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Tim Softley, F. Merkt, Martin Schaefer, Urs Hollenstein. PFI-ZEKE photoelectron and high resolution photoionization spectra of ND3 with MQDT simulations. Molecular Physics, 2010, 108 (07-09), pp.1069-1082. 10.1080/00268971003649315 . hal-00596289

HAL Id: hal-00596289 https://hal.science/hal-00596289

Submitted on 27 May 2011

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Molecular Physics



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Journal:	Molecular Physics
Manuscript ID:	TMPH-2009-0378.R1
Manuscript Type:	Special Issue Paper - In honour of Prof Richard Zare
Date Submitted by the Author:	19-Jan-2010
Complete List of Authors:	Softley, Tim; University of Oxford Merkt, F.; ETH Zurich Schaefer, Martin; ETH Zürich, Laboratorium für Physikalische Chemie Hollenstein, Urs; ETH Zurich
Keywords:	ZEKE spectroscopy, Rydberg spectroscopy, Multichannel quantum defect theory
Note: The following files were to PDF. You must view these	e submitted by the author for peer review, but cannot be converted files (e.g. movies) online.

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PFI-ZEKE photoelectron and high resolution photoionization spectra of ND₃ with MQDT simulations

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Abstract

The rotationally resolved PFI-ZEKE (pulsed-field ionization zero-kinetic energy) photoelectron spectrum of ND₃ has been recorded at the $v_2^+ = 0$, 1 and 2 thresholds, by single-photon VUV excitation from the ground-state. An assignment of the $\tilde{X}^{+2}A_2'' \leftarrow \tilde{X}^{-1}A_1'$ spectrum is presented, allowing a determination of the adiabatic ionization potential of ND₃ (82261.7(15) cm^{-1}) and of the rotational constants and positions of the $v_2^+ = 0$, 1 and 2 vibrational levels of the ND₃⁺ ion. These parameters are used in a multichannel quantum defect theory (MQDT) simulation of the highresolution photoionization spectrum in the range $82100 - 83300 \text{ cm}^{-1}$ [(R. Seiler *et al.*, J. Chem. Phys. 118 10024 (2003)]. A good simulation and an assignment of around 80% of the lines of the ND₃ photoionization spectrum are achieved, verifying the validity of the molecular constants derived from the PFI-ZEKE photoelectron spectrum and also the quantum defect parameters derived from *ab initio* calculations.

(1) Introduction

 The ammonia molecule has been, for many years, a model polyatomic system for studies of photoionization dynamics and photoelectron spectroscopy. The photoionization from the ground state is characterized by a large geometry change from pyramidal to planar leading to the characteristic long progression in the out-ofplane (umbrella) bending mode in the photoelectron spectrum [1]. The photoelectron spectrum of NH₃ has been studied with rotational resolution using pulsed-field ionization zero-kinetic-energy (PFI-ZEKE) photoelectron spectroscopy, both with VUV excitation from the ground state [2 - 4], and using (2 + 1') resonance-enhanced excitation via the \tilde{B} state [5]. A mass-analyzed threshold ionization (MATI) spectrum was obtained via the \tilde{B} and \tilde{C} states [6,7]. There have also been numerous resonance-enhanced multiphoton ionization (REMPI) studies of the Rydberg states [8 - 14] including some double-resonant studies of higher Rydberg states, and very recently a rotationally resolved study of photoelectron angular distributions has been reported [15].

Very high resolution photoionization spectra of four isotopomers of ammonia NH_3 , NH_2D , NHD_2 and ND_3 , were reported by Seiler et al [2]. In comparison with previous studies of the photoionization and photoelectron spectra of NH_3 , these spectra, recorded using a VUV laser source of bandwidth 0.008 cm⁻¹, contain very detailed information on the interactions between the various Rydberg series, and between Rydberg series and continua (including dissociation continua). To assist in the interpretation of these spectra, an *ab-initio* R-matrix calculation of quantum defect parameters for ammonia has been carried out, including the calculation of the geometry dependence of the quantum defects in the v_2 -umbrella-bending coordinate, and these parameters have been used to perform multichannel quantum defect theory (MQDT) simulations of the high-resolution photoionization spectrum of NH_3 [16]. To

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further test the validity of these quantum defect parameters and the MQDT formalism used for calculating the spectra [6, 7, 16], it is desirable to extend the MQDT calculations to the other isotopomers, ND₃, NH₂D, and ND₂H, for which highresolution photoionization and photoelectron spectra were also reported in [2,17]. Isotopic substitution does not change the electronic structure and therefore the same quantum defect matrix should be suitable for the simulation of all isotopomers. However, isotopic substitution does change the ionization potential, the nuclear spin statistics, and the rotational constants and vibrational frequencies of the neutral species and the molecular ion. These differences will not only change the rovibrational limits of each Rydberg series, but also the interactions between the Rydberg series, having strong effects on the line positions, spectral intensities and autoionization linewidths.

In recent work we reported an assignment of the PFI-ZEKE photoelectron spectra of the $v_2^+ = 3$ bands of NH₂D and NDH₂ and were able to use the information on rovibrational thresholds derived from these spectra to identify several Rydberg series in the photoionization spectra [17]. The ND₃ photoionization spectrum reported in [2] has not been assigned to date, the main difficulty being the uncertainty in the ionization potential of ND₃; the best value reported previously was 82280 ± 40 cm⁻¹ [8]. The rotational constants for the ND₃⁺ ion are also known to much lower precision than those of NH₃⁺ [18], and therefore the identification of the rovibrational Rydberg series limits in the photoionization spectrum of ND₃ is challenging.

In the present paper we report new experimental PFI-ZEKE photoelectron spectra of ND_3 which allow an accurate determination of the ionization potential, as well as the spectroscopic parameters of the ion. The accurate energies of the various ionization thresholds for specific vibration-rotation levels of the ion could then be

used, together with *ab initio* quantum defect parameters, to simulate and assign the photoionization spectrum of ND₃ using MQDT.

(2) PFI-ZEKE photoelectron spectra of ND₃

(2.1) Experimental

The PFI-ZEKE photoelectron spectra of ND₃⁺ in the region of the $v_2^+ = 0$, $v_2^+ = 1$ and $v_2^+ = 2$ ionization thresholds were recorded using an experimental apparatus similar to that described in Ref. [19]. In brief, the spectra were recorded following single-photon VUV excitation from the lowest rotation-inversion levels of the ground neutral state in a skimmed pulsed molecular beam of ND₃ gas. Tunable VUV radiation in the wavenumber range $82000 - 85000 \text{ cm}^{-1}$ was produced by resonance-enhanced difference-frequency mixing $v_{VUV} = 2v_1 - v_2$ in a krypton gas jet using the $(4p)^{5/2}P_{1/2}$ 5p' [1/2] $(J=0) \leftarrow (4p)^{6-1}S_0$ two-photon resonance at $2\tilde{v}_1 = 98855.071$ cm⁻¹. The tunability of the VUV radiation was achieved by scanning the frequency v_2 . The fundamental frequencies v_1 and v_2 were generated from the output of two pulsed dye lasers (Lambda Physik, Scanmate 2e), the first one being frequency tripled. The resultant VUV radiation had a bandwidth of about 0.4 cm⁻¹. The ND₃ gas sample was diluted in a 1:4 mixture with argon and introduced into the spectrometer via a pulsed supersonic expansion. This expansion was crossed by the VUV radiation beam at right angles in the middle of a set of six cylindrical electrodes used to apply the pulsed electric fields.

