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# **The Structure and Dynamics of Co-Citation Clusters: A MultipleͲPerspective CoͲCitation Analysis**

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# **Abstract**

**A multiple-perspective co-citation analysis method is introduced for characterizing and interpreting the structure and dynamics of co-citation clusters. The method facilitates analytic and sense making tasks by integrating network visualization, spectral clustering, automatic cluster labeling, and text summarization. Co-citation networks are decomposed into co-citation clusters. The interpretation of these clusters is augmented by automatic cluster labeling and summarization. The method focuses on the interrelations between a co-citation cluster's members and their citers. The generic method is applied to a three-part analysis of the field of Information Science as defined by 12 journals published between 1996 and 2008: 1) a comparative author co-citation analysis (ACA), 2) a progressive ACA of a time series of co-citation networks, and 3) a progressive document co-citation analysis (DCA). Results show that the multipleperspective method increases the interpretability and accountability of both ACA and DCA networks.**

**Keywords**: A multiple-perspective co-citation analysis, methodology, interpretation, summarization, visualization

# **Introduction**

Identifying the nature of specialties in a scientific field is a fundamental challenge for information science (Morris & Van der Veer Martens, 2008; Tabah, 1999). The growing interest in mapping and visualizing the structure and dynamics of specialties is due to a number of reasons:

- 1) the widely accessible bibliographic data sources such as the *Web of Science*, *Scopus*, and *Google Scholar* (Bar-Ilan, 2008; Meho & Yang, 2007) as well as domain-specific repositories such as *ADS*<sup>1</sup> and  $arXiv^2$ ;
- 2) freely available computer programs and web-based general-purpose visualization and analysis tools such as *ManyEyes*<sup>3</sup> and *Pajek*<sup>4</sup> (Batagelj & Mrvar, 1998), special-purpose citation analysis tools such as *CiteSpace*<sup>5</sup> (Chen, 2004; Chen, 2006), social network analysis such as *UCINET*<sup>6</sup>;
- 3) the intensified challenges for digesting the vast volume of data from multiple sources (e.g., e-Science, Digging into Data<sup>7</sup>, cyber-enabled discovery, SciSIP) (Lane, 2009).

 $\frac{1}{2}$  http://www.adsabs.harvard.edu/

 $^2$  http://arxiv.org/

http://manyeyes.alphaworks.ibm.com/ 4

http://vlado.fmf.uni-lj.si/pub/networks/pajek/ 5

http://cluster.cis.drexel.edu/~cchen/citespace/ 6

<sup>&</sup>lt;sup>6</sup> http://www.analytictech.com/ucinet6/ucinet.htm

 $\frac{7 \text{ http://www.diggingintodata.org/}}$ 

Co-citation studies are among the most common used methods in quantitative studies of science, especially including *Author Co-citation Analysis* (ACA) (Chen, 1999; Leydesdorff, 2005; White & McCain, 1998; Zhao & Strotmann, 2008b) and *Document Co-citation Analysis* (DCA) (Chen, 2004; Chen, 2006; Chen, Song, Yuan, & Zhang, 2008; Small & Greenlee, 1986; Small & Sweeney, 1985; Small, Sweeney, & Greenlee, 1985). Co-citation relations serve a fundamental grouping mechanism in co-citation studies. Researchers typically identify specialties in terms of aggregations of co-cited individual items. The ultimate goal is to obtain insights into emergent patterns. However, interpreting patterns identified in such studies remains a major bottleneck of the entire analytical process because essential tasks for interpretation such as categorization, summarization, synthesis, and integration are not only cognitively demanding but also inadequately supported. For instance, once co-citation clusters are identified, assigning the most meaningful labels for these clusters is currently a challenging task because any representative labels of clusters must characterize not only what clusters appear to represent, but also the salient and unique reasons for their formation.

In this article, we introduce a generic multiple-perspective method for both ACA and DCA studies. Our goal is to reduce the complexity of the sense-making and synthesizing process and to provide an enriched set of cues to facilitate a variety of common tasks in interpretation. The new procedure reduces analysts' cognitive burden by automatically characterizing the nature of a co-citation cluster in terms of 1) salient noun phrases extracted from titles, abstracts, and index terms of citing articles and 2) representative sentences as summarizations of clusters. The traditional co-citation analysis typically focuses on cited members of clusters as a primary source of evidence for interpretation. Focusing on citers can improve our understanding of the nature of a research front and its intellectual base.

Our work contributes to quantitative studies of science in two ways: 1) developing a generic and consistent procedure for both ACA and DCA studies, and 2) increasing the interpretability and accountability of co-citation analysis by shifting a considerable amount of burden from analysts to automatically generated structural and content cues.

The rest of the article is organized as follows. First, we outline existing studies of scientific knowledge domains and the field of information science in particular. We focus on their methodological strengths and weaknesses and major specialties identified in the field of information science. Next, we present a new, multiple-perspective, co-citation analysis methodology, including basic metrics and various algorithmic components. We then demonstrate the use of the method through a comparative ACA with reference to an earlier ACA, an ACA, and a DCA of the information science field, enlisting the support of sense-making cues produced by spectral clustering, automatic cluster labeling, abstract-based summarization, and interactive visualization. Finally, we discuss the strengths and limitations of the new approach and directions for future research and practice.

# **Co-Citation Analyses**

The number of co-citation studies is increasing not only in the field of information science but also in an increasingly larger number of fields (See Figure 1). There are many self-reflective studies of the field of information science by information scientists. In this section, we outline existing studies of information science, in particular, two major types of co-citation analyses and their major findings about the structure of the field.

# *Author Co-citation Analysis (ACA) of Information Science*

*Author Co-citation Analysis* (ACA) aims to identify underlying specialties in a field in terms of groups of authors who were cited together in relevant literature. An ACA study typically focuses on a network of cited authors connected by co-citation links.

Traditionally, ACA studies are limited to the first author of a cited reference only, primarily due to the lack of required data to perform all-author analysis. More recent studies have confirmed that all-author co-citation patterns reveal stronger groupings than first-author only patterns (Schneider, Larsen, & Ingwersen, 2009). In our study, first-author ACAs are used due to the data constraints.



**Figure 1. The growing number of co-citation analysis publications according to a topic search query of =***co-citation* **OR** *cocitation***@ in the Web of Science.** 

#### **ACA of Information Science (1972-1995) by White & McCain (1998)**

This widely known study has inspired many subsequent ACA studies. It presented a comprehensive view of information science based on 12 journals in library and information science across a 24-year span (1972-1995). It analyzed co-citation patterns of 120 most cited authors with factor analysis and multidimensional scaling. The authors drew upon their extensive knowledge of the field and offered an insightful interpretation of 12 specialties identified in terms of 12 factors. The most well-known finding of the study is that information science at the time consisted of two essentially independent camps, namely the information retrieval camp and the literature camp, including citation analysis, bibliometrics, and scientometrics. This study has become an exemplar of ACA studies in terms of its methodology and its account of information science as a discipline.

#### **ACA and ABCA of Information Science (1996-2005) by Zhao & Strotmann (2008a, 2008b)**

Zhao and Strotmann (2008a, 2008b) followed up White and McCain's study using the same set of 12 journals and the same number of 120 cited authors in an updated time frame of 1996-2005. Zhao and Strotmann (2008a) studied the intellectual base, defined by co-cited authors (ACA), and the patterns of citing authors called *author-bibliographic coupling analysis* (ABCA).

Zhao and Strotmann (2008b) found five major specialties and manually labeled them as *user studies*, *citation analysis*, *experimental retrieval, webometrics*, and *visualization of knowledge domains.* In contrast to the findings of (White & McCain, 1998), *experimental retrieval* and *citation analysis* retained their fundamental roles in the field, and the *user studies* specialty became the largest specialty. *Webometrics* and *visualization of knowledge domains* appeared to make connections between the retrieval camp and the citation analysis camp.

In their second study, Zhao and Strotmann (2008a) adapted the *bibliographic coupling* method introduced by Kessler (1963) and analyzed co-citing authors (ABCA). They compared the intellectual base (ACA) and research fronts (co-citing authors) during the period of 1996-2005. Again, the study was limited to the

topmost 120 citing authors using factor analysis and principle component analysis (PCA) to identify specialties.

