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An Interpretation of the Haasen-Kelly Effect

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Abstract: In 1957, P. Haasen and A. Kelly presented an account of experiments which showed that in Al and Ni single crystals the mere act of unloading during a tensile test caused a small but reproducible transient increase in flow stress, a 'yield-point'. The increase is proportional to the current work-hardened stress level. It occurs at the lowest temperatures, where diffusion is not possible, but it is enhanced at higher temperatures. The effect was interpreted as arising from dislocations which 'anchor themselves during unloading and that this process of anchoring, which prevents reverse plastic flow, is also responsible for the yield-point effect on reloading'. Recent ideas emphasising the role of dislocation dipoles as sources for slip provide a natural explanation for these effects.

(Ms date 18/12/2009)

1. Introduction: A simplified description of the work-hardened state envisages three idealised types of dislocation sources: (1) segments in small-angle boundaries which are mainly found in the 'carpets' or regions roughly parallel to glide planes, but also in the incidental dislocation boundary (IDB) structure within the geometrically necessary boundary structure (GDB) encasing slip bands (Kuhlmann-Wilsdorf and Hansen 1992); (2) primary screw dislocation dipoles which limit slip in a direction perpendicular to the Burgers vector; (3) primary edge dislocation dipoles which limit slip parallel to it, as sketched by Hirsch (1975). The dipole arrays act as staging posts for dislocations, exchanging with the mobile segments to produce ever finer and more numerous dipoles, but allowing the mobile segments to penetrate the array with a certain probability. The arrays are thus both sources and sinks for mobile dislocations. Edge dipoles are the most numerous sources.

In thinking about the dipole arrays, it is important to recognise¹ that the local resistance they pose to primary dislocations is not proportional to the square root of their dislocation density, nor even to their dipole density, but varies from dipole to dipole depending only on the height² of each dipole. The dipoles are spaced about ten times further apart than their average height. Because the dipole arrays consist of a distribution of heights, the arrays are 'statistically deformable', meaning that they have a mixture of weak and strong points. For screw arrays, there is a minimum height of dipole which can survive without crossslipping to extinction. For edge arrays, the smallest dipoles transform to faulted dipoles, which can act as sources of deformation twinning (Steeds 1967, Niewcas and Saada, 2002). As the applied stress increases, the maximum height of stable dipole diminishes, until at the onset of Stage III hardening, there are no screw dipoles remaining in the crystal, only edge dipoles

¹ This seems first to have been stated by Friedel (*Dislocations*, 1964, Pergamon Press, p 248): '. . .in many cases the distance h between slip planes. . .is so small that the maximum elastic interaction. . .between dislocations in neighbouring planes is large compared with the applied stress. The whole Taylor model then breaks down.'

 $^{^{2}}$ The 'height' of a dipole is the distance h measured perpendicular to the slip plane between the two dislocations of opposite sign making it up.

 and small-angle boundaries are left. Full confinement of the slip bands is then lost.

Within the dipole arrays there is opportunity to exchange partners. In the case of the edge dipoles, screw dislocations connecting one dipole with another can move to transfer partners. In general, higher (coarser) dipoles have more energy per unit length than finer (narrower) ones, and because of nonlinear effects, interstitial dipoles (half-planes pointing inwards) have greater energy than vacancy dipoles. As deformation proceeds, the dipole array thus not only becomes finer, it tends to contain more narrow vacancy dipoles than interstitial ones.

Niewcas (2002) presents beautiful detailed observations of the dipole debris produced by the monotonic deformation of Cu. Although the screw dislocations are not retained in the thin foils, the distribution of edge dislocation dipoles is broadly consistent with this simplified description.

2. The Haasen-Kelly (1957) Effect: When their classic paper on yield phenomena in face-centred cubic single crystals was published, what was at issue was whether or not the small yield points observed after ageing deformed crystals were due to the formation of Cottrell atmospheres at dislocations. Haasen and Kelly showed that the mere act of unloading the crystals produces a small but measurable yield point. Fig 1 shows a schematic diagram, redrawn from their paper. The crystals must be unloaded by more than 50% to produce the full effect. The effect is observed at temperatures too low for any deformationinduced defect to migrate, but it is enhanced at room The presence of impurities seems to reduce it. temperature. Upon reloading after unloading, the size of the yield point as defined in Fig. 1 is approximately proportional to the applied stress above the level at the end of stage I of the hardening curve. However, the effect is very small, the yield point at the lowest temperature amounting to about 1.5% of the applied

stress. It appears that similar effects are observed in zonerefined iron (Wray and Horne 1966).