PFI-ZEKE photoelectron spectra were recorded by monitoring the wavenumberdependent electron signal produced by delayed pulsed-field ionization of very high Rydberg states located below the successive ionization thresholds. A two-pulse electric field sequence was employed for field ionization in order to improve the

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spectral resolution. Table 1 lists the magnitudes of the pulses used for the three vibrational bands recorded; the differences of the fields employed reflect the very different intensities of the three observed bands. The first pulse served the purpose of eliminating prompt electrons and field ionizing the highest Rydberg states. It was immediately followed by a second pulse with opposite polarity which produced the electrons that were detected in the PFI-ZEKE photoelectron spectra. A resolution of $2 - 3 \text{ cm}^{-1}$ was achieved in the spectra which was sufficient to resolve the rotational structure of the photoelectron bands of ND₃. The field-induced shifts of the ionization potential arising from these pulses were calculated using the procedure described in Ref. [20] and are listed in Table 1. The VUV wavenumber was determined by calibrating the wavenumbers of the two dye lasers. This calibration was achieved by recording the laser-induced fluorescence spectrum of I₂ and optogalvanic spectra of Ar and Ne. The estimated accuracy of the ionization thresholds determined in this work is 1 cm⁻¹.

(2.2) Results

The experimental PFI-ZEKE photoelectron spectra obtained following single-photon excitation from the neutral vibronic ground state are shown in panel (a) of Figs. 1, 2 and 3. The Franck-Condon factor is highly unfavourable for the $v_2^+ = 0$ band relative to bands of higher v_2^+ , hence a spectrum of lower signal-to-noise ratio is obtained at that threshold. As is usual in PFI-ZEKE photoelectron spectroscopy, the wavenumbers of the observed peaks (when corrected for the field ionization shift – see above) correspond to the differences between the energies of the rovibrational ionization thresholds in question and the initial levels of the excitation, *i.e.*

$$hv = I_0 + G(V_2^+) + F(N^+, K^+) - F(J'', K''), \qquad (1)$$

where I_0 is the adiabatic ionization energy, $G(v_2^+)$ is the vibrational energy in the v_2 inversion (umbrella bending) mode of the ion (the only mode excited in these spectra) and the *F* terms are given by the rigid-rotor expression

$$F(N,K) = BN(N+1) + (C-B)K^{2}.$$
(2)

for the rotational energies of the ion $[(N, K) = (N^+, K^+)]$ and neutral ground state [(N, K) = (N'', K'')]. The values of F(N'', K'') for the $\tilde{X} {}^1A_1'$ ground state of ND₃ used in the simulations are taken from reference [21].

The general rovibronic selection rules for the photoionization (or for transitions to Rydberg states) of polyatomic molecules derived in Ref. [22] can be expressed as

$$\Gamma_{\rm rve}^+ \otimes \Gamma_{\rm rve}'' \otimes \Gamma_{\rm e} \supseteq \Gamma^*, \tag{3}$$

where Γ_{rve}^+ and Γ_{rve}'' represent the rovibronic symmetries of the cationic and neutral states in the molecular symmetry group $D_{3h}(M)$, Γ_e the symmetry of the photoelectron wave function, (i.e. A_1 ' and A_1 " for even- ℓ and odd- ℓ partial waves, respectively) and Γ^* the dipole moment representation (i.e. A_1 " in $D_{3h}(M)$). For ND₃ these rovibronic selection rules can be written as

$$\begin{array}{cccc}
A_1'' \leftrightarrow A_1' \\
A_2'' \leftrightarrow A_2' \\
E'' \leftrightarrow E'
\end{array}$$
(4)

for even- ℓ partial waves and

$$A_1'' \leftrightarrow A_1''$$

$$A_1' \leftrightarrow A_1'$$

$$A_2'' \leftrightarrow A_2''$$

$$A_2' \leftrightarrow A_2'$$

$$E'' \leftrightarrow E''$$

$$E' \leftrightarrow E'$$

(5)

for odd- ℓ partial waves.

A schematic diagram of the rotational energy levels of the $\tilde{X} {}^{1}A'_{1}$ vibronic ground state of ND₃ and of the first two out-of-plane bending levels (2⁰, 2¹; the notation implies $v_{2}^{v_{2}^{+}}$) of the $\tilde{X} {}^{2}A''_{2}$ ground state of ND₃⁺ is presented in Fig. 4. Because the

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out-of-plane bending mode of ND₃ is of a_2 " symmetry, out-of-plane bending levels with an even (odd) number of vibrational quanta transform as A_1 ' (A_2 ") and have the same rovibronic symmetry labels as the 2⁰ (2¹) levels. Distinct rovibronic selection rules and an overall different rotational structure are thus expected for transitions from the ground neutral state of ND₃ to out-of-plane bending levels of ND₃⁺ with even and odd numbers of vibrational quanta.

The general rovibronic photoionization selection rules in Eqs. (3) to (5) are rather unrestrictive and the full set of transitions predicted using them exceeds the number of transitions actually observed. To assist with the assignment of the spectra, simulations were carried out based on the orbital ionization model described in Ref. [23], which itself is an extension of the Buckingham, Orr and Sichel (BOS) diatomic photoionization model [24], to predict the strongest lines. The intensity distributions of the spectra displayed below the experimental spectra in panels (b) of Figs. 1, 2 and 3 were calculated using Equation (6) [23],

$$I(v^{+}, N^{+}, K^{+}, N'', K'') = \rho'' C \sum_{|\lambda^{*}| \le \ell^{*}} \frac{1}{2\ell'' + 1} Q(\ell'') |C_{\ell^{*}\lambda^{*}}|^{2} \Big[\ell'' |F_{\ell^{*}}^{E, \ell^{*} - 1}|^{2} + (\ell'' + 1) |F_{\ell^{*}}^{E, \ell^{*} + 1}|^{2} \Big].$$
(6)

In Equation (6), ρ'' and *C* represent the Boltzmann factor (including nuclear-spin statistical weight) and a proportionality constant, respectively, and ℓ'' represents the orbital angular momentum quantum number of the different terms of a single-centre expansion (with expansion coefficients $C_{\ell''\lambda'}$) of the molecular orbital ϕ'' out of which the photoelectron is ejected. $F_{\ell''}^{E,\ell}$ is a radial integral and

$$Q(\ell'') = (2N^{+} + 1) \begin{pmatrix} N^{+} & \ell'' & N'' \\ -K^{+} & \lambda'' & K'' \end{pmatrix},$$
(7)

where the term in parentheses represents a 3*j*-symbol (see Ref. [23] for more details).

To simulate the relative intensities of the various rotational lines of a given band, the product of the squared expansion coefficient $|C_{\ell^*\lambda^*}|^2$ and the term in square

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brackets in Eq. (6) were treated as a single parameter, the value of which was adjusted to best reproduce the observed intensities. If it is assumed that the molecular orbital out of which the photoelectron is ejected in the $\tilde{X} {}^{2}A_{2}'' \leftarrow \tilde{X} {}^{1}A_{1}'$ transition of ND₃ is a p_{2} orbital (i.e., $\ell'' = 1, \lambda'' = 0$) the sum in Eq. (6) reduces to a single term

$$I(v^{+}, N^{+}, K^{+}, N'', K'') = C''\chi'' \exp\left(-\frac{E''}{k_{B}T}\right)(2N^{+}+1)g'' \begin{pmatrix} N^{+} & 1 & N'' \\ -K^{+} & 0 & K'' \end{pmatrix}^{2}$$
(8)

where C'' is a constant, χ'' stands for the spin statistical factor and g'' is the degeneracy factor of the ground state rotational levels, i.e. 2N''+1 for K = 0 and 2(2N''+1) for $K \neq 0$ levels. The simulations presented in the panels (b) of Figs. 1, 2 and 3 were made using Eq. (8) assuming a rotational temperature of 15 K.

