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## Strength by Atomic Force Microscopy (A Kelly special issue)

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► **To cite this version:**

Kevin Kendall, Aman Dhir, Chin Yong. Strength by Atomic Force Microscopy (A Kelly special issue). Philosophical Magazine, 2010, pp.1. 10.1080/14786430903520732 . hal-00586129

**HAL Id: hal-00586129**

**<https://hal.science/hal-00586129>**

Submitted on 15 Apr 2011

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**Strength by Atomic Force Microscopy (A Kelly special issue)**

Journal:	<i>Philosophical Magazine &amp; Philosophical Magazine Letters</i>
Manuscript ID:	TPHM-09-Aug-0348.R1
Journal Selection:	Philosophical Magazine
Date Submitted by the Author:	10-Nov-2009
Complete List of Authors:	Kendall, Kevin; University of Birmingham, Chemical Engineering Dhir, Aman; University of Birmingham, Chemical Engineering Yong, Chin; Daresbury Lab, Computing
Keywords:	atomic force microscopy, fracture, indentation testing, molecular dynamic simulations
Keywords (user supplied):	





1 than compressive measurements. In conclusion, water contaminating the oxide surface in AFM  
2 strength testing is structured. Water layer squeezing removal can be predicted by molecular  
3 modelling which may be verified by AFM experiments to show that water can influence the  
4 strength of perfect crystals at the nanometer scale.  
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8 Key words:- AFM; molecular dynamics model; MgO; water squeezing.  
9

## 10 1. Introduction 11

12 In the book Strong Solids, Kelly and Macmillan [1] discussed the highest stress that could be  
13 withstood by a perfect material such as a single crystal of NaCl or MgO following the original  
14 calculations of Zwicky [2] and described the idea that a nanometre scale indenter would be likely to  
15 locate a region that was locally free of defects such as cracks or dislocations, leading to the idea of  
16 AFM strength testing of perfect crystals. Bowden and Gane [3] had pioneered such experiments  
17 using flat ended indenters inside a scanning electron microscope (SEM). Further work on spherical  
18 indentations in materials such as {100} MgO by Macmillan and Gane [4] showed that there was a  
19 sudden plastic indentation at a high load as the tip broke through the contaminant layer which is  
20 omnipresent inside SEM chambers [5,6]. They used the Hertz theory of elastic contact to interpret  
21 their results whereas Kelly had been interested in using molecular models to derive the maximum  
22 strength using a stress criterion of failure. Experimental AFM tips are normally supplied with a  
23 nominal tip radius down to 2nm, suggesting that the atomic facet making contact could be about  
24 4x4 atoms, so that Hertz theory of contact is not applicable. Moreover, a dynamic atomic theory of  
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Recently there has been much interest in the molecular interpretation of AFM experiments,  
especially using molecular dynamics computer simulations to provide a more satisfactory theory of  
strength than the models given in chapter 1 of Strong Solids. For example, a flat-ended MgO probe  
contacting a clean MgO crystal was analysed by Yong, Smith and Kendall [7-9] and an NaCl probe

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1 contacting an NaCl slab was described by Kendall, Yong and Smith [10] using the DL POLY code  
 2  
 3 which has been much used in atomic scale simulations [11]. The purpose of this paper is to review  
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 5 the AFM strength measurement using molecular simulations, then to look at the effects of probe  
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 7 size, shape and plasticity while finally considering the effect of contaminant layers on the crystal  
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 9 surfaces.

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10 Four steps are necessary in the atomic model:

- 11 a) defining acceptable interatomic potentials
- 12  
13 b) adding potentials together for all the atoms in the system, assuming the total energy in  
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15 the system to be built up from pairwise addition of constituent atom-atom interactions  
 16  
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 18 c) calculating thermal motions of the atoms to take the dynamic nature of the system into  
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20 account.
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22 d) Working out the equilibrium condition for a range of AFM scenarios, including surface  
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24 contamination.

