# Bivariate association analysis in selected samples: Application to a GWAS of two Bone Mineral Density phenotypes in males with high or low BMD 

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# Bivariate association analysis in selected samples: Application to a GWAS of two 

 Bone Mineral Density phenotypes in males with high or low BMDSaint-Pierre Aude ${ }^{1}$, Kaufman Jean-Marc ${ }^{2}$, Ostertag Agnes ${ }^{3}$, Cohen-Solal Martine ${ }^{3}$, Boland Anne ${ }^{4}$, Toye Kaatje ${ }^{2}$, Zelenika Diana ${ }^{4}$, Lathrop Mark ${ }^{4}$, de Vernejoul MarieChristine ${ }^{3}$, Martinez Maria ${ }^{1}$.
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#### Abstract

Our specific aims were to evaluate the power of bivariate analysis and to compare its performance with traditional univariate analysis in samples of unrelated subjects under varying sampling selection designs. Bivariate association analysis was based on the Seemingly Unrelated Regression (SUR) model that allows different genetic models for different traits. We conducted extensive simulations for the case of two correlated quantitative phenotypes, with the Quantitative Trait Locus making equal or unequal contributions to each phenotype. Our simulation results confirmed that the power of bivariate analysis is affected by the size, direction and source of the phenotypic correlations between traits. They also showed that the optimal sampling scheme depends on the size and direction of the induced-genetic correlation. In addition, we demonstrated the efficacy of SUR-based bivariate test by applying it to a real GenomeWide Association Study of Bone Mineral Density values measured at the Lumbar Spine and at the Femoral Neck in a sample of unrelated males with low Bone Mineral Density (LS Zscores <=-2) and with high Bone Mineral Density (LS and FN Zscores >0.5). A substantial amount of top hits in bivariate analysis did not reach nominal significance in any of the two single-trait analyses. Altogether, our studies suggest that bivariate analysis is of practical significance for GWAS of correlated phenotypes.


## INTRODUCTION

With the availability of high-density maps of single nucleotide polymorphisms (SNPs), association studies have become popular tools for identifying genes underlying complex human traits and diseases. For most current population-based genome-wide association studies (GWAS) statistical power is often limited due to the complex interplay among factors that influence the etiology of diseases ${ }^{1}$. Increasing sample size and multilocus or multivariate statistical analyses can improve the power for detecting association. Sample size is often restricted due to genotyping costs and limited sample resources. Several studies have demonstrated that analyzing samples selected with extreme values can be more powerful than analyzing samples randomly selected from the population ${ }^{2-4}$. In addition to using selected samples, another approach to increasing association test power is to perform joint analysis of multiple correlated phenotypes. For many common multifactorial traits, several correlated phenotypes are usually recorded for each individual during sample collection, but most often the phenotypes are analyzed separately in a univariate framework. Joint analysis of correlated phenotypes can theoretically provide greater power than that provided by analysis of individual phenotypes ${ }^{3,5-7}$. Multivariate analysis can also alleviate the multiple testing problem, caused by testing different traits separately, and thereby improve the ability to detect genetic variants whose effects are too small to be detected in univariate analysis ${ }^{8}$. Several multivariate approaches have been applied to linkage studies of correlated complex phenotypes, as osteoporosis and bone-related phenotypes ${ }^{9-12}$. Similarly, various methods, often based on Generalized Estimating Equations (GEE), have been proposed for performing multivariate association tests on population- or family-based data ${ }^{13-20}$. Of the two studies that have investigated the power of bivariate association test in population-based data, one applied the restricted bivariate association test that
assumes same Quantitative Trait Locus effects on each trait ${ }^{16,18}$. Such constraints in the model may have overestimated or underestimated the relative performance of bivariate over univariate analysis. Finally, GWAS studies using multivariate analysis are rare, especially in samples of subjects selected through their phenotype values, and further investigations using this approach are warranted ${ }^{4}$.

To this aim, we evaluated the statistical properties of joint association analysis of two correlated quantitative traits in samples of unrelated subjects through simulation studies, using the Seemingly Unrelated Regression (SUR) bivariate model that allows for different QTL effects on traits. The evaluation was conducted under different situations according to the sample selection design, genetic effects and residual correlation between the traits. We demonstrate the efficacy of SUR-based bivariate test by applying it to simultaneous GWAS analysis of two correlated bone phenotypes, Bone Mineral Density (BMD) at the Lumbar Spine and at the Femoral Neck, which are major risk factors of osteoporosis.

## METHODS

## SUR-based bivariate model

The Seemingly Unrelated Regression (SUR) model ${ }^{21}$ is a generalization of a classical linear regression model that consists of several regression equations with potentially different sets of explanatory variables. It thus allows for a differential effect of explanatory variables on phenotypes as well as the possibility that some variables might be associated with only one trait. Let's N be the total number of unrelated subjects ( $\mathrm{i}=1, . ., \mathrm{N}$ ), each having observations on two phenotypes $\mathrm{y}_{\mathrm{ji}}(\mathrm{j}=1,2)$. Consider a system of 2 equations, where the $j$ th equation is of the form: $y_{j}=X_{j} \times \beta_{j}+e_{j} ; y_{j}$ is a Nx1 vector of the phenotypic values, $\mathrm{X}_{\mathrm{j}}$ is a $\left(\mathrm{K}_{\mathrm{j}}+1\right) \mathrm{xN}$ matrix of explanatory variables with $\mathrm{K}_{\mathrm{j}}$
representing the number of explanatory variables in the model for phenotype j excluding the intercept; $\beta_{j}=\left(\beta_{0}^{j}, \beta_{1}^{j}, \ldots, \beta_{K_{j}}^{j}\right)^{t}$ is the $\left(\mathrm{K}_{\mathrm{j}}+1\right) \times 1$ vector of coefficients and $\mathrm{e}_{\mathrm{j}}$ is a Nx 1 vector of the residuals errors. The system of SUR can be written as:

$$
\binom{y_{1}}{y_{2}}=\left(\begin{array}{cc}
X_{1} & 0  \tag{1}\\
0 & X_{2}
\end{array}\right)\binom{\beta_{1}}{\beta_{2}}+\binom{e_{1}}{e_{2}}
$$

The SUR model allow for cross-equation correlation of the residual terms. The covariance matrix of all the residuals is assumed to be normally distributed with mean 0 and covariance matrix $E\left(e e^{t}\right)=\Omega=\Sigma \otimes I_{N}$ where $I_{N}$ is a NxN unit matrix and $\Sigma$ a 2 x 2 matrix with the following form:

$$
\Sigma=\left(\begin{array}{cc}
\sigma_{1}^{2} & r E \times \sigma_{1} \sigma_{2}  \tag{2}\\
r E \times \sigma_{1} \sigma_{2} & \sigma_{2}^{2}
\end{array}\right)
$$

$\sigma_{1}^{2}$ and $\sigma_{2}^{2}$ are the residual variances of $\mathrm{Y}_{1}$ and $\mathrm{Y}_{2}$ respectively and rE is the residual correlation between $\mathrm{Y}_{1}$ and $\mathrm{Y}_{2}$.

