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RESEARCH ARTICLE

**Fourier-Transform spectroscopy of HD in the Vacuum Ultraviolet
at $\lambda = 87 - 112 \text{ nm}$**

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Absorption spectroscopy in the vacuum ultraviolet (VUV) domain was performed on the hydrogen-deuteride molecule with a novel Fourier-Transform spectrometer based upon wave-front division interferometry. This unique instrument, which is a permanent endstation of the undulator-based beamline DESIRS on the synchrotron SOLEIL facility, opens the way to Fourier-Transform spectroscopy in the VUV range. The HD spectral lines in the Lyman and Werner bands were recorded in the 87-112 nm range from a quasi-static gas sample in a windowless configuration and with a Doppler-limited resolution. Line positions of some 268 transitions in the $B^1\Sigma_u^+(v' = 0 - 30) \leftarrow X^1\Sigma_g^+(v'' = 0)$ Lyman bands and 141 transitions in the $C^1\Pi_u(v' = 0 - 10) \leftarrow X^1\Sigma_g^+(v'' = 0)$ Werner bands were deduced with uncertainties of $0.04 \text{ cm}^{-1}(1\sigma)$ which correspond to $\Delta\lambda/\lambda \sim 4 \times 10^{-7}$. This extensive laboratory database is of relevance for comparison with astronomical observations of H₂ and HD spectra from highly redshifted objects, with the goal of extracting a possible variation of the proton-to-electron mass ratio ($\mu = m_p/m_e$) on a cosmological time scale. For this reason also calculations of the so-called sensitivity coefficients K_i were performed in order to allow for deducing constraints on $\Delta\mu/\mu$. The K_i coefficients, associated with the line shift that each spectral line undergoes as a result of a varying value for μ , were derived from calculations as a function of μ solving the Schrödinger equation using *ab initio* potentials.

1. Introduction

The $B^1\Sigma_u^+ - X^1\Sigma_g^+$ Lyman bands and the $C^1\Pi_u - X^1\Sigma_g^+$ Werner bands are the strongest electronic absorption systems in the hydrogen molecule. The electronic transition relates to the $1s - 2p$ transition in the hydrogen atom, also known as the Lyman- α line. In the molecular case the $2p$ -orbital is either aligned along the molecular axis, the $2p\sigma_u$ -orbital giving rise to the $B^1\Sigma_u^+$ state, or perpendicular to the molecular axis, the $2p\pi_u$ orbital, giving rise to the doubly degenerate $C^1\Pi_u$ state; the latter degeneracy is lifted by non-Born-Oppenheimer effects (Λ -doubling)

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1 giving rise to non-degenerate $C^1\Pi_u^+$ and $C^1\Pi_u^-$ states. Band structure is imposed
2 due to the rotational and vibrational substructure of the excited states, while in
3 most absorption studies only a few rotational states are populated in the lowest
4 $X^1\Sigma_g^+$ ($v = 0$) rovibronic ground state. The absorption spectrum of the Lyman and
5 Werner bands in the hydrogen molecule are blue-shifted from the atomic Lyman-
6 α transition at $\lambda = 121 \text{ nm}$. This is understood from the fact that the binding
7 energies in the $B^1\Sigma_u^+$ and $C^1\Pi_u$ states are less than in the $X^1\Sigma_g^+$ ground electronic
8 state. Hence the molecular absorption spectrum falls in the VUV-domain starting
9 at $\lambda = 112 \text{ nm}$ and progressing towards shorter wavelengths.

10 Because hydrogen is the most abundant molecular species in the universe, the
11 strong Lyman and Werner band systems are ubiquitously observed in outer space.
12 Nevertheless it took until 1970 for the first observation of molecular hydrogen in
13 space was reported by Carruthers [1] using a rocket borne spectrometer observing
14 from high altitudes, therewith evading atmospheric absorption of the vacuum ul-
15 traviolet radiation. Soon thereafter molecular hydrogen was also observed in the
16 line of sight of highly redshifted quasars [2, 3]. More recently in addition to the
17 main H_2 isotopomer also the hydrogen deuteride molecule has been detected in
18 quasars [4–6]. A special feature of the HD isotopomer is the phenomenon of break-
19 ing of the inversion symmetry, or the mixing between states of *gerade* and *ungerade*
20 symmetry [7]. One effect of this phenomenon is the interaction between $B^1\Sigma_u^+$ and
21 $C^1\Pi_u$ states with $EF^1\Sigma_g^+$ states, lending intensity for absorption in the $EF - X$
22 system in HD.

23 A seminal study on the absorption and emission spectra of the Lyman and Werner
24 systems in HD has been performed by Dabrowski and Herzberg using a classical
25 grating spectrograph [8]. The resolution obtained in this Doppler-limited study
26 was 1.0 cm^{-1} , while the accuracy of the line positions was several 0.1 cm^{-1} . Some
27 twenty years later the spectroscopy of some of the Lyman and Werner bands was re-
28 investigated using a tunable laser system in the vacuum ultraviolet and excitation
29 in a molecular beam [9], thus lowering the resolution to 0.25 cm^{-1} and the absolute
30 accuracy to below 0.1 cm^{-1} . Recently the spectra in the range $\lambda = 100 - 112 \text{ nm}$
31 were re-investigated with the use of an improved VUV-laser system, yielding spec-
32 tral linewidths of 0.02 cm^{-1} and absolute accuracies of 0.005 cm^{-1} [10]. Previously
33 the $B - X(v', 0)$ Lyman bands had been investigated for $v' = 0 - 2$ [11] and for
34 $v' = 15$ [12] at this high accuracy. The region near the ionization threshold in HD
35 had been investigated at high resolution employing a narrowband VUV laser [13].

36 Motivated by the need for accurate wavelength positions and in order to ex-
37 tract tight constraints on the variation of the proton-to-electron mass ratio from
38 quasar absorption data [14–16], now that also spectral lines of HD have been ob-
39 served and may be included in the analysis [4–6], we set out to reinvestigate the
40 VUV absorption spectrum of HD. The broadly covering investigation of Dabrowski
41 and Herzberg [8] does not have sufficient accuracy, *i.e.* is less accurate than the
42 high redshift lines obtained from astronomical observation. At the same time the
43 laser investigations [9–12] lack the broad coverage and still some gaps exist in the
44 knowledge of the laboratory data of HD.

45 The availability of the novel Fourier-Transform spectrometer in the vacuum ul-
46 traviolet range allowed us to remeasure in HD the Lyman absorption bands up
47 to $v' = 30$ and the Werner bands up to $v' = 10$. Wavelength positions of over
48 400 lines in the HD absorption spectrum were determined with an uncertainty of
49 0.04 cm^{-1} , or $\Delta\lambda/\lambda = 4 \times 10^{-7}$. The internal calibration of the FT instrument was
50 improved during the course of the investigation through the use of the previously
51 laser-calibrated lines of HD (at the 5×10^{-8} level) in the ranges where they are
52 available. As such the present investigation is also a test of the accuracy and the
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1 capabilities of the unique FT-instrument in the VUV-domain.

2 Methods to determine constraints on a variation of the proton-to-electron mass
3 ratio from spectral lines in molecules require three ingredients. Besides the spec-
4 tral line positions observed at high redshift, and an accurate laboratory data set of
5 wavelengths, also knowledge is required on the value of the sensitivity coefficients
6 that determine how far lines will shift as a result of a change in mass ratio. For
7 the case of H_2 such sensitivity coefficients were calculated by semi-empirical meth-
8 ods [15, 17], and alternatively by *ab initio* calculations [18]. In a previous study on
9 the laser calibration of part of the HD spectrum calculations of some sensitivity
10 coefficients were reported [10]. In the present paper such calculations are further
11 detailed and extended to the broad coverage of the spectrum.
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13

14 2. Experimental setup

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17 Absorption spectra of the hydrogen deuteride molecule HD have been recorded in
18 the $\lambda = 87 - 112 \text{ nm}$ range using a Fourier-Transform (FT) spectrometer, which is
19 installed as a permanent endstation on the VUV undulator-based DESIRS beam-
20 line on the French synchrotron facility SOLEIL [19]. The FT-instrument is the first
21 of its kind to achieve high resolution transmission spectra in this short-wavelength
22 windowless regime. Previously, with the aid of optical beam-splitters to perform
23 amplitude-division interferometry for dividing paths in the Michelson configura-
24 tion, a Fourier-Transform spectrometer had been operated at wavelengths as short
25 as $\lambda=140 \text{ nm}$ [20]. With the here described unique instrument the advantageous
26 properties of FT-spectroscopy, the capability to reach high spectral resolving power
27 $\lambda/\Delta\lambda$ as well as the multiplex capability, are extended to wavelengths beyond the
28 MgF_2 cutoff. This can be accomplished by replacing the amplitude-division concept
29 by a wavefront-division method in obtaining interferograms. The present recordings
30 of high resolution spectra of HD serve also as a demonstration of the obtainable
31 accuracies on wavelengths positions of spectral lines with the novel instrument,
32 owing to the availability of a multitude of accurately calibrated lines from laser
33 experiments.
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36 The FT-spectrometer can achieve an ultimate theoretical resolving power of
37 around 1 million over the entire VUV spectral range covered by the instrument
38 (40-180 nm), which is between 5 and 10 times better than the capabilities of state
39 of the art VUV grating-based spectrometers. A first version of the VUV FTS,
40 operating in the mid-UV range, has been described in detail [21]. Although the
41 underlying physical principles are similar, the DESIRS instrument has been im-
42 proved and can now be operated in the 40-180 nm range (6-30 eV). Here we give
43 a brief description on the main features of operation of the instrument, relevant to
44 the current study, while a more complete report is in preparation [22].
45
46

47 The interferometer is based upon a modified design of the traditional Fresnel bi-
48 mirror interferometer. Two roof reflectors, separated by a $100 \mu\text{m}$ gap and having
49 an angle of 0.35 mrad between each other are illuminated in the vicinity of the
50 gap by the coherent synchrotron radiation beam encoded with information on the
51 HD absorption features. The reflected beams from both reflectors then overlap
52 and interfere at the plane of the detector located at a distance of 1.3 m. The
53 inteferometric signal is recorded continuously at equal path difference intervals by
54 translating one of the reflectors. The source spectral distribution is then recovered
55 by performing a Fourier transformation onto the recorded interferogram. Working
56 in the VUV range requires special care, since optical and mechanical tolerances are
57 directly related to the operation wavelength. Therefore the motion of the reflector
58 is controlled by a sophisticated system which has been especially developed for the
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VUV FTS. Briefly, it consists of a highly sensitive multireflection deflectometer and a multipass Michelson interferometer, both employed to ensure that the required precision is achieved.