The pattern of peaks calculated using the orbital ionization model for $v_2^+ = 0$ (Fig. 1b) is roughly the same as for $v_2^+ = 2$ (Fig. 3b), because the vibronic symmetry is the same in both cases. The pattern is different for $v_2^+ = 1$ (Fig. 2b) however, because the a_2 " symmetry (D_{3h}) of the v_2 vibrational mode results in a different set of allowed rotational transitions. To assign the experimental spectra, the strong rotational features in the simulated vibrational bands are identified with the strong features in the experimental spectra. Lining up the simulated and experimental spectra allows an initial value for the sum $I_{v_2^+} = I_0 + G(v_2^+)$ to be estimated. Improved values of $I_{v_2^+}$ and of the rotational constants B^+ and C^+ of the ion can then be determined by a leastsquares fitting method to improve the fit. At the low temperature of the supersonic expansion only low rotational states are populated and centrifugal distortion effects are negligible.

Following a preliminary analysis as described above it was recognised that numerous transitions were observed which could not be identified using the orbital ionization model. The simulations shown in panel (c) of Figs. 1, 2 and 3 assume a relaxation of the orbital restrictions allowing transitions from orbital components of f

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character in addition to the *p* character. As discussed below, such relaxation does not necessarily reflect the underlying direct ionization cross sections, but was useful in assigning additional lines.

Tables 2, 3 and 4 give the assignments and observed line positions of the rotational features in each vibrational band. The wavenumbers of the observed bands lie slightly below the actual ionization thresholds by an amount given by the field-induced shifts listed in Table 1. The best-fit values of the adiabatic ionization energy, the vibrational intervals and the rotational constants of ND_3^+ are given in Table 5 and are compared to the best values from the literature, or to values extrapolated from the literature (e.g., from the work of Kraemer and Špirko [25] in which ab-initio calculations are combined with a fit to experimental data to calculate a potential energy surface for NH₃ and ND₃ from which spectroscopic constants can be derived). The experimental rotational constants and vibrational intervals fall within 0.1 cm⁻¹ and 3 cm⁻¹. respectively, of the literature values. The rotational constants for the $v_2^+ = 0$, 1 levels can also be compared to values obtained from high resolution REMPI spectra of the \tilde{C} ' 3p (n = 3) Rydberg state [26], also shown in Table 5. The good agreement between these values reflects the expected similar geometry between the Rydberg state and the ion. For the purpose of assigning the photoionization spectrum of ND₃, the most significant improvement in parameters derived from these measurements is in the experimental value of the adiabatic ionization potential $(82261.7 (7) \text{ cm}^{-1})$, which is now known with almost two orders of magnitude higher precision than the previous best value.

The $\Delta K = 0$ lines in Tables 2 to 4 originating from levels with K'' = 0 are of symmetry type $A'' \leftrightarrow A'$ and are uniquely associated with even- ℓ photoelectron partial

waves (see Eq. 4). The other lines are of type $E \leftrightarrow E$ and could in principle be described as associated with either even- ℓ or odd- ℓ partial waves because transitions involving near-degenerate E'' and E' levels are not resolved. [Note that although we refer to 'photoelectron partial waves' here, the actual excitation in a PFI-ZEKE photoelectron experiment is to a high Rydberg state with a given ℓ value rather than a true continuum]. As discussed previously [2,17], even- ℓ partial waves are likely to dominate the spectra and, in fact, all of the observed transitions can be explained by using even- ℓ partial waves alone. Four K'' = 0 transitions are unambiguously identified that can *only* be explained assuming even- ℓ photoelectron partial waves, and these include strong transitions in all three vibrational bands, most notably the 1_0 A_1 " $\leftarrow 0_0 A_1$ transition at 82270.4 cm⁻¹ in the $v_2^+ = 0$ band, the $0_0 A_1 \leftarrow 1_0 A_1$ " transition at 82936.4 cm⁻¹ in the $v_2^+ = 1$ band and the $1_0 A_1^- \leftarrow 0_0 A_1^-$ transition at 83665.7 cm⁻¹ in the $v_2^+ = 2$ band. This predominance of even- ℓ partial waves in the single-photon ionization of ND₃ substantiates our previous findings derived from the spectra of NH_3 [2], ND_2H and NH_2D [17]. In general the strongest features are identified as $\Delta K = K^+ - K^{"} = 0$.

The two $(v_2^+ = 1)$ or three $(v_2^+ = 0, 2)$ strongest features predicted by the orbital ionization model for each vibrational band are also observed as strong features in the experimental spectra (Figs. 1, 2 and 3) but with some differences in the relative intensities. As discussed above, several additional transitions are observed for which no intensity is predicted by the orbital ionization model, particularly in the $v_2^+ = 1$ and 2 bands. The spectra calculated using the relaxed selection rules shown in panel (c) of Figs. 1 to 3 contain nearly all of the observed features, but not always with the correct relative intensities. The inclusion of higher- ℓ'' components in the simulations (Eq. (6)) is therefore unlikely to represent the direct ionization cross-sections.

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One factor contributing to some of the intensity discrepancies may be the uncertainty about the relative populations of the neutral molecule rotational levels in the supersonic jet. For NH₂D and ND₂H it was previously found [17] that there was significant nuclear-spin-state inter-conversion in the supersonic expansion, attributable to an initial clustering near the jet orifice. The simulations shown in Figs. 1 - 3 assume a rotational temperature of 15 K; changing the temperature or the degree of nuclear-spin-state inter-conversion does not improve the fit especially for the weak features observed on the high wavenumber side of the $v_2^+ = 1$ and 2 bands.

The most likely explanation for the differences to the predictions of the orbital ionization model lies in the channel interactions between different Rydberg series. As has been well documented elsewhere [6, 7, 27, 28] the pseudo continuum of high-nRydberg states detected in PFI-ZEKE photoelectron experiments below a particular ionization threshold may interact with either bound Rydberg series converging to higher energy thresholds, or the continua associated with lower energy thresholds, and thereby borrow intensity from the stronger transitions to those interacting channels. Such channel interactions are not incorporated into the BOS orbital ionization model, but have been explained in our previous study of the (2 + 1') MATI spectra of NH₃ via the \tilde{B} and \tilde{C} states using multichannel quantum defect theory [6, 7]. Figures 1(d) to 3(d) show the photoionization spectra recorded in the same regions as the PFI-ZEKE photoelectron spectra by detecting ions produced by autoionization as a function of the laser wavenumber. These spectra indicate that the unexpectedly intense lines in the PFI-ZEKE photoelectron spectra always coincide with autoionization resonances in the photoionization spectrum. For example the strong $3_1 \leftarrow 2_1$ and $3_3 \leftarrow 0_0$ lines in the 0 - 0 band correspond to strong features in the photoionization spectrum near 82295 cm⁻¹; these photoionization resonances are tentatively assigned (see below) as transitions to $v_2^+ = 3$, n = 8 Rydberg states. The strong $4_2 \leftarrow 2_2$ feature in the $v_2^+ = 1$

band appears to coincide with a strong photoionization resonance near 83020 cm⁻¹ which is also believed to involve transitions to a group of $v_2^+ = 3$ autoionizing states, and the features at the high wavenumber end of the $v_2^+ = 2$ band of the photoelectron spectra may also be "borrowing" intensity from the overlapping autoionizing features. Such intensity borrowing, however, can only occur if the autoionizing features share a common ground state with the perturbed line of the PFI-ZEKE spectrum.