The SUR model is estimated using the generalized least squares method where the covariance matrix $\Omega$ is first estimated using ordinary least squares regression in system (1). Linear restrictions on coefficients can be tested by an F test. The F statistic for systems of equations is: $F=\left[\left(C \beta^{\prime}\right)^{t}\left(C \operatorname{cov}\left(\beta^{\prime}\right) C^{t}\right)^{-1}\left(C \beta^{\prime}\right)\right] / 2$
where, C is the matrix of restrictions on coefficients. Under the null hypothesis, the F statistic has a central Fisher distribution with 2 and $2 \mathrm{xN}-\mathrm{K}$ degrees of freedom where K is the total number of estimated coefficients $\left(\mathrm{K}=\mathrm{K}_{1}+\mathrm{K}_{2}+2\right)$. The goodness of fit of the whole system can be measured by the McElroy's r-square $\left(\mathrm{R}^{2}\right) . \mathrm{R}^{2}$ is the proportion of co-variance due to X taking into account the residual matrix covariance $\Omega^{22}$.

Here, we applied the SUR model to test association to two continuous phenotypes in unrelated subjects genotyped at one SNP marker, and $X_{j}$ is the Nx 1 vector of genotypes at the SNP. Under an additive model, the genotype for each individual $i$, noted $g_{i}$, is
coded as a function of the number of minor alleles, that is, 0,1 or 2 . We computed the SUR model free of constraints on the regression coefficients, that is, $\beta 1$ and $\beta 2$ were freely estimated. Under the null hypothesis of no association to either one or both phenotypes, the F statistic has a central Fisher distribution with 2 and $2 \times(\mathrm{N}-2)$ degrees of freedom. Separate association analyses of $\mathrm{Y}_{1}$ and $\mathrm{Y}_{2}$ can be conducted using traditional univariate linear regression model: $y_{j}=g x \beta_{j}+e_{j}$, where $y_{j}, g$, and $\beta_{j}$ are as described above but now $\mathrm{e}_{\mathrm{j}}$ is assumed to follow a normal distribution $\mathrm{N}\left(0, \sigma_{j}^{2}\right)$. The null hypothesis of no association $\left(\beta_{j}=0\right)$ can be tested against the alternative $\left(\beta_{j} \neq 0\right)$ with a Student statistic (t-test) with $\mathrm{N}-2$ degrees of freedom.

## Simulation study:

We considered genetic models of complex traits and specifically tried to generate correlated data mimicking as much as possible our real Bone Mineral Density (BMD) GWAS data (see below). Since a strong ( $\sim 0.5$ ) and positive phenotypic co-variation exists for BMD values at the Lumbar Spine (LS) and at the Femoral Neck (FN) ${ }^{23}$, we generated data for two positively correlated quantitative phenotypes. Further, in real datasets, as causal loci usually contribute a small proportion to the total phenotypic correlation, residual correlation approximates phenotypic correlation between traits. It is also more realistic to assume that the investigator has a priori knowledge on the magnitude and sign of the co-variation of the studied phenotypes than on the magnitude and sign of the QTL effect on each phenotype. Therefore, in all our scenarios, the sign of the residual correlation ( rE ) was positive, but the sign of the induced QTL correlation (rG) was either positive or negative. Also, our BMD GWAS study used a sampling design, with extreme truncate selection of unrelated males, aiming to improve power.

Therefore, we also generated samples of subjects drawn from the extremes of the phenotype(s) population distribution.

The main scenarios and parameter settings are shown in Table 1. The different settings allowed us to generate data for a QTL having same or different effect on the two positively correlated phenotypes, and the two sources of co-variation (QTL and residual) have same or opposite sign. Briefly, we assumed a bi-allelic QTL having additive effects $\left(\mathrm{a}_{\mathrm{j}}\right)$ on $\mathrm{Y}_{\mathrm{j}}(\mathrm{j}=1,2)$, with minor and major allele frequency q and p , respectively. The QTL contribution to $Y_{j}$ is the trait-specific QTL heritability, $h^{2}{ }_{j}$. Here, we focussed our power investigation to QTLs explaining a relatively small part of the trait variance, i.e., from $0.5 \%$ to $3 \%$ which, for complex traits, seemed to us more realistic. The genotypic means $\left(m_{j k}\right)$ of $Y j$ are equal to $2 q \times a_{j},(q-p) \times a_{j}$ and $-2 p \times a_{j}$ when $k$, the number of minor alleles, is equal to 0,1 and 2 respectively and with $a_{j}=$ $\left.V_{\left[h^{2}\right.}{ }_{\mathrm{j}} / 2 \mathrm{pq}\right]$. We varied the sign of $\mathrm{a}_{\mathrm{j}}$ : both were of same or opposite sign and the QTL correlation (rG) was, thus, equal to +1 or -1 , respectively. We first generated samples of subjects unselected for their traits values (denoted as Su ). Second, we generated subjects selected from the $2.5 \%$ (i.e., trait value $\leq-2$ ) and $30 \%$ (i.e., trait value $>0.5$ ) left and right tail of the population distribution of $\mathrm{Y}_{1}$ (denoted as S 1 ). Third, we included $\mathrm{Y}_{2}$ in the selection design, that is, we selected subjects from the $2.5 \%$ and $30 \%$ left and right tail of the population distribution of $Y_{1}$ and $Y_{2}$ (denoted as S2). These truncate selection criteria (trait value $\leq-2$ or $>0.5$ ) are the values we have used in our real BMD GWAS. Under S1 and S2, we generated samples with equal number of subjects drawn from the left ( $\mathrm{N} / 2$ ) and the right ( $\mathrm{N} / 2$ ) side of the phenotypes distributions.

Traits values of $\mathrm{N}(300,1000)$ unrelated subjects were generated as follows. For a given combination of parameter values ( $\mathrm{rE}, \mathrm{h}^{2}{ }_{1}, \mathrm{~h}^{2}{ }_{2}, \mathrm{rG}$ ), we first draw QTL alleles from a binomial distribution with parameter q , and built genotypes under Hardy-Weinberg
equilibrium. Then, conditionally on the generated genotype, $\mathrm{g}_{\mathrm{k}}(\mathrm{k}=0,1,2)$, we jointly drew the values of $Y_{1}$ and $Y_{2}$ via a bivariate normal distribution with mean $\left(m_{1 k}, m_{2 k}\right)^{t}$ and variance matrix $\Omega$, given in equation (2). Third, under sampling S1 or S2, we applied the corresponding truncate selection, that is individuals not fulfilling the selection criteria were withdrawn from the sample. Steps 1 to 3 were repeated until reaching the required left and right truncated sample sizes of (N/2) subjects.

Each replicate was analyzed with SUR-based bivariate and with two separate univariate analyses using the systemfit package of R software (http://www.r-project.org/) using the genotypes at the QTL, that is, the SNP is the causal variant. The mean and standard deviation of each association statistic ( $F$ test and $t_{1}, t_{2}$ tests) were derived from $K$ replicates. Power and type I error rates of each association test were calculated as the proportion of replicates with a test statistic exceeding a given theoretical threshold ( $\mathrm{R} \alpha$ ) value, at nominal significance levels, $\alpha=5 \%, 1 \%, 0.1 \%$ and $10^{-5}$. Type 1 errors were estimated in the settings were $\mathrm{h}^{2}=\mathrm{h}^{2}{ }_{2}=0$ with $\mathrm{K}=20000$ replicates. Power rates were derived with $\mathrm{K}=1000$ replicates. To compare the performance of bivariate and that of univariate association analysis, we computed the proportion of replicates where $t_{1}$ and $t_{2}$ were both lower than $\mathrm{R} \alpha$. One minus this proportion estimated the probability to detect association to either one of the two phenotypes. To adjust for the two univariate association tests, we applied the Bonferroni correction, that is, we used the theoretical thresholds $\mathrm{R} \alpha / 2$.