As it is important for the recalibration and the error estimation procedures, the multireflection Michelson interferometer is briefly described hereafter (a more detailed description can be found elsewhere [19, 23]). The still reflector has its back side fixed to a stable solid optical block while the back surface of the moving reflector creates a small angle with respect to the surface of the optical block, thus creating a small angle air wedge (fig. 1). When inserting a He-Ne laser beam probe in this wedge with an appropriate entrance angle, the laser beam can be exactly retro-reflected and overlapping the entrance path (after p reflections between the two planes of the wedge as shown in the inset of Fig. 1). This multireflection set-up is the moving arm of a traditional Michelson interferometer used here as a control system. The sinusoidal interferometric signal period given by the interferometer is then directly related to the p parameter. Owing to the multireflection amplification, the period of the signal is roughly inversely proportional to the number of reflections p , namely, period $\approx \lambda_{laser}/2p$ (note that this is the period in terms of the displacement of the moving reflector). The VUV interferometric signal is then triggered at regular path difference steps following a sampling comb generated from the HeNe interferometric signal (twice per signal period). The p parameter can be set in-situ in the 7 to 16 range. This allows to adapt the sampling interval of the interferogram as a function of the smallest wavelength in the spectrum in order to have at least two points per fringe (Nyquist condition). This is a powerful way to keep the relative spectral resolution close to the maximum value, determined by the number of recorded samples, over a large spectral range.

Ideally, the geometry of the control system is perfectly known, and therewith the value of the sampling interval for a given p as well. Hence, the spectral scale is also perfectly determined for each value of p . In practice, some geometrical parameters are not well known, and are difficult to measure. The consequence is that the spectral calibration deviates from the ideal values, the deviation being p -dependent and in the order of a few 10^{-7} . Most of the measurements in the present study were done at $p = 8$ and a minor part at $p = 7$.

OPHELIE2, the undulator feeding the DESIRS beamline provides a VUV pseudo-white radiation with a broadband Gaussian-like spectrum with a $\delta E/E$ relative spectral bandwidth of 7%. The position of the spectral window can be

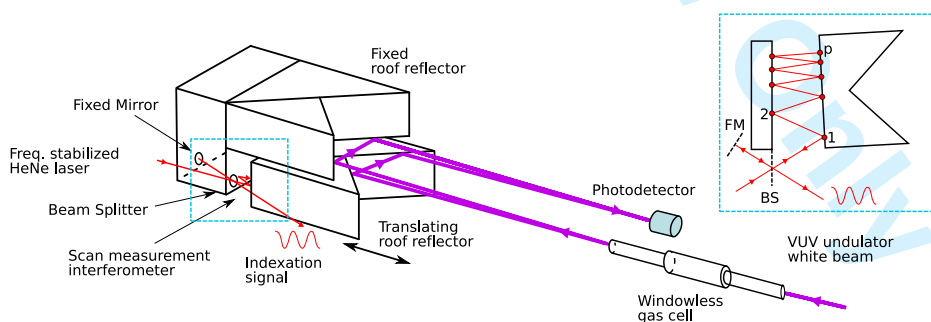


Figure 1. Experimental layout of the VUV FT spectrometer setup. The VUV wavefront division interferometer is facing the VUV synchrotron beam. The two roof-shape reflectors are slightly tilted in order to make the two reflected beams overlap and interfere on a photodiode. A part of the scanning measurement setup is shown on the back side. The incident frequency-stabilized HeNe laser beam is splitted by a beam splitter (BS), the reference beam is reflected at normal incidence by a plane fixed mirror (FM), the transmitted beam is reflected p times between the back of the moving VUV reflector and a plane mirror part of the reference optical block that includes the fixed VUV reflector. All the fixed optical elements are part of the same optical block in order to minimize possible differential errors. The multireflection setup ensures the required high sensitivity for the movement indexation.

1 easily tuned over the whole VUV range, by tuning the magnetic field of the undu-
2 lator, operated in the linear vertical polarization mode [24]. Only the fundamental
3 radiation of the undulator is used. The higher harmonics are being cut-off by a free
4 flow gas filter acting as a low-energy pass filter [25]. The undulator white beam is
5 only reflected by three mirrors at a 20 deg grazing incidence angle before enter-
6 ing the FTS, ensuring a high spectral brightness. This is the relevant photometric
7 parameter for wavefront-division interferometry as this technique requires a high
8 density spatially coherent photon flux. The broad bandwidth synchrotron beam
9 is then sent towards a differentially-pumped multipurpose gas sample chamber,
10 containing the sample. The measured HD gas is introduced into a free flow win-
11 dowless T-shaped gas cell, which consists of a cylindrical steel tube 100 mm long
12 and 30 mm inside diameter. This configuration leads to an inhomogeneous density
13 distribution along the direction of the synchrotron radiation beam. By regulating
14 the pressure at the gas cell input an integrated column density up to a few times
15 10^{18} particles per cm^2 can be achieved. Beyond the interaction with the gas the
16 synchrotron light is used as an input source for the FTS.

17 Interferograms are recorded "on the fly", *i.e.* sampling is performed during the
18 continuous translation of the moving arm of the interferometer yielding a typical
19 scan time of 3 minutes, during which 512 Ksamples are aquired. Each final spectrum
20 at a certain column density represents a summation over 100 individual spectra.
21 The total time to acquire such spectrum spanning over 5000 cm^{-1} is approximately
22 two hours. Fig. 2 shows an example of such averaged spectrum.

23 All measurements were done at room temperature, where the Doppler width for
24 HD is $0.7 - 0.8 \text{ cm}^{-1}$. Therefore the ultimate instrumental resolution is not needed.
25 Instead, it was optimised to gather a sufficient amount of points per spectral line
26 and keep the collection time for an interferogram as low as possible so it can be
27 used for improving the signal to noise ratio (S/N is proportional to the square
28 root of the number of averaging individual spectra). For the present study an
29 optimized measurement time/resolution conditions with an acceptable S/N ratio
30 were achieved by setting the instrumental line width between 0.3 and 0.4 cm^{-1}
31 corresponding to a resolving power of about 350000.

32 It is worth mentioning that the capabilities of the FTS were not fully exploited
33 due to a relatively poor signal-to-noise ratio in some of the spectral regions covered
34 by the instrument. FTS is a photon noise-limited technique and the S/N ratio
35 obtained is proportional to the square root of the photon flux. The latter was sub-
36 optimal due to slight misalignment and especially due to small amounts of carbon
37 contamination on some of the FTS and beamline optics giving rise to absorption
38 in the spectral region of interest.

3. Experimental results and discussion

39 Some 400 absorption lines of the Lyman and Werner bands of HD have been
40 measured with absolute accuracies of 0.04 cm^{-1} (*i.e.* 4×10^{-7} relative accuracies).
41 The transition frequencies are presented in Table 1 for the Lyman bands and Table
42 2 for Werner bands, respectively. Some of the line positions have previously been
43 calibrated at better accuracies - 5×10^{-8} [10–12], while Hinnen *et al.* [9] performed
44 a lower resolution laser based study with a claimed accuracy of 3.5×10^{-7} . For the
45 remainder the best results known are those from Dabrowski and Herzberg [8] with
46 accuracies of few $\times 10^{-6}$. The present results therefore yield an order of magnitude
47 improvement in accuracy for the majority of the lines.