(3) MQDT simulation of the photoionization spectrum of ND₃

The spectroscopic constants derived from the rotationally resolved PFI-ZEKE photoelectron spectra of ND₃ were used to carry out a simulation of the photoionization spectrum using Multichannel Quantum Defect Theory (MQDT). The methodology employed is described in more detail elsewhere [16] and follows closely the theory described in references [6, 7, 29, 30]. In this scattering-theory approach the long-range 'channels' define the set of possible quantum states of the system when the electron is at long range from the ion core. The electron may either be a free electron with given angular momentum ℓ dissociating from a quantum-state specified ion core N^+ , K^+ , v^+ (an 'open' channel), or a Rydberg electron of specified ℓ bound to an ion core N^+ , K^+ , v^+ (a 'closed' channel). In both cases the total angular momentum quantum number excluding spin, N, is also specified. For closed and open channels the total energy lies respectively below or above the threshold for the particular N^+ , K^+ , v^+ ion core state. [To simplify notation below, v_2^+ is replaced by v^+ , as channels with non-zero values of the other vibrational quantum numbers are omitted, and thus the v_2 mode is assumed to be the only active one.]

The total photoionization cross section at a given energy is equal to the sum of partial photoionization cross sections into the set of N_0 open channels, summed over all populated initial levels. The photoionization spectrum is calculated by evaluating the total cross section as a function of energy on a fine energy grid (0.01 cm⁻¹ in the present case). The partial photoionization cross section at energy *E* for excitation from an initial rotational level *J*", *K*" into the open channel $N^+ K^+ v^+ \ell N$ (represented by the label *i*) is given by

$$\sigma_{J'K'' \to i}(E) = \frac{4\pi^2 \zeta \omega}{3(2J''+1)} \sum_{N} \left| D_i^{(N)}(E) \right|^2,$$
(9)

where $D_i^{(N)}(E)$ is the reduced transition dipole moment between the initial state and the final channel $|i\rangle$, ζ is the fine structure constant, and ω is the photon energy (atomic units). The energy-dependent reduced transition dipole moments are related to the transition dipole moments in the rovibronic eigenchannel representation, $D_{\alpha}^{(N)}$, using the expression,

$$D_i^{(N)} = \sum_{\rho} e^{i\eta_i} T_{i\rho} e^{i\pi\tau_{\rho}} \sum_{\alpha} D_{\alpha}^{(N)} A_{\alpha\rho} .$$
⁽¹⁰⁾

In this equation, ρ labels one of the N₀ independent solutions of the Schrödinger equation at this energy E, and α labels the eigenchannels defined in the expansion

$$\Psi_{\rho} = \sum_{\alpha} A_{\alpha\rho}(E) \Psi_{\alpha}(E).$$
(11)

The eigenchannel wavefunction Ψ_{α} is given by

$$\Psi_{\alpha} = \sum_{i} U_{i\alpha} \left[f_{i} - g_{i} \tan(\pi \mu_{\alpha}) \right] |i\rangle , \qquad (12)$$

where f_i and g_i are regular and irregular radial Coulomb functions, and $|i\rangle$ is the ion core and electronic angular momentum parts of the wavefunctions which characterize each channel *i*. μ_{α} is the eigenchannel quantum defect and $U_{i\alpha}$ is the transformation matrix between the long-range basis and the eigenchannel basis.

A further frame transformation relates the transition moments in equation (10) to a set of transition moments $\langle NK\ell\lambda|d|J''K''\lambda''\rangle$ defined in a close-coupled channel (or short-range) basis equivalent to a Hund's case (b) representation

$$D_{\alpha}^{(N)} = \sum_{i} \left(U_{\alpha i}^{T} \right)^{(N)} \sum_{\ell \lambda} \left\langle N^{+} K^{+} \left| K \lambda \right\rangle^{(lN)} \left[\int \mathrm{d}Q \left\langle \mathbf{v}^{+} \left| Q \right\rangle^{(N^{+}K^{+})} \left\langle N K \ell \lambda \left| d \right| J^{''} K^{''} \lambda^{''} \right\rangle \left\langle Q \left| \mathbf{v}^{''} \right\rangle^{(N^{*}K^{*})} \right] \right]$$
(13)

 $\langle v^+ | Q \rangle^{N^+K^+}$ and $\langle Q | v'' \rangle^{N'K''}$ are vibrational wavefunctions and the factors in square brackets in Eq. (13), including the vibrational overlap integral, are treated as variable input parameters in the present calculations.

To determine the transformation matrix $U_{i\alpha}$ in Eqs. (12) and (13) the rovibronic quantum defect matrix in the long-range basis $\mu_{ii'}$ is constructed by relating it to a set of input quantum defects defined in the close-coupled Hund's case (b) basis,

$$\mu_{ii'} \equiv \mu_{\mathbf{v}^{*}N^{*}K^{*}\ell;\mathbf{v}^{+'}N^{+'}K^{+'}\ell'}^{(N)} = \sum_{K\lambda} \sum_{K'\lambda'} \left\langle N^{*}K^{+} \middle| K\lambda \right\rangle^{(\ell N)} \left[\int dQ \left\langle \mathbf{v}^{+} \middle| Q \right\rangle \mu_{\ell\lambda,\ell'\lambda'}(Q) \left\langle Q \middle| \mathbf{v}^{+'} \right\rangle \right] \left\langle \lambda^{*}K^{*} \middle| N^{+'}K^{+'} \right\rangle^{(\ell'N)},$$

$$(14)$$

where the $\mu_{\ell\lambda,\ell'\lambda'}$ matrix elements are treated as input parameters, determined in this work principally by *ab-initio* calculation [16]. The quantum defect matrix $\mu_{ii'}$ is then diagonalized, as in ref [29], to determine the $U_{i\alpha}$ elements as the eigenvectors and the eigenchannel quantum defects μ_{α} as the eigenvalues.

The T matrix in Eq. (10) is given by

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$$T_{i\rho}(E) = \sum_{\alpha} U_{i\alpha}^{(N)} \cos[\pi(-\tau_{\rho} + \mu_{\alpha}^{(N)})]A_{\alpha\rho}$$

and the coefficients $A_{\alpha\rho}$ and scattering phases τ_{ρ} are determined from the generalized eigenvalue equation [29]:

$$\Gamma \mathbf{A} = \tan(\pi\tau) \mathbf{A}$$

$$\Gamma_{i\alpha} = U_{i\alpha}^{(N)} \sin[\pi(\nu_i + \mu_{\alpha}^{(N)})] \quad \text{for } i \text{ closed}$$

$$\Gamma_{i\alpha} = U_{i\alpha}^{(N)} \sin(\pi\mu_{\alpha}^{(N)}) \quad \text{for } i \text{ open}$$

$$\Lambda_{i\alpha} = 0 \quad \text{for } i \text{ closed}$$

$$\Lambda_{i\alpha} = U_{i\alpha}^{(N)} \cos(\pi\mu_{\alpha}^{(N)}) \quad \text{for } i \text{ open}$$
(16)

 v_i is the effective principal quantum number in channel *i* at the total energy *E*.