Their analysis of current citing authors found that the global two-camp structure was still evident. They also found that the literatures camp, namely *citation* and *bibliometrics*, "remained remarkably stable and unperturbed by the Web revolution", and that *webometrics* became an important component in this camp. Furthermore, *webometrics* was more active during 1996-2000 than 2001-2005.

# *Document Co-citation Analysis (DCA)*

Document Co-citation Analysis (DCA) studies a network of co-cited references (Small, 1980, 2003). The fundamental assumption is that co-citation clusters reveal underlying intellectual structures. The notion that cited documents are in effect concept symbols was introduced by Small (1978). He found a high degree of uniformity in how specific concepts and specific references to documents (cited documents) were associated in chemistry literature. These cited documents serve as symbols for scientific ideas, methods, and experiments. This idea is further extended to clusters of noun phrases extracted from citation contexts of cited documents (Schneider, 2006). From the concept symbol perspective, the study of a co-citation network focuses on interpreting the nature of a cluster of cited documents and interrelationships between clusters.

DCA is expected to reveal more specific patterns than ACA because cited references in DCA carry more specific information than cited authors in ACA. The nature of the use of a cited reference in a DCA network should be relatively easier to identify and less ambiguous to interpret than the nature of the use of a cited author in an ACA network. We expect that both DCA and ACA networks would lead us to unique insights and it will be valuable to establish a comprehensive methodology that can be consistently applied to both types of analysis so that one can compare and cross reference the results.

# **DCA of Library and Information Science (1990-2004) by Aström (2007)**

In contrast to ACA studies, there are much fewer DCA studies in the literature. A DCA by Aström (2007) studied papers published between 1990 and 2004 in 21 library and information science journals. Results were depicted in multidimensional scaling (MDS) maps. Aström's study also identified the two-camp structure found by (White & McCain, 1998). On the other hand, Aström found an *information seeking and retrieval* camp, instead of the *information retrieval* camp as in (White and McCain, 1998).

# *Determining the Nature of Specialties: A Bottleneck*

An increasing number of analytical tasks in ACA and DCA are now facilitated by computer programs. However, researchers and analysts still have to deal with a large amount of diverse and complex information. We address some of the current challenges and how we propose to facilitate the process.

Both ACA and DCA studies focus on structural patterns of co-cited authors or references. It is a common practice in ACA studies to identify research specialties in terms of co-citation clusters or multivariate factors and then interpret the nature of these specialties. While manually labeling a co-citation cluster can be a very rewarding process of learning about the underlying specialty and result in insightful and easy to understand labels, it requires a substantial level of domain knowledge and it tends to be time consuming and cognitively demanding because of the synthetic work required over a diverse range of individual publications. In addition, it is hard for others to follow the heuristics and criteria used in the original analytic reasoning process.

Traditionally, researchers often identify the nature of a co-citation cluster based on common themes among its members. For example, White and McCain (1998) tapped on their decades of domain knowledge and identified what members of specialties have in common. Similarly, Zhao and Strotmann (2008a, 2008b) also focused on common areas shared by member authors of each factor. The emphasis on common areas is a practical strategy; otherwise, comprehensively identifying the nature of a specialty can be too complex to handle manually. In addition to identify common characteristics, co-citation analysts need to synthesize a diverse range of potentially conflicting information, aggregate and categorize lower

level evidence to arrive at a coherent interpretation at a higher level abstraction. One can leverage algorithmically generated semantic cues so as to facilitate these cognitively demanding tasks and reduce potential biases and uncertainties.

Algorithmically labeling co-citation clusters is a crucial step towards improving the overall efficiency of citation analysis. The *Institute for Scientific Information* (ISI) and others pioneered various approaches. A fundamental challenge for automatic labeling is due to the practically limited vocabulary that one can possibly extract from a given data source because the best possible candidates may never appear in the data per se. A promising strategy is to expand the vocabulary pool by tapping into multiple data sources such as the *Wikipedia* (Carmel, Roitman, & Zwerdling, 2009). Similarly, Zuccala (2006) selected cluster labels from classification codes assigned to papers written by authors in a cluster. Our goal is to facilitate an otherwise entirely manual labeling process so that analysts may evaluate and choose algorithmically generated terms. It is our intention that human analysts will still maintain a full control of the interpretation and sense making stages of the citation analysis.

# *Identifying Specialties in Information Science*

How is the field of information science itself organized? What are the major components in its structure? How many specialties are there? These questions have been addressed in the literature. Now we are seeking additional insights by using a multiple-perspective approach.

Many researchers have studied the structural and dynamic properties of specialties in information science in terms of clusters, multivariate factors, and principle components (Morris & Van der Veer Martens, 2008; Persson, 1994; Tabah, 1999; White & Griffith, 1982). A recent study of information science (Ibekwe-SanJuan, 2009) mapped the structure of information science at the term level using a text analysis system *TermWatch* and a network visualization system *Pajek*, but it did not address structural patterns of cited references. Researchers also studied the structure of information science qualitatively, especially with direct inputs from domain experts. For example, Zins conducted a *Critical Delphi* study of information science, involving 57 leading information scientists from 16 countries (Zins, 2007a, 2007b, 2007c, 2007d). Our present study focuses on quantitative approaches.

Janssens, Leta, Glänzel, and De Moor (2006) studied the full-text of 938 publications in five library and information science journals with Latent Semantic Analysis (LSA) (Deerwester, Dumais, Landauer, Furnas, & Harshman, 1990) and agglomerative clustering. They found an optimal 6-cluster solution in terms of a local maximum of the mean silhouette coefficients (Rousseeuw, 1987) and a stability diagram (Ben-Hur, Elisseeff, & Guyon, 2002). Their clusters were labeled with single-word terms selected by tf\*idf (p. 1625), which are not as informative as multiword terms for cluster labels.

Klavans, Persson, and Boyack (2009) recently raised the question of the true number of specialties in information science. They suspected that the number is much more than the 11 or 12 as reported in ACA studies such as (White & McCain, 1998) and (Zhao & Strotmann, 2008a, 2008b), but significantly fewer than the 72 reported in their own study, which is also based on the 12 journals between 2001 and 2005.

# **Method**

Building on the work of these relevant studies, we introduce a multiple-perspective co-citation analysis method. The term *multiple-perspective* refers to the analysis of structural, temporal, and semantic patterns as well as the use of both citing and cited items for interpreting the nature of co-citation clusters. We focus on ACA and DCA in this article. In this section, we first set the context of our work with reference to the traditional procedure and introduce several citation-related and structure-related metrics for subsequent discussions. Then we explain three components of the new procedure, namely, clustering, labeling, and sentence selection. We briefly introduce *CiteSpace*, the system we use to perform the study.

# *Data*

We applied the new method to a domain analysis of information science as defined by the same 12 journals used by White and McCain (1998) and Zhao and Strotmann (2008a) but over a longer time span

(1996-2008). Since the initial selection of the 12 journals was more than a decade ago, they may no longer be the best cohort to track the field of information science. On the other hand, from the point of view of validation and continuity with regard to previous studies, these journals are rich enough to demonstrate the multiple-perspective method.

The 12-journal *Information Science* dataset, retrieved from the *Web of Science*, contains 10,853 unique bibliographic records, written by 8,408 unique authors from 6,553 institutions and 89 countries. These articles cited 129,060 unique references for a total of 206,180 times. They cited 58,711 unique authors and 58,796 unique sources. See Table 1 for details.