Fig. 1 (adapted from Haasen and Kelly (1957)). The definition of the observed yield point, $\Delta\sigma$, is shown. The plastic strain interval is estimated from another diagram in their paper.

3. A simple interpretation: The stress required to split an edge dislocation dipole is given by Brown and Nabarro (2004) as

$$\sigma_{c} \approx \frac{\mu b}{8\pi (1-\nu)h} \left(1 \pm \frac{6\gamma_{G} (1+\nu)(1-2\nu)^{3}}{\pi^{2} (1-\nu)^{2}} \right) = \sigma_{A} \left(1 \pm \frac{\Delta \sigma_{A}}{\sigma_{A}} \right).$$
(1)

Here, μ is the shear modulus, *b* the magnitude of the Burgers vector, *h* is the dipole height, ν is Poisson's ratio, and γ_G is the Grüneisen constant, about equal to two for most materials, and a measure of non-linear effects. The term outside the bracket is the usual splitting stress in linear elasticity, as derived for

example by Kelly and Groves (1970). Under such a stress. linear elasticity shows that a dipole can be flipped from one stable configuration to another and split entirely, each dislocation then becoming mobile, free to travel separately to For the dipole to act as a source of another obstacle. dislocations, the splitting stress equals the applied stress, σ_{A} . The term inside the bracket is an estimate of the correction due to non-linear elasticity. It *increases* the flipping stress but *decreases* the splitting stress for interstitial dipoles, and does the opposite for vacancy dipoles. One can imagine that compressive regions are elastically harder than tensile ones, so it becomes more difficult to force dislocation half-planes over one another when they point toward each other, but easier when they point away from each other.

Brown and Nabarro also show that screw dislocations connecting dipoles of opposite sign are subject to an effective stress tending to convert interstitial dipoles into vacancy ones. The magnitude of the stress is about 10% of the stress required to split the dipoles, if the dipoles are spaced about ten times their height. But the stress required to split the dipoles is equal to the current level of the work-hardened flow stress, so the screws cannot respond to the small conversion forces unless the crystal is unloaded.

One has here a possible basis for an interpretation of the Haasen-Kelly effect: upon unloading, screw dislocations can move so as to convert interstitial dipoles into vacancy ones, thereby increasing slightly the stress required to split them so as to release the dislocations. The magnitude of the effect is just proportional to the flow stress. The process requires slip alone, no diffusion is necessary.

Equation (1) predicts a surprisingly large effect. The fractional change in splitting stress is predicted to be about 13% if

Poisson's ratio³ is taken to be about 1/3. The experimental value is much less than this. In order to achieve agreement between theory and experiment, a slightly more complicated analysis is required.

4. *A more realistic interpretation:* According to Nabarro and Brown (2004), the action of the mobile screw dislocations is to convert dipole arrays with equal sizes of vacancy and interstitial dipoles into arrays with smaller vacancy dipoles and larger interstitial ones, whilst conserving both the number of dipoles and total vacancy/interstitial content of the array. Only if the array connects with external surfaces can material be extruded or intruded from the slip bands. This happens in persistent slip bands in cyclic plasticity, but in unidirectional deformation most slip bands do not connect with outer surfaces. The unloading impact on interstitial and vacancy dipoles of equal size is to create smaller vacancy dipoles, harder to split on reloading, as well as larger interstitial dipoles, easier to split on reloading. Not all dipoles can be modified in this way, only some of the edge dipoles — those connected to screw dislocations – whereas the screw dipoles (if any) and the links of dislocations in the small-angle boundaries are likely to be unmodified on unloading.

Fig. 2 shows schematically what can happen. On the left is sketched $n_s(\sigma)$, the number of dipoles per unit area which can act as a source of mobile dislocations under the stress σ . Under load, all the dipoles which can be split at stresses lower than σ_A are wiped out, whereas the stronger dipoles remain. On unloading, the step-function discontinuity in dipole density is modified: some narrower vacancy dipoles are created, which increases the density above the step, but also some wider interstitial dipoles, which increases the density below it. At the

³ The value of Poisson's ratio to be inserted here is *not* the value one uses to produce accurately the ratio between the line energies of edge and screw dislocations, but it is the value which gives the ratio between the shear modulus and the bulk modulus. Using the tables given by Hirth and Lothe (1992) one finds that for all the metals discussed here the value can be taken to be $0.33 \pm .03$.

step itself, the density is reduced by an appreciable fraction. The non-linear forces producing the rearrangement of the dipoles are small, so only dipoles very close to those at the step are affected. The dipole distribution is modified without external plastic strain, only the motion of the short segments of screw dislocations can produce some reverse strain