## RESULTS

## SIMULATION STUDY

Tables 2 and 3 present the mean (and sd) association statistic of the SUR-based bivariate ( F test) and of the traditional univariate tests ( t test), respectively when $\mathrm{N}=1$

000 for 66 scenarios under the alternative hypothesis and when $\mathrm{q}=0.4$. For a given QTL heritability value, the results did not vary, as expected, with q.

Bivariate association statistics: In randomly selected samples, the results in Table 2 show several well-established power figures. First, mean F statistics of bivariate association analysis increase with the size of the trait-specific QTL heritability $\left(\mathrm{h}^{2}{ }_{1}\right.$ and/or $h^{2}{ }_{2}$ ) irrespective of rG and rE . Second, the power is highest in presence ( $\mathrm{rG} \neq 0$ ) than in absence $(\mathrm{rG}=0)$ of pleitropic effects: the highest power is achieved when $\mathrm{rG}=-1$, that is, when the correlation induced by the QTL effect and the residual correlation are opposite in sign. Third, the results also confirm that the power of bivariate association test varies with the size of the residual correlation: when $\mathrm{rG}=0$ or $\mathrm{rG}=-1$, the power increases with rE ; conversely, when $\mathrm{rG}=+1$ it decreases with rE . These general trends are observed irrespective of the sampling selection designs. Applying extreme truncate selection increases the power of bivariate association analysis, but the optimal selection design depends on the true genetic model. When $\mathrm{rG}=0$ or $\mathrm{rG}=-1$, extreme selection on one trait (S1) is more efficient than extreme selection on both traits (S2). Conversely, when $\mathrm{rG}=+1$, S 2 is more efficient than S 1 . Overall, under Su or S 1 , the highest mean F statistics are obtained when $\mathrm{rG}=-1$, irrespective of rE . Under S 2 , the highest power is achieved when $\mathrm{rG}=+1$ or when $\mathrm{rG}=-1$, depending on the size of rE . Interestingly, when the traits are moderately ( $\mathrm{rE}=0.20$ ) correlated, mean F statistics have greater values when $\mathrm{rG}=+1$ than when $\mathrm{rG}=-1$.

Univariate association statistics Table 3 shows again several well-established power figures. In randomly selected samples, the power of univariate analysis increases with the QTL heritability $\left(\mathrm{h}^{2} / \mathrm{h}^{2}{ }_{2}\right)$ and varies little with the size of the residual correlation, rE. For phenotype $Y_{1}$, under a given QTL heritability $\left(h^{2}\right)$ value, the mean statistic values of all models are similar in the randomly selected samples. Applying extreme
truncate selection increases the power of univariate association analysis of $\mathrm{Y}_{1}$. Under S1, the power remains similar whichever rG. Under S2, the power is the highest and the lowest for the pleiotropic models $\mathrm{rG}=+1$ and $\mathrm{rG}=-1$, respectively. When $\mathrm{rG}=-1$ or $\mathrm{rG}=0$, the power of univariate association analysis is greater under S1 than under S2. The reverse trend is obtained when $\mathrm{rG}=+1$. For phenotype $\mathrm{Y}_{2}$, the power of univariate analysis depends on rG and rE. Further, applying extreme selection does not always lead to a gain in power. Indeed, when $\mathrm{rG}=-1$ the power of univariate analysis is the greatest in the unselected samples $(\mathrm{Su})$. When $\mathrm{rG}=0$ the mean t statistic values in the selected samples are biased and inflated. The magnitude of the bias is greater under S2 than under S1. Under S1, the bias increases with rE.

Overall, applying selection criteria on one or both traits is an optimal sampling design when $\mathrm{rG}=+1$ : the power of each separate univariate analysis is improved over that in randomly selected samples. When $\mathrm{rG}=-1$, applying extreme truncate selection leads to both a substantial gain and decrease in power for $Y_{1}$ and $Y_{2}$, respectively. For the situations in which the QTL does not exert pleiotropic effects $(\mathrm{rG}=0)$, the highest power of univariate analysis of $Y_{1}$ is obtained in the selected samples. However, the mean $t$ statistic values for $\mathrm{Y}_{2}$, the trait no associated to the QTL, are also increased. Type I error rates of separate univariate analyses may thus be inflated, especially in selected samples and when the residual correlation is high.

Type I error rates: When the QTL/SNP has no effect on $Y_{1}$ and $Y_{2}$, the values of the mean and standard deviation of both bivariate and univariate association tests are close to the theoretical values, regardless of the residual correlation, minor allele frequency of the studied SNP and of the selection sampling design (Supplementary Table 1.A). Indeed, SUR-based bivariate and each separate univariate association tests have correct type I error rates (Supplementary Table 1.B). However, the false-positive rates of
univariate association analyses for detecting association to either or both the two traits are, as expected, inflated: the estimated rates are roughly two times higher than the theoretical rates. Applying a Bonferroni correction (denoted as U_b) leads to slightly conservative significance levels, especially when the residual correlation between the traits is strong.

Power comparisons : The power to detect association to either or both of the two traits using SUR-based bivariate analysis was compared to the power of separate univariate analysis of $\mathrm{Y}_{1}$ and $\mathrm{Y}_{2}$ adjusted for multiple testing by the Bonferroni correction (denoted as $U_{-} b$ ). Figure 1.A shows the power curves (at significance of $10^{-5}$ ) against the QTL heritability $\left(\mathrm{h}^{2}, \mathrm{~h}^{2}{ }_{2}\right)$ when $\mathrm{N}=1000$, for moderately ( $\mathrm{rE}=0.2$ ) or strongly $(\mathrm{rE}=0.6)$ correlated traits. Power curves under S 1 and S 2 are shown in Figure 1.B, when $\mathrm{h}^{2}{ }_{1}=\mathrm{h}^{2}{ }_{2}=0.005, \mathrm{~N}=1000$ and $\mathrm{rE}=0.2$ or 0.6 .

