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# Quick and Direct Method for Determining $J_C$ in Bulk Superconductors from Magnetic Field Diffusion Measurements

Bruno Douine, Frédéric Sirois, *Senior member IEEE*, Jean Leveque, Kevin Berger, Charles-Henri Bonnard, The-Cuong Hoang and Smaïl Mezani

Abstract— The knowing the critical current density  $J_C$  is important to calculate AC losses in superconducting applications. Usually  $J_C$  can be obtained from magnetization measurements or electric measurements based on global quantities as the magnetic flux or the voltage. In this paper a quick and direct magnetic method for determining  $J_C$  is proposed. It is based on direct measurements of local magnetic field in the gap between two bulk HTS pellets. Field penetration measurements were carried out on HTS pellets at 77 K by applying increasing axial magnetic fields with a quasi constant sweep rate. This determination of  $J_C$  is theoretically based on Bean model.  $J_C$  is deduced from the complete penetration magnetic field  $B_P$ .  $B_P$  is deduced from the delay  $T_P$  between the applied magnetic field  $B_a(t)$  and the magnetic field at the center between the two pellets  $B_{\theta}(t)$ . Numerical calculations allow deducing  $J_C$  more precisely from theoretical calculations and measurements. The numerical calculations are made with the power law  $E=E_C(J/J_C)^n$ . For the determination of  $J_C$  the influence of the gap due to Hall probe sensor and the applied magnetic field rise rate are taken into account. The influence of thermal is also studied.

Index Terms— Superconductor, magnetic field diffusion, critical current density

#### I. INTRODUCTION

The value of  $J_C$  can be derived from different experimental techniques as transport current, magnetization cycle [1], [2] or ac susceptibility [3]. The electrical transport method is not valid in the case of pellet. Magnetic methods are called indirect method because relation between measurement and  $J_C$  is not direct. Magnetization methods need complex and expensive devices as Physical Properties Measurement System or other set up [1], [2]. For AC susceptibility method the relation between measure and  $J_C$  is complicated because it needs calculation of demagnetizing factor, integration and so on [3], [4].

The main contribution of the present work is to propose a quick and direct magnetic  $J_C$  determination method. In this

method HTS sample is submitted to an axial applied magnetic field  $B_a(t)$  (Fig. 1).  $B_a(t)$  is considered as linear function of times even if the shape of  $B_a(t)$  does not matter with Bean model:

$$B_a(t) = V_b t$$

At the center of the pellet the magnetic field begins to increase with delay time  $T_P$  when  $B_a$  reaches the complete magnetic field  $B_P$  (Fig. 2). For short cylinders and with the Bean model [5], an explicit expression of the penetration magnetic field  $B_P$  can be calculated as the axial magnetic field created in the center of solenoid of null internal radius [6]:

$$B_{P} = \frac{\mu_{0} J_{C} \cdot L}{4} \cdot ln \left( \frac{\sqrt{R^{2} + \left(\frac{L}{2}\right)^{2}} + R}{\sqrt{R^{2} + \left(\frac{L}{2}\right)^{2}} - R} \right)$$
 (1)

L is the length of the cylinder and R its radius.

(1) equivalent of  $B_p$  formula given by different authors [2], [7], [8].

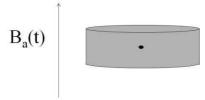


Fig. 1. Sample geometry

The principle of this method is measuring  $B_P$  and deducing  $J_C$ . In this paper, firstly, experimental results are presented and discussed. Secondly, computational method is exposed. Thirdly numerical simulations with COMSOL allow studying the influence of Hall probe depth and rise rate.

#### II. EXPERIMENTAL SETUP AND RESULTS

Some authors already used Hall probes to determine magnetic field distribution in superconducting sample [9]-[13]. In our method the complete penetration magnetic field is detected with an axial Hall probe placed between two HTS pellets (Fig. 3) at the center of pellet. At this point the magnetic field has only axial component so magnetic field

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is well measured with this Hall probe. These two pellets are theoretically considered as one pellet. So in a first time the influence of the Hall probe thickness e is neglected. Discussion about this hypothesis will be done in section IV.