48 The spectral range $90000-115000 \text{ cm}^{-1}$ was divided into five different measure-
49 ments regions, each covering around 5000 cm^{-1} . In order to have sufficiently strong
50

1 but saturated absorption features for each transition with rotational number up
2 to $J = 5$, scans at several column densities for each spectral region are necessary.
3 We have performed measurements at four different column densities for each spec-
4 tral window, taking into account that the bands tend to become stronger towards
5 shorter wavelength.
6

7 A Fourier-Transform spectrum is characterised by a constant noise level deter-
8 mined ideally by the photon flux reaching the detector and the number of averaged
9 individual spectra. Each spectral line therefore exhibits its own signal-to-noise ratio
10 determined by the amount of absorption. All lines with $S/N < 6$ were discarded to
11 ensure that the fitting procedure was accurate. Since measurements were performed
12 at four different column densities, at least two of the four spectra will contain a
13 specific line unsaturated. The final line position is then averaged over these two
14 measurements.
15

16 Assuming proper sampling Fourier-Transform spectroscopy provides an intrinsi-
17 cally linear frequency scale. Initially, calibrations were performed using as a ref-
18 erence the Ar $(3p)^5(2P_{3/2})9d[3/2] \leftarrow (3p)^6 1S_0$ transition, known with an accuracy of
19 0.03 cm^{-1} [27]. However, during the analysis it was found that setting the FT
20 spectrometer at different p parameters introduces small variations in the calibra-
21 tion branch geometry (see inset Fig.1). Because this effect introduces systematic
22 errors of $\sim \text{few} \times 10^{-7}$ a recalibration procedure was implemented, relying on the
23 many HD lines in the spectrum that are known to an accuracy of 5×10^{-8} from laser
24 based studies [10–12]. The recalibration led to a linear correction of the spectrum
25 and an improvement on the accuracy of the frequency axis.
26

27 The statistical uncertainty of a line position in a FT-spectrum with noise is
28 governed by the formula [28]:
29

$$\Delta\sigma \sim \frac{W}{\sqrt{N_w}} \cdot \frac{f}{S/N} \quad (1)$$

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34 where W is the FWHM of the line, N_w represents the number of the experimental
35 points determining the line (defined as number of points above the half maximum
36 level), S/N is the signal to noise ratio for the specific line and f is a geometrical
37 factor relating to how well the kernel function matches the line shape. In the case
38 of room temperature gas cell spectrum of HD for the Lyman and Werner bands
39 the Doppler effect completely determines the lineshape of the non-saturated lines.
40 Then using typical values of $W \sim 0.8 \text{ cm}^{-1}$, $N_w = 4$, $f \sim 1$ and $S/N > 6$ a
41 statistical value of 0.07 cm^{-1} is estimated. However, this is a worst case estimation
42 when the line is determined in only one scan with the worst S/N ratio. In practice
43 we have at least two spectra measured at different column densities ensuring that
44 at least one of them has a much higher S/N ratio. Another estimation of the
45 statistical uncertainty can be derived from estimating the spread of the transitions
46 of the Fourier spectrum with respect to the laser calibrated lines [10–12] (Δ^L in
47 the tables). Such a comparison between data sets yields a standard deviation of
48 0.03 cm^{-1} for the deviations. As a conservative estimate we put 0.04 cm^{-1} as the
49 standard deviation.
50
51

52 The $R(J)$ and $P(J + 2)$ transitions of a certain vibrational band probe the same
53 rotational level of the upper state. These combination differences can be compared
54 with the high-precision far-infrared data from the quadrupole spectrum [26] and
55 used for verification. Based on the 0.04 cm^{-1} uncertainties for single lines the
56 estimated uncertainties for the combination differences amount to 0.06 cm^{-1} . Fig.
57 3 shows that the present results are consistent and fall well within these error
58 margins. It can be seen that combination differences constructed from weaker lines
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60

(R(3) - P(5)) result in larger scattering around the true value.

In Tables 2 and 3 the fourth column Δ^D represents the deviations between the present data with those of Dabrowski and Herzberg. For lower energies up to $B - X(17, 0)$ the difference of the present results with respect to the previous is negative with an average value of -0.23 cm^{-1} , while for higher energies it is positive with an average value of 0.17 cm^{-1} . The sudden change at $B - X(17, 0)$ can also be observed in [9]. The linearity of the FTS and the independent observations by Hinnen with laser spectroscopy suggest that this change may be the result of the calibration procedure in the classical studies.

The present results were compared with the data of Hinnen *et al.* [9]. On average a systematic offset of 0.06 cm^{-1} is found, while in few cases the difference reaches 0.12 cm^{-1} which is outside the estimated error margin. The error estimation of 0.035 cm^{-1} in [9] was overly optimistic; later it was found that the I_2 -reference calibration was offset by 0.06 cm^{-1} due to the fact that only a single spatial mode of the multimode laser beam was used in the calibration procedure in our laboratory. The $B - X(17, 0)$ R(3) line was excluded in the analysis due to an unrealistically large difference of 1 cm^{-1} , possibly due to a typo in [9]. Calibration problems also led to a reassignment of $B - X(13, 0)$ R(2) to the $EF - X(6, 0)$ band in [9]; in the present study it is shown that the initial assignment by Dabrowski and Herzberg [8] was correct. With the present results the combination difference involving this line lies well within the estimated value (see Figure 3).

Table 1.: Transition energies (in cm^{-1}) for lines in the Lyman bands of HD. The estimated uncertainty is $0.04 \text{ cm}^{-1}(1\sigma)$ except for some very weak or blended lines. Δ^L and Δ^D represent differences of the present values with the previously reported by laser [10–12] and classical [8] spectroscopy respectively. The last column contains the sensitivity coefficient for each transition to a possible variation of the proton-to-electron mass ratio. Lines marked with b were blended in the spectrum.

	This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i
$B - X(0, 0)$									
R(0)	90 428.96	0.01		-0.00654					
R(1)	90 398.19	0.00		-0.00695	P(1)	90 310.38	0.00		-0.00790
R(2)	90 307.55	0.05		-0.00811	P(2)	90 161.86			-0.00969
R(3)	90 157.53			-0.00987					
$B - X(1, 0)$									
R(0)	91 574.94	-0.04		-0.00038					
R(1)	91 541.65	-0.01		-0.00084	P(1)	91 457.69	-0.02		-0.00173
R(2)	91 447.22	0.00		-0.00203	P(2)	91 307.91	0.00		-0.00347
R(3)	91 292.31	0.01		-0.00384	P(3)	91 098.59	0.01		-0.00590
R(4)	91 078.00			-0.00609	P(4)	90 831.11			-0.00864
$B - X(2, 0)$									
R(0)	92 692.90	-0.02		0.00528					
R(1)	92 657.39	-0.02		0.00483	P(1)	92 576.74			0.00407
R(2)	92 559.69			0.00359	P(2)	92 425.83	-0.02		0.00224
R(3)	92 400.55			0.00175	P(3)	92 214.30			-0.00014
R(4)	92 181.08			-0.00050	P(4)	91 943.60			-0.00290
$B - X(3, 0)$									
R(0)	93 784.41	0.03	-0.39	0.01061					
R(1)	93 746.89		0.59	0.01014	P(1)	93 669.17	-0.02		0.00940
R(2)	93 646.31	-0.02	-0.49	0.00888	P(2)	93 517.30	-0.01	-0.13	0.00763
R(3)	93 483.39	0.00	-0.13	0.00703	P(3)	93 303.85	0.02	-0.11	0.00525
R(4)	93 259.26	0.00	-0.18	0.00474	P(4)	93 030.25	0.01	-0.13	0.00251
R(5)	92 975.56		-0.11	0.00177					
$B - X(4, 0)$									
R(0)	94 850.22	-0.02	-0.54	0.01557					
R(1)	94 811.00			0.01505	P(1)	94 735.92	-0.03	-0.28	0.01435
R(2)	94 707.77		-0.23	0.01379	P(2)	94 583.19	0.01	-0.38	0.01263
R(3)	94 541.37		-0.22	0.01188	P(3)	94 367.92		-0.14	0.01024
R(4)	94 312.99		-0.57	0.00958	P(4)	94 091.68		0.01	0.00751
R(5)	94 024.26		-0.04	0.00665					