In randomly selected samples (Figure 1.A), the relative advantage of SUR-based bivariate over univariate association analysis is more obvious when $\mathrm{rG}=-1$ and/or the traits are strongly correlated $(\mathrm{rE}=0.6)$ but also when $\mathrm{rG}=+1$ and the traits are moderately correlated ( $\mathrm{rE}=0.2$ ). Under S 1 (Figure 1.B), SUR-based bivariate is slightly less powerful than univariate analysis when $\mathrm{rG}=+1$ and $\mathrm{rE}=0.6$ or when $\mathrm{rG}=0$ and $\mathrm{rE}=0.2$. For strongly correlated traits, the power rates are equal to $94.5 \%$ (SUR) vs. $29.3 \%$ (U_b) when $\mathrm{rG}=-1 ; 44.0 \%$ (SUR) vs $32.3 \%$ (U_b) when $\mathrm{rG}=0 ; 36.8 \%$ (SUR) vs $39.9 \%$ ( $\mathrm{U} \_\mathrm{b}$ ) when $\mathrm{rG}=+1$. For moderately correlated traits, the power rates are equal to $64.6 \%$ (SUR) vs $31.7 \%$ (U_b) when $\mathrm{rG}=-1 ; 32.9 \%$ (SUR) vs $34.9 \%$ (U_b) when $\mathrm{rG}=0 ; 43.7 \%$ (SUR) vs $32.6 \%$ (U_b) when rG=+1. Under S2 (Figure 1.B), SUR-based bivariate shows same or slightly lower power than univariate analysis except when $\mathrm{rG}=-1$ or when $\mathrm{rG}=0$ and $\mathrm{rE}=0.6$ where it outperforms univariate test. As already noted above selecting on $Y_{1}(S 1)$ is the most efficient sampling design when $r G=-1$ or when $r G=0$
and the traits are strongly correlated ( $\mathrm{rE}=0.6$ ). Selecting on both traits ( S 2 ) is the most efficient design when $\mathrm{rG}=+1$. Overall, when $\mathrm{rE}=0.6$, the power of SUR is the greatest ( $94.5 \%$ ) when $\mathrm{rG}=-1$ and under S 1 , while the power of univariate analysis is the greatest $(56.8 \%)$ when $\mathrm{rG}=+1$ and under S 2 . When $\mathrm{rE}=0.2$, the power of SUR and univariate analysis are both the greatest ( $72.5 \%$ and $72.9 \%$ ) when $\mathrm{rG}=+1$ and under S 2 . As shown in Supplementary Table 2, all these trends are confirmed under various parameter settings.

## ANALYSES OF EMPIRICAL BMD-GENOME-WIDE ASSOCIATION DATA

BMD GWAS data: Subjects were recruited from the Network in Europe on Male Osteoporosis study ${ }^{24,25}$. Subjects selected from this cohort were unrelated males $>18$ and $<68$ years of age. In addition, the subjects were selected by bone densitometry (measured at the Lumbar Spine and at the Femoral Neck) criteria, having either low BMD (LS-Z-scores $\leq-2, \mathrm{n}=175$ ) or high BMD (both LS- and FN-Z-scores $>0.50$, $\mathrm{n}=155$ ). Further details of the study sample are provided in Supplementary Table 3. Genotyping was carried out at the Centre National de Génotypage (CNG, Evry, France) using the Illumina 370 K platform. SNPs and DNA data were subjected to standard quality control analyses with PLINK ${ }^{26}$ (details are provided in Supplementary Methods).

Association analysis: Our primary analysis was the joint association analysis of LSZscores and FN-Zscores by means of SUR-based bivariate test. For comparison purpose, we also applied separate univariate association analyses of LS and FN Zscores. We used single marker analysis assuming additive genetic effects. The mean F statistic of our SUR-based genome-wide association analysis was equal to 1.018 $(\mathrm{sd}=1.022$, median $=0.70)$. The mean t statistic of LS and FN were $-0.0167(\mathrm{sd}=1.011$,
median $=-0.0165)$ and $-0.0129(\mathrm{sd}=1.006$, median $=0.0104)$, respectively. These results indicated that there was no meaningful inflation of univariate as well as bivariate association analyses.

Results: SUR-based bivariate analyses identified a substantial number (35) of SNPs with strong evidence of association ( P -value $<10^{-4}$ ). Interestingly, several of the identified SNPs failed to reach nominal (P-value $<5 \%$ ) significance under separate univariate analyses for either one or the two BMD phenotypes. Genome-wide bivariate and univariate association results were compared in terms of statistical significance and ranks of the SNPs identified in either one of the two approaches. For each SNP, we kept the lowest P-value (denoted as Best_U) of LS or FN univariate association analysis. Univariate P values were not corrected for multiple testing. We ranked the Best_U Pvalues from the lowest to the highest. We similarly ranked the P-values from SURbased bivariate analysis of LS and FN. Figure 2 plots the significance levels in each procedure for the top 100 most associated SNPs identified from SUR-based (Figure 2.A) or from univariate (Figure 2.B) analyses. We found that a majority (52) of the top SNPs in SUR-based bivariate analysis also show strong $\left(\mathrm{P}<3 \times 10^{-4}\right)$ association signal in univariate analyses. For a substantial number (16) of the remaining SNPs, univariate analyses fail to reach nominal ( $\mathrm{P}<5 \%$ ) significance (Figure 2.A) On the other hand, all of the top 100 SNPs in univariate analyses (Figure 2.B) are also highly significant $\left(\mathrm{P}<8 \times 10^{-4}\right)$ in bivariate analysis. Table 4 shows details of the association results for the top 10 SNPs in SUR-based and in each separate univariate analysis. The table also shows P -values and ranks found in each of the two other procedures. The genetic contributions ( $\mathrm{R}^{2}$ values) of the 10 top SNPs are not great, as expected for any relatively common polymorphic locus. Three of the top 10 SNPs from bivariate analysis also rank well (i.e., are in the set of top 300 SNPs ) in univariate analyses of LS and/or FN. They
are located on 6 q 25 : rank $=2, \mathrm{P}=1.3 \times 10^{-5}(\mathrm{LS})$ and rank $=1, \mathrm{P}=1.2 \times 10^{-5}(\mathrm{FN})$; on $15 \mathrm{q} 14-$ q15: $\operatorname{rank}=2635, \mathrm{P}=8.4 \times 10^{-3}(\mathrm{LS})$ and rank $=3, \mathrm{P}=1.7 \times 10^{-5}(\mathrm{FN})$; and on 22q13: rank=1, $\mathrm{P}=3.5 \times 10^{-6}(\mathrm{LS})$ and rank $=8, \mathrm{P}=3 \times 10^{-5}(\mathrm{FN})$. All the remaining 7 SNPs show a much stronger association signal in bivariate than in univariate analyses, including 2 of the 3 best SUR-based association signals. For the most significant result, on 22 q 11.2 $\left(\mathrm{P}=5.44 \times 10^{-6}\right.$ ), the QTL explains $3.85 \%$ of the joint (co)variance of LS and FN. This value likely over-estimates the contribution in unselected populations. Nonetheless, univariate analyses failed to detect association $(\mathrm{P}>0.07)$ with this SNP. Conversely, all top 20 SNPs identified from univariate analysis of either LS or FN belong to the set of top 42 SNPs from SUR-based bivariate analysis. Overall, our analyses showed that univariate analysis did not identify new strongly associated SNPs as compared to those detected in bivariate analysis. Conversely, SUR-based analysis identified strongly associated SNPs that were not detected in univariate analysis.