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26 Previous theories of solid surface interactions under water have been dominated by  
 27  
28 DLVO continuum theory (see Ref. 18) which deals with extended surfaces at relatively  
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30 large separation, balancing ionic repulsions between charged double layers against the  
 31  
32 van der Waals attraction. The aim of this paper is to progress to atomistic modelling,  
 33  
34 ignoring double layer ionic effects in the first instance.

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## 35 36 37 2. Model set-up; clean surfaces

38 The probe and slab set-up is shown in Fig 1. The slab consisted of 28x28 rows of either NaCl  
 39  
40 or MgO lattice. The Na<sup>+</sup>-Cl<sup>-</sup> inter-ionic spacing was 0.279 nm, while for MgO, the Mg<sup>2+</sup>-O<sup>2-</sup>  
 41  
42 inter-ionic spacing was 0.2104 nm. Periodic boundary conditions were applied in the x-y  
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44 (horizontal) direction to mimic an infinite crystal surface with the (100) surface oriented at the  
 45  
46 z (vertical) direction. A small rectangular probe of 6 layers thick was constructed and this was  
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48  
 49 varied in cross-section from the smallest possible 2x2 shown in Fig 1 to 18x18 atoms to  
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1 simulate increasing size of the AFM probe. Alternatively, pyramidal probes were constructed  
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 3 with varying contact areas from 2x2 to 10x10 atoms. These probes are small enough to ensure  
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 5 that they do not interact with its image neighbour in the periodic boundary conditions.

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7  
 8 Fig 1 Schematic of the smallest 2x2 probe approaching a crystal slab. The probe was  
 9 moved towards the slab by displacing the probe rigid layer downwards, keeping the  
 10 slab rigid atoms fixed. The free atoms could then find their equilibrium positions  
 11 while the bath atoms maintained the temperature at 300K.

12  
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 14  
 15 The layers of atoms were classified into three different groups as shown in Fig 1. The first  
 16 three layers of atoms, labelled free, near the contacting surfaces where commensurate contact  
 17 was to take place were allowed to move freely to reach their equilibrium positions. No  
 18 constraint was placed on these outer layers of atoms and this ensured that the natural outcome  
 19 of the atomic configurations at the surface was entirely due to the interatomic adhesion forces.  
 20 However, the fourth and fifth layers of atoms were coupled to the Berendsen et al [12] heat  
 21 bath to maintain the temperature of the whole system at 300K. The final layer of atoms,  
 22 labelled rigid, was held fixed and gradually displaced to push the nanoprobe towards the  
 23 surface. The initial gap between the surface slab and the probe was a vertical distance to the  
 24 (100) surface plane,  $d_z$ , of around 1.5nm and this was gradually closed, thereby increasing the  
 25 probe interaction with the slab. The surface slab and probe were orientated such that they were  
 26 in commensurate contact. In each step when the probe position is updated, the whole system is  
 27 allowed to equilibrate before the forces experience by the rigid probe along the z-component,  
 28  $F_z$ , is being sampled. This corresponds to an approach rate of  $6 \cdot 10^{-4} \text{ ms}^{-1}$  for equilibration  
 29 before the interaction force is calculated. The whole process was repeated for different  
 30 distances so that a force profile of surface interactions was obtained.

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### 3. Results for clean surfaces

1 In several papers [7-9] the equilibrium was calculated for each incremental step as the contact  
2 process occurred. A still picture from the movie for NaCl just before the point of complete  
3 fracture is shown in Fig 2, but this does not reflect the true situation because all the atoms are  
4 in continuous motion. A movie is available at  
5 <http://www.fuelcells.bham.ac.uk/media/nacl-md.shtml>, showing all the atoms  
6 vibrating around their equilibrium positions as the nanoprobe approaches and then retracts  
7 from the NaCl slab.  
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20 The potential chosen for this simulation contained three terms,  
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$$w = -e^2/r - C/r^6 + A \exp(-r/\rho) \quad (1)$$