The expression in the square brackets in Eq. (14) determines the coupling between channels associated with different vibrational thresholds of the ND₃⁺ ion, and is thus responsible for vibrational autoionization. The coupling between channels with different v^+ quantum numbers is assumed, for the purposes of these calculations, to be negligible for $\Delta v^+ > 1$. For the $\Delta v^+ = 1$ matrix elements, rather than integrating over the vibrational wavefunction, we use the following harmonic approximation to the matrix elements [31] (which effectively ignores the very small dependence of the vibrational wavefunctions on the rotational quantum numbers N^+ and K^+);

$$\mu_{\ell\lambda\nu\ell'\lambda'\nu'} = \int \mathrm{d}Q \langle \mathbf{v}^+ \left| Q \right\rangle^{(N^+K^+)} \mu_{\ell\lambda\ell'\lambda'}(Q) \langle Q \left| \mathbf{v}^+ \right\rangle^{(N^+K^+)} = \left(\frac{\mathrm{d}\mu_{\ell\lambda\ell'\lambda'}}{\mathrm{d}Q}\right)_e \left[\frac{h}{8\pi^2 c\omega}\right]^{\frac{1}{2}} (\mathbf{v}^+)^{\frac{1}{2}}$$
(17)

(15)

 where v^+ is the vibrational quantum number of the closed channel undergoing autoionization, and ω is the vibrational frequency. There is also a symmetry selection rule applying to these off-diagonal matrix elements which restricts the number of $\ell\lambda$ - $\ell'\lambda'$ pairs for which the derivative in Eq. (17) needs to be evaluated [16]. Note that this rule is applied in D_{3h} symmetry in which, for example, p π and d δ correlate to the same representation. Hence the non-zero elements include both pairs with opposite parity (e.g., p π - d π) as well as one pair with the same parity (d π - d δ).

Equation (17) ignores all vibrational modes other than the out-of-plane bend and is a purely harmonic approximation. Evaluation of (17) requires knowledge of how the short-range electronic quantum-defect matrix elements $\mu_{\ell\lambda\ell'\lambda'}$ vary with the v_2^+ normal vibrational coordinate at the equilibrium geometry. The variation is determined in this work by *ab-initio* calculation as described elsewhere [16]. For the matrix elements *diagonal* in the v^+ quantum number, we set the integral over the vibrational coordinate equal to the value at the planar equilibrium geometry, assuming only a small variation of the quantum defects over the range of geometries over which the vibrational wavefunctions of the low vibrational levels extend.

The diagonal quantum defects employed in the MQDT calculation $\mu_{\ell\lambda\ell\lambda}$ have been slightly adjusted from the *ab-initio* values to give a better fit to the photoionization spectrum of NH₃ [16] and are listed together with the off-diagonal elements and the off-diagonal vibrational integrals (from Eq (17)) in Table 6. The best match to the experimental intensities is obtained by setting all the transition dipole moment parameters in Eq. (13) to zero, except for those involving $\ell = 0$. Note however that because there is substantial $\ell = 0 - \ell = 2$ mixing in this system the Rydberg states

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populated have a mixture of *ns* and *n*d character. The rotational temperature in the supersonic expansion for the experiments of Ref [2] was estimated to be 5 - 10 K, and therefore the spectrum is calculated as a sum of partial photoionization cross sections out of the 6 lowest energy levels of ND₃ which are the only ones significantly populated. The channels included in the calculation were those with $v^+ = 0$ to 3 and $\ell = 0$ to 2. The partial photoionization cross section calculation (Eq. (9)) is carried out for a specific total angular momentum *N*, and this, together with symmetry considerations [7], restricts the number of rotational quantum numbers N^+K^+ that need to be included.

Fig. 5 compares the MQDT simulation obtained with an overview of the experimental photoionization spectrum from reference [2]. The simulation has been colour coded according to the initial rotational level from which the transitions originate. The strong features observed at either end of the experimental spectrum are well reproduced in the simulated spectrum and much of the structure observed in the central region of the spectrum is also reproduced. Figs. 6 and 7 give expanded views of two regions of the spectrum. The degree of qualitative match between simulation and experiment is extremely sensitive to the diagonal elements of the quantum defect matrix used as input and to the positions of the ro-vibrational ionic thresholds. Most of the features in the calculated spectrum are identified as autoionizing levels belonging to series converging on the $v_2^+ = 1$ state of the ion, but a number of transitions belonging to higher vibrational levels ($v_2^+ = 2$ and 3) have also been identified as shown in Fig. 5, including the n = 10, $v_2^+ = 2$, $3_0 A_1^- \leftarrow 0_0 A_1^-$ transition, three transitions (n = 9, 11, 13) of the $v_2^+ = 2, 1_0 A_1^- \leftarrow 0_0 A_1^-$ series and the intense n = 9, v_2^+ = 3, $1_1 E'' \leftarrow 1_1 E'$ transition at the high-wavenumber end of the spectrum. These vibrational assignments were made by allowing the transition moments to one

particular vibrational channel (selected in turn) to be non-zero, while setting all transition moments to other vibrational channels to zero.

Overall the assignment and detailed identification of Rydberg series in the v_2^+ = 1 region of the ND₃ high-resolution photoionization spectrum is less straightforward than for the NH₃ spectrum [2]. The region near the $v_2^+ = 0$ threshold, where series were readily identified in the photoionization spectrum of NH₃, is quite weak for ND₃, and at higher wavenumber there are no obvious series appearing in between the v_2^+ = 0 and $v_2^+ = 1$ thresholds (whereas for NH₃ the $1_0 A_2' \leftarrow 0_0 A_2''$ series dominates this region of the spectrum). Nevertheless, it is possible to make use of the likely correlation between the transitions that are strong in the PFI-ZEKE photoelectron spectra of ND_3 and those series that have high intensity in the photoionization spectra. As illustration, Figure 8 displays one long progression that can be assigned as a series converging to the $v_2^+ = 1$, $1_1 E' \leftarrow 2_1 E''$ rovibronic threshold which corresponds to a strong transition in the $v_2^+ = 1$ PFI-ZEKE photoelectron spectrum at 82967 cm⁻¹. The $1_1 E'' \leftarrow 1_1 E'$ transition also appears with high intensity in the $v_2^+ = 1$ band of the PFI-ZEKE photoelectron spectrum at 82946 cm^{-1} and a series converging to this threshold can be identified in the photoionization spectrum of ND₃ from n = 17 - 23, and is well reproduced in the MQDT simulation shown in Fig. 7.

The series and fractions of series identified, assigned and simulated in the high-resolution photoionization spectrum of ND₃ are summarised in Table 7. The central region of the spectrum between 82450 cm^{-1} and 82850 cm^{-1} is chosen for illustration and shown with series assignments in Fig. 8. A large percentage of the strong spectral features can be assigned by the MQDT simulation, which is a powerful tool in the interpretation of such complex photoionization spectra.

