Performances of G-Pisa: a middle size gyrolaser

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Angela Di Virgilio[1], Maria Allegrini[2], Jacopo Belfi[2], Nicolò Beverini[2], Filippo Bosi[1], Giorgio Carelli[2], Enrico Maccioni[2], Marco Pizzocaro[2], Alberto Porzio[3], Ulrich Schreiber[4], Salvatore Solimeno[3], and Fiodor Sorrentino[5]

[1] INFN Sezione di Pisa, Pisa, Italy

[2] Università di Pisa, and CNISM unità di Pisa, Pisa, Italy

[3] Università di Napoli, and CNISM unità di Napoli, Naples, Italy

[4] Forschungseinrichtung Satellitengeodaesie, Technische Universitaet Muenchen, Fundamentalstation Wettzell, Germany

[5] INFN Sezione di Firenze, Florence, Italy

E-mail: angela.divirgilio@pi.infn.it

Abstract. G-Pisa is an experiment dealing with a high sensitivity laser gyroscope with area of the order of $1\,\mathrm{m}^2$. It aims at improving the performances of the mirrors suspensions of the future generations gravitational wave antenna Virgo. The experimental set-up consists in a He-Ne ring laser with a 4 mirrors square cavity. The device is operational on a stable regime, with the laser operating both single mode or multi mode. The low-frequency sensitivity, $0.001-1\,\mathrm{Hz}$, is limited by the environmental noise, but it has been checked that the requirements for the Inverted Pendulum tilts control given for AdVirgo are fulfilled, ($10^{-8}\,\mathrm{rad}/\sqrt{\mathrm{Hz}}$ at $30mHz$).

PACS numbers: 04.80.Nn, 95.55.Yn, 42.55.F, 06.30.Gv, 42.79.Qx

Submitted to: *Class. Quantum Grav.*

1. Introduction

Inside the gravitational wave experimental community there is a large interest for inertial devices sensitive to rotations and tilts, necessary for active controls. AdVirgo plans to implement the tilts control for the Inverted Pendulum, which is the first stage of the SuperAttenuator suspension, designed to support and orientate the interferometer mirrors. The sensitivity requirements of AdVirgo for the IP control is usually expressed in power spectrum of the angle, and it is $10^{-8}\,\mathrm{rad}/\sqrt{\mathrm{Hz}}$ above $30mHz$ [1].
Laser gyroscopes are devices sensitive to inertial angular motion, based on the Sagnac effect: in a closed cavity rotating at angular velocity Ω the two counter propagating beams complete the path at different times. The main advantage of such devices in comparison to mechanical based system is that the coupling among different degrees of freedom is very little, since they don't have moving parts. Different kinds of such devices have been developed mainly for navigation. We distinguish between passive (fiber optic gyros) and active (ring lasers) Sagnac interferometers. Passive device measures the phase shift between the two beams, while the active one measures the frequency difference, an inherently more accurate measurement. Small fiber gyros (FOG) are typically used for navigation and have so far a resolution of $2 \times 10^{-8}\ rad/sec/\sqrt{Hz}$[2], while the large ring laser gyros used in geophysics and geodesy reach the level of 10^{-12} rad/s, and are still improving. The requirements of ADVirgo for tilt control espressed as angular velocity is $2 \times 10^{-9}\ rad/sec/\sqrt{Hz}$, a factor 10 lower than available FOG devices, which could be likely improved in the near future.
In the following we will focus on active ring laser (gyro). One application of large gyros is the monitoring of the variations of the Earth angular velocity vector. The orientation with respect to the Earth axis is important since the induced signal is proportional to the scalar product between the normal of the gyro area and the Earth axis, see equation 1. For horizontal gyros the signal is zero at the equator and maximum at the pole; at intermediate latitudes, both horizontal and vertical cavities work fine. Up to now the reached resolution is 10^{-8} of the Earth rotation rate [7, 8, 9, 10, 11].The Sagnac frequency, i.e., the beat signal between the two output beams, is:

$$\delta\phi = 4A\,\mathbf{n}\cdot\mathbf{\Omega}/(\lambda P) + \phi_\rho$$

where A and P are the area and the perimeter of the cavity respectively, λ is the wavelength of the laser beam, $\mathbf{n}$ is the normal vector of the plane of the ring cavity and $\mathbf{\Omega}$ is the induced vector of rotation. ϕ_ρ is denoting additional, usually very small, contributions to the Sagnac frequency due to non-reciprocal effects in the laser cavity, such as Fresnel drag [12] and shot noise. A laser gyro can monitor with high accuracy the orientation of the laboratory reference frame. The sensitivity of G (located in the Laser Ranging Station of Wettzell in Germany) is getting closer and closer to VLBI sensitivity providing independent measurement for the comprehension of the Earth reference frame; in poor words we can say that at the moment geodesy is the most successful application of large gyrolaser, and it is becoming a fundamental instrument for geophysics [4] as well. But it can be used as well to improve the performances of future gravitational wave antennas [3, 5, 6, 13]. Application for gravitational wave antennas detectors needs dedicated apparatus, the emphasis is more on small device, with very high duty cycle, working in an environment where large resonances due to the proper frequencies of the metallic structure are present, which in principle could spoil the sensitivity through up conversion produced by the non linear dynamic of the laser. The large ring laser gyros built by the joint ring laser working group in New Zealand and Germany have sides of the order of several meters. "G" [14, 15] located at the Geodetic Observatory in Wettzell (Germany) is a monolithic square with 4 m sides, "UG2", a rectangle with 40 m by 20 m sides, is the largest ring[16]. In principle the larger the area the better the sensitivity, but the best gyro so far, is "G", which is operating very close to the quantum limit, and its measured noise power spectrum is of the order of 10^{-12} rad/s/$\sqrt{\text{Hz}}$, with a duty cycle close to 100%. The Allan deviation has not shown any systematic effects on a time scale of about 3 hours, and the sensor drift is normally below 1.5 parts in 10^8 of the Earth rotation ($1.1 \cdot 10^{-12}$ rad/s). Among the different instruments developed by the German NewZealand group, there is a very compact and flexible mechanical design, called GEOSENSOR, espressely design to be transportable. Existing GEOSENSORS are used mainly for geophysics, and have sides of 2 m, which is considered too large to be implemented inside a suspension. G-Pisa is based on the GEOSENSOR design, has been built by a INFN, University and CNISM of Pisa and Naples colaboration, financed by INFN commission V in order to learn the technique for future application in Virgo and for General Relativity tests. For G-Pisa, the GEOSENSOR design has been changed in order to be scalable down to 0.9 m, further scaling of the device is in principle feasible, but a new mechanical design is necessary. In the following section the limits in sensitivity due to shot noise are discussed. The third section describes the experimental apparatus. The fourth section discusses the results in sensitivity to be compared with the AdVirgo requirements. At the end the conclusions come, with considerations about our near future plan.

2. Sensitivity limits

In large gyros the shot noise of light gives the fundamental limit to sensitivity:

$$\Omega_{sn} = \frac{c}{2\pi\, K\, L} \sqrt{h\, \nu\, \mu \frac{T}{2P\, t}}$$

where c is the speed of light, L the side of the square ring, h the Plank Constant, ν the frequency of the light, μ the total cavity losses, T is the transmmision of each mirror, P is the total radiation power exiting from the cavity, t the observation time, and K is the scale factor of the instrument, which depends on geometry and wavelength, whose value in a square cavity at a wavelength of 632.8 nm is $1.58 \times 10^6 \times L$. In figure 1 the shot noise limit is shown for various values of the parameters μ, T and P and an observation time of 1 s.