<b>Start</b>	End	<b>Citing Sources: Journal Title</b>	Abbr.	<b>Records</b>	<b>Citations</b>	<b>Cites</b>
					(TC)	per
						Paper
1996	2008	Annual Review of Information Science and Technology	<b>ARIST</b>	158	1,584	10.03
1996	2008	Electronic Library	EL	1,346	835	0.62
1996	2008	Information Processing & Management	IP&M	1,037	6,398	6.17
1996	2008	Information Technology and Libraries	<b>ITL</b>	474	721	1.52
1996	2008	Journal of Documentation	<b>JOD</b>	1,057	3,716	3.52
1996	2008	Journal of Information Science	<b>JIS</b>	653	2,510	3.84
1996	2000	Journal of the American Society for Information Science	<b>JASIS</b>	851	8,211	9.65
2001	2008	Journal of the American Society for Information Science and Technology	<b>JASIST</b>	1,410	6,857	4.86
1996	2008	Library & Information Science Research	<b>LISR</b>	565	1,462	2.59
1996	2008	Library Resources & Technical Services	<b>LRTS</b>	542	579	1.07
1996	1996	PROGRAM-Automated Library and Information Systems	P-ALIS	124	41	0.33
1996	2008	PROGRAM-Electronic Library and Information Systems	P-ELIS	1,215	$\overline{376}$	0.31
1996	2008	Scientometrics	<b>SCM</b>	1,421	8,447	5.94

**Table 1. The Information Science (1996-2008) dataset defined by 12 source journals.** 

# *Extending the Traditional Procedure*

The primary goal of co-citation analysis is to identify the intellectual structure of a scientific knowledge domain in terms of the groupings formed by accumulated co-citation trails in scientific literature. The traditional procedure of co-citation analysis for both DCA and ACA consists of the following steps:

- 1. Retrieve citation data from sources such as the *Science Citation Index* (SCI), *Social Science Citation Index* (SSCI), *Scopus*, and *Google Scholar*.
- 2. Construct a matrix of co-cited references (DCA) or authors (ACA).
- 3. Represent the co-citation matrix as a node-and-link graph or as a multidimensional scaling (MDS) configuration with possible link pruning using Pathfinder network scaling or minimum spanning tree algorithms.
- 4. Identify specialties in terms of co-citation clusters, multivariate factors, principle components, or dimensions of a latent semantic space using a variety of algorithms for clustering, communityfinding, factor analysis, principle component analysis, or latent semantic indexing.

# 5. Interpret the nature of co-citation clusters.

The interpretation step is the weakest link. It is time-consuming and cognitively demanding, requiring a substantial level of domain knowledge and synthesizing skills. In addition, much of attention routinely focuses on co-citation clusters per se, but the role of citing articles that are responsible for the formation of such co-citation clusters may not be always investigated as an integral part of a specialty. While the focus on the target of citation may reveal seminal members of a specialty, it does not necessarily reflect the dynamics of the specialty in terms of the impact on its citers. Researchers have used citing information to summarize the essence of a co-citation cluster. For example, Small (1986) introduced a method for generating specialty narratives by walking through a co-citation network and selecting passages that cite the core documents in a co-citation cluster. There are also other studies that take citing information into account (Schneider, 2009).

Given the diversity and complexity of relationships between citers and cited entities (Cronin, 1981), synthesizing the nature of a co-citation cluster is cognitively too demanding for analysts to handle manually. The lack of algorithmic support for these tasks forces analysts to rely on their own domain knowledge and their experience. It makes it hard to differentiate evidence-based findings from heuristics and speculations. Such ambiguity may hinder subsequent evaluation and scholarly communication of research findings. These problems motivate us to develop a multiple-perspective method to improve the robustness of the traditional procedure.

Our new method extends and enhances traditional co-citation methods in two ways: 1) by integrating structural and content analysis components sequentially into the new procedure and 2) by facilitating analytic tasks and interpretation with automatic cluster labeling and summarization functions. The new procedure is highlighted in yellow in Figure 2, including clustering, automatic labeling, summarization, and latent semantic models of the citing space (Deerwester et al., 1990).



**Figure 2. New functions facilitate and enhance the interpretation of co-citation clusters.** 

# *Metrics*

Our new procedure adopts several structural and temporal metrics of co-citation networks and subsequently generated clusters. Structural metrics include betweenness centrality, modularity, and silhouette. Temporal and hybrid metrics include citation burstness and novelty.

The betweenness centrality metric is defined for each node in a network. It measure the extent to which the node is in the middle of a path that connects other nodes in the network (Brandes, 2001; Freeman, 1977). High betweenness centrality values identify potentially revolutionary scientific publications (Chen, 2005) as well as gatekeepers in social networks. For example, if a node provides the only connection between two large but otherwise unrelated clusters, then this author would have a very high value of betweenness centrality. Recently, power centrality introduced by Bonacich (1987) is also drawing a lot of attention in dealing with networks in which someone's power depends on the power of those (s)he is socially related to, for example, in (Kiss & Bichler, 2008).

In the context of this study, the modularity Q measures the extent to which a network can be divided into independent blocks, i.e. modules (Newman, 2006; Shibata, Kajikawa, Taked, & Matsushima, 2008). The modularity score ranges from 0 to 1. A low modularity suggests a network that cannot be reduced to clusters with clear boundaries, whereas a high modularity may imply a well-structured network. On the other hand, networks with modularity scores of 1 or very close to 1 may turn out to be some trivial special cases where individual components are simply isolated from one another. Since the modularity is defined for any network, one may compare different networks in terms of their modularity, for example, between ACA and DCA networks.

The silhouette metric (Rousseeuw, 1987) is useful in estimating the uncertainty involved in identifying the nature of a cluster. The silhouette value of a cluster, ranging from -1 to 1, indicates the uncertainty that one needs to take into account when interpreting the nature of the cluster. The value of 1 represents a perfect separation from other clusters. In this study, we expect that cluster labeling or other aggregation tasks will become more straightforward for clusters with the silhouette value in the range of 0.7~0.9 or higher.

Burst detection determines whether a given frequency function has statistically significant fluctuations during a short time interval within the overall time period. It is valuable for citation analysts to detect whether and when the citation count of a particular reference has surged. For example, after the September 11 terrorist attacks, citations to earlier studies of Oklahoma City Bombing were increased abruptly (Chen, 2006). It can be also used to detect whether a particular connection has been significantly strengthened within a short period of time (Kumar, Novak, Raghavan, & Tomkins, 2003). We adopt the burst detection algorithm introduced in (Kleinberg, 2002).

Sigma  $(Y)$  is introduced in (Chen, Chen, Horowitz, Hou, Liu, & Pellegrino, 2009a) as a measure of scientific novelty. It identifies scientific publications that are likely to represent novel ideas according to two criteria of transformative discovery. As demonstrated in case studies (Chen et al., 2009a), Nobel Prize and other award winning research tends to have highest values of this measure. In this study, Sigma is defined as (*centrality+*1)*burstness* such that the brokerage mechanism plays more prominent role than the rate of recognition by peers.

# *Clustering*

We adopt a hard clustering approach such that a co-citation network is partitioned to a number of nonoverlapping clusters. It is more efficient to use non-overlapping clusters than overlapping ones to differentiate the nature of different co-citation clusters, although it is conceivable to derive a soft clustering version of this particular component. Resultant clusters are subsequently labeled and summarized.

In this article, co-citation similarities between items *i* and *j* are measured in terms of cosine coefficients. If *A* is the set of papers that cites *i* and *B* is the set of papers that cite *j*, then  $w_{ij} = \frac{|A \cap B|}{\sqrt{|A| \times |B|}}$ , where  $|A|$  and  $|B|$ 

are the citation counts of *i* and *j*, respectively; and  $|A \cap B|$  is the co-citation count, i.e. the number of times they are cited together. Alternative similarity measures are also available. For example, Small (1973) used  $w_{ij} = \frac{|A \cap B|}{|A \cup B|}$ , which is known as the Jaccard index (Jaccard, 1901).

A good partition of a network would group strongly connected nodes together and assign loosely connected ones to different clusters. This idea can be formulated as an optimization problem in terms of a cut function defined over a partition of a network. Technical details are given in relevant literature (Luxburg, 2006; Ng, Jordan, & Weiss, 2002; Shi & Malik, 2000). A *partition* of a network *G* is defined by a set of sub-graphs  $\{G_k\}$  such that  $G = \bigcup_{k=1}^K G_k$  and  $G_i \cap G_j = \emptyset$ , for all  $i \neq j$ . Given sub-graphs *A* and *B*, a *cut function* is defined as follows:  $cut(A, B) = \sum_{i \in A, i \in B} w_{ij}$ , where  $w_{ij}$ 's are the cosine coefficients mentioned above. The criterion that items in the same cluster should have strong connections can be optimized by maximizing  $\sum_{k=1}^{K} cut(G_k, G_k)$ . The criterion that items between different clusters should be only weakly connected can be optimized by minimizing  $\sum_{k=1}^{K} cut(G_k, G - G_k)$ . In this study, the cut function is normalized by  $\sum_{k=1}^{K} \frac{\text{cut}(G_k, G - G_k)}{\text{vol}(G_k)}$  $\frac{\text{cut}(G_k, G - G_k)}{\text{vol}(G_k)}$  to achieve more balanced partitions, where  $\text{vol}(G_k)$  is the sum of the weights of links in  $G_k$ , i.e.  $vol(G_k) = \sum_{i \in G_k} \sum_j w_{ij}$  (Shi & Malik, 2000).