Our study used a design, with extreme truncate selection of unrelated males, aiming to improve power. The approach of studying samples drawn from the extremes of the population distribution of BMD has been used in several linkage studies of BMD variation ${ }^{25,27}$, but rarely in association studies ${ }^{28}$, and to our knowledge, never in samples drawn from the population of males. Due to our relatively small GWA sample size, no SNP showed evidence of association to either one or both BMD phenotypes at genome-wide significance threshold of $1.7 \times 10^{-7}(0.05 / 298783$ SNPs $)$. However, we used an extreme truncate selection design that, as shown by our simulation studies, has increased power over unselected samples. Our SUR-based bivariate association analyses identified strong association $\left(\mathrm{P}<8.4 \times 10^{-6}\right)$ with 3 genomic regions ( $6 \mathrm{q} 22.1,15 \mathrm{q} 14$ and 22q11). These SNPs have not yet been reported to be associated with bone density in previous GWAS ${ }^{29-31}$. Two of them, on 15q14-15 and 22q11, are located in genes that
are known to be expressed in skeletal muscle ${ }^{32-33}$ : GLUT 11 encoded by SLC2A11 on $22 q 11$ and RYR3, on 15q14-15. Because muscle contraction has a major impact on bone density, this might represent an indirect role of these genes on bone density.These genetic variants, whether they are site-specific or possibly shared (pleiotropic), may warrant further follow-up genetic studies on BMD and other bone-related phenotypes.

## DISCUSSION

We have evaluated the performance of bivariate association analysis based on the Seemingly Unrelated Regression (SUR) model, which allows different genetic models for different traits. To our knowledge, this is the first study to specifically derive the power and the relative performance of bivariate association analysis in selected samples of unrelated subjects. Our main results coincide with well-known power figures ${ }^{6-8}$ and confirmed that bivariate association analysis outperforms univariate analysis when the QTL exerts pleiotropic effects and the relative increase in power is greatest when correlation of the QTL is opposite in sign to the residual correlation. The most powerful sampling selection design varied with the genetic model, specifically with the size and the direction of the induced-QTL correlation. Applying truncate selection on one trait was found the most efficient sampling design when the genetic and the residual correlations are opposite in signs. The same most efficient design was found when the QTL does not exert pleiotropic effects: the power of the SUR-based bivariate association test was found as good as or better than that of univariate association test, depending on the size of the residual correlation. Finally, when the QTL exerts pleiotropic effects and both sources (QTL and residual) of co-variation are of same sign, applying selection criteria on both traits was found the optimal sampling selection
design. Under this sampling design, the performance of SUR-based bivariate test relatively to univariate analysis decreases with the size of the residual correlation.

So far, two studies have investigated the power of bivariate association in unselected population-based data, and they both applied bivariate association test based on Generalized Estimating Equations ${ }^{16,18}$. The former applied a general GEE-based model that allows, as the SUR model, for different QTL effects on the two traits. The second study used a GEE-based bivariate model that assumed same QTL effects on the phenotypes. Our results are congruent with those reported by the first study. The restricted bivariate test estimates, as the univariate test, a single parameter (i.e., the SNP regression coefficients on each trait are all set equal). Under the restricted bivariate model, the gain in power of bivariate analysis is enhanced and reduced when the QTL has similar effect and when it affects one trait only, respectively. Clearly, rarely, knowledge of this magnitude about a complex trait is known a priori. Thus, we do not recommend using restricted bivariate models even in unselected data.

Our bivariate genome-wide association analysis of Lumbar Spine and Femoral Neck BMD values, conducted in a sample of unrelated males with low BMD (LS Zscores $\leq$ 2) and high BMD (LS and FN Zscores $>0.5$ ), consistently demonstrated the advantage of the SUR-based bivariate test over separate univariate analysis. All of the top hits in univariate analysis also showed strong evidence of association in bivariate analysis. Conversely, additional SNP associations were detected with the bivariate method that did not reach nominal significance in single-trait analyses: this was achieved without adjusting significance of univariate analyses for multiple testing.

In conclusion, our results showed that SUR-based models are useful to detect association for correlated phenotypes. However, our results also showed that similar power levels can be achieved whether the QTL exerts or not pleiotropic effects. Thus,
disentangling pure pleiotropic from residual covariation remains a challenge even in bivariate association analysis.

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Conflict of interest: none

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## Titles and legends to figures

Figure 1: Power rates at $\alpha=10^{-5}$ of SUR-based bivariate analysis and univariate analysis adjusted for multiple testing by Bonferroni correction (U_b), in samples of $\mathrm{N}=1000$ subjects and under various parameters settings: QTL heritability $\left(\mathrm{h}^{2} / \mathrm{h}^{2}{ }_{2}\right)$, sign of the induced genetic correlation (rG), residual correlation (rE).
(A) Power estimates against QTL heritability for moderately ( $\mathrm{rE}=0.2$ ) or strongly $(\mathrm{rE}=0.6)$ correlated traits, in randomly selected samples $(\mathrm{Su})$
(B) Power estimates under extreme selection ( S 1 or S 2 ) for moderately ( $\mathrm{rE}=0.2$ ) or strongly ( $\mathrm{rE}=0.6$ ) correlated traits and QTL heritability $\left(\mathrm{h}^{2}{ }_{1}=\mathrm{h}^{2}{ }_{2}=0.005\right)$

Figure 2: Overlap in significance of results from bivariate and univariate (Best_U) association analysis.
(A) Top 100 hits in SUR-based bivariate association test: $-\log _{10} \mathrm{P}$-values of univariate analysis against $-\log _{10} \mathrm{P}$-values of SUR-based bivariate analysis
(B) Top 100 hits in univariate association test: $-\log _{10} \mathrm{P}$-values of SUR-based bivariate analysis against $-\log _{10} \mathrm{P}$-values of univariate analysis

Table 2: Mean (and sd) of the SUR-based bivariate association statistic (F test) in samples of $\mathrm{N}=1000$ subjects for various parameter settings: QTL heritability $\left(\mathrm{h}^{2} / \mathrm{h}^{2}{ }_{2}\right)$, sign of the induced genetic correlation (rG), residual correlation (rE), and sampling selection design.

| $\mathrm{r}_{\mathrm{E}}$ | $\mathbf{r}_{\mathbf{G}}$ | $\mathbf{h}^{2} / \mathbf{h}^{2}{ }_{2}$ | ${ }^{1}$ Sampling |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{gathered} \mathrm{Su} \\ \mu \mathrm{~F} \text { (sd) } \end{gathered}$ | $\begin{gathered} \text { S1 } \\ \mu \mathrm{F}(\mathrm{sd}) \end{gathered}$ | $\begin{gathered} \text { S2 } \\ \mu \mathrm{F} \text { (sd) } \end{gathered}$ |
| 0.2 | 0 | 0.005/0 | 3.69 (2.61) | 10.10 (4.34) | 9.23 (4.18) |
|  |  | 0.01/0 | 6.17 (3.32) | 18.94 (5.86) | 17.97 (5.74) |
|  |  | 0.03/0 | 17.02 (6.08) | 59.02 (10.56) | 55.3 (10.32) |
|  | +1 | 0.005/0.005 | 5.08 (2.99) | 11.42 (4.86) | 15.17 (5.41) |
|  |  | 0.005/0.01 | 7.45 (3.66) | 14.07 (5.04) | 19.08 (6.58) |
|  |  | 0.01/0.01 | 9.50 (4.42) | 22.89 (6.86) | 29.84 (7.89) |
|  |  | 0.03/0.03 | 26.90 (7.34) | 72.04 (12.89) | 92.88 (14.41) |
|  | -1 | 0.005/0.005 | 7.26 (3.92) | 13.91 (5.30) | 9.57 (4.48) |
|  |  | 0.005/0.01 | 10.57 (4.36) | 17.22 (5.65) | 11.05 (4.88) |
|  |  | 0.01/0.01 | 13.69 (5.42) | 27.72 (7.40) | 19.29 (6.56) |
|  |  | 0.03/0.03 | 39.95 (9.40) | 89.83 (13.86) | 68.63 (13.23) |
| 0.6 | 0 | 0.005/0 | 4.88 (3.04) | 11.26 (4.51) | 9.96 (4.47) |
|  |  | 0.01/0 | 8.79 (4.04) | 22.54 (6.75) | 19.78 (6.16) |
|  |  | 0.03/0 | 25.04 (7.34) | 69.67 (11.85) | 62.92 (11.30) |
|  | +1 | 0.005/0.005 | 4.09 (2.69) | 10.41 (4.49) | 12.22 (4.78) |
|  |  | 0.005/0.01 | 6.36 (3.60) | 12.67 (5.06) | 15.60 (5.52) |
|  |  | 0.01/0.01 | 7.33 (3.85) | 20.35 (6.34) | 23.81 (6.76) |
|  |  | 0.03/0.03 | 20.42 (6.53) | 63.56 (11.19) | 73.11 (11.61) |
|  | -1 | 0.005/0.005 | 13.70 (5.32) | 20.94 (6.59) | 16.02 (5.84) |
|  |  | 0.005/0.01 | 19.71 (6.52) | 27.35 (7.55) | 21.20 (6.92) |
|  |  | 0.01/0.01 | 26.06 (7.40) | 42.83 (9.58) | 34.26 (8.87) |
|  |  | 0.03/0.03 | 78.65 (14.17) | 143.61 (19.15) | 124.18 (17.77) |