For the continuous line (good mirrors, but not the best ones) $\mu = 40$ ppm, $T = 0.2$ ppm and $P = 10^{-8}$ W, for the dotted line absorption has been reduced to

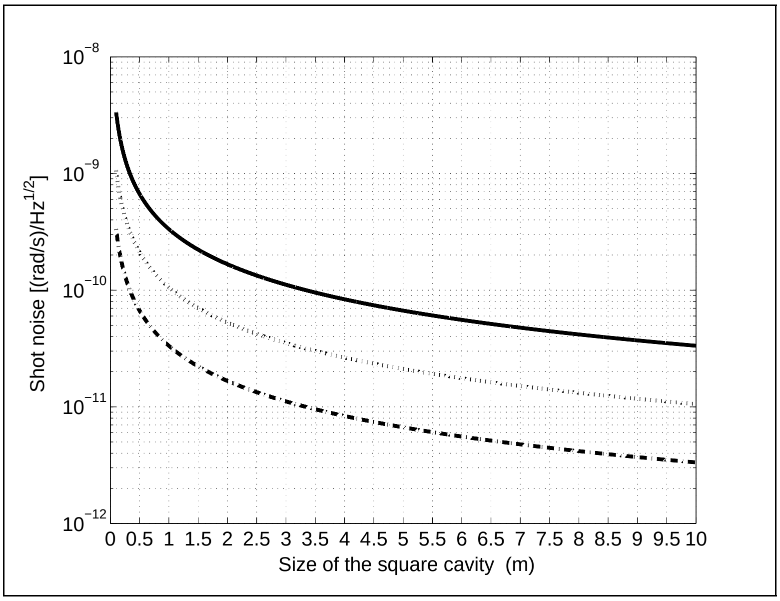

Figure 1. Shot noise limit as a function of the square cavity side. The three different traces correspond to sets of mirrors of different quality. Continuous line absorption $\mu = 40$ ppm, transmission $T = 0.2$ ppm and power $P = 10^{-8}$ W, dotted line $\mu = 4\,ppm$, point-dotted line $T = 10^{-7}$

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4 ppm, and for the point-dotted line the transmitted power has also been increased to 10^{-7} W (top quality mirrors). It should be noted that with equivalent mirror quality the laser cavity losses increase by decreasing its length; as a consequence for very small rings it becomes more difficult to obtain reasonable high output power. As a fact, for a ring side of the order of 1 m or lower, it would be unlucky to have an output power of the order of $10^{-8}\,W$, independently from the mirror quality. In short, a device with L below 1 m could reasonably reach a sensitivity of 10^{-9} rad/s/$\sqrt{\text{Hz}}$, while to reach 10^{-11} rad/s/$\sqrt{\text{Hz}}$ devices larger than 2 m are required. Backscattering-induced frequency pulling and lock-in pose severe limitation to the ring laser performances. It is usually avoided by introducing a bias, which separates the wavelengths of the two counter-propagating laser modes. The Earth rotation can be used in order to give the necessary bias. The parameter which sets the magnitude of the mode pulling is the lock-in threshold frequency l, where $l \approx c\, s\, \lambda\, / (\, \pi\, d\, P\,)$, where c is the speed of light, s is the fraction of the laser field amplitude which is scattered by each mirror, λ is the laser wavelength, d is the beam waist and P is the ring perimeter.

In figure 2 the dashed lines show the lock-in limit as a function of the side of a square ring, for a beam waist of 0.5 mm and different values of of the scattering coefficient s. The continuous line shows the Sagnac frequency given by the Earth rotation for a device horizontally located at latitude 43° as a function of the ring size. In general the lock-in problem, fig. 2, poses more severe limits at the size of a gyrolaser with the requirements given for AdVirgo, and a device with side at least 1 m is necessary, at least until the mirrors losses are not substantially decreased. Larger perimeters ring