Spectral clustering is an efficient and generic clustering method (Luxburg, 2006; Ng et al., 2002; Shi & Malik, 2000). It has roots in spectral graph theory. Spectral clustering algorithms identify clusters based on eigenvectors of Laplacian matrices derived from the original network. Spectral clustering has several desirable features compared to traditional algorithms such as *k*-means and single linkage (Luxburg, 2006):

- 1. It is more flexible and robust because it does not make any assumptions on the forms of the clusters;
- 2. It makes use of standard linear algebra methods to solve clustering problems; and
- 3. It is often more efficient than traditional clustering algorithms.

Our multiple-perspective method utilizes the same spectral clustering algorithm for both ACA and DCA studies. Despite its limitations (Luxburg, Bousquet, & Belkin, 2009), spectral clustering provides clearly defined information for subsequent automatic labeling and summarization to work with. In this study, instead of letting the analyst to specify how many clusters there should be, the number of clusters is uniformly determined by the spectral clustering algorithm based on the optimal cut described above.

#### *Automatic Cluster Labeling*

Candidates of cluster labels are selected from noun phrases and index terms of citing articles of each cluster. These terms are ranked by three different algorithms. In particular, noun phrases are extracted from titles and abstracts of citing articles. The three term ranking algorithms are *tf\*idf* (Salton, Yang, & Wong, 1975), *log-likelihood ratio* (LLR) tests (Dunning, 1993), and *mutual information* (MI). Labels selected by *tf\*idf* weighting tend to represent the most salient aspect of a cluster, whereas those chosen by log-likelihood ratio tests and mutual information tend to reflect a unique aspect of a cluster.

Garfield (1979) has discussed various challenges of computationally selecting the most meaningful terms from scientific publications for subject indexing. Indeed, the notion of citation indexing was originally proposed as an alternative strategy to deal with some of the challenges. White (2007a, 2007b) offers a new way to capture the relevance of a communication in terms of the widely known *tf\*idf* formula.

#### *Automatic Summarization of Citers' Abstracts*

Each co-citation cluster is summarized by a list of sentences selected from the abstracts of articles that cite at least one member of the cluster. Sentences are selected based on the following principles.

A good summary should have a sufficient and balanced coverage with minimal redundant information (Sparck Jones, 1999). Automatic multi-document summarization typically constructs a short summary by selecting the most representative sentences from a set of topically related documents. Teufel and Moens (2002) have proposed an intriguing strategy for summarizing scientific articles based on the rhetorical status of statements in an article. Their strategy specifically focuses on identifying the new contribution of

a source article and its connections to earlier work. Automatic summarization techniques have been applied to areas such as identifying drug interventions from MEDLINE (Fiszman, Demner-Fushman, Kilicoglu, & Rindflesch, 2009).

In this study, sentences are ranked by *Enertex* (Fernandez, SanJuan, & Torres-Moreno, 2007). Given a set *S* of *N* sentences, let *M* be the square matrix that for each pair of sentences gives the number of nominal words in common (nouns and adjectives). Sentences are ranked by an energy function *E*, which is defined for each sentence  $s_i \in S$  as follows:

$$
E(s_i) = \sum_{j=1}^{N} M^2_{ij}
$$

Two sentences,  $s_1$  and  $s_2$ , are not directly connected if they do not have overlapping words. However, they can be indirectly connected if there is a sentence  $s_3$  such that  $s_3$  overlaps with  $s_1$  and  $s_2$  respectively. The energy function *E* takes into account indirect connections between sentences. According to Fernandez et al. (2007), the energy function *E* in Enertex provides an efficient approximation of sentence ranking scores with regard to algorithms such as PageRank (Brin & Page, 1998), LexRank (Radev & Erkan, 2004), and TextRank (Mihalcea & Tarau, 2004).

In this study, summarization sentences were also ranked by two new functions *gtf* and *gft<sub>idf*</sub>, which are further simplified approximations of the energy function *E*. Given sentences  $s_i$  and  $s_j$  in **S** and a word *w* in a set *W*, let  $w_s$  be the frequency of word *w* in sentence *s*. *idf<sub>w</sub>* is the inverse document frequency of word *w* in sentences. Then, *gtf* and *gftidf* are defined as follows for each sentence *s*i with respect to *N* sentences. *gftidf* scores are *idf* weighted *gtf* scores.

$$
gtf(s_i) = \sum_{w \in W, j=1}^{N} w_{s_i} w_{s_j}
$$

$$
gtf_{idf}(s_i) = \sum_{w \in W, j=1}^{N} w_{s_i} w_{s_j} idf_w^2
$$

Computing *gtf* scores is faster than computing *E*, but bear in mind they are approximations to *TextRank* and *LexRank* ranking scores.

#### *CiteSpace*

The ACA and DCA studies described in this article were conducted using the *CiteSpace* system (Chen, 2004; Chen, 2006). *CiteSpace* is a freely available Java application for visualizing and analyzing emerging trends and changes in scientific literature. *CiteSpace* supports a unique type of co-citation network analysis – *progressive network analysis* – based on a time slicing strategy and then synthesizing a series of individual network snapshots defined on consecutive time slices. Progressive network analysis particularly focuses on nodes that play critical roles in the evolution of a network over time. Such critical nodes are candidates of intellectual turning points. Further technical details and case studies are available in (Chen, 2006). *CiteSpace* has been actively maintained and updated with new visual analytic features as well as theoretical developments (Chen et al., 2009a; Chen et al., 2008; Chen, Zhang, & Vogeley, 2009b). Metrics such as burstness, centrality, modularity, and silhouette metrics described above are implemented and incorporated in various visualizations in *CiteSpace*. For example, purple rims of nodes indicate the importance of nodes in terms of betweenness centrality  $(20.1)$ . Three types of link similarity measures are currently supported: cosine, Dice, and Jaccard similarity coefficients.

In *CiteSpace* visualizations, clusters are labeled by candidate terms selected by ranking algorithms such as tf\*idf, log-likelihood ratio tests, or mutual information. Cluster labels are placed at the weight centers of clusters in a cluster view or at the end of a timeline in a timeline view. The cluster view displays a network in a node-and-link diagram. The timeline view displays a network by arranging its clusters along horizontal timelines. The design of the timeline view is inspired by the *DIVA* system (Morris, DeYong, Wu, Salman, & Yemenu, 2002). While in *DIVA* the analyst needs to work out appropriate labels manually, in *CiteSpace* the selection of labels is supported by nine ranked lists of candidate labels.

In addition to sense-making cues such as clusters, labels, and summarizations, analysts may interact with various visualizations of co-citation clusters and their members. Interactive functions in *CiteSpace* correspond to three levels of units of analysis. At the network level, functions operate on networks, including global visualizations of networks: a node-and-link cluster view and a timeline view. At the cluster level, functions operate on individual clusters such as showing all the citers to a cluster or hiding a cluster. At the basic entity level, functions are restricted to individual entities, for example, showing the citation history of a cited reference.

Figure 3 shows a screenshot of the timeline visualization, in which clusters are displayed horizontally alone timelines. In timeline visualizations, the legend above the display area marks every 5 years. The label of each cluster is shown at the end of the cluster's timeline. Cited references or authors are depicted as circles filled with citation rings. The color of each ring corresponds to the time slice in which citations were made. The thickness of a ring is proportional to the amount of citations received in that time slice. Thus, a large-sized circle denotes a highly cited unit, i.e. reference or author. In timeline visualizations of cited authors, a cited author is positioned based on the earliest year in which he/she was cited in the dataset. A possible extension of this design would differentiate citations to the same author in different years.



**Figure 3. The interactive visualization interface of** *CiteSpace* **showing a timeline visualization of clusters and their labels.** 

Two additional colors, red and purple, are used to highlight special attributes of a node. A red ring indicates that a citation burst is detected in the corresponding time slice. A purple ring is added to a node if its betweenness centrality is greater than 0.1; the thickness of the ring is proportional to its centrality value.