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	This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i
<i>B - X(5, 0)</i>									
R(0)	95 891.06	-0.01	-0.24	0.02013					
R(1)	95 850.19 ^b	0.02	-0.61	0.01959	P(1)	95 777.59	-0.01	-0.31	0.01898
R(2)	95 744.52	0.03	-0.38	0.01832	P(2)	95 624.01	0.01	-0.29	0.01724
R(3)	95 574.84	-0.01	-0.16	0.01644	P(3)	95 407.13	0.05	-0.07	0.01486
R(4)	95 342.49	-0.03	0.49	0.01411	P(4)	95 128.38		-0.22	0.01214
R(5)	95 049.15		0.15	0.01113	P(5)	94 789.74		0.14	0.00880
<i>B - X(6, 0)</i>									
R(0)	96 907.23	0.01	-0.27	0.02439					
R(1)	96 864.77 ^b	0.01	-0.53	0.02389	P(1)	96 794.54	0.01	-0.23	0.02325
R(2)	96 756.80	0.02	-0.50	0.02255	P(2)	96 640.17	0.03	-0.23	0.02154
R(3)	96 584.11	0.00	-0.34	0.02065	P(3)	96 421.72			0.01922
R(4)	96 348.08	0.03		0.01831	P(4)	96 140.71		-0.09	0.01647
R(5)	96 050.31		0.01	0.02231	P(5)	95 799.01		-0.19	0.01313
<i>B - X(7, 0)</i>									
R(0)	97 899.04	0.00	-0.47	0.02831					
R(1)	97 855.13	0.01	-0.31	0.02778	P(1)	97 787.10	0.00	-0.40	0.02722
R(2)	97 744.94 ^b	0.00	-0.67	0.02644	P(2)	97 631.96	-0.01	-0.53	0.02550
R(3)	97 569.39	0.01	-0.11	0.02452	P(3)	97 412.01	-0.02	-0.39	0.02318
R(4)	97 329.80	0.03		0.02217	P(4)	97 128.84		-0.17	0.02045
R(5)	97 027.90		-0.17	0.02298	P(5)	96 784.41		-0.10	0.01711
<i>B - X(8, 0)</i>									
R(0)	98 866.80	-0.01		0.03193					
R(1)	98 821.46	0.02	-0.21	0.03138	P(1)	98 755.59 ^b	-0.01		0.03087
R(2)	98 709.15	0.00	-0.33	0.03007	P(2)	98 599.73	-0.01	-0.31	0.02915
R(3)	98 530.80	-0.02	-0.30	0.02809	P(3)	98 378.35	-0.01		0.02684
R(4)	98 287.77 ^b	-0.05		0.02575	P(4)	98 093.07			0.02416
R(5)	97 981.89		-0.20	0.02854					
<i>B - X(9, 0)</i>									
R(0)	99 810.94	0.00	-0.25	0.03530					
R(1)	99 764.34	0.00	-0.20	0.03472	P(1)	99 700.36	0.00	-0.24	0.03425
R(2)	99 650.20	0.01	-0.32	0.03337	P(2)	99 543.88		-0.18	0.03256
R(3)	99 469.46		-0.44	0.03140	P(3)	99 321.22	-0.03	-0.33	0.03024
R(4)	99 223.72	-0.01	-0.15	0.02895	P(4)	99 034.04 ^b			0.02753
R(5)	98 917.88 ^b			0.03040	P(5)	98 684.47		-0.04	0.02418
<i>B - X(10, 0)</i>									
R(0)	100 731.64 ^b		-0.46	0.03836					
R(1)	100 683.60		-0.40	0.03779	P(1)	100 621.74		-0.20	0.03734
R(2)	100 567.38		-0.22	0.03647	P(2)	100 464.56		-0.04	0.03565
R(3)	100 383.88		-0.26	0.03449	P(3)	100 240.49		-0.23	0.03337
R(4)	100 134.54		-0.36	0.03206	P(4)	99 951.28		-0.19	0.03070
R(5)	99 820.95 ^b		-0.31	0.03378	P(5)	99 598.95		-0.04	0.02736
<i>B - X(11, 0)</i>									
R(0)	101 624.40		-0.29	0.04119					
R(1)	101 581.01		0.82	0.04055	P(1)	101 518.29		0.76	0.04018
R(2)	101 463.13		-0.55	0.03913	P(2)	101 357.37		0.01	0.03852
R(3)	101 278.70		-0.34	0.03678	P(3)	101 137.92			0.03618
R(4)					P(4)				
R(5)	100 703.29		0.08	0.03580	P(5)	100 493.71			0.02973
<i>B - X(12, 0)</i>									
R(0)	102 503.53			0.04376					
R(1)	102 453.02 ^b		-0.45	0.04316	P(1)	102 394.91		-0.43	0.04261
R(2)	102 332.80		-0.36	0.04179	P(2)	102 236.45		-0.35	0.04112
R(3)	102 147.32		-0.18	0.03982	P(3)	102 009.93		-0.22	0.03883
R(4)	101 890.90 ^b			0.03744	P(4)	101 716.76		-0.17	0.03616
R(5)	101 570.43		-0.12	0.03812					
<i>B - X(13, 0)</i>									
R(0)	103 356.32		0.14	0.04606					
R(1)	103 305.85		-0.41	0.04519	P(1)	103 247.83		-0.47	0.04512
R(2)	103 191.57		-0.05	0.04035	P(2)	103 089.23		-0.63	0.04345
R(3)	102 985.10		-0.04	0.03877	P(3)	102 862.81		-0.33	0.04091
R(4)	102 725.62		-0.33	0.03902	P(4)	102 575.48		-0.08	0.03475
R(5)	102 409.26			0.03986					
<i>B - X(14, 0)</i>									
R(0)	104 186.14		-0.34	0.04821					
R(1)	104 133.52		-0.13	0.04762	P(1)	104 078.65 ^b			0.04725
R(2)	104 010.40		-0.32	0.04623	P(2)	103 919.09		-0.52	0.04562

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	This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i	
1										
2										
3	R(3)	103 817.85		-0.24	0.04422	P(3)	103 690.49	-0.34	0.04338	
4	R(4)	103 557.02		-0.26	0.04182	P(4)	103 394.35	-0.18	0.04072	
5	<i>B - X(15, 0)</i>									
6	R(0)	104 992.05		-0.85	0.04653					
7	R(1)	104 938.50		-0.81	0.04828	P(1)	104 887.83		0.04919	
8	R(2)	104 814.05		-0.35	0.04753	P(2)	104 724.97	-0.30	0.04396	
9	R(3)	104 619.74 ^b			0.04576	P(3)	104 495.39	-0.05	0.04408	
10	R(4)	104 357.09 ^b			0.04350	P(4)	104 197.97 ^b		0.04207	
11	R(5)	104 027.40		-0.07	0.04314					
12	<i>B - X(16, 0)</i>									
13	R(0)	105 781.66	-0.02	0.12	0.05186					
14	R(1)	105 727.07	0.00		0.05128	P(1)	105 675.13 ^b	0.02	0.16	
15	R(2)	105 601.02	-0.02	0.49	0.04987	P(2)	105 514.62	0.01	-0.08	
16	R(3)	105 404.63	-0.01	-0.17	0.04786	P(3)	105 284.03	0.04		
17	R(4)	105 139.53 ^b		-0.30	0.04536	P(4)	104 984.94	-0.22	0.04447	
18	<i>B - X(17, 0)</i>									
19	R(0)	106 546.11		0.43	0.05333					
20	R(1)	106 490.13 ^b			0.05269	P(1)	106 440.31	0.15	0.05252	
21	R(2)	106 362.16		0.15	0.05124	P(2)	106 278.99	0.45	0.05081	
22	R(3)	106 163.30 ^b		0.37	0.04924	P(3)	106 047.04		0.04856	
23	R(4)	105 895.13 ^b			0.04682	P(4)	105 746.06	0.31	0.04588	
24	<i>B - X(18, 0)</i>									
25	R(0)	107 292.96		0.15	0.05477					
26	R(1)	107 236.54		0.20	0.05416	P(1)	107 187.30	0.14	0.05389	
27	R(2)	107 107.80		0.14	0.05273	P(2)	107 025.90	0.13	0.05227	
28	R(3)	106 908.03		0.18	0.05067	P(3)	106 793.48	0.26	0.05007	
29	R(4)					P(4)	106 491.81		0.04741	
30	<i>B - X(19, 0)</i>									
31	R(0)	108 017.12		0.47	0.05596					
32	R(1)	107 959.24		0.35	0.05529	P(1)	107 912.30	0.47	0.05510	
33	R(2)	107 828.45		0.40	0.05387	P(2)	107 750.11	0.42	0.05349	
34	R(3)	107 625.82		0.42	0.05181	P(3)	107 516.17	0.37	0.05123	
35	R(4)	107 352.90		0.38	0.04939	P(4)	107 212.34	0.34	0.04860	
36	<i>B - X(20, 0)</i>									
37	R(0)	108 721.84 ^b		0.12	0.05698					
38	R(1)	108 663.84		0.26	0.05634	P(1)	108 617.08	0.26	0.05611	
39	R(2)	108 532.89			0.05484	P(2)	108 454.82	0.41	0.05452	
40	R(3)	108 330.69 ^b		0.51	0.05256	P(3)	108 220.76 ^b		0.05231	
41						P(4)	107 916.77	0.66	0.04961	
42	<i>B - X(21, 0)</i>									
43	R(0)	109 406.64 ^b		-0.04	0.05786					
44	R(1)	109 346.46		0.24	0.05721	P(1)	109 302.00 ^b	0.24	0.05700	
45	R(2)	109 213.09		0.28	0.05579	P(2)	109 139.02	0.36	0.05542	
46	R(3)	109 007.01			0.05374	P(3)	108 903.33 ^b	0.35	0.05321	
47	R(4)	108 729.80		0.35	0.05127	P(4)	108 596.69 ^b		0.05059	
48	<i>B - X(22, 0)</i>									
49	R(0)	110 071.36		0.36	0.05855					
50	R(1)	110 012.15		0.31	0.05778	P(1)	109 967.22	0.34	0.05775	
51	R(2)	109 880.65		0.32	0.05570	P(2)	109 804.25	0.24	0.05613	
52	R(3)					P(3)	109 569.08 ^b		0.05381	
53	R(4)	109 376.84		0.36	0.04924	P(4)	109 264.50	0.33	0.05053	
54	<i>B - X(23, 0)</i>									
55	R(0)	110 715.06		0.00	0.05915					
56	R(1)	110 654.10			0.05849	P(1)	110 611.67	-0.19	0.05831	
57	R(2)	110 518.46 ^b		0.85	0.05707	P(2)	110 448.01	0.57	0.05674	
58	R(3)	110 309.35		0.53	0.05502					
59	R(4)	110 028.28		0.40	0.05250					
60	<i>B - X(24, 0)</i>									
61	R(0)	111 347.02		-0.10	0.05895					
62	R(1)					P(1)	111 242.51		0.05877	
63	R(2)	111 138.09		0.05	0.05439	P(2)	111 080.02	0.29	0.05656	
64	R(3)	110 930.39		0.30	0.05442	P(3)	110 851.28	0.36	0.04838	
65	R(4)	110 649.65		0.50	0.05246					
66	<i>B - X(25, 0)</i>									
67	R(0)	111 955.75		-0.13	0.05989					
68	R(1)	111 893.57 ^b		-0.10	0.05919	P(1)	111 853.85 ^b	0.36	0.05905	

