1 Detection of the cerebral aqueduct

Several methods to enhance vessel-like structures in 2D and 3D grayscale images are reviewed in [14]. Some efficient methods are based on properties of eigenvalues of the Hessian matrix  $\mathcal{H}$  [17, 28, 7, 13, 19]. These multi-scale methods operate in a Gaussian scale space on which they calculate second-order derivatives, build the Hessian matrix  $\mathcal{H}$ , and decompose it depending on its eigenvalues  $\lambda_1$ ,  $\lambda_2$  and  $\lambda_3$  such that  $|\lambda_1| < |\lambda_2| < |\lambda_3|$ . The eigenvalues are analyzed to determine the likelihood for each voxel (i, j, k) to belong to a curvilinear structure. This analysis is based on the following assumptions: 1)  $\lambda_1 \approx 0$ ; 2)  $\lambda_2 \approx \lambda_3 < 0$ ; and 3)  $|\lambda_1| \ll |\lambda_2|$ .

The tubular structure filter implemented in [7] is used to enhance the cerebral aqueduct. Let  $F_{\sigma} = \{f_{ijk}^{\sigma}\}$  the filter in [7] such that:

$$f_{ijk}^{\sigma} = \begin{cases} 0 & \text{if } \lambda_2 > 0 \text{ or } \lambda_3 > 0, \\ (1 - e^{-\frac{\mathcal{R}_A^2}{2\alpha^2}}) e^{-\frac{\mathcal{R}_B^2}{2\beta^2}} (1 - e^{-\frac{\mathcal{S}^2}{2c^2}}) & \text{otherwise,} \end{cases}$$
 (5)

where  $\mathcal{R}_A = |\lambda_2|/|\lambda_3|$ ,  $\mathcal{R}_B = |\lambda_1|/\sqrt{|\lambda_2\lambda_3|}$ ,  $\mathcal{S} = \sqrt{\lambda_1^2 + \lambda_2^2 + \lambda_3^2}$ , with some weights  $\alpha \in [0, 1]$ ,  $\beta \in ]0,1]$  and  $c \in [0,500]$ . Figure 7 compares extracted curvilinear structures in the ROI  $\mathcal{R}$  using methods from [28] (Fig. 7-b) and [7] (Fig. 7-c). It shows that unlike the filter in [28], that in [7] allows to dissociate strict tubular structures from others. The cerebral aqueduct part has more highlighted values in Fig. 7-c by adjusting the filter with a higher weight to detect lines  $(\alpha = 0.7)$ . The aqueduct is the longest connected component found in the most median sagittal planes.

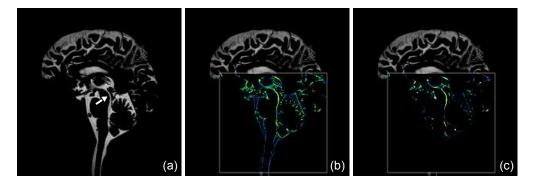


Figure 7: Detection of the cerebral aqueduct in the ROI  $\mathcal{R}$  (median plane cross-section). From left to right: (a) original thickened image; (b) filtered image by [28] ( $\sigma = 0.5$ ); (c) filtered image by [7] using 5 scale spaces  $\sigma$  from 0.4 to 0.9 and with  $\alpha = 0.7$ ,  $\beta = 0.2$  and c = 200.

#### 3.2.2 Ventricles reconstruction

Considering the cerebral aqueduct part as the marker, we would like to reconstruct all the ventricles. For this problem, methods such as fast marching [30], level set [30] or active contour models [4] are well known. However, the following two problems may hinder the reconstruction by the above methods: 1) the cerebral aqueduct part is too small as a marker to initialize a model; 2) motion artifacts may generate significant intensity inhomogeneities even in the ventricular spaces.