A line connecting two items in the visualization represents a co-citation link. The thickness of a line is proportional to the strength of co-citation. The color of a line represents the time slice in which the cocitation was made for the first time. A useful byproduct of spectral clustering is that tightly coupled clusters tend to be placed next to each other and visually form a supercluster.

# **Results**

The results of the single-slice comparative ACA (2001-2005) are described first, followed by the findings of progressive ACA and DCA (1996-2008). The comparative ACA was limited to the 5-year period of 2001-2005 in order to synchronize with the time period of the study of Zhao and Strotmann (2008a). The full 13-year range of 1996-2008 was used in the other two progressive studies. Within each study, we summarize the prominent co-citation clusters in terms of their leading members, automatically generated labels based on information extracted from citing articles, and sentence summarization based on sentences in citing articles' abstracts.

# *A Comparative ACA (2001-2005)*

The comparative ACA was conducted with reference to the ACA study of Zhao and Strotmann (2008a). Recall that Zhao and Strotmann identified 11 specialties based on 120 most cited authors in 2001-2005 and manually labeled these specialties by examining each specialty's members. They labeled one of factors as 'undefined.' We chose the top 120 most cited authors in the same time period using a single 5 year time slice in *CiteSpace*. Twelve author co-citation clusters were identified with a modularity of 0.5691, suggesting that inter-cluster connections are considerable but not overwhelming. The mean silhouette value of 0.7219 indicates a satisfactory partition of the network. The labels of these clusters were chosen from titles of their citers by *tf\*idf* (See Figure 4). In contrast, Zhao and Strotmann (2008a) derived their labels from cited authors.



**Figure 4. A 120-author ACA network containing 11 clusters, generated with a single 5-year time**  slice (2001-2005). Clusters are labeled by citers' title terms using t<sup>\*</sup>idf weighting. An undefined **cluster (#11) is omitted.** 

Determining the number of specialties is a key issue in a co-citation analysis. In factor analysis, it is a common practice to identify specialties in terms eigenvectors with eigenvalues of 1 or greater. Zhao and Strotmann (2008a) also took into account other information such as the Scree plot, the total variance explained, communalities and correlation residuals. We tracked the number of clusters as the size of the ACA network increases (See Table 2). In general, the number of ACA clusters grows as the size of the ACA network increases. As shown in Figure 5, networks of 300~500 cited authors may be a good compromise with high values in both modularity and silhouette.

TWORK 2. THE SIZE OF FLOTT HELIVOIRS GIRL HIGHLIGHT OF FLOTT CHISTORS. FILL GSC & SHIGHTS voal allie siloe.								
<b>Cited</b> #	% of Total	$#$ Links	# ACA Clusters	<b>Modularity Q</b>	<b>Mean Silhouette</b>			
<b>Authors</b>	<b>Authors</b>							
	(24, 648)							
60	0.24	234	4	0.4430	0.8202			
110	0.45	469		0.5030	0.8293			
120	0.49	514	12	0.5691	0.7219			
200	0.81	915	20	0.6162	0.7974			
300	1.22	1336	36	0.6864	0.6418			
400	1.62	1712	46	0.7527	0.6763			
500	2.03	2245	58	0.7718	0.6679			
1000	4.06	5737	117	0.8725	0.5408			

Table 2. The size of ACA networks and the number of ACA clusters. All use a single 5-year time slice.



#### **Figure 5. The change of modularity and silhouette values as the network size increases.**

We compared 12 co-citation clusters  $(C_i)$  and 11 factors  $(F_i)$  in Zhao and Strotmann's ACA in terms of their overlapping members. Since each author can only appear in one cluster but may appear in multiple factors, one matching factor was selected only if the author has the greatest factor loading in absolute values; if no such factor was found, the author had no match. The overall overlapping rate is 82%, computed as follows:

$$
\frac{\left| \left( \bigcup_{i=1}^{12} C_i \right) \cap \left( \bigcup_{j=1}^{11} F_j \right) \right|}{\left| \bigcup_{i=1}^{12} C_i \right|} = \frac{98}{120} = 0.82
$$

Each cluster was projected as a distribution of its members over the 11 factors and the no-match category. Cluster *C*<sub>i</sub>'s projection on factor  $F_j$  is computed as:  $\frac{|C \cap F_j|}{|C_i|}$ . As shown in Table 3, cluster *C*<sub>3</sub>'s projection on  $F_{\text{webometrics}}$  is  $\frac{|C_3 \cap F_{\text{webometrics}}|}{|C_3|} = \frac{19}{29} = 0.6552$ .

Figure 6 depicts the overall matching patterns between clusters (diamonds) and factors (circles) in a similarity graph. The thickness (and darkness) of a line indicates the strength of the match. Figure 6 shows three types of patterns.

Type 1a-1c: a cluster primarily corresponds to a single factor, denoted as  $C_i \Leftrightarrow F_i$ .

- $(1a)$   $C_0 \Leftrightarrow F_{\text{knowledge management}}$
- $(1b) C_3 \Leftrightarrow F_{\text{webometrics}}$
- $(1c) C_7 \Leftrightarrow F_{\text{IR systems}}$

Type 2a-2b: two or more clusters are subsets of the same factor, i.e. for *K* clusters,  $\bigcup_{k=1}^{K} C_{i_k} \subseteq F_j$ .

(2a)  $C_1 \cup C_2 \cup C_4 \subseteq F_{scientometrics}$ 

(2b)  $C_4 \cup C_8 \subseteq F$  mapping of science

Type 3a: one cluster is split into *L* factors, i.e.  $\bigcup_{l=1}^{L} F_{j_l} \subseteq C_i$ .

(3a)  $F_{information}$  behavior  $\cup F_{users}$  judgements of relevance  $\cup F_{children}$  information behavior  $\subseteq C_{10}$ 







**Figure 6. An associative network of clusters (diamonds) and factors (circles) with 10% or more overlaps (thickness of line). Cluster labels are shown in two parts: terms chosen by tf\*idf and by log-likelihood ratio.** 

Factor labels given by Zhao and Strotmann tend to be conceptually higher-level terms than automatically generated cluster labels. For example, *patent analysis* is a broader term of *patent citation*; and *IR systems*  is a broader term of *document retrieval*. Structurally, spectral clusters tend to be more specific groupings than factors. For instance, as shown in 2b, the *mapping of science* factor contains clusters such as *C4: network diagram* (by tf\*idf): *co-citation analysis* (by LLR), and *C8: document space/Kohonen network*. In summary, 1) spectral clustering and factor analysis identified about the same number of specialties, but they appeared to reveal different aspects of co-citation structures and 2) cluster labels chosen from citers of a cluster tend to be more specific terms than those chosen by human experts. These findings suggest that the multiple perspective method has the potential to provide additional insights in complementary to existing methods and provide an intermediate level of support for interpreting the nature of specialties.

# *A Progressive ACA (1996-2008)*

This progressive ACA was a 13-year multiple-slice analysis of all the 5,963 records in types of article and review. A progressive co-citation analysis takes multiple co-citation networks from consecutive time intervals as input and produces a merged network to represent the evolution of the underlying domain (Chen, 2004). The inclusion of review-type records was to cover ARIST publications, which are classified as reviews. By including top-150 most cited authors from every year between 1996 and 2008, we obtained a merged network of 633 cited authors with 7,162 author co-citation links and 40 co-citation clusters. This 633-author network has a lower modularity (0.2278) than the smaller 120-author network in the comparative ACA  $(0.5691)$ . Furthermore, the mean silhouette value  $(0.6929)$  of the larger network is also lower than that of the 120-author network (0.7219). The larger network has a much higher intercluster connectivity.

Figure 7 shows a timeline visualization of the 40 ACA clusters with automatically generated cluster labels. The display shows labels of highly cited authors in major clusters only. These clusters appear to be more interpretable than clusters in the comparative ACA. Visually, one may identify a few superclusters at the granularity of Zhao and Strotmann's factors. For example, clusters  $C_2$ ,  $C_4$ ,  $C_7$ , and  $C_8$  form a supercluster that corresponds to the *scientometrics* factor.