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	This work	Δ^L	Δ^D	K_i	This work	Δ^L	Δ^D	K_i
R(2)	111 757.99		-0.11	0.05777	P(2)	111 688.70	-0.02	0.05751
R(3)	111 541.22		-0.06	0.05568	P(3)	111 450.51	-0.05	0.05530
<i>B - X(26, 0)</i>								
R(0)	112 541.15		-0.06	0.05975				
R(1)	112 476.57		-0.21	0.05898	P(1)	112 440.10	-0.22	0.05922
R(2)	112 336.43		-0.21	0.05758	P(2)	112 274.05	-0.24	0.05738
R(3)	112 121.84		-0.15	0.05556	P(3)	112 033.43	-0.23	0.05510
R(4)	111 834.16		-0.21	0.05314				
<i>B - X(27, 0)</i>								
R(0)	113 112.48		0.27	0.06004				
R(1)	113 048.26		0.16	0.05933	P(1)	113 010.15	0.04	0.05921
R(2)	112 907.91 ^b		-0.13	0.05785	P(2)	112 845.38	0.22	0.05768
R(3)	112 692.66		0.06	0.05571	P(3)	112 605.12	-0.06	0.05548
<i>B - X(28, 0)</i>								
R(0)								
R(1)	113 598.48		-0.01	0.05907	P(1)			
R(2)	113 456.06		0.30	0.05759	P(2)	113 397.16	0.28	0.05747
R(3)	113 238.14		0.38	0.05549				
<i>B - X(29, 0)</i>								
R(0)	114 198.02		-0.04	0.05951				
R(1)	114 132.33		-0.08	0.05882	P(1)	114 097.04	-0.12	0.05871
R(2)	113 989.70		-0.54	0.05728	P(2)	113 930.94	-0.07	0.05717
					P(3)	113 689.27	0.12	0.05500
<i>B - X(30, 0)</i>								
R(0)	114 711.98		0.09	0.05898				
R(1)	114 644.87		0.15	0.05825	P(1)	114 611.72	-0.03	0.05823
R(2)	114 500.52			0.05673	P(2)	114 444.83	-0.06	0.05665

4. Calculation of the sensitivity coefficients

The present experimental investigation on the spectroscopy of HD is motivated by the possibility to include these lines in a search for a variation of the proton-electron mass ratio on a cosmological time scale [10]. In recent years HD lines have been observed in quasar absorption spectra at high redshift [4, 5], and in the most recent study on the J2123 system at redshift $z = 2.05$ HD lines are included in addition to H₂ lines to derive a constraint on $\Delta\mu/\mu$, where $\Delta\mu$ is the difference between proton-to-electron mass ratio in the present epoch $\mu_0 = m_p/m_e$ (at zero redshift) and the mass ratio μ_z for the absorbing cloud (at high redshift z) [6]. An important ingredient for such an analysis is the knowledge of the so-called sensitivity coefficients, defined as [15, 17]:

$$K_i = \frac{d(\ln\lambda_i)}{d(\ln\mu)} = \frac{\mu}{\lambda_i} \frac{d\lambda_i}{d\mu} = -\frac{\mu}{\sigma_i} \frac{d\sigma_i}{d\mu} \quad (2)$$

where $\lambda_i = 1/\sigma_i$ and $\sigma_i = E_i^{up}(v', J') - E_i^{low}(v'', J'')$ is the transition frequency. These K_i coefficients determine how much each spectral line shifts as a result of a possible variation in μ corresponding to:

$$\frac{\lambda_i^z}{\lambda_i^0} = (1 + z_{abs})(1 + \frac{\Delta\mu}{\mu} K_i) \quad (3)$$

with z_{abs} the overall redshift of the absorbing hydrogen cloud, λ_i^z the transition wavelength at high redshift and λ_i^0 the wavelength in the laboratory frame (zero redshift).

Table 1. Transition energies (in cm^{-1}) for lines in the Werner bands of HD. The estimated uncertainty of all transitions is $0.04 \text{ cm}^{-1}(1\sigma)$. Δ^L and Δ^D represent differences of the present values with the previously reported by laser [10–12] and classical [8] spectroscopy respectively. The last column contains the sensitivity coefficient for each transition to a possible variation of the proton-to-electron mass ratio.

	This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i
C(v=0)														
R(0)	99 276.28	0.02	-0.68	-0.00391										
R(1)	99 279.88	0.02	-0.25	-0.00389	Q(1)	99 186.39	0.01	-0.33	-0.00486					
R(2)	99 240.47	-0.02	-0.29	-0.00441	Q(2)	99 100.14	0.00	0.00	-0.00589	P(2)	99 009.18	0.00	-0.23	-0.00677
R(3)	99 158.41	0.01		-0.00529	Q(3)	98 971.63		-0.14	-0.00726	P(3)	98 836.76	-0.03		-0.00857
R(4)	99 032.36			-0.00627	Q(4)	98 801.81	-0.02		-0.00880	P(4)	98 624.40	0.01	-0.25	-0.01051
R(5)					Q(5)	98 592.04		-0.16	-0.01078	P(5)	98 373.33		-0.15	-0.01282
C(v=1)														
R(0)	101 289.54 ^b			0.00562										
R(1)	101 289.54 ^b			0.00559	Q(1)	101 199.80			0.00467					
R(2)	101 243.53		-0.52	0.00507	Q(2)	101 109.49		-0.58	0.00359	P(2)	101 022.66			0.00284
R(3)	101 152.28		-0.17	0.00450	Q(3)	100 974.85			0.00219	P(3)	100 846.23			0.00105
R(4)	101 002.18		0.14	0.01675	Q(4)	100 796.90		-0.34	0.00056	P(4)	100 627.41			-0.00085
R(5)					Q(5)	100 576.98		-0.06	-0.00152	P(5)	100 367.27		-0.10	-0.00280
C(v=2)														
R(0)	103 201.94		-0.19	0.01381										
R(1)	103 196.68		0.73	0.01402	Q(1)	103 112.24		0.50	0.01286					
R(2)	103 140.20		-0.40	0.01685	Q(2)	103 017.84		-0.88	0.01177	P(2)	102 934.86		0.18	0.01111
R(3)	103 056.65		-0.04	0.01532	Q(3)	102 877.20		-0.12	0.01030	P(3)	102 753.58			0.00960
R(4)	102 909.43		-0.65	0.01139	Q(4)	102 691.29		-0.21	0.00859	P(4)	102 524.13		-0.09	0.01111
R(5)	102 719.69		-0.12	0.00928	Q(5)	102 461.51			0.00645	P(5)	102 271.56			0.00823
C(v=3)														
R(0)	105 018.45		-0.58	0.02434										
R(1)	105 010.26		-0.36	0.02186	Q(1)	104 925.58		-1.13	0.01987					
R(2)	104 953.13		-0.50	0.02055	Q(2)	104 827.24			0.01875	P(2)	104 751.40			0.02171
R(3)	104 847.31		-0.38	0.01914	Q(3)	104 680.69		-0.01	0.01722	P(3)	104 567.18		-0.27	0.01755
R(4)	104 693.38		-0.32	0.01765	Q(4)	104 487.03		-0.23	0.01544	P(4)	104 337.10		-0.06	0.01493
R(5)	104 492.03		-0.05	0.01585	Q(5)	104 247.40		-0.13	0.01320	P(5)	104 062.30		-0.10	0.01221
C(v=4)														
R(0)	106 731.61		0.02	0.02667										
R(1)	106 719.94		0.10	0.02656	Q(1)	106 641.22		0.17	0.02573					
R(2)	106 657.23		0.05	0.02582	Q(2)	106 539.02		0.14	0.02459	P(2)	106 464.53		0.38	0.02408
R(3)	106 543.53		0.10	0.02462	Q(3)	106 386.60		0.08	0.02299	P(3)	106 276.79		0.04	0.02234
R(4)	106 379.16		0.24	0.02331	Q(4)	106 185.13		0.44	0.02119	P(4)	106 041.10			0.02032
R(5)					Q(5)	105 935.89		0.36	0.01886	P(5)	105 758.51		0.29	0.01784
C(v=5)														
R(0)	108 349.85		0.26	0.03148										
R(1)	108 333.86		0.33	0.03126	Q(1)	108 259.75		0.29	0.03056					
R(2)	108 264.59		0.41	0.03053	Q(2)	108 153.69		0.37	0.02940	P(2)	108 082.75		0.49	0.02895
R(3)	108 141.72			0.02948	Q(3)	107 995.45		0.44	0.02775	P(3)	107 890.75		0.49	0.02712
R(4)	107 961.79		0.68	0.02978	Q(4)	107 786.23		0.40	0.02586	P(4)	107 648.46		0.43	0.02514
R(5)	107 686.60		0.60	0.03137	Q(5)	107 527.48		0.47	0.02346					

continue on the next page

Table 1. continued...