22 where  $e$  is the electron charge,  $r$  is the distance between atoms and  $C$  relates to the second-  
23 neighbour van der Waals interaction. The parameters  $A$  and  $\rho$  relate to the repulsive ionic core  
24 interactions. These constants are fitted empirically to the experimentally determined properties  
25 of NaCl such as elastic constants and crystal lattice parameters [13]. The first term is the  
26 electrostatic attraction between Na and Cl ions, the second the van der Waals attraction and the  
27 third term is the repulsion between the ions, the last two terms comprising the well-known  
28 Buckingham potential.  
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39 Fig 2 Molecular dynamics model of a sodium chloride 8x8 atom probe approaching a  
40 slab of NaCl to form new bonds with the surface atoms  
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43 For Fig 2, the potentials were added pairwise, evaluating the long-range electrostatic potentials  
44 by 3D periodic Ewald summation using the partial charge values of  $\pm 0.988$  for Na and Cl  
45 ions. Then, atomic trajectories were solved by the Verlet leapfrog algorithm with a fixed time  
46 step of 0.5fs. Initially, all moveable atoms were assigned initial velocities from a Gaussian  
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1 distribution equivalent to a temperature of 300K. The system was then allowed to equilibrate  
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 3 until a stable mean configurational energy was achieved, usually taking about 80 ps.  
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 7 A typical force versus distance curve for the 8x8 NaCl probe is given in Fig 3. The probe  
 8  
 9 movement started on the right as shown by the bold line and it was clear that there was near  
 10  
 11 zero force of attraction at this stage. The probe was then moved towards the slab until an  
 12  
 13 attractive force was experienced.  
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 16 Fig 3 Force per ion versus distance curves for approach from right to left  
 17 and withdrawal of the 8x8 NaCl nanoprobe showing the jump to contact  
 18 and the equilibrium at zero force  
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 22 Then a sharp change in  $F_z$  was observed, the 'jump to contact'. Further displacement caused  
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 24 the force to approach zero, the equilibrium contact position. Subsequently, the probe was  
 25  
 26 compressed as it was pushed into the slab giving elastic indentation to the left of Fig 3. The  
 27  
 28 withdrawal was essentially reversible but the 'jump from contact' or fracture of the bond was  
 29  
 30 slightly delayed, indicating cohesion hysteresis, although the strength was essentially the same.  
 31  
 32 This indicates that strength should be calculated equally on both make and break of the bonds.  
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 34 By changing the size of the nanoprobe, the average work of cohesion  $W$  in joules per square  
 35  
 36 metre could be calculated from the model and compared with the breaking stress (ie pull-off  
 37  
 38 force /contact area) in GPa as shown in Table 1.  
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 40

41 Table 1 Work of cohesion  $W$  and average breaking stress for the different size NaCl probes

Contact size	area/nm <sup>2</sup>	W/ Jm <sup>-2</sup>	stress/GPa
(2 × 2)	0.3114	0.47	4.03
(4 × 4)	1.2455	0.48	3.06
(6 × 6)	2.8023	0.44	2.55



1	(8 × 8)	4.9818	0.45	2.42
2				
3	(10 × 10)	7.7841	0.45	2.38
4				
5	(14 × 14)	15.257	0.44	2.08
6				
7	(18 × 18)	25.220	0.43	2.03

8  
9 It can be seen that the work of cohesion remained almost constant, as assumed in the  
10 continuum theory of fracture [14] but the stress decreased as the AFM probe got bigger as  
11 expected from fracture mechanics theory. In other words, the stress criterion of fracture  
12 assumed by Kelly does not apply in this model. In addition, it may be seen that the energy is  
13 dominated by the electrostatic forces for NaCl; a van der Waals probe contact would have W  
14 around  $0.1\text{Jm}^{-2}$ . The maximum strength was calculated to be 4.03 GPa compared to 2.4 GPa  
15 calculated in the book Strong Solids.  
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#### 24 **4. Elastic and plastic deformation**