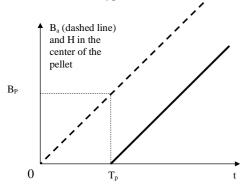


Fig. 2. Linear magnetic applied field and theoretical magnetic field at the center of the pellet versus time

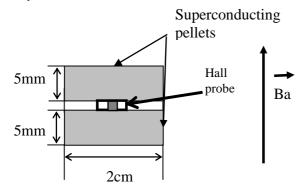


Fig. 3. Hall probe location and HTS pellet dimensions

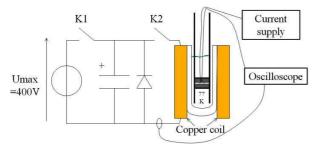


Fig. 4. Experimental set up

Figure 4 shows our experiment with the pulsed field magnetization process [14] that is used to apply magnetic field with a copper coil. A previously charged capacitor is discharged through this copper coil. It allows obtaining quasi constant rise rate V<sub>b</sub> equals to 660T/s. With this process there is no need of superconducting coil in order to obtain high magnetic field of several Tesla. The applied magnetic field  $B_a(t)$  is deduced from copper coil current and the magnetic field at the center of the two pellets  $B_0(t)$  is measured with Hall probe. Figure 5 shows the experimental results. As you can see in surrounded part of Figure 5, the beginning of  $B_0(t)$  has not exactly the same shape as the

beginning of  $B_a(t)$ . As it will be confirmed in section IV, this is due to the necessary space between pellets to place Hall probe. So the determination of the penetration time  $T_P$ is done as follow. The measured magnetic field curve at the pellet center is modified around T<sub>P</sub> to be a copy of applied magnetic field  $B_a(t)$  (dotted line in Fig. 5). All along time the difference between curves is constant and equal to  $T_P$ .  $T_P$  determined then  $B_P$  is deduced from the curves.

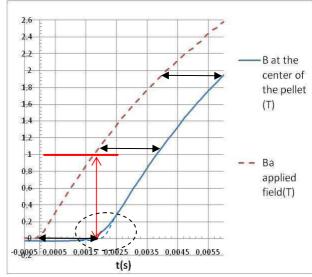


Fig. 5. Applied magnetic field and measured magnetic induction at the center of the pellet

For our two YBCuoO pellets (Fig.3), measured  $B_P$  is 1T (Fig. 5).  $J_C$  deduced from  $B_P$  and (1) is 110A/mm<sup>2</sup>. It seems a realistic value of  $J_C$  at 77K.

Three questions remain. What are the influence of Hall probe depth and the influence of rise rate on this  $J_C$ determination? What about thermal effect? To answer these questions numerical simulation is necessary.

#### III. COMPUTATIONAL METHOD

Pellet magnetization with axial applied magnetic is a 2D axisymetric problem. PDE interface of COMSOL 4.1 is used with or without heat transfer module. The field profiles can be computed by Faraday's law, Ampere's theorem and constitutive laws of superconducting material usually used for numerical simulation [14]-[15]:

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \times \vec{H} = \vec{J}$$
(2)

$$\nabla \times \overrightarrow{H} = \overrightarrow{J} \tag{2}$$

$$E = \rho(J)J \text{ with } \rho(J) = \frac{E_C}{J_C} \left(\frac{|J|}{J_C}\right)^{n-J}$$
(3)

$$B = \mu_0 H \tag{4}$$

To allow computing convergence a small value  $\rho_0$ , equals 1e-3\* $E_C/J_C$ , is added to  $\rho(J)$  [16]. The common parameters used in these simulation are the value of n (=15 as realistic

value for HTS at 77K) and the dimensions of pellet (R=1cm and L=1cm for one pellet study or 2\*0.5cm for two pellets study). In PDE interface the applied magnetic field  $B_a(t)$  is a condition applied at the external boundary. For thermal study convection cooling is used in heat transfer module. Thermal parameters are taken from [14].

## IV. INFLUENCE OF RISE RATE, THERMAL EFFECT AND SENSOR THICKNESS.

To answer to the three questions of section II, three sets of simulation are made.

The value of rise rate  $V_b$  changes the distribution of magnetic field and current density due to the power law (3) instead of Bean model [17]. So the measured  $B_P$  value must depend on rise rate. To study this phenomena (Fig. 6) simulation is made with one pellet with constant rise rate  $V_b$  equals 1, 10 and 100 T/s and with  $J_C$ =1A/m². For this value of  $J_C$ ,  $B_P$  equals 9.1mT.

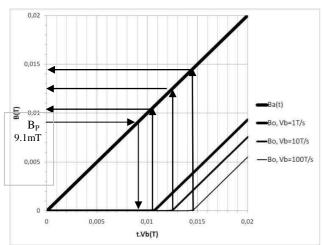


Fig. 6. Applied magnetic field and magnetic induction at the center of the pellet for different rise rates.