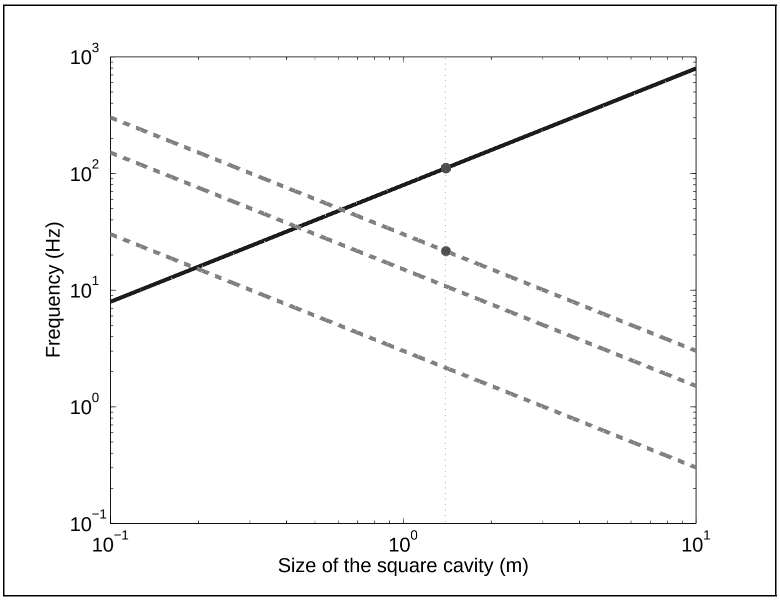

Figure 2. Continuous line shows the Sagnac frequency, the three dashed lines show the lock-in threshold frequency for three different set of mirrors (from bottom to top: s=10^{-4}, $5{\cdot}10^{-4}$ and 10^{-3}). Highlighted intersections represent the G-Pisa case, $s = 10^{-3}$.

has several advantages: larger cavity provides more powerful laser, since the Earth bias depends on the relative alignment of the ring with respect to the Earth rotational axis, a larger ring allows higher flexibility, i.e. there is larger choice of how and were locate the instrument, a larger volume of gas provides a long term stability of the gas itself. For this reasons 1 m side seems a reliable choice, while 0.5 m side seems risky. The sensitivity requirements for our application is not as high as top quality gyrolaser, but, in term of sensitivity and bandwidth response, it is not in the range of ordinary commercially available inertial sensors. As it has been said in the introduction G-Pisa has been financed in order to learn the technique and study possible application, it has not been so far part of AdVirgo program, implementation of this instrument for AdVirgo is a purely engineering problem: given the available space and the relative orientation with the Earth axis it is possible to provide a mechanical design. In order to fit inside the available space such ring could be rectangular more than squared, the real parameter being the perimeter, but the square device is the optimal one, since in this case the ratio $perimeter/area$ is minimum, and the device is more symmetric in general.

3. Experimental set-up

G-Pisa is a square cavity 5.60 m in perimeter and 1.96 m^2 in area. The mechanical design is flexible and each side of the square can be scaled from 1.40 m down to 0.90 m with minor changes. The mechanical system is mounted onto an optical table and has a stainless steel modular structure: 4 boxes, located at the corner of the square and containing the mirrors holders inside, are connected by tubes, so to form a ring vacuum chamber with a total volume of about $5 \cdot 10^{-3}$ m^3. The vacuum chamber, is entirely filled with a mixture of He and a 50% isotopic mixture of ^{20}Ne and ^{22}Ne. The total pressure of the gas mixture is set to 560 Pa with a partial pressure of Neon of 20 Pa. In the center of one of the tubes there is a Pyrex insertion, a capillary with 4 mm internal diameter, approximately 15 cm long, which is the discharge tube. Capillary internal diameter has been chosen in order to favor selectively $TEM00$ cavity mode excitation. While the discharge in the laser medium of "G" and analog systems is excited by a RF source, where two coils couple the RF oscillator to the gas, in our system we choose a capacitive coupling. Two halves of a copper cylinder are used as electrodes and are part of the resonant circuit of the RF source. The laser medium in this way is included in the active circuit and the fluctuations in the plasma density do not affect the coupling of the RF source to the discharge, but only the oscillator frequency, about 115 MHz. This kind of discharge provides a very good passive stability and made possible to regulate the laser output power very close to the laser threshold since the first runs. The discharge is 5 cm long, but different lengths will be tested in the next months to minimize the effect of plasma intensity fluctuations around the laser threshold. The discharge tube has four micro-metric screws used to align the Pyrex capillary with the mirrors and the optical cavity.