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26 The 8x8 rectangular NaCl nanoprobe behaved elastically and separated cleanly despite the  
27 large attractive interatomic forces. More commonly, for MgO and also for pyramidal probes,  
28 the forces rose so high as the separation occurred that the atoms were displaced from their  
29 normal positions and irreversible plastic deformation took place. Fig 4 shows the computed  
30 results for a stepped NaCl nanoprobe, of contact size 8x8 in contrast to a stepped probe with  
31 contact size of 4x4. As stress was applied to the 8x8 contact (Fig 4 top), separation did not  
32 occur, but the step acted as a defect which promoted plastic deformation, allowing the NaCl  
33 crystal probe to extend in line with the applied force. The smaller contact (Fig 4 bottom) also  
34 began to deform plastically, but separation then took place at the interface such that the  
35 nanoprobe, was released but extra energy was expended in creating a plastic defect hole in the  
36 probe. This model shows that there should be an elastic/plastic transition for larger  
37 nanoprobes, such that material transfer from the probe to the slab occurred. By modelling  
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1 [increased contact sizes of NaCl pyramidal probes \[8\], it was shown that small contacts eg 2x2](#)  
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 3 [were brittle but larger contacts eg 8x8 became plastic as the nanoprobe was pulled off.](#)  
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 7 Plastic deformation could also be induced by preloading the probe in compression such that  
 8  
 9 plastic collapse occurred at high force. This introduced defects into the probe, causing  
 10  
 11 subsequent plastic flow when the probe was withdrawn [8].

12 Fig 4 (top) Major plastic deformation observed in the 8x8 contact model of the  
 13 pyramidal NaCl nanoprobe.  
 14 (bottom) Results for 4x4 NaCl contact show clean detachment with minor plastic  
 15 deformation  
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## 21 **5. Influence of plastic flow on strength**

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 23 The influence of the plastic flow on the observed strength measurement could be studied by  
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 25 comparing the reversibility of the force curves during jump to contact then pull-off. Fig 5  
 26  
 27 shows the force distance curves computed for the pyramidal NaCl probe shown in Fig 4  
 28  
 29 (bottom). The jump to contact during approach caused no damage to the lattice structure and  
 30  
 31 the strength calculated [by dividing the total z-component force in the base of the probe by the](#)  
 32  
 33 [area of the contact](#) was 3.6 GPa. This was somewhat higher for the pyramidal probe than that  
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 35 calculated for a flat 4x4 NaCl probe seen in Table 1 which gave a strength of 3.1 GPa.

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37 Fig 5 [Force per ion in 10x10 rigid layer vs displacement curve for pyramidal 4x4 NaCl](#)  
 38 [probe. The jump to contact appears perfectly elastic but the pull-off dissipates energy without](#)  
 39 [raising the force significantly. The stress required for compressive collapse was much higher.](#)  
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Deleted: Force per ion vs displacement curve for pyramidal 4x4 NaCl probe. The jump to contact appears perfectly elastic but the pull-off dissipates energy without raising the force significantly. The stress required for compressive collapse was much higher.

41  
 42 The most significant observation from Fig 5 was that the compressive [collapse](#) strength of the  
 43  
 44 NaCl probe, 19.3 GPa, was very much higher than the tensile strength of 3.6 GPa. This is more  
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 46 like a hardness measurement in which plastic flow is required to produce an indentation,  
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 48 typically requiring three times more pressure than tensile yielding.  
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MgO showed very similar behaviour but at higher stresses and with more plastic deformation during pull-off. The 6x6 pyramidal MgO probe gave a jump-to-contact strength of 14.4 GPa without any lattice damage. On pull-off, the same stress was observed, demonstrating reversibility. But then substantial plastic deformation occurred and the jump-from-contact occurred in a series of steps with large dissipation (Fig 6) indicating increased toughness.

Fig 6 Force vs displacement curve for 6x6 pyramidal MgO probe showing that the jump to contact was perfectly elastic. The pull-off was at the same force but dissipated energy plastically. The steps in the breaking curve were due to sudden motion of defects within the nanoprobe, which remained attached to the slab.

Compression of the probe into the slab eventually caused plastic collapse at a stress of 65 GPa, showing that the compressive strength was about five times higher than the tensile strength.