Grayscale reconstruction [34] is a very useful operator from mathematical morphology that provides satisfactory results here. Let  $\delta_{f,B_{\rm d}}^{(1)}(g)$  be the elementary geodesic dilation of a grayscale image g inside f (g is called the marker image and f is the mask) such that  $\delta_{f,B_{\rm d}}^{(1)}(g) = (g \oplus B_{\rm d}) \wedge f$ , where  $\wedge$  stands for the point-wise minimum and  $g \oplus B_{\rm d}$  is the geodesic dilation of g by an isotropic structuring element  $B_{\rm d}$  chosen as the unit ball. The geodesic dilation of size  $n \geq 0$  is obtained by:

$$\delta_{f,B_{d}}^{(n)}(g) = \underbrace{\delta_{f,B_{d}}^{(1)} \circ \delta_{f,B_{d}}^{(1)} \circ \cdots \circ \delta_{f,B_{d}}^{(1)}(g)}_{p, \text{ times}}.$$
(6)

The grayscale reconstruction by dilation  $\rho_{f,B_d}(g)$  of f from g is calculated by iterating geodesic dilations of g inside f until idempotence such that:

$$\rho_{f,B_{d}}(g) = \bigvee_{n \ge 1} \delta_{f,B_{d}}^{(n)}(g), \qquad (7)$$

where  $\vee$  stands for the point-wise maximum.

The ventricular space volume is retrieved by dilation of the previously detected cerebral aqueduct used as the marker image, using the parallel reconstruction algorithm proposed in [34]. Figure 8 shows the result of such a reconstruction using a 6-connectivity.

## 4 CSF volumes analysis

As the ground truth is not available for clinical data, the segmentation method for the total volume assessment was first validated on phantom MR images. Experiments were carried out on four phantoms of known volume (image size:  $250 \times 250 \times 128$  voxels) and 17 clinical MR images (image size:  $\sim 260 \times 790 \times 160$  voxels).

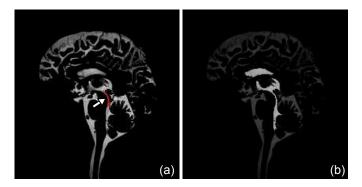


Figure 8: Ventricular space retrieving using a grayscale reconstruction by dilation of the cerebral aqueduct inside the original image: (a) the original image (the mask) and the cerebral aqueduct (the marker) colored in red; (b) result of the grayscale reconstruction.

#### 4.1 Images acquisition

MR images were acquired in the sagittal plane on a 1.5 T system (Magnetom Avanto; Siemens Medical Solutions, Erlangen, Germany). The MR sequence in [9], called SPACE (Sampling Perfection with Application optimized Contrast using different flip-angle Evolution), is a variant of the T2-weighted turbo spin echo sequence with variable flip-angles. The sequence was as follows: repetition time TR (ms)/echo time TE (ms), 2400/762; turbo factor of 141;  $250 \times 250$  mm field of view;  $256 \times 256$  acquisition matrix; 1 mm isotropic resolution; number of excitations 1.4; 160 slices; acquisition time, 3 min [9].

### 4.2 Complexity and computation time

The complexity in time is dominated by the homotopic thickening step and is  $\mathcal{O}(n \log n)$  where n is the number of points in  $\overline{C}_{\text{inner}} \cap C_{\text{lim}}$ . It may be reduced to be linear by parallelizing the homotopic thickening process. The total computation time for segmentation and separation was performed from 3 to 6 minutes on an Intel Pentium Dual Core 1.60 GHz / 2 GB for each clinical MR image.

#### 4.3 Validation on phantoms

Images were acquired from blood bags and synthetic resin phantoms with various shapes and volumes (see an example in Fig. 9). Phantoms 1 and 2 have regular shape while phantoms 3 and 4 have more tortuous one.