**Figure 7. 40 ACA clusters (1996-2008) (***CiteSpace* **parameters: Nodes=633, Edges=7,162, top N=150, time slice length=1, modularity=0.2278, mean silhouette=0.6929, clusters=40).** 

Table 4 shows automatically chosen cluster labels of the 6 largest ACA clusters along with their size and silhouette value. Top-ranked title terms by LLR were selected as cluster labels. The largest cluster *interactive information retrieval* (#31) has 199 members. Its negative silhouette value of -0.090 suggests a heterogeneous citer set. The second largest cluster (#17), with 95 members, is labeled as *information retrieval*. Other candidate labels for the cluster include *probabilistic model* and *query expansion*, confirming that this cluster deals with classic information retrieval issues. The third largest cluster (#7) is *bibliometric analysis*.

#	$\mathbb{N}$	Silhouette Title terms by tf*idf	Title Terms by LLR (p=0.0001)
	31 199	$-0.090$ (80.30) interactive information retrieval $(62.46)$ information retrieval $(55.45)$ information science	$(79.31)$ interactive information retrieval $(53.64)$ user information problem $(53.64)$ various aspect
17 <sup>1</sup>	95	$0.143$ (71.02) information retrieval $(41.44)$ probabilistic model $(37.94)$ query expansion	$(68.19)$ information retrieval $(49.81)$ probabilistic model $(38.49)$ magazine article
$\overline{7}$	37	$0.272$ (22.87) bibliometric analysis $(17.07)$ social science $\parallel$ (13.82) publication productivity	$(31.51)$ bibliometric analysis $(22.79)$ social science $(22.67)$ career path
$\overline{2}$	33	$0.343$ (20.97) scientific productivity $(14.98)$ statistical analysis $(14.76)$ analyzing scientific productivity	$(24.24)$ theoretical population genetic $(24.16)$ statistical analysis $(23.54)$ new method
11	32	$0.682$ (20.72) webometric analysis $(18.44)$ informetric purpose $(18.44)$ data collection method	$(32.65)$ webometric analysis $(28.16)$ data collection method $(28.16)$ informetric purpose
8	30 <sup>1</sup>	$0.330$ (19.68) information retrieval $(18.42)$ citation analysis $(16.12)$ information retrieval area	$(34.42)$ journal co-citation analysis $(34.42)$ intellectual space $(34.42)$ information retrieval area

**Table 4. The 6 largest ACA clusters of a 633-author network (1996-2008).** 

Table 5 lists top-10 most cited authors of the six largest ACA clusters, including Spink\_A and Saracevic\_T in *interactive information retrieval* (#31), Salton\_G, Robertson\_SE, and van Rijsbergen\_CJ in *information retrieval* (#17), Garfield\_E, Moed\_HF, and Merton\_RK in *bibliometric analysis* (#7), Egghe\_L, Price\_DJD, and Lotka\_AJ in *statistical analysis* (#2). The *webometric analysis* cluster (#11) includes Cronin\_B, Rousseau\_R, and Lawrence\_S. The *journal co-citation analysis* (#8) includes Small H, Leydesdorff L, and White HD.

Note that one may reach different insights into the nature of a co-citation cluster if different sources of information are used. The cited members of a cluster define its intellectual base, whereas citers to the cluster form a research front. The major advantage of our approach is that it enables analysts to consider multiple aspects of the citation relationship from multiple perspectives.

Cluster $\#$ and Label by LLR $\ $	<b>Citations</b>	<b>Burst</b> Centrality	Sigma	Author	<b>Major Citers (some subtitles are</b> omitted due to the limited space)
31. interactive information retrieval	329	0.03		<b>SPINK A</b>	(19) Sutcliffe AG (2000) empirical
		0.02		<b>SARACEVIC T</b>	studies of end-user information
	299	0.04		<b>INGWERSEN P</b>	searching
	299	0.02		<b>BELKIN NJ</b>	

**Table 5. The six largest ACA clusters with most cited members and major citers of each cluster.** 



# *The Progressive DCA (1996-2008)*

In the progressive DCA, co-citation networks were first constructed with the top-100 most cited documents in each of the 13 one-year time slices between 1996 and 2008. Then, these networks were merged into a network of 655 co-cited references. The merged network was subsequently decomposed into 50 clusters. Table 6 summarizes these clusters. We first provide an overview of these clusters and discuss the five largest clusters in detail.

# **Overview**

The 50 clusters vary considerably in size. The largest cluster #18 contains 150 members, which is 22.90% of the entire set of 655 references. The five largest clusters altogether reach 51.60%. In contrast, there are six clusters contain only two members.

The network's overall mean silhouette value is 0.7372, which is the highest among the three co-citation networks we analyzed in this article. In general, the silhouette value of a cluster is negatively correlated with its size (-0.654). For example, the largest cluster, #18, has the lowest silhouette value of -0.024, indicating its diverse and heterogeneous structure. In contrast, the second largest cluster, #43, has a more homogenous structure with a reasonably high silhouette value of 0.522. The fifth largest cluster, #2, has a very high silhouette value of 0.834. The following discussion will focus on the five largest clusters and their interrelationships.



**Table 6. The five largest clusters sorted by size.** 



# **Five Major Clusters: Cited References as the Intellectual Base**

The five largest document co-citation clusters are *interactive information retrieval* (#18), *academic web* (#43), *information retrieval* (#46), *citation behavior* (#44), and *h index* (#2). We analyzed two aspects of each specialty: 1) prominent members of a cluster as the intellectual basis and 2) themes identified in the citers of the cluster as research fronts.

Table 7 summarizes top-cited cluster members and their structural, temporal, and saliency metrics such as citation count ( $\phi$ ), betweenness centrality ( $\sigma$ ), citation burstness ( $\tau$ ), and sigma – a novelty indicator ( $\Sigma$ ) (Chen et al., 2009a). The most cited references in the *interactive information retrieval* cluster are Kuhlthau 1991 on information seeking and Bates 1989 on browsing and berrypicking. The first four references are related to information needs and user-centric approaches. However, we did not expect to see the  $5<sup>th</sup>$  reference, the ACA study by White 1998, because in our mind it firmly belongs to a citation analysis specialty. On the other hand, the low silhouette value of the *interactive information retrieval* cluster suggests that a diverse and complex range of research fronts may have drawn upon the knowledge of this cluster. The following discussion on the second aspect – themes identified among citers – may give us additional insights into the nature of this cluster.

The stars in the *academic web* cluster (#43) are Lawrence 1999 and Kleinber 1999. Both papers were published outside the domain defined by the 12 source journals; instead, they appeared in *Nature* and *JACM*. This is an example of how one discipline (information science) was influenced by another (computer science). It would explain why the cluster was dominated by the work of '*outsiders*.' In contrast, the *information retrieval* cluster (#13) is, as one would expect, dominated by the work of '*insiders*,' namely, books by Salton and by van Rijsbergen. Similarly, the *citation behavior* cluster (#35) was dominated by '*insiders*,' for example, Garfield's book on citation indexing, Small's 1973 paper on co-citation, Price's 1965 paper on networks of scientific papers, and White and Griffith's 1981 paper introducing author co-citation. A key that may distinguish *insiders* from *outsiders* is that insiders may cite the original cluster, but outsiders will probably not.

The core of the fifth largest cluster, the *h index* cluster (#2), is Hirsch 2005, which originally introduced the concept of h-index. The strongest citation burst of 15.75 was detected in the citation history of Hirsch 2005. As our analysis will demonstrate, the *h index* cluster is one of the most active areas of research in recent years.

The average age of core papers in a cluster is an estimation of the time the cluster was formed. According to the average age of top-5 core papers, the 37-year old *citation* cluster is the oldest – formed around 1973, its average year of publication, whereas the *h-index* cluster is the youngest – 5 years old, formed in 2005. In between, the *information retrieval* cluster (#13) is 31 (formed in 1979); the *interactive information retrieval* cluster (#18) is 18 formed in 1992; and the *academic web* cluster (#43) is 11 (formed in 1999).

<b>Cluster</b>	$\boldsymbol{\omega}$				<b>Cited References</b>
#					
18	118	$0.00\,$	0.04	0.00	Kuhlthau, C. C. (1991) Inside the search process: Information seeking from
					the user's perspective. Journal of the American Society for Information
					Science, 42 (5), 361-371.
	95	4.79	0.04		0.19   BATES MJ (1989) The design of browsing and berrypicking techniques for
					the online search interface. ONLINE REV, 13, 407.
	85	8.52	0.03	0.11	Dervin, B. and Nilan, M. (1986). Information needs and uses. Annual
					Review of Information Science and Technology (ARIST), v. 21, pp 3-33.