Four spherical mirrors with 6 m radius curvature were chosen for the resonator, and two micro-metric lever arms acting on the tilts of each mirror, make it possible a fine tuning of the cavity alignment. Mirrors reflectivity is optimized for the emission line around 632.8 nm. The free spectral range of the cavity is 53.6 MHz, the horizontal beam waist is 0.68 mm, the sagittal beam waist 0.56 mm and the intra-cavity ring-down time is 20 μs. In order to achieve long term stability of the perimeter the laser gyro optical frequency will be locked to a reference laser. This will involve the measurement of the radio frequency beat note between the gyrolaser output and the reference laser. For such application the capacitive coupling will introduce less noise than the inductive one. The two outputs (clockwise and counter-clockwise sense of circulation) from one cavity mirror are combined by means of a 50% intensity beam splitter and detected by a photodiode. The photodiode current is voltage converted by a trans-impedance stage with a gain of 10^9 and 1 ms rise time. The two single beam outputs are also monitored by means of two fiber-coupled photomultipliers. The laser modal structure has been detected injecting the output beams in a high finesse linear cavity. The signals are acquired and analyzed off-line. Fig.3 shows a picture of the apparatus.

4. Behavior of the gyrolaser signal and sensitivity measurements

In the present set-up our instrument is basically free running, this means that because of thermal expansion it exhibits different regimes: normal single-mode operation, split mode and chaotic regime. For thermal expansion the perimeter changes and the laser sometime has to change the number of wavelengths contained in the perimeter (mode