In conclusion, it is evident that a number of complex processes can influence nanoprobe strength including the nature of the crystalline material, the atomic contact, its loading history, the shape of the probe, tension or compression and the propensity for plastic flow.

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## 6. Influence of surface contamination

The cohesive forces for clean NaCl surfaces were seen to be very large, leading to plastic effects and irreversibility, with adhesive energies around  $0.47 \text{ Jm}^{-2}$ . Of course, this can only be true for atomically clean surfaces, as tested in high vacuum experiments with baked out materials. In practical AFM testing, ubiquitous contamination such as nitrogen or water adsorbs on the surface and this has a very large effect of reducing the adhesive energy to much smaller values around  $0.1 \text{ Jm}^{-2}$  or even lower if thicker layers of contamination build up leading to energy and force oscillations first proposed by Kendall [15]. For example, Fig 7 shows a computational model of a pyramidal 6x6 MgO probe pushed towards an MgO slab

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1 whose surface was covered by inert gas particle spheres with xenon-like van der Waals  
 2 attributes at 100K.  
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7 Fig 7 a),b) Stills from a movie of molecular dynamics model of 6x6 MgO pyramidal  
 8 probe approaching an MgO slab coated with a monolayer of xenon molecules at  
 9 100K; c) force distance curve approaching from right to left, showing steps as  
 10 molecules are squeezed out.  
 11

12  
 13 The 6×6 MgO probe was surrounded by the Lennard Jones (LJ) xenon-like spheres and it was  
 14 immediately evident that these xenon molecules formed structured layers around the probe and  
 15 upon the slab surface, with 3 distinct layers easily visible (Fig 7, a & b). Each sphere was weakly  
 16 interacting with the surface atoms with an energy parameter of  $\epsilon = 0.02$  eV and  $\sigma = 0.305$  nm at a  
 17 temperature of 100 K. Fig. 7c shows the response of the MgO probe in the presence of the  
 18 contaminant, with the contact force increasing from right to left as the gap was squeezed. The  
 19 contamination prevented the jump-to-contact in this case but there were four significant steps; first  
 20 at 0.02nN where a slight bump could be seen, second at 0.1 nN as the third layer of xenon was  
 21 penetrated at 3.5nm; next at 0.35 nN as the second xenon layer was squeezed out at 3.2nm; and  
 22 finally at 0.9 nN as the probe collapsed plastically at high force because the first xenon layer could  
 23 not be squeezed out by the probe.  
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 36 Similar calculations had been carried out previously by Gao et al [16] but their probe, shown in Fig  
 37 8, had not been suitable for experimental study because of its infinite length. However, they did  
 38 show that the structuring phenomenon was moderated by the alignment of the solid surfaces, with  
 39 commensurate crystals showing strong liquid structuring in the model.  
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47 Fig 8 Molecular dynamics model of Gao et al [16] showing the flat parallel plate  
 48 configuration with liquid in between; the solid surfaces were infinite in the y direction.  
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1 That simulation had shown squeezing out of the contaminant molecules in discrete steps, rather like  
2 the experimental results found in mica experiments by Horn, Pashley et al [17-19]. AFM  
3 experiments have not found this effect consistently, although Lim et al [20] showed stepwise  
4 squeezing out of organic molecules such as n-dodecanol from a graphite substrate, depending  
5 strongly on the size of the AFM tip, with finer tips ( $R_{tip}=25\text{nm}$ ) giving reliable force measurement.  
6 They detected about 6 layers of molecules squeezing step-wise from the graphite, and also  
7 suggested the full tip contact with the graphite could be obtained using  $\text{Si}_3\text{N}_4$  AFM probes. Most  
8 previous experiments on this effect with water have been carried out with mica surfaces in the  
9 presence of ions [21] and this has been modelled by Leng [22] to show the repulsions associated  
10 with structured water layers. The purpose of our study was to use an AFM geometry to test the  
11 strength of MgO in the presence of water.