4. Conclusions

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The work described in this paper, when coupled with our previous work in references [2, 6, 7, 16, 17], provides information on the several ro-vibrational ionization thresholds of four isotopomers of ammonia. The band origins for the observed transitions are collected in Table 8. Rotational constants and vibrational intervals for the ND₃⁺ ion have also been derived from experiment for the first time. The underlying motivation for this work was to extend the assignment of the high-resolution photoionization spectrum, and MQDT calculations carried out on NH₃ to the photoionization spectrum of ND₃. The good agreement using the same set of electronic parameters for both isotopomers, despite the very different rotational and vibrational constants, nuclear spin statistical weights and vibronic dynamics indicates the reliability of these parameters. Whereas the agreement between the measured and calculated line positions is good, the intensities are not described so well by the calculations. We attribute the discrepancies to the fact that predissociation has not been included in the calculations, even though it is known that many Rydberg states of ammonia are predissociative.

The ammonia molecule is a model system with which to study photoionization in polyatomic molecules and reveals many fascinating features; the studies presented in this work and references [2,16,17] have substantially extended the understanding of the highly excited states of ammonia, while still leaving room for detailed considerations of the predissociation of these states in the future, and of the competition with autoionization.

Acknowledgements

We are grateful for financial support of this work to the Swiss National Science Foundation (project No 200020-125030), to the Petroleum Research Fund of the American Chemical Society, and to the Engineering and Physical Sciences Research Council.

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Table and Figure Captions

Figure 1 (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^+ {}^2A_2''$ ($v_2^+=0$) $\leftarrow \tilde{X} {}^1A_1'$ transition of ND₃. The lines are assigned using the notation $N^+{}_{K^+} \leftarrow N_{K''}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d) Experimental photoionization spectrum of ND₃.

Figure 2 (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^{+2}A_{2}''$ ($v_{2}^{+}=1$) $\leftarrow \tilde{X}^{-1}A_{1}'$ transition of ND₃. The lines are assigned using the notation $N^{+}{}_{K^{+}} \leftarrow N_{K'}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d) Experimental photoionization spectrum of ND₃.

Figure 3: (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^{+2}A_2''(v_2^+=2) \leftarrow \tilde{X}^{-1}A_1'$ transition of ND₃. The lines are assigned using the notation $N^+_{K^+} \leftarrow N_{K''}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization

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model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d) Experimental photoionization spectrum of ND₃.

Figure 4: Energy level diagram showing schematically the rotational levels of the lowest vibrational level of the \tilde{X} (${}^{1}A_{1}$) ground state of ND₃ (bottom panel) and of outof-plane bending levels of the \tilde{X}^{+} (${}^{2}A_{2}^{-}$ ") ground state of ND₃⁺, with even values of v_{2}^{+} (top left panel) and odd values of v_{2}^{+} (top right panel). The rovibronic symmetry labels of all levels in the $D_{3h}(M)$ molecular symmetry group is indicated next to the levels.

Figure 5: Comparison of the photoionization spectrum of ND₃ (bottom trace, from Ref. [2]) and the MQDT simulation (top trace) calculated using quantum defects from reference [16]: the separate contributions from each initial rotational state are colour coded.

Figure 6: Expanded view of the MQDT simulation (top trace) of the ND₃ photoionization spectrum (bottom trace, ref [2]). The simulated spectrum was computed using quantum defects from reference [16]: the $v_2^+ = 1$ region is dominated by a series of transitions originating from the $1_1 E'$ ground state level converging to the $v^+ = 1$, $1_1 E' \leftarrow 2_1 E''$ rovibronic threshold.

Figure 7: Expanded view of the MQDT simulation (top trace) of the ND₃ photoionization spectrum (bottom trace, ref [2]). The simulated spectrum was computed using quantum defects from reference [16]: $v_2^+ = 1$ region showing a part of the Rydberg series converging to the $1_1 E' \leftarrow 1_1 E''$ rovibronic threshold.

Figure 8: Example of series assignments based on the MQDT calculations in a selected region of the high resolution photoionization spectrum of ND₃ (reported in Ref [2].)

Table 1: Two-pulse sequences used to record the PFI-ZEKE photoelectron spectra of ND₃. The shifts of the ionization thresholds were estimated as described in reference [20].

Table 2: Assignment of rotational lines (in the notation $N^+_{K^+} \leftarrow N''_{K^*}$) of the $v_2^+ = 0$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.7 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{calc} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

Table 3: Assignment of rotational lines (in the notation $N^+\kappa^+ \leftarrow N''_{\kappa'}$) of the $v_2^+ = 1$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.5 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{calc} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

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Table 4: Assignment of rotational lines (in the notation $N^+{}_{K^+} \leftarrow N''_{K^*}$) of the $v_2^+ = 2$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.45 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{cale} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

Table 5: Spectroscopic parameters of ND₃/ND₃⁺. Parameters labelled 'Expt' are from the present work, while those labelled 'REMPI' are from the 2 + 1 REMPI studies of the \tilde{C}' state of ND₃ [26]. Other values are determined as follows: ^(a) Theoretically determined from an adjusted *ab-initio* potential surface [25]. ^(b) Infrared spectrum of ND₃⁺ recorded in solid neon [31]. ^(c) Calculated using the equation $C_{0(ND_3)} \approx \frac{1}{2}C_{0(NH_3)}$. ^(d) Calculated using the $C_2 - C_1$ and $C_1 - C_0$ values in reference [25]. (e) Experimental measurement from REMPI studies in ref [8].

Table 6: Diagonal and off-diagonal elements of the quantum defect matrix used in the MQDT simulations (from ref [16]). The final row lists the vibrationally integrated off-diagonal elements as given in Eq (17).

Table 7 Summary of series or parts of series identified in the high-resolution photoionization spectrum of ND₃.

Table 8 Ionization energies (band origins for transitions to specific vibrational thresholds) derived from the present work and references [2,16,17] for NH₃, NH₂D, NHD₂ and ND₃.

~,^↑ Ţ 1~ (a) electron signal (arb. units) (b) \downarrow T Ę (c) ion signal (arb. units) (d) wave number / cm⁻¹

 Figure 1: (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^+ {}^2A_2'' (v_2^+=0) \leftarrow \tilde{X}^+A_1'$ transition of ND₃. The lines are assigned using the notation $N^+{}_{K^+} \leftarrow N_{K'}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d) Experimental photoionization spectrum of ND₃.



Figure 2 (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^+ {}^2A_2'' (v_2^+=1) \leftarrow \tilde{X} {}^1A_1'$ transition of ND₃. The lines are assigned using the notation $N^+{}_{K^+} \leftarrow N_{K'}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization

model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d)

Experimental photoionization spectrum of ND₃.

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Figure 3: (a) PFI-ZEKE photoelectron spectrum of the $\tilde{X}^+ {}^2A_2''$ ($v_2^+ = 2$) $\leftarrow \tilde{X}^- {}^1A_1'$ transition of ND₃. The lines are assigned using the notation $N^+{}_{K^+} \leftarrow N_{K''}''$ (b) Simulation of the PFI-ZEKE photoelectron spectrum using the orbital ionization model (Eq. 8). (c) Simulation based on a less restrictive photoionization model. (d) Experimental photoionization spectrum of ND₃.



Figure 4: Energy level diagram showing schematically the rotational levels of the lowest vibrational level of the \tilde{X} (${}^{1}A_{1}$) ground state of ND₃ (bottom panel) and of outof-plane bending levels of the \tilde{X}^{+} (${}^{2}A_{2}^{-}$ ") ground state of ND₃⁺, with even values of v_{2}^{+} (top left panel) and odd values of v_{2}^{+} (top right panel). The rovibronic symmetry labels of all levels in the $D_{3h}(M)$ molecular symmetry group is indicated next to the levels.