	This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i		This work	Δ^L	Δ^D	K_i
C(v=6)														
R(0)	109 871.21		0.15	0.03528										
R(1)	109 850.40		0.11	0.03512	Q(1)	109 781.47		0.11	0.03441					
R(2)	109 772.96		0.11	0.03488	Q(2)	109 671.44		0.10	0.03319	P(2)	109 604.16		0.29	0.03280
R(3)	109 629.39		0.25	0.03933	Q(3)	109 507.41		0.23	0.03153	P(3)				
R(4)	109 477.83		0.35	0.03378	Q(4)	109 290.46		0.22	0.02956	P(4)	109 156.85		0.36	0.02959
					Q(5)	109 021.84			0.02706					
C(v=7)														
R(0)	111 294.07			0.03868										
R(1)	111 261.05			0.04435	Q(1)	111 205.51			0.03725					
R(2)	111 199.89		0.50	0.03991	Q(2)	111 091.55		0.17	0.03602	P(2)	111 026.96		0.05	0.03623
R(3)	111 060.02		0.13	0.03637	Q(3)	110 921.59		0.50	0.03431	P(3)	110 817.86		-0.08	0.04037
R(4)	110 865.93		-0.12	0.03409	Q(4)	110 696.84		-0.03	0.03221	P(4)	110 583.77		-0.13	0.03472
					Q(5)	110 418.59		0.39	0.02964					
C(v=8)														
R(0)	112 621.21		-0.45	0.04019										
R(1)	112 594.09		0.12	0.03992	Q(1)	112 530.27		0.14	0.03911					
R(2)	112 507.62		0.16	0.03887	Q(2)	112 412.34		0.36	0.03782	P(2)	112 354.08		-0.07	0.03777
R(3)	112 362.23			0.03723	Q(3)	112 236.35		-0.06	0.03601	P(3)	112 150.94		0.02	0.03597
R(4)	112 158.17		-0.27	0.03541	Q(4)	112 003.52		-0.15	0.03388	P(4)	111 891.52		-0.19	0.03373
C(v=9)														
R(0)														
R(1)	113 811.18		0.01	0.04040	Q(1)	113 753.07		0.11	0.03993					
R(2)					Q(2)	113 630.93		-0.14	0.03860	P(2)				
R(3)	113 563.36			0.03782	Q(3)	113 448.76		0.52	0.03674	P(3)	113 368.09		0.18	0.03650
R(4)	113 346.81		0.34	0.03632	Q(4)	113 207.64		0.25	0.03451	P(4)				
C(v=10)														
R(0)	114 959.56		-0.25	0.04045										
R(1)	114 922.83		0.15	0.04001	Q(1)	114 869.71		0.32	0.03966					
R(2)	114 822.46			0.03896	Q(2)	114 743.22		0.30	0.03829	P(2)	114 692.45		-0.01	0.03809
R(3)	114 657.07		0.08	0.03760	Q(3)	114 554.48		0.11	0.03634	P(3)	114 479.73		0.07	0.03614
R(4)					Q(4)	114 304.66		0.04	0.03397	P(4)				

The K_i coefficients have previously been calculated for H_2 through semi-empirical methods [15, 17] and via first principles calculations [18]. Here we adopt the method of calculating the coefficients, by solving the Schrödinger equation for ground and excited states using *ab initio* potentials to derive level energies and transition wavelengths. The sensitivity coefficient for a given line is calculated as the derivative of its wavelength or of its wavenumber with respect to the mass ratio μ . Thus, the first step is to calculate energies of the upper levels of transitions belonging to excited electronic states and energies of lower levels belonging to the ground electronic state. These energy levels are obtained by solving the Schrödinger equation of the ro-vibrational motion in a given electronic state. The second step is to calculate wavenumbers as differences between level energies, then to derive wavelengths of transitions. These steps in the calculations are repeated for several values of the mass ratio μ chosen to be close to the mass ratio of the present epoch. The results allow the determination of the derivative of the wavelength of a given line with respect to μ . At present the proton-to-electron mass ratio measured by Mohr and Taylor [29] with a relative accuracy of 2×10^{-9} is equal to $\mu_0 = 1836.15267247(80)$. This value was taken as the central value for determining the K_i .

4.1. Calculation of level energies

In the present case, the wavelengths of interest are those of electronic transitions between ro-vibrational levels of the $B^1\Sigma_u^+$, $C^1\Pi_u$, $B'^1\Sigma_u^+$, $D^1\Pi_u$ excited states and of the ground electronic state $X^1\Sigma_g^+$. The four excited states B , B' , C and D states are well known to be strongly coupled and it is necessary to go beyond the adiabatic approximation. The principle of the present level calculations is similar to the one described in the study of the D_2 VUV emission spectrum [30]. Using high accuracy *ab initio* adiabatic potentials and taking into account the radial couplings between the B and $B'^1\Sigma_u^+$ states and between the C and $D^1\Pi_u$ states, as well as the $(\Sigma^+ - \Pi^+)$ rotational couplings, we performed calculations of energies of the upper bound levels belonging to these states, by solving a system of four radial coupled equations, given in matrix form as :

$$\left\{ -\frac{1}{2\mu_n} \left[\mathbf{I} \frac{d^2}{dR^2} - \mathbf{I} \frac{J'(J'+1)}{R^2} + \mathbf{A}(R) + 2\mathbf{B}(R) \frac{d}{dR} \right] + \mathbf{U}(R) - E \right\} \varphi(R) = 0 \quad (4)$$

where μ_n is the reduced mass of the HD nuclei given by:

$$\mu_{HD} = \frac{m_p \times m_D}{m_D + m_p} \quad (5)$$

and m_D is the deuterium nucleus mass. In atomic units, the mass unit is m_e , then the proton-to-electron mass ratio μ is numerically equal to m_p in atomic units used in our calculations. \mathbf{I} is the identity matrix and $\mathbf{U}(R)$ is the diagonal matrix of adiabatic potential curves. The diagonal elements of the $A(R)$ matrix are the adiabatic corrections, whereas the off-diagonal elements involve both non adiabatic couplings between states of the same symmetry ($\Sigma - \Sigma$ or $\Pi - \Pi$) and the rotational couplings between $\Sigma - \Pi$ states, and finally $B(R)$ is the radial coupling matrix. More details for the formalism are described by Senn *et al.* [31]. The potential energy curves and relevant parameters for the excited states were taken from the work of Wolniewicz and coworkers [32–34].

The $\varphi(R)$ is the eigenvector matrix containing the expansion coefficients $\varphi_i(R)$ of the total ro-vibrational wave function of the molecule in the adiabatic basis of

1 the electron-rotational wave functions. In the present case, the nonadiabatic wave
 2 function $\varphi_i(R)$ is a four-component vector :

$$\varphi_i(R) = \{\varphi_{n,i}(R), \varphi_{n',i}(R) \dots\}. \tag{6}$$

7 The label n refers to the particular electronic state belonging to $\{B, B', C, D\}$, and
 8 the label i is an ordering index according to increasing energies.

9 It is convenient to transform the coupled equations by a unitary transformation
 10 which makes the first derivative radial coupling vanish. In the transformed equa-
 11 tions, written in the so-called diabatic representation, the matrix of the hamiltonian
 12 has diagonal elements given by diabatic potentials, which may cross even between
 13 states of same symmetry, and off-diagonal elements given by electronic couplings
 14 between the diabatic states with no radial derivatives. We used, in the present
 15 study, the Fourier Grid Hamiltonian (FGH) method [31], an efficient and accurate
 16 method for bound state problems, to solve the coupled equations, as well as the
 17 one-state Schrödinger equation (see below eq.9). The advantage of this method is to
 18 provide all the energy values and the coupled-channel wave functions in one single
 19 diagonalisation of the Hamiltonian matrix expressed in a discrete variable repre-
 20 sentation (DVR). As the rotational interaction only affects the Σ^+ and Π^+ states,
 21 a system of coupled equations without rotational coupling has to be solved for the
 22 Π^- component. After solving the diabatic coupled equations, the solutions were
 23 transformed back to the adiabatic representation for the four-component $\varphi_i(R)$.
 24 The percentage of the electronic character n is obtained by :

$$\rho_i(n) = \int [\varphi_{n,i}(R)]^2 dR. \tag{7}$$

25 with the normalisation : $\rho_i(B) + \rho_i(C) + \rho_i(B') + \rho_i(D) = 1$.
 26 The electronic component $\varphi_{n,i}(R)$ takes into account not only the bound vibra-
 27 tional states but also the vibrational continuum. The percentage corresponding
 28 to a particular vibrational state v_n of the electronic state n can be obtained by
 29 expanding over a set of vibrational functions $\varphi_{n,v}(R)$, solutions of the uncoupled
 30 equation for adiabatic state n :

$$\rho_i(n, v) = \left| \int \varphi_{n,v}(R) \varphi_{n,i}(R) dR \right|^2. \tag{8}$$

31 The $X^1\Sigma_g^+$ ground state [35] is isolated from the other excited states, therefore its
 32 vibrational energy levels were calculated by solving the one Schrödinger equation
 33 (eq 9) for each rotational quantum number J'' in the adiabatic approximation
 34 adding the corresponding centrifugal term to the *ab initio* potential $U_x(R)$, which
 35 includes the adiabatic correction into the Born-Oppenheimer potential, computed
 36 by Wolniewicz [35]. The relativistic and the radiative corrections [36] were also
 37 taken into account in the present calculations.

$$\left\{ -\frac{1}{2\mu_n} \frac{d^2}{dR^2} + \frac{J''(J'' + 1)}{2\mu_n R^2} + U_x(R) - E_x \right\} \varphi_x(R) = 0. \tag{9}$$

38 The weak effect of excited states of the symmetries $\Sigma_{g(u)}$ and $\Pi_{g(u)}$, which leads to
 39 the regular nonadiabatic shifts ΔE_x of the levels of the ground state $X^1\Sigma_g^+$, was
 40 taken into account by means of the semiempirical relations [37]:

$$\Delta E_x = E_{\Sigma_g} + E_{\Sigma_u} + J''(J'' + 1)(E_{\Pi_g} + E_{\Pi_u}) \quad (10)$$

Where:

$$E_{\Sigma_{g(u)}} = \frac{\langle \varphi_x | E_x^{ad} - V_x(R) | \varphi_x \rangle}{\mu_n} \sum_i a_i(\Pi_{g(u)}) \eta^i \quad (11)$$

$$E_{\Pi_g} = \frac{1}{\mu_n^2} \sum_i b_i(\Pi_g) \eta^i \quad (12)$$

$$E_{\Pi_u} = \frac{1}{\mu_\alpha^2} \sum_i b_i(\Pi_u) \eta^i \quad (13)$$

where μ_α is the difference of mass of the deuterium nucleus and the hydrogen nucleus given by: $\mu_\alpha = (m_D + m_p)/(m_D - m_p)$. η is a the mass-dependent quantum number given by: $\eta = (v_x + \frac{1}{2})/\sqrt{\mu_n}$. The energies $E_{\Sigma_{g(u)}}$ and $E_{\Pi_{g(u)}}$ belong, respectively, to the electronic states $\Sigma_{g(u)}$ and $\Pi_{g(u)}$. φ_x represents the ro-vibrational wave function associated to the energy E_x . $V_x(R)$ is the adiabatic energy potential of the ground state X including the centrifugal barrier. Here, the mass-independent coefficients a_i and b_i of the polynomial expansions were determined from the experimental energy levels for homonuclear isotopomers H_2 , D_2 , and T_2 .