${ }^{1} \mathrm{Su}$ : unselected sample; S 1 : sample selected on $\mathrm{Y}_{1}$ distribution; S2: sample selected on $Y_{1}$ and $Y_{2}$ distributions.

Table 3: Mean (and sd) of the traditional univariate association statistic (t test) in samples of $\mathrm{N}=1000$ subjects for various parameter settings: QTL heritability $\left(\mathrm{h}^{2} / \mathrm{h}^{2}{ }_{2}\right)$, sign of the induced genetic correlation (rG), residual correlation (rE), and sampling selection design.

| $\mathrm{r}_{\mathrm{E}}$ | $\mathrm{r}_{\mathrm{G}}$ | $\mathrm{h}^{2} / \mathrm{h}^{2}{ }_{2}$ | ${ }^{1}$ Sampling |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | SU |  | S1 |  | S2 |  |
|  |  |  | $\mathrm{Y}_{1} \mu \mathrm{t}$ (sd) | $\mathbf{Y}_{2} \mu \mathrm{t}$ (sd) | $\mathrm{Y}_{1} \mu \mathrm{t}$ (sd) | $\mathbf{Y}_{2} \mu \mathrm{t}$ (sd) | $\mathrm{Y}_{1} \mu \mathrm{t}$ (sd) | $\mathbf{Y}_{2} \mu \mathrm{t}$ (sd) |
| 0.2 | 0 | 0.005/0 | 2.26 (1.01) | -0.03 (1.00) | 4.23 (0.99) | 0.98 (1.02) | 4.02 (1.00) | 2.59 (1.05) |
|  |  | 0.01/0 | 3.15 (1.01) | -0.02 (0.97) | 5.95 (0.98) | 1.41 (1.00) | 5.78 (0.96) | 3.60 (1.00) |
|  |  | 0.03/0 | 5.53 (1.06) | 0.00 (1.00) | 10.69 (0.96) | 2.33 (0.96) | 10.34 (0.98) | 6.34 (1.01) |
|  |  | 0.005/0.005 | 2.23 (1.00) | 2.20 (0.98) | 4.15 (0.97) | 3.21 (1.07) | 4.99 (0.97) | 4.83 (1.03) |
|  |  | 0.005/0.01 | 2.19 (0.97) | 3.23 (1.02) | 4.19 (0.97) | 4.21 (0.99) | 5.36 (1.02) | 5.69 (1.07) |
|  |  | 0.01/0.01 | 3.18 (1.00) | 3.19 (1.04) | 5.96 (1.01) | 4.72 (1.04) | 7.06 (0.96) | 6.93 (1.09) |
|  |  | 0.03/0.03 | 5.57 (1.01) | 5.57 (0.98) | 10.64 (1.01) | 8.60 (1.07) | 12.28 (0.96) | 12.57 (1.13) |
|  | -1 | 0.005/0.005 | 2.20 (1.01) | -2.26 (1.01) | 4.18 (1.00) | -1.26 (0.99) | 3.15 (0.99) | 0.36 (1.02) |
|  |  | 0.005/0.01 | 2.26 (0.99) | -3.22 (0.97) | 4.21 (0.92) | -2.16 (0.99) | 2.69 (1.03) | -0.60 (0.99) |
|  |  | 0.01/0.01 | 3.18 (1.04) | -3.17 (1.04) | 5.95 (0.98) | -1.95 (1.01) | 4.56 (0.96) | 0.44 (0.97) |
|  |  | 0.03/0.03 | 5.57 (1.01) | -5.58 (1.04) | 10.68 (0.97) | -3.91 (1.01) | 8.51 (0.96) | 0.29 (0.95) |
| 0.6 | 0 | 0.005/0 | 2.23 (1.00) | 0.00 (0.96) | 4.19 (0.97) | 2.35 (0.98) | 3.89 (0.99) | 2.69 (0.97) |
|  |  | 0.01/0 | 3.13 (0.99) | -0.05 (0.98) | 6.01 (1.00) | 3.26 (0.97) | 5.64 (0.97) | 3.87 (0.98) |
|  |  | 0.03/0 | 5.55 (1.02) | 0.01 (0.98) | 10.62 (0.98) | 5.44 (0.96) | 10.08 (0.96) | 6.63 (0.96) |
|  |  | 0.005/0.005 | 2.22 (1.00) | 2.24 (0.99) | 4.17 (1.00) | 4.06 (1.02) | 4.58 (0.99) | 4.59 (1.01) |
|  |  | 0.005/0.01 | 2.25 (1.01) | 3.24 (1.03) | 4.17 (1.00) | 4.79 (1.03) | 4.90 (0.94) | 5.40 (0.99) |
|  |  | 0.01/0.01 | 3.17 (1.03) | 3.18 (1.00) | 5.97 (1.01) | 5.83 (1.01) | 6.52 (0.96) | 6.58 (1.00) |
|  |  | 0.03/0.03 | 5.55 (1.01) | 5.60 (1.03) | 10.70 (0.98) | 10.47 (0.99) | 11.48 (0.93) | 11.75 (0.99) |
|  | -1 | 0.005/0.005 | 2.20 (1.02) | -2.30 (1.02) | 4.13 (0.97) | 0.48 (0.95) | 3.23 (0.97) | 0.81 (0.92) |
|  |  | 0.005/0.01 | 2.23 (1.00) | -3.21 (1.00) | 4.15 (1.00) | -0.20 (1.00) | 2.97 (0.99) | 0.03 (0.97) |
|  |  | 0.01/0.01 | 3.10 (1.02) | -3.22 (1.01) | 5.99 (0.96) | 0.70 (0.97) | 4.75 (0.97) | 1.11 (0.95) |
|  |  | 0.03/0.03 | 5.52 (1.04) | -5.60 (1.05) | 10.68 (0.95) | 0.57 (0.93) | 8.89 (0.92) | 1.69 (0.88) |

${ }^{1}$ Su: unselected sample; S1: sample selected on $\mathrm{Y}_{1}$ distribution; S2: sample selected on $Y_{1}$ and $Y_{2}$ distributions.