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## 23 **7. Simulation of water between MgO surfaces**

24 To investigate the question of how water could be squeezed out from oxide surfaces in AFM  
25 strength testing, the model illustrated in Fig 9, was set up. The baseline comparison was with clean  
26 MgO which gave the results shown in Fig 6. The calculations for clean MgO were compared to the  
27 model with 3 layers of water molecules positioned on the slab as the probe was moved downwards  
28 (Fig 9a). The potential for water interacting with MgO was derived from de Leeuw and Parker [23].

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29 The calculations showed that the jump to contact forces (Fig 9b) were much reduced by the  
30 presence of the water molecules. As the probe moved towards the slab, some water molecules  
31 jumped across the gap to cover the probe surface in a monolayer, causing a dip in the approach  
32 force curve as the gap between the MgO surfaces was fully filled with water. Then one layer of  
33 water was squeezed out as shown by the increase in force followed by a drop. Two more layers  
34 were then squeezed out at increasing force, but the final layer could not be removed in this model.  
35 On withdrawal, the force curves were not reversible but showed some hysteresis as the water  
36 penetrated back into the gap between probe and slab. It was clear that the MgO probe could now be  
37 removed from the MgO slab without any plastic deformation, which was impossible for the clean

1 surfaces. The maximum tensile stress at pull-off was 1.57 GPa compared to 14.4 GPa for clean  
2  
3 surfaces, illustrating the factor of nine weakening effect of water in tension.  
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7 Fig 9a) Pyramidal 6x6 MgO probe moving towards an MgO slab covered with 3 layers of water  
8 molecules; b) force distance curve revealing the filling of the gap then the oscillations as three layers of  
9 water were squeezed out, leaving one layer resisting removal, showing hysteresis

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11 A key question was whether the strength of the MgO was increased by the surface  
12 contaminant, as suggested in Strong Solids. To test this, the force on the probe was increased  
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14 until the MgO collapsed plastically. With water present, the collapse stress for the 6x6 MgO  
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16 probe was 9.6 GPa compared to 65 GPa for the clean probe, showing that the contamination  
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18 had given a factor of seven weakening in compression.  
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23 One of the most interesting features of this model is that there are now several zeros in the  
24 force versus separation curve, depending on the number of water molecule layers separating  
25  
26 the surfaces, intimating that the probe could appear to be in equilibrium at several separation  
27  
28 values depending on the applied force. There were three discrete equilibria at gaps of 0.5 nm,  
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30 0.75 nm and 1nm. This raises the question of colloidal stability of MgO particles in water,  
31  
32 where the  $kT$  of thermal energy of the particles will push the contacts into one of the energy  
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34 wells by squeezing out one or more water layers [24].  
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### 38 Conclusions

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40 Strength of perfect crystals can be measured in the Atomic Force Microscope if the theory of crystal  
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42 fracture and plasticity is understood. Molecular dynamics models of NaCl and MgO probes pushed  
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44 into perfect crystal substrates have been used to interpret the processes at the nanometer level for  
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46 comparison with AFM tests.  
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48 Clean surfaces of NaCl or MgO attract each other and pyramidal probes give the expected 'jump to  
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50 contact' followed by continued approach to equilibrium at zero force. This process was found to be  
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1 elastic and reversible with NaCl flat probes, showing that the nanocrystals could be pulled apart  
2 without damage and that the strength of 4.03 GPa was reversible, ie equal on approach and pull-off,  
3 though slight 'cohesion hysteresis' was observed. NaCl followed an energy criterion of fracture in  
4 this case, showing essentially brittle fracture, with strength diminishing for larger probes as  
5 expected from fracture mechanics.  
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10 Plastic flow of the NaCl probes could be encouraged by several means:- first by enlarging the  
11 contact region, second by changing the probe shape and thirdly by damaging the probe. MgO  
12 showed the same effects but differed from NaCl in that plastic flow always dominated the  
13 behaviour. Another measure of MgO strength was the probe collapse which was observed when  
14 increased compression of the probe onto the slab were made. Plastic collapse of the probe took  
15 place at a well defined compressive stress of 65 GPa, larger than the tensile strength of 14.4 GPa  
16 measured at jump to contact and pull-off.  
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26 When the MgO surfaces were contaminated with water molecules, there was a very significant  
27 change in behaviour. First, the jump to contact was now periodic as layers of molecules were  
28 squeezed out from the gap between probe and slab. Second, the process of detachment was now  
29 easier and the MgO probe could be detached at low tensile stress of 1.57 GPa without damage.  
30 Third, the strength of the MgO probe as it collapsed on severe compression into the slab was  
31 altered. The compressive strength was diminished by a factor 7 in the presence of the water  
32 molecules.  
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#### 43 References