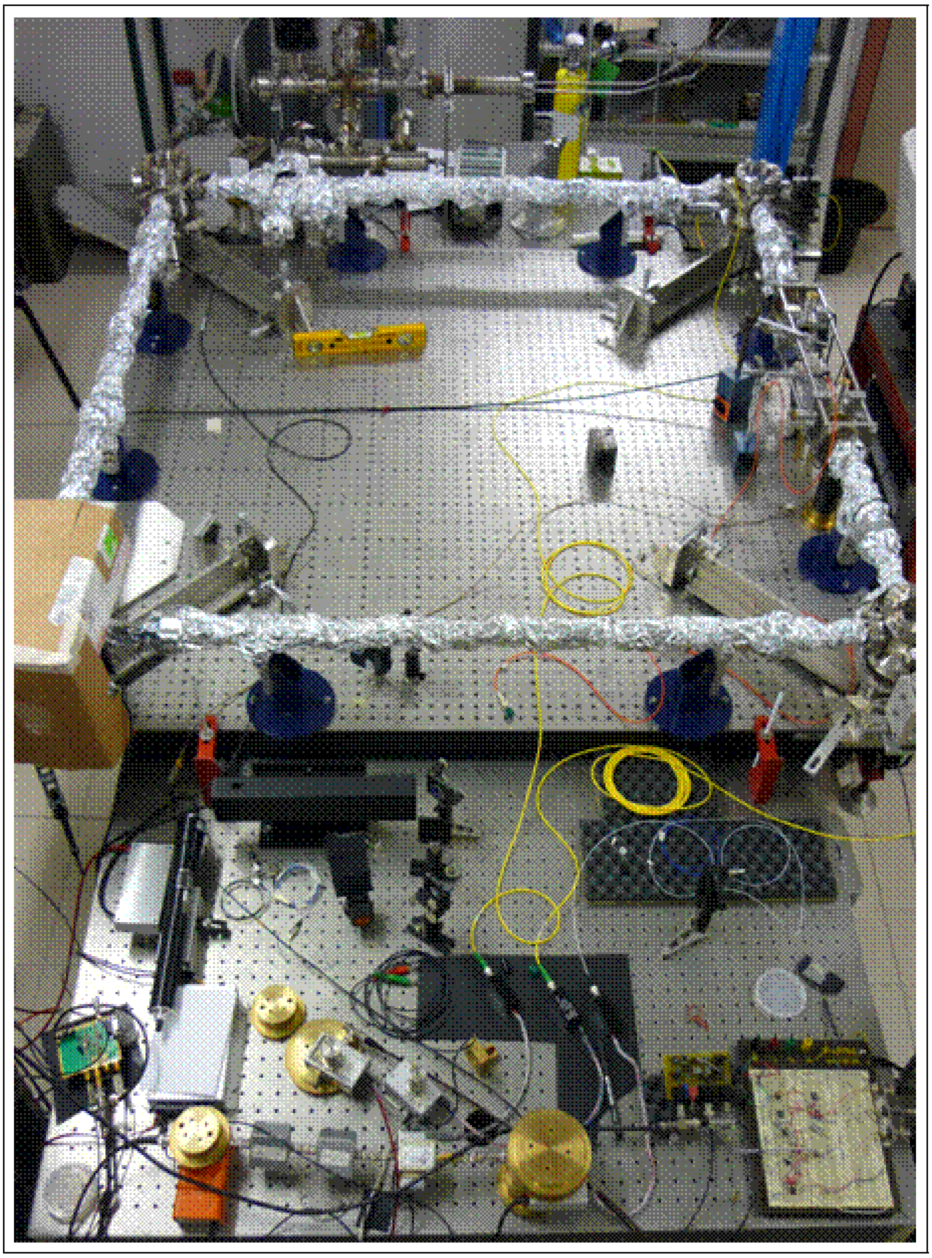

Figure 3. The G-Pisa apparatus. The G-Pisa apparatus is on top of a standard breadboard, optical fibers are used to handle signals, and the laser used as reference to actively control the perimeter is visible.

jumps). Sometime the two counter propagating modes are separated by a free spectral range, which is 53.6 MHz for the present set up of G-Pisa. In this regime (split mode) the instrument could be as well useful, but requires a much different analysis and data acquisition since the beat note is as high as the free spectral range plus or minus the Sagnac frequency[16], and the clockwise or anticlockwise mode can be split. Increasing the discharge voltage it is possible to operate the laser in single mode or multi mode. It has been observed stable operation up to 4 longitudinal modes. A detailed description of the behavior of the apparatus is given in refs. [18, 19]. Mode jumps and splits can be easily avoided with thermal stabilization and with the perimeter active control, which we plan to implement in the near future. In the following the focus will be on the normal operation and relative sensitivity. G-Pisa is located in a very noisy environment without thermal control. Typically it works in normal operation for $10-20$ minutes before a mode jump takes place, and from time to time we observe a split mode, which persists usually for some minutes, until both beams return on the same longitudinal mode and then the standard operation and Sagnac signal are recovered. Fig. 4 shows a tipical raw signal, approximately 6 minutes time span.