To allow comparison between rise rates on one figure, magnetic field in Figure 6 is represented versus  $t^*V_b$ . The measured  $B_P$  increases with  $V_b$ . This is due that J in superconductor is higher than  $J_C$  until almost two times for  $100 \, \mathrm{T/s}$  (Fig. 7). So if J is higher  $T_P$  and  $B_P$  are also higher. To correctly using (1), based on Bean model, small values of rise rate, lower than  $1 \, \mathrm{T/s}$ , are necessary. Future experiments with superconducting coil and low rise rate will be made to confirm this.

To study the influence of Hall probe thickness e (Fig. 8) simulation is made with two pellets with two different depth (e=0.5 and 1mm) typical of Hall probe depth and compare with one pellet without hall probe (e=0mm). Figure 8 shows that measured  $T_P$  and  $B_P$  increase with e. It is due to the shape of the current density distribution near the centre of the pellets [Fig.9]. Without Hall probe (one pellet on Fig.7) the null current density area has circular shape. But due to Hall probe, this null current area becomes two areas with almost circular shape. So with Hall probe current density penetrates quicker than without probe (Fig.8). As expected

the probe depth should be maximally reduce but with numerical simulation  $B_P$  and  $J_C$  values can be corrected.

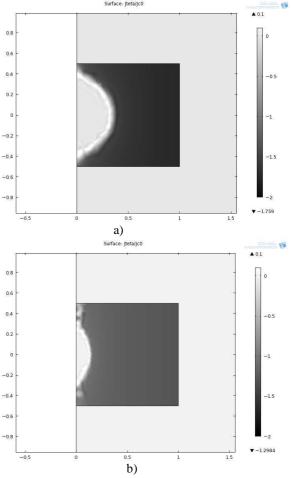


Fig. 7. Current density distribution in superconducting pellet at Vb=100T/s a) and Vb=1T/s b) for  $B_a=B_P$ .

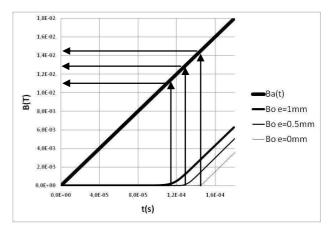


Fig. 8. Applied magnetic field and magnetic field at the center of the pellet for different Hall probe thicknesses.

Thermal effects on  $J_C$  determination are also numerically studied. For this  $J_C(T)$  is taken and heater module is used in COMSOL.

$$J_C(T) = J_C\left(\frac{T_C - T}{T_C - T_0}\right) \tag{4}$$

 $T_0$ =77K is the liquid nitrogen bath constant temperature and  $T_c$ =100K [14].

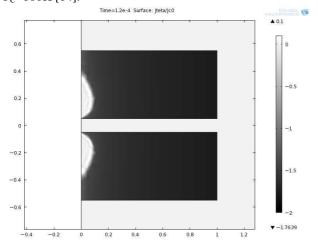


Fig. 9 Current density distribution in superconducting pellet for e=1mm.

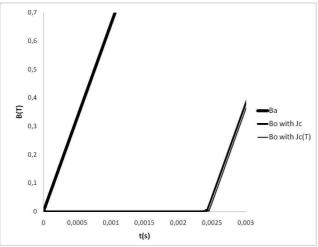


Fig. 10 Thermal effects on magnetic diffusion.

Quicker rise rate is higher thermal effects are. So the value of  $V_b$  taken for simulation is a quick rise rate 660T/s and corresponds to measurement. For this value and for  $J_C$  equals  $100 \text{A/mm}^2$ , thermal effects are negligible on  $B_P$  (Fig. 10) because temperature rising in superconductor is weak about  $1^\circ$  or  $2^\circ$ . As a result the J variation in superconductor due to thermal effects is also weak during the magnetic field penetration phase. In this  $J_C$  determination method thermal effects can be neglected.

Finally, the best  $J_C$  value are numerically determine to have closest numerical and experimental results of  $B_0(t)$ . For n-value fixed at 15, e fixed at 0.5mm, the found best  $J_C$  equals 55A/mm². It is about half of measured one (110A/mm²) mainly because rise rate is very high.

#### V. CONCLUSION.

In this article a quick and direct  $J_C$  determination method is presented. The experimental set up is relatively simple because it needs only one copper coil and one capacitor bank. It is a relatively precise method but it is important

taking into account rise rate and sensor depth. Thermal effects can be neglected. The corrected value of  $J_C$  is lower than measured one mainly because of high experimental rise rate. The influence of n-value has to be studied because it is related to the influence of rise rate. A negative point is this method does not allow to determine  $J_C(B)$  but it is a good method to quickly obtain a first value of  $J_C$  for bulk HTS samples.

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