Table 1: Outline of the main scenarios and varying parameter values in the bivariate data simulations

| Main scenarios |  |  |  | Parameter values |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| QTL Model | Heritability ( $\mathrm{h}^{2}$ ) | ffect size (aj) |  | q | $\mathrm{h}^{2}{ }_{\text {j }}$ | rE | N | Sampling Design |
| I. Null | $\mathrm{h}^{2}=\mathrm{h}^{2}=0$ | $\mathrm{a}_{1}=\mathrm{a}_{2}=0$ | 0 | 0.1/0.4 | $\mathrm{h}^{2}{ }_{1}=0$ \& $\mathrm{h}^{2}=0$ | 0.4 / 0.6 | 1000 / 300 | Su / S1 / S2 |
| II. No pleiotropic effect | $\mathrm{h}^{2}>0 ; \mathrm{h}^{2}=0$ | $a_{1}>0 ; a_{2}=0$ | 0 | 0.1/0.4 | $h^{2}{ }_{1}=\{0.5 \% / 1 \% / 3 \%\}$ \& $h^{2}=0$ | 0.4 / 0.6 | 1000 / 300 | Su / S1/S2 |
| III. Pleiotropic effect |  |  |  |  |  |  |  |  |
| $\mathrm{a}_{\mathrm{j}}$ : same direction | $\mathrm{h}^{2}{ }_{1}=\mathrm{h}^{2}$ | $a_{1}=a_{2}$ | + | 0.1/0.4 | $h^{2}{ }_{1}=h^{2}{ }_{2}=\{0.5 \% / 1 \% / 3 \%\}$ | $0.4 / 0.6$ | 1000 / 300 | Su / S1 / S2 |
|  | $\mathrm{h}^{2}{ }_{1} \neq \mathrm{h}^{2}{ }_{2}$ | $\mathrm{a}_{1} \neq \mathrm{a}_{2}$ | + | 0.1/0.4 | $\begin{gathered} \mathrm{h}^{2}{ }_{1}=0.5 \% \text { \& } \mathrm{h}^{2}=\{1 \% / 3 \%) ; \\ \mathrm{h}^{2}{ }_{1}=1 \% \text { \& } \mathrm{h}^{2}{ }_{2}=3 \% \end{gathered}$ | 0.4 / 0.6 | 1000 / 300 | Su / S1 / S2 |
| $\mathrm{a}_{\mathrm{j}}$ : opposite direction | $\mathrm{h}^{2}=\mathrm{h}^{2}$ | $\mathrm{a}_{1}=-\mathrm{a}_{2}$ | - | 0.1/0.4 | $h^{2}{ }_{1}=h^{2}{ }_{2}=\{0.5 \% / 1 \% / 3 \%\}$ | $0.4 / 0.6$ | 1000 / 300 | Su / S1 / S2 |
|  | $\mathrm{h}^{2}{ }_{1} \neq \mathrm{h}^{2}$ | $a_{1} \neq-a_{2}$ | - | 0.1/0.4 | $\begin{gathered} \mathrm{h}^{2}{ }_{1}=0.5 \% \text { \& } \mathrm{h}^{2}=\{1 \% / 3 \%) ; \\ \mathrm{h}^{2}{ }_{1}=1 \% \text { \& } \mathrm{h}^{2}{ }_{2}=3 \% \end{gathered}$ | 0.4 / 0.6 | 1000 / 300 | Su / S1 / S2 |

${ }^{1} \mathrm{a}_{\mathrm{j}}=\sqrt{ }\left[\mathrm{h}_{\mathrm{j}}{ }^{2} \cdot / 2 \mathrm{pq}\right]$, where q is the Minor Allele Frequency

Table 4：Association results：Top 10 most associated SNPs from SUR－based bivariate or from separate univariate analysis of LS and FN BMD