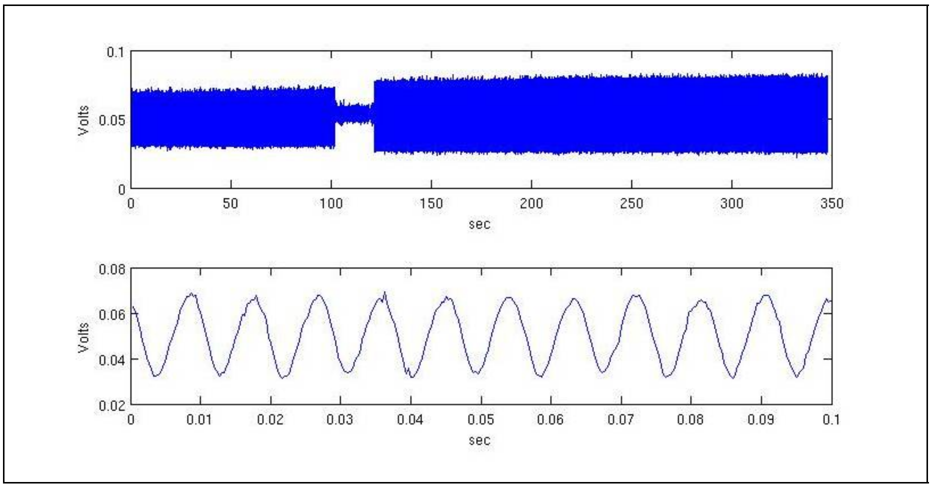

Figure 4. Standard operation Sagnac signal. After approximately 100 *sec* a mode jump of one of the two Laser mode takes place and for about 20 *sec* the instrument is blind. In the bottom figure, 0.1 *sec* time span is shown and the beat note is well visible.

The rotational sensitivity is obtained reconstructing the phase of the beat note, and differentiating it, in order to obtain the angular velocity. The mean value of this signal gives the Earth rotational speed, and it has been checked that this mean value is compatible with the Earth rotation and the latitude in Pisa. To evaluate the sensitivity the mean value is usually subtracted. The power spectrum of the signal makes the estimate of sensitivity, which is the relevant parameter for the possible improvements of the gravitational waves interferometer suspension; since G-Pisa especially at low frequency is limited by environmental noise it has to be considered an upper limit, and is natural to take the best measurement taken in a quieter environment. Typical spectrums are reported in fig. 5. The horizontal line is the expected shot noise limit, the transverse line shows the requirement for the Virgo suspensions [1], expressed as angular velocity. Three different measurements are shown, taken at different time and in different conditions. The blue line was one of our first measurements, and the large structure around $7Hz$ was due to the resonance of the legs of the optical table supporting the ringlaser. After the first set of measurements the optical table legs have been fixed to the floor and the table has been as well seismically isolated with a set of pneumatic dampers. The green curve shows a typical spectrum, taken during the day, when there is a lot of activity around the laboratory right inside the Department of Physics of the University of Pisa, which is located in the town center. This spectrum shows a very large peak around $2Hz$ which has been proved to be due to a horizontal rotation resonance of the table itself. The level of this peak depends of course from the environmental activity. We have done a very long, unattended, measurement all the night long, with low acquisition rate; from this long run the pieces in which the system was optimally working have been extracted, analyzed, and among them the spectrum with the lowest profile below $1Hz$ is shown in figure in red. It correspond to 2 o'clock in the morning and shows that the measured sensitivity of G-Pisa is even better than the AdVirgo requirements [1]. We note that the set of mirrors used for these preliminary tests were not "top quality" mirrors (from ring-down measurement the mean loss of these mirrors have been evaluated to be of the order of 4×10^{-5}). A set of top quality mirrors will be installed in the near future, accordingly improvent of the performances of G-Pisa is expected. It is important