The relationship between the dipole density and the plastic strain increment de_p caused by a stress increment $d\sigma$ is

$$de_{P} = 2\lambda bn_{s}(\sigma)d\sigma, \qquad (2)$$

where λ is the mean free path of each of the two liberated dislocations split from the dipole. For strains very near to the unloading and reloading event, we can assume a constant source density and a constant mean free path, so

$$\frac{d\sigma}{de_P} \approx 2\lambda b \frac{1}{n_s(\sigma)}.$$
(3)

On the right-hand side of Fig. 2 is sketched the stress-strain curve upon reloading. We see that the 'premature yielding' of Fig. 1 results from the extra interstitial dipoles produced by the rearrangement, and the 'yield point' is produced by the extra vacancy dipoles. The shape of the observed stress-strain curve is roughly reproduced if about half the sources at the step undergo rearrangement. We see that the magnitude of the yieldpoint, as defined in Fig. 1, is lower than the fractional change in splitting stress estimated in Eq. (1) by a factor of about 6, bringing it much more in line with the experimental observations.



On the left hand side is sketched the density of Fig. 2. dislocation sources (abscissa) as a function of the applied stress under load (ordinate). There is a step discontinuity at the current stress level. On unloading, screw dislocations move to create larger interstitial dipoles and smaller vacancy dipoles, thereby modifying the distribution the immediate in neighbourhood of the discontinuity. The corresponding stressstrain curve is sketched in the right-hand diagram. The slope of the stress-strain curve is proportional to the reciprocal of the If no rearrangement occurs, it follows the source density. dashed line. Rearrangement produces a yield point at the onset of plastic flow. The slopes of the straight-line segments on the reloading curve have been estimated from equation (3), using the known slope of the basic work-hardening curve in Fig. 1.

The sketch of Fig. 2 is the outcome of a crude attempt to reproduce the experimental curve. It is based upon the assumption that no macroscopic instability occurs upon yielding. However, the curve of Fig. 1 shows a short range of strain in which the stress-strain curve shows zero or even negative slope. In this range, the Considère condition for plastic

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59 60 stability is clearly violated. Although Haasen and Kelly make no mention of it, some sort of Lüders band probably propagates through their specimens at yield. The reduced slope of the curve produced by modelling in Fig. 2 can produce plastic instability and result in an apparent zero or negative slope in the output of the tensile testing machine. A more sophisticated model must take this into account before one can reliably derive the source density distribution from the experimental data.

At temperatures where cross-slip of the screw dislocations can occur, the slip required for the rearrangement will be facilitated because the screws will be more flexible, not constrained to one glide plane. Rearrangement of more pairs of dipoles will occur. Cross-slip is accomplished by the thermally activated motion of jogs, with an activation energy around 0.1eV, that is, cross-slip becomes fast between 20K and 77K, the temperature range where an enhancement of the Haasen-Kelly effect is observed. The action of impurities is to anchor the jogs, greatly slowing the cross-slip, so impeding the rearrangement. Thus one finds a simple semi-quantitative explanation for the temperature and impurity dependence of the effect.

There is one further point worth mentioning: for edge dipoles in the shape of elongated isolated loops, there may be a bowing stress to overcome, as well as a passing stress. Bowing under stress forces the dislocations to be curved at the point of splitting, so it reduces the nominal splitting stress for an infinite The bowing stress is equal to the nominal straight dipole. passing stress if the dipole is about $8\pi(1-\nu) \approx 17$ times longer than Under these circumstances, it is easy to use the its height. calculations of Brown (2006) to estimate the reduction in passing stress: it is reduced by about 50%. However, the diagram of Fig. 2 is unchanged. All that happens is that the contribution of the passing (splitting) stress to the overall flow stress is reduced by a factor that depends upon the shape of the dipole loops. Such a factor will further reduce the size of the yield point.

The interpretation of the Haasen-Kelly effect proposed here is unlikely to be unique. However in the voluminous literature on work-hardening I can find no other attempt at an explanation more detailed than that given by Haasen and Kelly in their original paper. Their explanation, quoted in the abstract, is succinct and correct!

5. *Conclusions:* The assumption that a major component of dislocation sources in unidirectional deformation comprises edge dislocation dipoles leads to a simple semi-quantitative explanation of the Haasen-Kelly effect.

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Captions for Figures

Fig. 1 (adapted from Haasen and Kelly (1957)). The definition of the observed yield point, $\Delta \sigma$, is shown. The plastic strain interval is estimated from another diagram in their paper.

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