Table 7. Most frequently cited references in the five largest document co-citation clusters ranked by citation counts  $\varphi$ .  $\overline{B}$  **I**  $\overline{C}$  **C**<sup>*i*</sup> **ID** *c* 



# **Five Major Clusters: Citing Articles as Research Fronts**

Research fronts of a document co-citation cluster were characterized by terms extracted from the citers of the cluster. Nine methods of ranking extracted terms were implemented in *CiteSpace* by choosing terms from three sources – titles, abstracts, and index terms of the citers of each cluster – and three ranking

algorithms, namely, tf\*idf weighting (Salton et al., 1975), log-likelihood ratio tests (LLR) (Dunning, 1993; Witten & Frank, 1999), and mutual information (MI)(Witten & Frank, 1999). Top-ranked terms became candidate cluster labels.

The reliability of these term ranking methods was measured by a consensus score  $r = 0.1*(n + 1)$ , where n is the number of other methods that also top rank the same term. It turned out that the best three ranking methods were: 1) title terms ranked by LLR, 2) index terms ranked by LLR, and 3) title terms ranked by tf\*idf (See Figure 8). tf\*idf and LLR produced identical labels for 36 clusters out of 50 (72%). Table 8 summarizes candidate labels chosen by different methods.



**Figure 8. The best consensus-conforming ranking methods: 1) title terms by LLR, 2) index terms by LLR, and 3) title terms by tf\*idf.** 

We discussed earlier that the largest cluster (#18) has 150 members and it has the lowest silhouette value (See Table 6). It turned out that the cluster was cited by 185 citing articles in the dataset. A total of 869 terms were extracted from the titles of these citing articles. In order to verify the heterogeneity of this set of citers, the term similarity network was decomposed using singular value decomposition (SVD). As a result, the term space was indeed multi-dimensional in nature because the largest connected component of the term similarity network contains only 353 terms, which is 40.62% of the 869 terms. In contrast, the *h index* cluster (#2) was much more homogeneous; the cluster was the citation footprint of 39 citing articles. Table 8 includes the silhouette value of each cluster.

**Table 8. The candidate cluster label terms selected by 6 of the 9 methods. The numbers under term sources are the consensus scores of the corresponding methods. The 3 mutual information methods are not shown due to lower scores (6.8, 6.8, 6.1 for index terms, titles, and abstracts). The most popular terms across the six methods are chosen to be the cluster labels.** 





The second largest cluster was labeled as *academic web* by LLR, but the top-ranked index term was *webometrics*, which was also the name of a specialty identified by Zhao and Strotmann. The index term

*webometrics* is broader and more generic than the term *academic web*. This observation suggests that a manual labeling process is probably very similar to the indexing process after all.

The identification of the *h-index* cluster is unique because there was no such cluster in the 1996-2008 ACA. This is a good example why one should consider both ACA and DCA so that distinct DCA clusters such as the *h-index* one can be detected.

The time span  $\tau$  between a research front and its intellectual base can be estimated as the difference between their average years of publications:

$$
\tau(C_i) = \frac{\sum_{deciters(C_i)}year(d)}{|citers(C_i)|} - \frac{\sum_{ceC_i}year(c)}{|C_i|} + 1
$$

For example, *citation behavior* (#35) has the longest time span,  $\tau$  (*C*<sub>35</sub>) = 2000-1973=28 years. IR has the second longest time span  $\tau$  (*C*<sub>13</sub>) = 2000-1979=22. The time span for *interactive IR* is  $\tau$  (*C*<sub>18</sub>) = 2000-1992=9 years; for *academic web* (#43),  $\tau$  ( $C_{43}$ ) = 2003-1999=5 years; and for *h-index* (#2),  $\tau$  ( $C_{2}$ ) = 2007-2005=3 years.

Table 9 lists the most representative citing articles in each cluster. For example, Thelwall has a prominent role in the research front of the *academic web* cluster (#43). He authored 3 of the top 5 citing articles of the cluster, including Thelwall\_2003 which cited 14 references of the cluster.





#### **Automatic DCA Cluster Summarization**

Summarization sentences were ranked by the earlier described energy function *E* (Fernandez et al., 2007). Table 10 highlights two top-ranked summarization sentences for the same five DCA clusters we discussed earlier. Analysts can enhance their understanding of a cluster based on the additional contextual information provided by summarization sentences. The TreeTagger (Schmid, 1999) trained on the Penn Tree Bank, was used here for sentence segmentation.



The *h* index cluster (#2) is the most active one in terms of citation burstness. The top 10 sentences from this cluster represented themes such as studies of the h-index and its variations (the  $2^{\hat{n}d}$ -4<sup>th</sup>,  $7^{\hat{n}}$ -8<sup>th</sup> and 10<sup>th</sup> sentences), the studies of web-based citation patterns (the  $1<sup>st</sup>$  sentence), and new resources of scientometrics, i.e. Scopus and Google Scholar (the  $5<sup>th</sup>$ ,  $6<sup>th</sup>$ , and  $9<sup>th</sup>$  sentences).

Considering that the system only has abstracts rather than full-texts to work with, the results are very encouraging because selected sentences will largely increase the ability of an analyst, or even a layman, to comprehend the meaning and significance of clusters in citation analysis much more easily.

### **Visual Exploration**

The DCA network shown in Figure 9 was generated by *CiteSpace*. The 655 references and 6,099 cocitation links were divided into 50 clusters with a modularity of 0.6205, which represents a considerable amount of inter-cluster links. Major clusters are labeled in the visualization in red color with the font size proportional to the size of clusters. The colors of co-citation links reveal that the earliest inter-cluster connection is between *interactive IR* and *IR*, followed by connections between *interactive IR* and *citation behavior*, then by the more recent connections between *academic web, citation behavior,* and *IR*, and finally, the most recent connections between *h index*, *citation behavior*, *academic web*.



**Figure 9. An overview of the co-citation networks. Cited references with highest sigma values are labeled.** 

Figure 10 shows a timeline visualization of the 50 clusters and their interrelationships. Each cluster is plotted horizontally. Each timeline runs from left to right with its label displayed to the right. The design of the timeline visualization is inspired by the work of Morris, Yen, Wu, and Asnake (2003) and further enhanced by automatic clustering labeling with multiple algorithms. Analysts can visually identify a variety of characteristics of a cluster, such as the length of its history, its citation classics, citation bursts, and how it is connected to other clusters. For example, in the citation behavior cluster, Garfield's 1979 book on citation index stands out with the highest betweenness centrality of 0.09. Many large citation circles would identify a high-impact specialty, whereas many red rings of citation bursts would highlight emerging specialties.



**Figure 10. A timeline visualization of the 50 DCA clusters (655 nodes, 6,099 links, modularity=0.6205, mean Silhouette=0.7372). Cluster labels are automatically generated from title terms of citing articles of specific clusters.** 

It is clear in the timeline visualization that the *h-index* cluster is new and growing fast. The new cluster includes not only a highly cited article, but also with a strong surge of citations. Hirsch\_2005, the original article that introduces the h-index, has the strongest citation burst (See Figure 11).



**Figure 11. The burst of citations to Hirsch\_2005.** 

If we start from the top of the timeline visualization and move down line by line, we can see many representative references in these clusters. For example, *Film Archive* (#11) is a relatively new cluster, containing Jansen 2000 on searching for multimedia on the web as a major reference. Similarly, the most cited reference in *information retrieval* (#13) is Salton's book. Further down the timeline list is the *citation behavior* cluster (#35), which features Garfield\_1979 prominently. Many co-citation links join *citation behavior* and *academic web*. Some long-range co-citation links connect the *h-index* cluster and other clusters such as the *academic web* cluster and the *power law* cluster.

# **Discussion**

We have introduced a multiple-perspective co-citation procedure that consistently supports both ACA and DCA. We have demonstrated how an integration of spectral clustering, automatic cluster labeling, and automatic multiple-abstract summarization can provide informative and insightful cues for analysts to make sense and interpret the nature of co-citation clusters and their interrelationships.