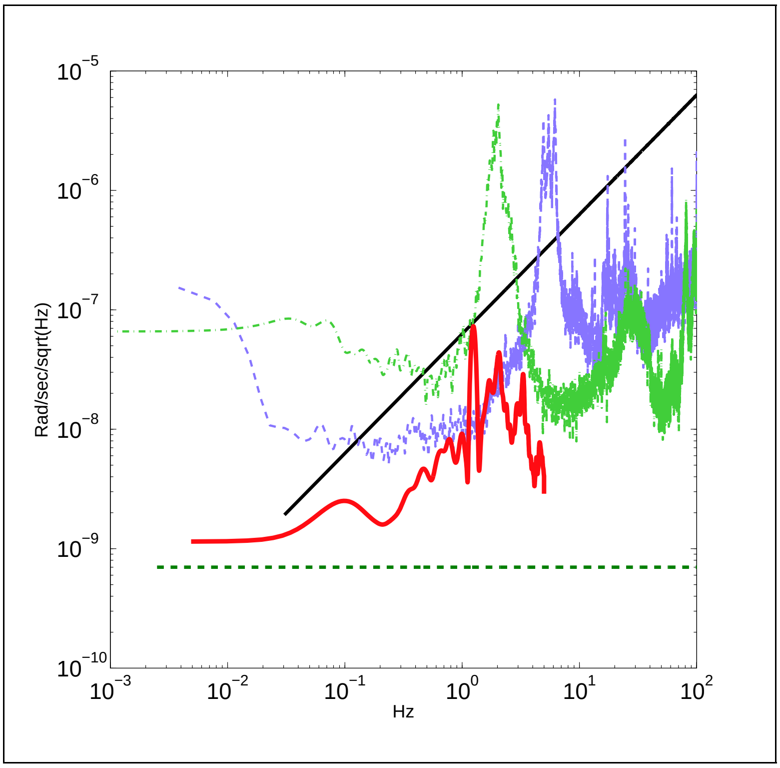

Figure 5. Comparison between the best low-frequency measurements. Light blue spectrum and green spectrum refer respectively to the case of rigid and passively air-damped optical table. The red curve shows the best measurement obtained at night, in a quiet environment. The horizontal dotted line is the expected G-Pisa shot noise, the transverse line shows the AdVirgo requirement for IP tilt control.

to remind that the sensitivity measured with the 4 m side gyrolaser G, located in Wettzel (Germany), is more than a factor 1000 better than the measurements shown in fig. 5. By means of a simultaneous measurement of rotational noise, performed with the G-Pisa gyrolaser, and translational noise obtained by a three axial linear accelerometer, it was possible to set an upper limit to the correlation between rotations and translations to a level of 0.5% [6]. The perimeter control has been successfully closed by moving one of the 4 mirrors using a piezo, showing that controlling the perimeter G-Pisa runs continuosly in standard operation, mode jumps and splits have not been observed so far. Acting on a single mirror, the relative phase bteween the backward scattered radiation from the different mirrors is affected in different ways. Because the coupling between the two counterpropagating beam is given by the interferometric sum of the single backscattering sources, the lock in frequency can be strongly affected by this correction[19].

5. Conclusions

The gyrolaser G-Pisa is operational since one year. Interruptions of the normal operation are due to thermal expansion induced mode jumps and split mode regime. The preliminary active perimeter control of G-Pisa has shown that the ringlaser can run continuously, whitout interruptions.

The low frequency measured power spectrum (below 1 Hz) is typically around $10^{-8}\,(\mathrm{rad/s})/\sqrt{\mathrm{Hz}}$, which looks like to be real motion. In very quiet environment sensitivity measurements down to $10^{-9}\,(\mathrm{rad/s})/\sqrt{\mathrm{Hz}}$ have been obtained, which is much better than the limit needed to control the tilts of the Virgo suspensions, planned for AdVirgo. A device with perimeter 4 m is adequate for this purpose, a design with rectangular shape rather than square is feasible in order to fit inside the available space. A gyrolaser is a device more sensitive than the present requirements of AdVirgo, it cannot be excluded that in a very near future a relatively small and compact fiber baser Sagnac gyro (FOG) can fulfill the requirements.

Acknowledgments

We have to acknowledge the encouragement given by Armando Reale, who has given great support to our work. We have to mention Antonio Pasqualetti and his crew at EGO, Roberto Cosci and Riccardo Macchia, for the help in setting up the whole vacuum circuit, and Francesco and Mario Francesconi, from the University of Pisa, for the help in the electronics development. Special thanks goes to Gabriele Balestri, Andrea Di Sacco, Pino Fausto and Alessandro Soldani, INFN-Pisa, for the help necessary to realize the mechanical support.

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