Similar calculations of the level energies were reported by Abgrall and Roueff [38] using the same *ab initio* data but different method to solve the Schrödinger equation. As previously mentioned we used the the Fourier Grid Hamiltonian method, based on a Discret Variable Representation (DVR) of the wavefunctions and of the Hamiltonian, while Abgrall and Roueff used the Numerov method. Our 4-state calculations led to the same energies as reported in [38] for all levels involved in the current study, with largest discrepancy being $\pm 0.01 \text{ cm}^{-1}$ for some high vibrational levels.

It must be noted that the full effect of *ungerade - gerade* symmetry-breaking in HD is not accounted for. There exist specific levels that undergo a *u-g* interaction between $B^1\Sigma_u^+$ and $C^1\Pi_u$ states on the one hand and $EF^1\Sigma_g^+$ states on the other hand (with a selection rule $\Delta J = 0$) giving rise to perturbations and level mixings. These effects are not included in our close coupling calculations because only incomplete *ab initio* coupling operators are available [?]. In order to estimate this effect a tentative calculation was performed for the example of the $B - X(25, 0) R(3)$, one of the most strongly affected lines. This yields a shift of 5.11 cm^{-1} and an increase in the sensitivity coefficient by approximately 7% induced by the EF coupling. An extended analysis of this *u-g* symmetry-breaking effect will be the subject of a future study.

4.2. Determination of $d\lambda_i/d\mu$

From the level energies calculated above, the wavelengths of transitions can be deduced. The entire procedure described has to be performed for several values of the reduced mass of nuclei μ_n , involving several values of the proton-to-electron

1 mass ratio μ chosen to be close to μ_0 . In these conditions, the variation of a given
 2 wavelength λ_i versus μ is close to linear and its slope represents the derivative
 3 $d\lambda_i/d\mu$.

4 In the previous investigations [17] on a possible variation of μ , the statistical
 5 analysis of the recent observations of spectroscopic features in cold hydrogen clouds
 6 in the line of sight of two quasar light sources (Q 0405-443 and Q 0347-383), based
 7 on highly accurate laboratory wavelength measurements of H_2 lines, led to an order
 8 of magnitude of 2×10^{-5} for $\Delta\mu/\mu$ over 12 Gyears. This sets the scale to deduce a
 9 value of the derivative $d\lambda_i/d\mu$; the variation step of μ should be chosen to obtain
 10 a few points within this interval. In our case the calculations have been performed
 11 for the present value of $\mu_0 = 1836.15267261$ and another six values of μ separated
 12 by 0.02 and spanning from $\mu = 1836.10267261$ to $\mu = 1836.20267261$.

13 $R(J)$, $P(J)$ and $Q(J)$ transitions were calculated for each of the values of μ
 14 mentioned above. Then for each transition, the variation of wavelength versus μ was
 15 plotted and its slope was calculated by a linear fit. The fit provides, together with
 16 the slope, the uncertainty of its determination, the standard deviation of the fit and
 17 finally the χ^2 value. In Fig.4 we show two examples of the variation in wavelength
 18 of $B^1\Sigma_u^+(v=5) \leftarrow X^1\Sigma_g^+(v=0)$ R(0) and $C^1\Pi_u(v=0) \leftarrow X^1\Sigma_g^+(v=0)$ P(4)
 19 transitions due to variation in μ , as well as their linear fits.

20 The values of the K_i coefficients and their uncertainties were then deduced from
 21 the calculated values of the slopes and their uncertainties using equation (4). For
 22 completeness sensitivity coefficients were calculated for all experimentally observed
 23 lines, even for those beyond the Lyman-cutoff at $\lambda < 91$ nm in which domain
 24 the molecular hydrogen lines cannot be observed under the usual astrophysical
 25 conditions of a high density of H I. The values for the resulting K_i coefficients are
 26 listed in Tables 1 and 2 with the molecular transition frequencies.

27 The range of values for the K_i -coefficients for the HD lines observable in high-
 28 redshifted objects lie in the range -0.01 to 0.05 , similarly as in H_2 . These values
 29 are small, *i.e.* much smaller than for the proposed experiments involving detection
 30 schemes of μ variation on a laboratory time scale [39, 40]. This is due to the fact
 31 that the Lyman and Werner lines are electronic transitions, while the electronic
 32 energy in molecules is nearly mass-independent (in so far as the Born-Oppenheimer
 33 approximattion holds). In the comparison with high-redhsift H_2 and HD lines the
 34 sensitivity for detection of μ variation comes from the extremely large intervals of
 35 $\sim 10^{10}$ years. The here presented K_i coefficients for HD were in fact already used
 36 in the treatment of data in the J2123 quasar object at redshift $z = 2.05$ [41].

42 5. Conclusions

43 We report on a Fourier tranform spectroscopic study of HD in the VUV spectral
 44 domain at $\lambda = 87 - 112$ nm. Some 268 transitions in the $B^1\Sigma_u^+(v' = 0 - 30) \leftarrow$
 45 $X^1\Sigma_g^+(v'' = 0)$ Lyman bands and 141 transitions in the $C^1\Pi_u(v' = 0 - 10) \leftarrow$
 46 $X^1\Sigma_g^+(v'' = 0)$ Werner bands were deduced from a quasi static gas sample using a
 47 novel VUV Fourier transform spectrometer at the Soleil Synchrotron facility. The
 48 estimated accuracies of the wavelength calibration is 0.04 cm^{-1} , which is verified
 49 by ground state combination differences. Accuracies of $\Delta\lambda/\lambda \sim 4 \times 10^{-7}$ match the
 50 accuracies as typically obtained in high redshift observations of the same molecular
 51 lines. The calculated sensitivity coefficients make the data relevant for the investi-
 52 gations of possible variation of the fundamental constants on a cosmological time
 53 scale.

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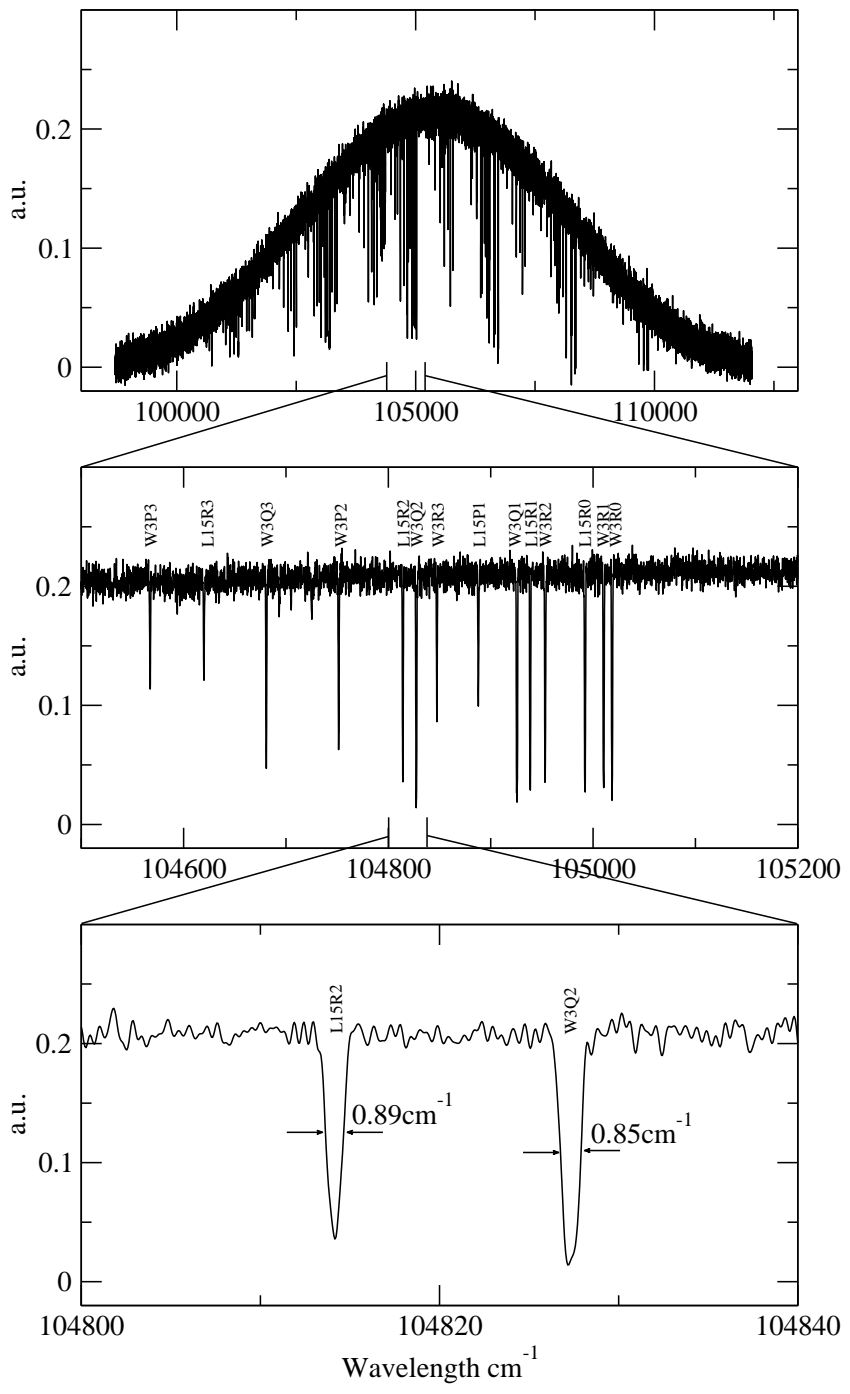