# *Major Findings*

First, the 5-year comparative ACA shows that, at the highest level, both ACA studies identified compatible specialties such as *document retrieval*, *information behavior*, and *webometrics*. On the other hand, spectral clustering identified some distinct clusters that belong to the same factor-induced specialties. For example, the *network diagram* (#4) and *document space* (#8) clusters correspond to the *mapping of science* specialty in Zhao and Strotmann. The study also reveals that human experts tend to choose broader-term labels, equivalent to the level of index terms, whereas algorithmically chosen terms from titles or abstracts tend to be more specific and limited to terms actually used by the authors.

The 13-year progressive ACA (1996-2008) of 633 cited authors in 40 clusters resulted in a clearer global structure than the 5-year single-slice ACA. We have shown that cluster membership and citer-focused labeling provide complementary information to form a comprehensive image of the field.

Finally, the progressive DCA of 655 cited references detects a distinct and fast growing cluster – the *h index* cluster, which is absent from the progressive ACA. The *h index* cluster emerged in 2005. While we do not expect to find it in the comparative ACA of 2001-2005, it is interesting that the 1996-2008 ACA did not detect it. Therefore, we recommend that both ACA and DCA should be conducted whenever possible to maximize the coverage of the intellectual landscape of a subject domain.

# *Limitations and Future Work*

The information science field in our study was defined in terms of the 12 library and information science journals. Although the selection was adopted by several previous studies, the validity of the 12 journals needs to be established in a broader context, for example, by using journal co-citation analysis and subject category analysis. Newer journals such as *Information Retrieval* and *Journal of Informetrics* should be added in future studies and some of the journals may need to be replaced. Furthermore, we exclusively relied on the Web of Science as the single data source. Other sources such as Scopus and Google Scholar would provide additional and unique insights.

We found the comparison with the study of Zhao and Strotmann very valuable. It offered us an opportunity to compare the analysis conducted by human experts to the interpretation cues provided by our automatic labeling and summarization methods. In a long run, we strongly recommend cross-study comparisons so that one can establish a comparable platform to accommodate findings made by different researchers. In part due to the already lengthy article, we decided not to include a comparative DCA study. We focused on co-citation networks in this article. Alternative studies such as bibliographic coupling of journals, authors, documents, and subject categories are also useful methods. Furthermore, we did not include an investigation of direct citation networks in our study. Some recent work in this area can be found in (Garfield, 2004; Morris & Van der Veer Martens, 2008). We recommend that these alternative studies should be considered and compared thoroughly in the future work.

The quality of cluster labeling in general depends on the variety, breadth, and depth of the set of candidate terms. We have extracted candidate cluster labels from citing articles' titles and abstracts. It is also desirable to compare these labels with candidate terms from cited references in the DCA or cited authors' publications in ACA. However, such data is not readily available due to the fact that the CR field in the ISI data format does not include the title of a cited reference. Furthermore, a cited reference may not even be a source record in the entire collection of the Web of Science. In contrast, human analysts may choose the most appropriate label terms from a much wider range of sources beyond the terms found in the immediate dataset, although this could be a double-edged sword. On the one hand, human analysts are free from the limitations of a specific data source. On the other hand, they may need to deal with a potentially much larger search space, which can be a daunting task, especially for those who do not have an encyclopedic knowledge of the subject domain. Utilizing external information sources such as the Wikipedia and the World-Wide Web is a promising direction to resolve the problems due to the limited term space problem. An interesting approach was reported recently in (Carmel et al., 2009).

Sentence selection algorithms in this study were applied to abstracts. Ideally, we expect an improved performance with full text of scientific papers. This is an avenue for further research. A thorough evaluation of the merits of individual labeling approaches is an area in which further research is needed. It is rare to see a citation analysis being evaluated with built-in gold standards in a dataset. Efforts should be made to build a dataset and judgments of domain experts on specialties and the nature of various cluster groupings. Researchers would greatly benefit from such data repositories and benchmark data in order to better validate new techniques and individual interpretations and conclusions.

Spectral clustering for the purpose of network decomposition is exclusive in nature although in reality it is often sensible to allow overlapping clusters due to multiple roles individual entities may play. Spectral clustering of co-citation networks tends to generate distinct clusters with high-precision, whereas human experts tend to aggregate entities into broadly defined clusters. Future work should focus on how to compromise exclusive clusters and how to further aggregate distinct but tightly coupled clusters into super-clusters at a comparable level of abstraction to human experts.

Although some cluster labels make good sense, some labels are still puzzling and some members of clusters may not be as intuitive as others. Some of the labels appear to be strongly biased by particular citing articles, especially when the size of a cluster is relatively small. Algorithmically generated cluster labels are limited to deal with clusters that have multiple aspects formed by a diverse range of citing papers. Clusters with low mean silhouette values tend to be subject to such limitations more than high silhouette clusters. On a positive note, metrics such as modularity and silhouette provide useful indicators of uncertainty that analysts should take into account when interpreting the nature of clusters. We have been looking for a labeling algorithm that is consistently better than others. Since we do not have datasets with gold standards, this cannot be validated systematically except by making comparisons across the 9 sets of candidate labels.

A few more fundamental questions need to be thoroughly addressed. If labels selected from citers differ from those from citees, how do we reconcile the difference? How do we make sense of the citer-citee duality? One of the fundamental assumptions for co-citation analysis is that co-citation clusters do represent something substantial as real as part of the reality although they might be otherwise invisible. Given that some co-citation clusters appear to be biased by the citation behavior of particular publications, it may become necessary to re-examine the assumption, especially whether co-citation clusters represent something that is truly integral to the scientific community as a whole.

# **Conclusions**

In conclusion, the new co-citation analysis procedure has the following advantages over the traditional one:

- 1. It can be consistently used for both DCA and ACA.
- 2. It uses more flexible and efficient spectral clustering to identify co-citation clusters.

- 3. It characterizes clusters with candidate labels selected by multiple ranking algorithms from the citers of these clusters and reveals the nature of a cluster in terms of how it has been cited.
- 4. It provides metrics such as modularity and silhouette as quality indicators of clustering to aid interpretation tasks.
- 5. It provides integrated and interactive visualizations for exploratory analysis.

These features enhance the interpretability and accountability of co-citation analysis. Modularity and silhouette metrics provide useful quality indicators of clustering and network decomposition. This is a valuable addition to the traditional methods such as estimating the strength of a membership based on factor loading. Multiple channels of candidate labels selected from multiple sources have confirmed that clustering labeling is indeed a complex phenomenon that requires multiple perspectives. Our new procedure provides a range of options for analysts to choose cluster labels. In return, the labeling tasks have shed new insights into the behavior of classic information retrieval models and term weighting techniques. Sentence selection was based on weighting functions. In the future we aim to explore the impact of adding linguistic features to these functions such as the argumentative roles of sentences, namely introduction, method, results, conclusion, and novelty, in order to enhance the sentence selection functions. The integration of these techniques in a unifying framework will enable analysts, researchers, and students to investigate and understand the dynamic interrelationship between an intellectual base and an inspired research front. Multiple perspective approaches also provide a cross-validation basis for evaluation and comparison.

The ACA and DCA studies have updated the intellectual landscape formed by a series of previous studies, notably the ACA by White and McCain (1998) and Zhao and Strotmann (2008a, 2008b). The earlier landscape characterized by two predominant camps of information retrieval and citation analysis has evolved into more distinct specialties. The deep impact of the World-Wide Web is evident, responsible for the growth in areas such as webometrics and web search (i.e. the interactive information retrieval cluster in both ACA and DCA). The emergence of the h index in the DCA landscape also indicates the evolution of the information science field. The comparative ACA is a valuable exercise that has characterized the commonality and uniqueness of distinct analytical methods of co-citation networks. In conclusion, the integrative procedure and the analysis of the information science field contribute to co-

citation analysis by improved interpretability and accountability. One can also repeatedly and periodically conduct ACA and DCA with simplified and reduced operational costs. We expect that the integrated implementation provides a rich and evolving platform for research, evaluation, and education for the information science community.

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# **Notes**

*CiteSpace* is freely available at http://cluster.cis.drexel.edu/~cchen/citespace/. Supplementary materials of the study are available at http://cluster.cis.drexel.edu/~cchen/papers/2009/infosci/ .

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