|  | Chr．（Locus） | Closest Gene | Pos（bp） | SNP | ${ }^{1}$ Min． | ${ }^{2}$ MAF | SUR |  |  | Univ．LS |  |  | Univ．FN |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | P | ${ }^{4}$ Rank | ${ }^{3} \mathbf{R}$（\％） | ${ }^{5} \mathbf{P}$ | ${ }^{4}$ Rank | ${ }^{5} \mathrm{R}^{2}$（\％） | ${ }^{5} \mathbf{P}$ | ${ }^{4}$ Rank | ${ }^{5} \mathrm{R}^{2}(\%)$ |
|  | 2q37．1 | SP100 | 231037761 | rs1649866 | A | 0.33 | $2.03 \mathrm{E}-05$ | 8 | 3．41\％ | 0.539 | 162064 | 0．12\％ | 0.086 | 25794 | 0．95\％ |
| 䧳 |  |  | 231042007 | rs1678160 | G | 0.33 | $1.45 \mathrm{E}-05$ | 4 | 3．52\％ | 0.574 | 172327 | 0．10\％ | 0.072 | 21500 | 1．04\％ |
| 示 | 3 q 25 | LEKR1 | 158200574 | rs6799034 | C | 0.43 | $1.81 \mathrm{E}-05$ | 6 | 3．45\％ | 0.970 | 289752 | 0．00\％ | $2.41 \mathrm{E}-02$ | 7166 | 1．63\％ |
| T | 6 q 22.1 | LOC643884 | 113858994 | rs2049924 | A | 0.29 | $8.42 \mathrm{E}-06$ | 3 | 3．69\％ | $1.80 \mathrm{E}-03$ | 607 | 3．09\％ | 0.363 | 109135 | 0．27\％ |
| 号 | 6 q 25 | TIAM2 | 155533083 | rs998318 | G | 0.31 | $2.94 \mathrm{E}-05$ | 10 | 3．30\％ | $1.30 \mathrm{E}-05$ | 2 | 5．94\％ | $1.22 \mathrm{E}-05$ | 1 | 5．98\％ |
| $\infty$ | 12p13－p12 | PZP－A2MP | 9254198 | rs1017301 | C | 0.34 | $2.24 \mathrm{E}-05$ | 9 | 3．38\％ | 0.223 | 67841 | 0．48\％ | $1.13 \mathrm{E}-03$ | 348 | 3．36\％ |
| O | 15q14－15 | RYR3 | 31680776 | rs2437143 | C | 0.38 | $6.97 \mathrm{E}-06$ | 2 | 3．75\％ | $8.41 \mathrm{E}-03$ | 2635 | 2．21\％ | $1.65 \mathrm{E}-05$ | 3 | 5．80\％ |
| 0 | 19p13．11 | FAM125A | 17392450 | rs2303680 | G | 0.41 | $1.92 \mathrm{E}-05$ | 7 | 3．43\％ | 0.743 | 222673 | 0．03\％ | $4.66 \mathrm{E}-02$ | 13886 | 1．27\％ |
| ［10 | 22q11．2 | SLC2A11 | 22534158 | rs2275979 | A | 0.18 | $5.44 \mathrm{E}-06$ | 1 | 3．85\％ | 0.523 | 157609 | 0．13\％ | 0.067 | 20101 | 1．08\％ |
|  | 22q13 | LL22NC03 | 43026421 | rs3935378 | T | 0.49 | $1.64 \mathrm{E}-05$ | 5 | 3．48\％ | 3．54E－06 | 1 | 6．69\％ | $2.95 \mathrm{E}-05$ | 8 | 5．47\％ |
|  | 1q32－41 | CAMK1G | 207787465 | rs996146 | T | 0.11 | $6.39 \mathrm{E}-05$ | 24 | 3．06\％ | $1.65 \mathrm{E}-05$ | 3 | 5．80\％ | $5.19 \mathrm{E}-05$ | 10 | 5．14\％ |
| 0 | 1 q 41 | ESRRG | 214946534 | rs2813711 | A | 0.13 | $7.13 \mathrm{E}-05$ | 29 | 3．02\％ | $3.68 \mathrm{E}-05$ | 10 | 5．34\％ | $2.36 \mathrm{E}-05$ | 5 | 5．59\％ |
| ¢ | 2q11．2 | AFF3 | 99943239 | rs11887597 | C | 0.48 | $1.08 \mathrm{E}-04$ | 36 | 2．90\％ | $2.42 \mathrm{E}-05$ | 7 | 5．60\％ | 0.0005639 | 156 | 3．77\％ |
| $\geq$ | 3 q 22.3 | PIK3CB | 139883989 | rs531577 | C | 0.49 | $1.37 \mathrm{E}-04$ | 40 | 2．85\％ | $2.89 \mathrm{E}-05$ | 9 | 5．53\％ | 0.0004341 | 113 | 3．95\％ |
| 5 | 6 q 25.2 | TIAM2 | 155533083 | rs998318 | G | 0.31 | $2.94 \mathrm{E}-05$ | 10 | 3．30\％ | $1.30 \mathrm{E}-05$ | 2 | 5．94\％ | $1.22 \mathrm{E}-05$ | 1 | 5．98\％ |
| E | 7 q 11.23 | CCDC146 | 76658736 | rs10252204 | A | 0.40 | $6.29 \mathrm{E}-05$ | 23 | 3．07\％ | $1.97 \mathrm{E}-05$ | 5 | 5．72\％ | 0.001236 | 382 | 3．32\％ |
| 은 | 10q21．2 | LOC729184 | 62158387 | rs1904418 | G | 0.32 | $7.68 \mathrm{E}-05$ | 31 | 3．06\％ | $1.71 \mathrm{E}-05$ | 4 | 5．89\％ | 0.0004438 | 115 | 3．97\％ |
| 응 | 16p13 | NPM1P3 | 5551122 | rs1969139 | C | 0.31 | $1.38 \mathrm{E}-04$ | 42 | 2．82\％ | $2.88 \mathrm{E}-05$ | 8 | 5．48\％ | 0.0003619 | 93 | 4．01\％ |
| $\bigcirc$ | 16q21 | SLC38A7 | 57262362 | rs9806843 | G | 0.43 | $8.55 \mathrm{E}-05$ | 33 | 2．97\％ | $1.99 \mathrm{E}-05$ | 6 | 5．69\％ | 0.0005906 | 169 | 3．73\％ |
|  | 22q13．31 | LL22NC03 | 43026421 | rs3935378 | T | 0.49 | $1.64 \mathrm{E}-05$ | 5 | 3．48\％ | $3.54 \mathrm{E}-06$ | 1 | 6．69\％ | $2.95 \mathrm{E}-05$ | 8 | 5．47\％ |
|  | 1 p 21.1 | LOC126987 | 106644698 | rs1330226 | C | 0.30 | $8.56 \mathrm{E}-05$ | 34 | 2．97\％ | $4.64 \mathrm{E}-05$ | 18 | 5．20\％ | $2.70 \mathrm{E}-05$ | 6 | 5．52\％ |
| Z | 1q32－41 | CAMK1G | 207787465 | rs996146 | T | 0.11 | $6.39 \mathrm{E}-05$ | 24 | 3．06\％ | $1.65 \mathrm{E}-05$ | 3 | 5．80\％ | $5.19 \mathrm{E}-05$ | 10 | 5．14\％ |
| $\stackrel{\square}{0}$ | 1 q 41 | ESRRG | 214946534 | rs2813711 | A | 0.13 | $7.13 \mathrm{E}-05$ | 29 | 3．02\％ | $3.68 \mathrm{E}-05$ | 10 | 5．34\％ | $2.36 \mathrm{E}-05$ | 5 | 5．59\％ |
| $\geq$ | 2p21 | C2orf34 | 44846991 | rs11679997 | T | 0.15 | $6.73 \mathrm{E}-05$ | 28 | 3．05\％ | $2.99 \mathrm{E}-03$ | 960 | 2．81\％ | $3.14 \mathrm{E}-05$ | 9 | 5．45\％ |
| 5 | 6 q 25.2 | TIAM2 | 155533083 | rs998318 | G | 0.31 | $2.94 \mathrm{E}-05$ | 10 | 3．30\％ | $1.30 \mathrm{E}-05$ | 2 | 5．94\％ | $1.22 \mathrm{E}-05$ | 1 | 5．98\％ |
| E | 7 p 22.2 | SDK1 | 3411837 | rs6952184 | C | 0.09 | $5.97 \mathrm{E}-05$ | 20 | 3．08\％ | $4.09 \mathrm{E}-05$ | 14 | 5．28\％ | $1.68 \mathrm{E}-05$ | 4 | 5．79\％ |
| 은 | 12q21．31 | TSPAN19 | 83921735 | rs1581563 | G | 0.16 | $8.36 \mathrm{E}-05$ | 32 | 2．97\％ | $4.31 \mathrm{E}-05$ | 15 | 5．25\％ | $2.73 \mathrm{E}-05$ | 7 | 5．51\％ |
| $\stackrel{4}{\circ}$ | 15q14－15 | RYR3 | 31680776 | rs2437143 | C | 0.38 | $6.97 \mathrm{E}-06$ | 2 | 3．75\％ | $8.41 \mathrm{E}-03$ | 2635 | 2．21\％ | $1.65 \mathrm{E}-05$ | 3 | 5．80\％ |
| $1+$ | 20p12－p11．2 | NXT1 | 23219822 | rs4815192 | T | 0.46 | $6.45 \mathrm{E}-05$ | 26 | 3．06\％ | $9.81 \mathrm{E}-05$ | 41 | 4．78\％ | $1.39 \mathrm{E}-05$ | 2 | 5．92\％ |
|  | 22q13．31 | LL22NC03 | 43026421 | rs3935378 | T | 0.49 | $1.64 \mathrm{E}-05$ | 5 | 3．48\％ | $3.54 \mathrm{E}-06$ | 1 | 6．69\％ | $2.95 \mathrm{E}-05$ | 8 | 5．47\％ |

${ }^{1}$ Minor allele；${ }^{2}$ Minor allele frequency；${ }^{3}$－square of the whole system taking into account the residual（co）variance matrix；${ }^{4}$ rank of the identified SNP；${ }^{5}$－square from linear regression；${ }^{5}$ Unadjusted univariate P values．