Figure 5: Comparison of the photoionization spectrum of ND₃ (bottom trace, from Ref. [2]) and the MQDT simulation (top trace) calculated using quantum defects from reference [16]: the separate contributions from each initial rotational state are colour coded.





Figure 6: Expanded view of the MQDT simulation (top trace) of the ND₃ photoionization spectrum (bottom trace, ref [2]). The simulated spectrum was computed using quantum defects from reference [16]: the $v_2^+ = 1$ region is dominated by a series of transitions originating from the $1_1 E'$ ground state level converging to the $v^+ = 1$, $1_1 E' \leftarrow 2_1 E''$ rovibronic threshold.



Figure 7: Expanded view of the MQDT simulation (top trace) of the ND₃

photoionization spectrum (bottom trace, ref [2]). The simulated spectrum was computed using quantum defects from reference [16]: $v_2^+ = 1$ region showing a part of the Rydberg series converging to the $1_1 E' \leftarrow 1_1 E''$ rovibronic threshold.



Figure 8: Example of series assignments based on the MQDT calculations in a selected region of the high resolution photoionization spectrum of ND₃ (reported in Ref [2].)

Band	2_0^0	2_0^1	2_0^2
Discrimination pulsed field / Vcm ⁻¹	+0.133	+0.133	+0.066
Extraction pulsed field/ Vcm ⁻¹	-0.266	+0.133	-0.266
Induced shift of ionization threshold /cm ⁻¹	-1.7	-1.5	-1.45

Table 1: Two-pulse sequences used to record the PFI-ZEKE photoelectron spectra of

ND₃. The shifts of the ionization thresholds were estimated as described in reference

[20].

$\widetilde{v}_{\mathrm{exp}}/\mathrm{cm}^{-1}$	$\widetilde{v}_{\rm exp} - \widetilde{v}_{\rm calc} / {\rm cm}^{-1}$	Assignment
		$N^{+}{}_{K^{+}} \leftarrow N''_{K''}$
82227.7	-0.05	$2_2 \leftarrow 3_2$
82229.7	0.10	$2_1 \leftarrow 3_1$
82239.0	-0.10	$1_1 \leftarrow 2_1$
82259.6	-0.05	$1_1 \leftarrow 1_1$
82270.4	-0.15	$1_0 \leftarrow 0_0$
82281.0	-0.05	$2_1 \leftarrow 1_1$
82290.5	-0.1	$3_2 \leftarrow 2_2$
82292.8	0.15	$3_1 \leftarrow 2_1$
82298.5	-0.1	$3_1 \leftarrow 2_2$
82300.0	-0.1	$3_3 \leftarrow 0_0$
82313.1	-0.05	$3_1 \leftarrow 1_1$

Table 2: Assignment of rotational lines (in the notation $N^+_{K^+} \leftarrow N''_{K'}$) of the $v_2^+ = 0$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.7 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{calc} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

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$\widetilde{V}_{\rm exp}$ / cm ⁻¹	$\widetilde{v}_{\rm exp} - \widetilde{v}_{\rm calc} / {\rm cm}^{-1}$	Assignment	
		$N^{+}{}_{K^{+}} \leftarrow N''_{K''}$	
82915.8	0.05	$2_1 \leftarrow 3_1$	
82921.8	0.05	$2_1 \leftarrow 3_2$	
82925.6	-0.1	$1_1 \leftarrow 2_1$	
82936.4	-0.1	$0_0 \leftarrow 1_0$	
82939.1	-0.15	$2_2 \leftarrow 2_1$	
82946.2	-0.05	$1_1 \leftarrow 1_1$	
82952.7	0.05	$2_1 \leftarrow 2_2$	
82967.2	0.1	$2_1 \leftarrow 1_1$	
82970.4	-0.05	$3_2 \leftarrow 2_1$	
82976.2	-0.2	$3_2 \leftarrow 2_2$	
82978.0	0.05	$3_1 \leftarrow 2_1$	
82984.1	0.05	$3_1 \leftarrow 2_2$	
82991.1	-0.1	$3_2 \leftarrow 1_1$	
82994.8	-0.2	$4_1 \leftarrow 3_2$	
82998.6	0.05	$3_1 \leftarrow 1_1$	
83009.1	-0.2	$3_0 \leftarrow 0_0$	
83012.1	-0.1	$4_2 \leftarrow 2_1$	
83018.4	0.1	$4_2 \leftarrow 2_2$	
83019.6	-0.2	$4_1 \leftarrow 2_1$	
83025.7	-0.1	$4_1 \leftarrow 2_2$	7

Table 3: Assignment of rotational lines (in the notation $N^+{}_{\kappa^+} \leftarrow N''_{\kappa^*}$) of the $v_2^+ = 1$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.5 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{cale} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

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$\widetilde{v}_{\mathrm{exp}}$ / cm ⁻¹	$\widetilde{v}_{\mathrm{exp}} - \widetilde{v}_{\mathrm{calc}} / \mathrm{cm}^{-1}$	Assignment
		$N^{+}{}_{K^{+}} \leftarrow N''_{K''}$
83609.7	0.05	$1_1 \leftarrow 3_2$
83622.9	-0.05	$2_2 \leftarrow 3_2$
83624.0	0.1	$2_1 \leftarrow 3_1$
83 634.2 🧹	-0.1	$1_1 \leftarrow 2_1$
83640.3	-0.15	$1_1 \leftarrow 2_2$
83647.8	0.1	$2_2 \leftarrow 2_1$
83651.6	-0.1	$3_3 \leftarrow 3_3$
83653.9	0.15	$2_2 \leftarrow 2_2$
83655.1	0.1	$1_1 \leftarrow 1_1$
83660.9	0.1	$2_1 \leftarrow 2_2$
83665.7	0.1	$1_0 \leftarrow 0_0$
83668.4	0.1	$2_2 \leftarrow 1_1$
83675.4	0.1	$2_1 \leftarrow 1_1$
83685.0	0.1	$3_1 \leftarrow 2_1$
83698.8	0.05	$3_2 \leftarrow 1_1$
83705.8	0.1	$3_1 \leftarrow 1_1$
83710.5	0.05	$5_4 \leftarrow 3_1$
83721.1	0.1	$5_5 \leftarrow 2_2$
83725.0	0.15	$4_2 \leftarrow 2_2$
83731.6	-0.15	$4_1 \leftarrow 2_2$

Table 4: Assignment of rotational lines (in the notation $N^+{}_{K^+} \leftarrow N''_{K'}$) of the $v_2^+ = 2$ band of the PFI-ZEKE photoelectron spectrum of ND₃. The reported line positions in the first column have not been corrected for the shift due to the pulsed field ionization. The field-free thresholds can be obtained by adding 1.45 cm⁻¹ to each of the numbers in column 1 (using the data presented in Table 1.) The calculated wavenumbers \tilde{v}_{cale} are obtained from Eqs. (1) and (2) using the best fit rotational constants, vibrational intervals and the ionization energy given in Table 5.