It has been observed (Fig. 10) that both segmentations, the semi-manual by an expert as explained in [9] and the grayscale reconstruction [34], have resulted in an overestimation. Instead, the methods of homotopic thickening and level set initialized by a fast marching have produced underestimated but close results. The guided homotopic thickening on phantoms has resulted in an accuracy of  $98.5\% \pm 1.8$  against  $94.6\% \pm 4.0$  for the semi-manual segmentation by an expert.

#### 4.4 Statistical analysis on clinical data

Clinical images were acquired from different subjects (ages between 25 and 84 years): seven healthy volunteers, two patients with a communicating hydrocephalus just two days after their surgery, and eight patients among which seven communicating hydrocephalus (CH) and one

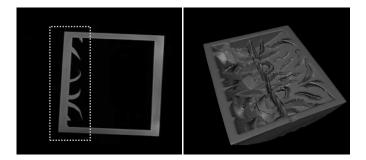


Figure 9: Example of a synthetic resin phantom MR image. Cross-section of the phantom (left). The 3D reconstruction of the rectangular region is shown in the right figure.

non-communicating hydrocephalus (NCH). Due to the limited number of clinical images, the CH and NCH patients have not been distinguished. In addition, the two patients who just have undergone their surgery were removed from the analysis because according to physicians, the CSF has not had enough time to reach the whole subarachnoidian space.

#### 4.4.1 Classification of clinical data

Following the proposal in [9] to use ratios to classify data, a linear discriminant analysis [6] was first performed on the clinical dataset using volumes of the ventricular and intracranial subarachnoid spaces as the input variables. Let TP, FP, TN and FN the respective numbers of true positives, false positives, true negatives and false negatives. The sensitivity  $S_{\rm e}$  and the specificity (or recall)  $S_{\rm p}$  are respectively defined as  $S_{\rm e} = TP/(TP+FN)$  and  $S_{\rm p} = TN/(TN+FP)$ . The additional  $F_1$ -score metric is also used to validate the classifier. It is defined as  $F_1 = 2pS_{\rm e}/(p+S_{\rm e})$  where p stands for the precision, defined by p = TP/(TP+FP). The predicted classification on the clinical data results in a sensitivity/specificity/ $F_1$ -score of 100%, which is a suitable result to discriminate between healthy people and pathological cases (Fig. 11). A similar observation was made on data from [9].

This first result appears to confirm such as in [9] that the relationship between the ventricular CSF space volume and the intracranial subarachnoid could be an efficient functional parameter to distinguish healthy people from pathological cases.

#### 4.4.2 Linear regression model for healthy adults

Observing the previous result has provided us the idea of carrying out a linear regression on the healthy people subset that results from the linear discriminant analysis step. Let  $V_{\rm V}$  and  $V_{\rm S}$  the respective volumes of the ventricular and intracranial subarachnoid spaces. We use the linear model:  $V_{\rm S} = \beta_0 + \beta_1 V_{\rm V} + \epsilon$ , and optimize the intercept  $\beta_0$  and the slope  $\beta_1$  by minimizing the residual error  $\epsilon$ . We obtain  $\beta_0 = 0$  and  $\beta_1 = 0.1071$ , namely:

$$V_{\rm V} = 0.1071 V_{\rm S} \tag{8}$$

Table 2 includes some statistics about the model: 1) the coefficient of determination  $R^2$  (= 98.43%) indicates that the predictor explains rather well the answer; 2) the F statistic (= 312.8) and the p-value (= 1.06e-05  $\ll$  0.05) show further that the null hypothesis ( $\beta_1 = 0$ ) can be rejected with a strong presumption. In addition, the graphical residuals analysis reinforces the linear regression assumptions (Fig. 12).

Table 2: Optimal linear regression model from the clinical data set.

Model	$R^2$	$\sigma^2$	Standard Error	F	p-value
$\overline{V_{\rm V} = 0.1071 V_{\rm S}}$	0.9843	12.25	0.0061	312.8	1.06e-05

The left figure of Fig. 13 shows the distribution of ventricular and intracranial subarachnoid volumes with the model obtained from (8). The right figure illustrates the same model with the distribution of the data from [9].