Figure 2. This spectrum represents one of the five windows covering the entire investigated spectral range - 90000-115000 cm^{-1} . It is a product of averaging 100 individual spectra. The Gaussian-like envelope represents the synchrotron radiation spectrum in which the absorption features of HD are encoded. The measurements were taken at room temperature and pressure at the input of the gas cell of 5.6×10^{-3} mbar. The bottom part of the figure focuses on a zoom on $B^1\Sigma_u^+(v = 15) \leftarrow X^1\Sigma_g^+(v = 0)$ R(2) and $C^1\Pi^-(v = 3) \leftarrow X^1\Sigma_g^+(v = 0)$ Q(2) transitions from Lyman and Werner band which are shortly labeled as L15R2 and W3Q2. It can be seen that the linewidths are determined by Doppler broadening. It should be noted also that for better visibility the spectrum has been interpolated.

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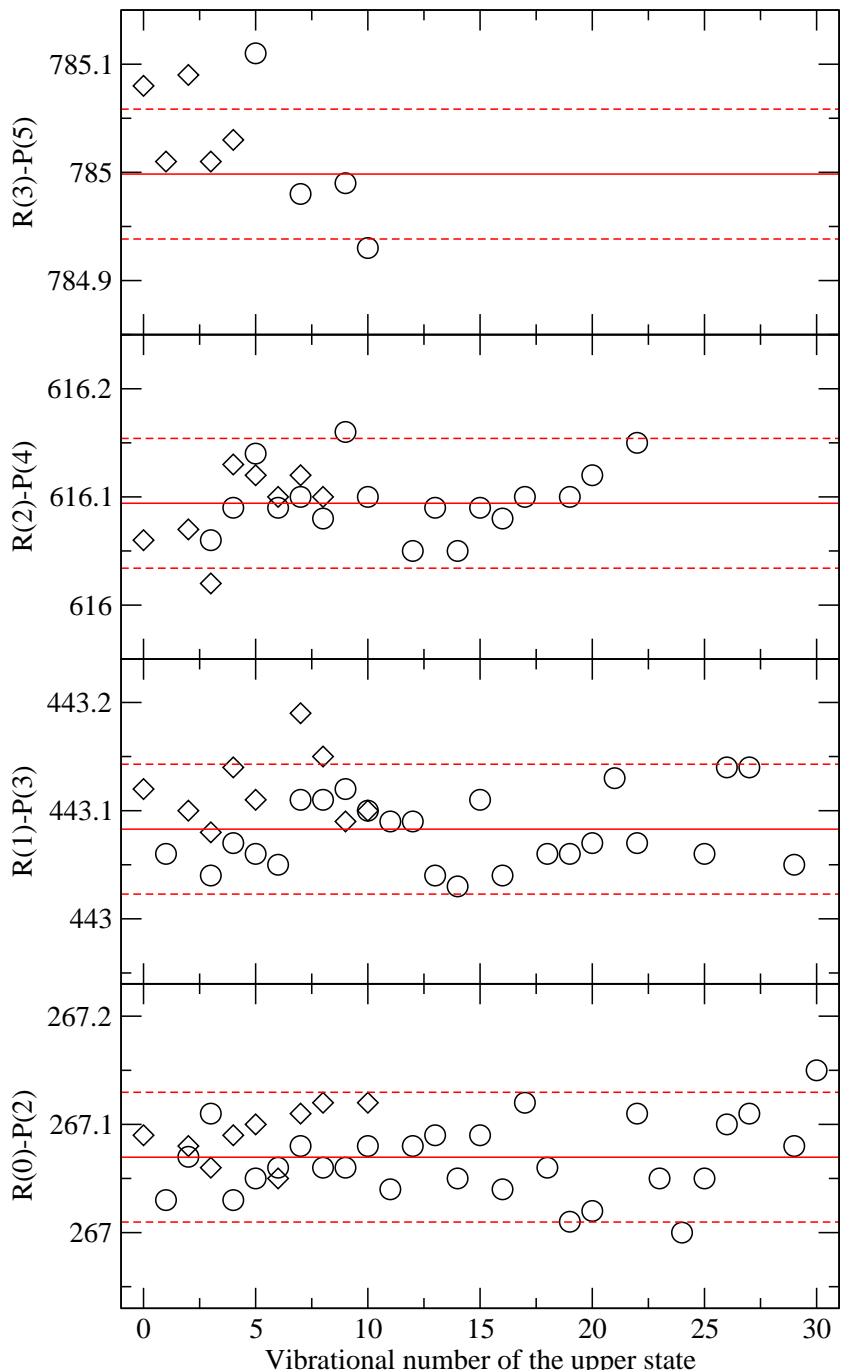


Figure 3. Combination differences, *i.e.* differences between $R(J)$ and $P(J + 2)$ transition frequencies, as constructed from the results of Table 2 and Table 3. Values are compared to the $\Delta J = 2$ splittings as accurately known from far-infrared FTS [26]; this is represented by the central line. The dashed lines indicate the estimated 1σ error bars of 0.06 cm^{-1} . The X axis represents the vibrational number of the upper state. Combination differences calculated from transitions belonging to the Lyman band are shown with circles, while the ones belonging to the Werner band are shown with diamonds.

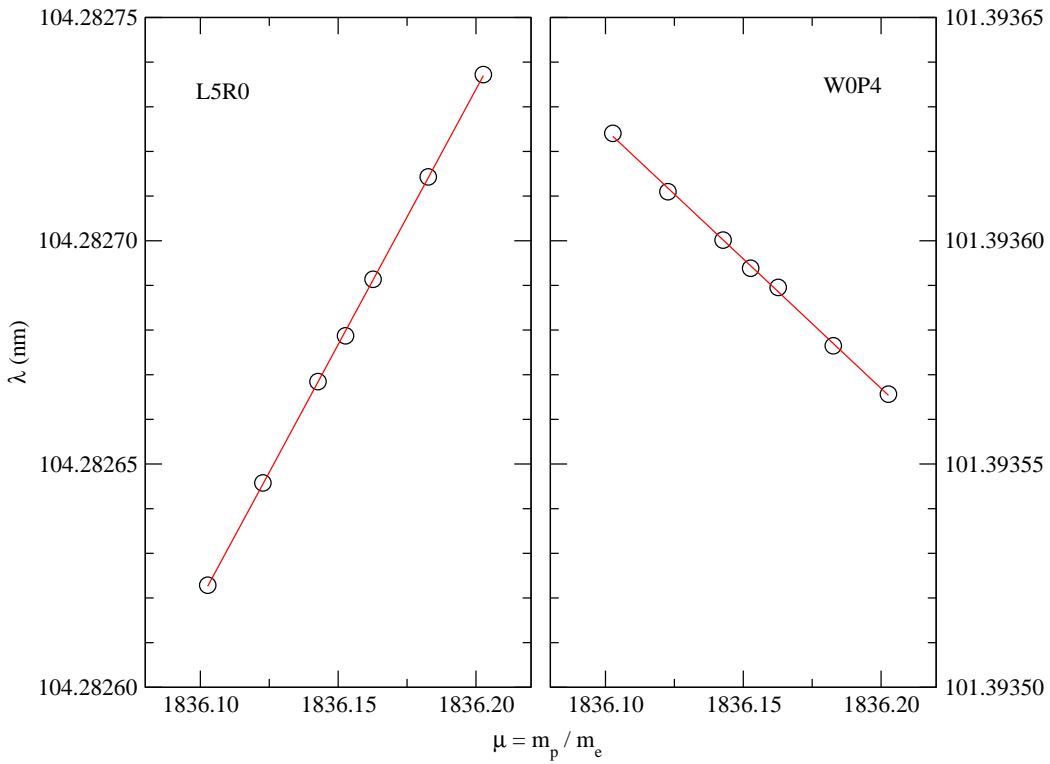


Figure 4. The wavelengths of the $B^1\Sigma_u^+(v=5) \leftarrow X^1\Sigma_g^+(v=0)$ R0 and $C^1\Pi^+(v=0) \leftarrow X^1\Sigma_g^+(v=0)$ P4 transitions were deduced using calculations based on *ab initio* adiabatic potentials for seven different values of the proton-to-electron mass ratio around the presently known value. The sensitivity coefficients K_i are deduced from the slope of the linear regression of these points.

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