Parameter	$v_2^+ = 0$	$v_2^+ = 1$	$v_2^+ = 2$
Vibrational term value (cm ⁻¹) Expt	0	686.5(20)	1395.2 (20)
Literatu	ire 0	686 ^(a)	1393 ^(a)
		683.3 ^(b)	
Rotational constant B^+ (cm ⁻¹) Expt	5.350 (20)	5.230 (20)	5.070(20)
Literatu	1 Ire 5.347 ^(a)	5.214 ^(a)	5.078 ^(a)
REMP	I 5.361 (1)	5.232 (1)	
Rotational constant C^+ (cm ⁻¹) Expt	2.675 (50)	2.700 (50)	2.730 (50)
Literatu	1 $2.6238^{(c)}$	2.6538 ^(d)	2.6828 ^(d)
REMI	PI 2.626 (1)	2.646 (1)	
Adiabatic ionization Expt	82261.7 (15)	82948.2(15)	83656.9(15)
energy ($hc.cm^{-1}$) Literatu	re $82280 (40)^{(e)}$		

Table 5: Spectroscopic parameters of ND₃/ND₃⁺. Parameters labelled 'Expt' are from the present work, while those labelled 'REMPI' are from the 2 + 1 REMPI studies of the \tilde{C}' state of ND₃ [26]. Other values are determined as follows: ^(a) Theoretically determined from an adjusted *ab-initio* potential surface [25]. ^(b) Infrared spectrum of ND₃⁺ recorded in solid neon [31]. ^(c) Calculated using the equation $C_{0(ND_3)} \approx \frac{1}{2}C_{0(NH_3)}$. ^(d) Calculated using the $C_2 - C_1$ and $C_1 - C_0$ values in reference [25]. (e) Experimental measurement from REMPI studies in ref [8].

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lλ	sσ	рσ	рπ	dσ	dπ	dδ
$\mu_{\ell\lambda}$	0.966	0.366	0.577	-0.084	-0.103	0.133
<i>ℓ</i> λ - ℓ'λ'	sσ - dσ	pπ - dδ	sσ - pσ	pσ - dσ	pπ - dπ	$d\pi - d\delta$
μελείλ	0.095	- 0.075				
$\mu_{\ell\lambda\nu\ell'\lambda'\nu+1}$			-0.020	0.024	-0.018	0.015

Table 6: Diagonal and off-diagonal quantum elements of the electronic quantum defect matrix used in the MQDT simulations (from ref [16]). The final row lists the vibrationally integrated off-diagonal elements as given in Eq (17).

URL: http://mc.manuscriptcentral.com/tandf/tmph

	Molecule			Ion		
	Molecule	- C		Ion		
<i>J</i> ''	Molecule	Symmetry	V2 ⁺	Ion N ⁺	K^+	Symme
J " 1	Molecule K'' 1	Symmetry E'	v ₂ ⁺ 1	Ion N^+ 1	K^+	Symme E''
J" 1 1	Molecule K'' 1 1	Symmetry E' E'	V2 ⁺ 1 1	Ion N ⁺ 1 2	K^+ 1 1	Symme E'' E''
J" 1 1 0	Molecule K" 1 1 0	Symmetry E' E' A ₂ "	v ₂ + 1 1 1	Ion N ⁺ 1 2 1	$\begin{array}{c} K^+ \\ 1 \\ 1 \\ 0 \\ \end{array}$	Symme <i>E</i> '' <i>E</i> '' <i>A</i> ₂ '
J" 1 1 0 0	Molecule 	Symmetry E' E' A_2 " A_1 '	v_2^+ 1 1 2	Ion N ⁺ 1 2 1 1	K^+ 1 1 0 0 0	Symme <i>E</i> '' <i>E</i> '' <i>A</i> ₂ ' <i>A</i> ₁ ''
J" 1 1 0 0	Molecule K" 1 1 0 0	Symmetry E' E' A2" A1'	v ₂ ⁺ 1 1 1 2	Ion N ⁺ 1 2 1 1 1	K ⁺ 1 0 0	Symme E" E" A2' A1"
J" 1 1 0 0 0	Molecule K" 1 1 0 0 0 0 0 0	Symmetry E' E' A_2 " A_1 ' A_1 '	v2 ⁺ 1 1 1 2 2	Ion N ⁺ 1 2 1 3	K^+ 1 1 0 0 0 0	Symme E" E" A2' A1"

Table 7 Summary of series or parts of series identified in the high-resolution

photoionization spectrum of ND₃.

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$\begin{array}{r} 36\\ 37\\ 39\\ 40\\ 42\\ 43\\ 45\\ 46\\ 47\\ 49\\ 50\\ 51\\ 52\\ 53\\ 55\\ 56\\ \end{array}$	
$\begin{array}{r} 36\\ 37\\ 39\\ 40\\ 42\\ 43\\ 45\\ 47\\ 49\\ 50\\ 52\\ 53\\ 55\\ 56\\ 57\\ \end{array}$	
$\begin{array}{r} 36\\ 37\\ 39\\ 40\\ 42\\ 43\\ 44\\ 45\\ 46\\ 47\\ 49\\ 51\\ 52\\ 53\\ 55\\ 56\\ 57\\ 58\end{array}$	

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IsotopomerIonizationIonizationIonizationIonizationEnergy/cm ⁻¹ Energy/cm ⁻¹ Energy/cm ⁻¹ Energy/cm ⁻¹ $(v_2^+ = 0)$ $(v_2^+ = 1)$ $(v_2^+ = 2)$ $(v_2^+ = 3)$ NH_382158.751(16) $v_2^- = 1$ $v_2^- = 1$ NH_2D83027(3)83790 (5)84792.9 (6)ND_2H82261.7(15)82948.2(15)83656.9 (15)							
Energy/cm ⁻¹ Energy/cm ⁻¹ Energy/cm ⁻¹ Energy/cm ⁻¹ $(v_2^+ = 0)$ $(v_2^+ = 1)$ $(v_2^+ = 2)$ $(v_2^+ = 3)$ NH_382158.751(16) u u NH_2D83027(3)83790 (5)84792.9 (6)ND_2H82261.7(15)82948.2(15)83656.9 (15)	Isotopomer	Ionization	Ionization	Ionization	Ionization		
$(v_2^+ = 0)$ $(v_2^+ = 1)$ $(v_2^+ = 2)$ $(v_2^+ = 3)$ NH_382158.751(16)83027(3)83790 (5)84792.9 (6)NH_2D83027(3)83790 (5)84792.9 (6)ND_2H82990(3)84595.9 (8)ND_382261.7(15)82948.2(15)83656.9 (15)		Energy/cm ⁻¹	Energy/cm ⁻¹	Energy/cm ⁻¹	Energy/cm ⁻¹		
NH ₃ 82158.751(16) Image: Second se		$(\boldsymbol{v}_2^+=\boldsymbol{0})$	$(v_2^+ = 1)$	$(v_2^+ = 2)$	$(v_2^+ = 3)$		
NH ₂ D 83027(3) 83790 (5) 84792.9 (6) ND ₂ H 82990(3) 84595.9 (8) ND ₃ 82261.7(15) 82948.2(15) 83656.9 (15)	NH ₃	82158.751(16)	0,				
ND ₂ H 82990(3) 84595.9 (8) ND ₃ 82261.7(15) 82948.2(15) 83656.9 (15)	NH ₂ D		83027(3)	83790 (5)	84792.9 (6)		
ND ₃ 82261.7(15) 82948.2(15) 83656.9(15)	ND ₂ H		82990(3)		84595.9 (8)		
	ND ₃	82261.7(15)	82948.2(15)	83656.9 (15)			

Table 8 Ionization energies (band origins for transitions to specific vibrational thresholds) derived from the present work and references [2,16,17] for NH₃, NH₂D, NHD₂ and ND₃

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