## 5 Conclusion

This work uses a new sequence of whole body MRI and succeeds in providing good estimations of the volumes of the CSF. The volumes are automatically retrieved through segmentation and separation steps, which use image properties, anatomical and geometrical features, as well as topological assumptions on the CSF. The proposed method seems to confirm the assumption that the proportional relationship between the ventricular and intracranial subarachnoid volumes allows to discriminate healthy and pathological cases. As the database is currently in expansion, our tool facilitates the refinement of these results in future work.

This new ability to quantify CSF volumes, which is a main parameter for the diagnosis, for the treatment decisions, for the monitoring of patients, and finally for clinical research, may represent an important breakthrough in the field of computer-aided neuro-imaging.

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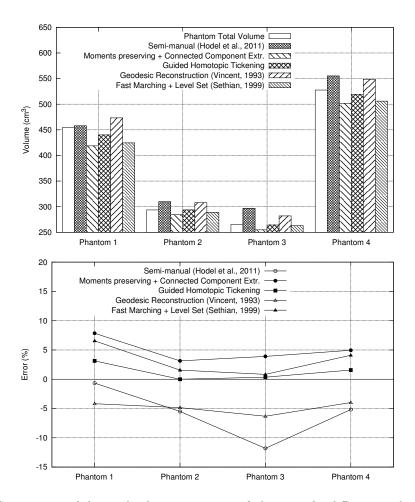


Figure 10: Comparisons of the total volume assessment of phantoms for different methods. Top: total volume measurement for objects that result from: the semi-manual segmentation by an expert as described in [9]; the initial inner object extraction (Section 2.1); the homotopic thickening process (Section 2.3); a grayscale reconstruction method [34] and a fast marching followed by a level set method [30], both using the inner object as a marker. Bottom: errors on the total volume measurement for the previous methods.

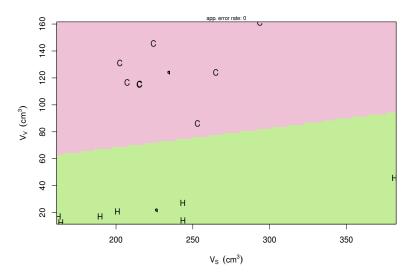


Figure 11: Resulting partition plots on clinical data by using a linear discriminant analysis considering two classes: "Healthy (H) and Pathological (C)".

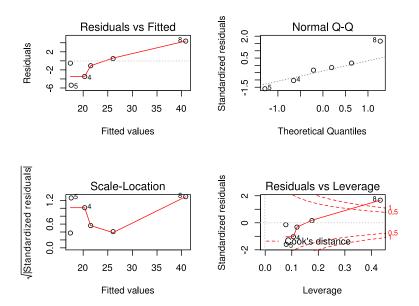


Figure 12: Residual plots from the linear regression on clinical data.

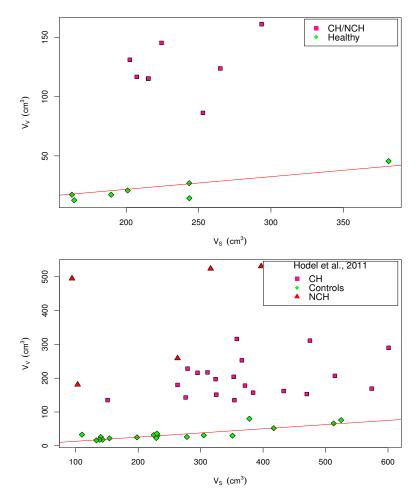


Figure 13: Linear model on  $V_{\rm V} \sim V_{\rm S}$  distributions. Top: the resulting linear regression on the healthy people subset of the clinical dataset; bottom: the linear model fitted on the healthy people subset of the dataset from [9].