- 44 1. A. Kelly and N.H. Macmillan, *Strong Solids*, 3<sup>rd</sup> Edition, Clarendon Press Oxford  
45 1986, pp.47-50; A. Kelly, *Strong Solids*, 1<sup>st</sup> edition, Clarendon, Oxford 1966.  
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- 48 2. F. Zwicky, *Phys Zeit* 24(1923)p.131  
49  
50  
51  
52  
53  
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56  
57  
58  
59  
60

- 1 3. N. Gane and F.P. Bowden, J Appl Phys 39(1968) p.1432.
- 2
- 3 4. N.H. Macmillan and N. Gane, J Appl Phys 41 (1970)p.672.
- 4
- 5 5. N. Gane, Proc R Soc Lond A317((1970)p.367.
- 6
- 7 6. J.B. Pethica and D. Tabor, Surf Sci 89 (1979) p.182.
- 8
- 9 7. C.W. Yong, W. Smith and K. Kendall, J Mater Chem 12(2002)p.593.
- 10 8. C.W. Yong, W. Smith, [A.Dhir](#) and K. Kendall, [Tribology Letters 26\(2007\)p.235](#).
- 11
- 12 9. C.W.Yong, K. Kendall and W. Smith, Phil Trans R Soc Lond A362(2004)p.1915.
- 13
- 14 10. K. Kendall, C.W. Yong and W. Smith, J Adhesion 81(2004)p. 21.
- 15
- 16 11. W. Smith and T. Forrester, DL\_POLY, version 2.12 (CCLRC,Daresbury Laboratory,
- 17 UK, 2001; Smith, W., (ed) *Molecular Simulation*, 32(2006) p.933.
- 18
- 19 12. H.J.C. Berendsen, J.P.M. Postma, W.F.van Gunsteren, A. DiNola, and J.R. Haak, J
- 20 Chem Phys 81(1984)p.3684.
- 21
- 22 13. C.R.A. Catlow, K.M. Diller and M.J. Norgett, J. Phys. C 10(1977) p.1395.
- 23
- 24 14. K. Kendall, *Molecular adhesion and its applications*, Kluwer Academic, New York
- 25 2001
- 26
- 27 15. K.Kendall, J Adhesion 5(1973)p.179.
- 28
- 29 16. J. Gao, W.D. Luedtke and U. Landman, Phys Rev Lett 79(1997) p.705.
- 30
- 31 17. R.G.Horn and J.N. Israelachvili, J Chem Phys 75(1981) p.1400.
- 32
- 33 18. J.N. Israelachvili, *Intermolecular and Surface Forces*, Academic Press, London
- 34 1985,pp.198-201.
- 35
- 36 19. R.M. Pashley and J.N. Israelachvili, J Colloid Interface Sci 101(1984) p.511.
- 37
- 38 20. L.T.W. Lim, A.T.S. Wee and S.J. Oshea, Langmuir 24(2008) p.2277.
- 39
- 40 21. D. Gourdon and J.N. Israelachvili, Phys Rev Lett 96(2006)099601.
- 41
- 42 22. Y. Leng, Y., J Phys Condens Matter 20(2008)354017.
- 43
- 44 23. N.H. de Leeuw and S.C. Parker, Phys. Rev. B 58 (1998)p.13901.
- 45
- 46 24. [K. Kendall](#), [A. Dhir](#) and [S. Du](#), Nanotechnology 20(2009)275701 (4pp)
- 47
- 48
- 49
- 50
- 51
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- 53
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- 57
- 58
- 59
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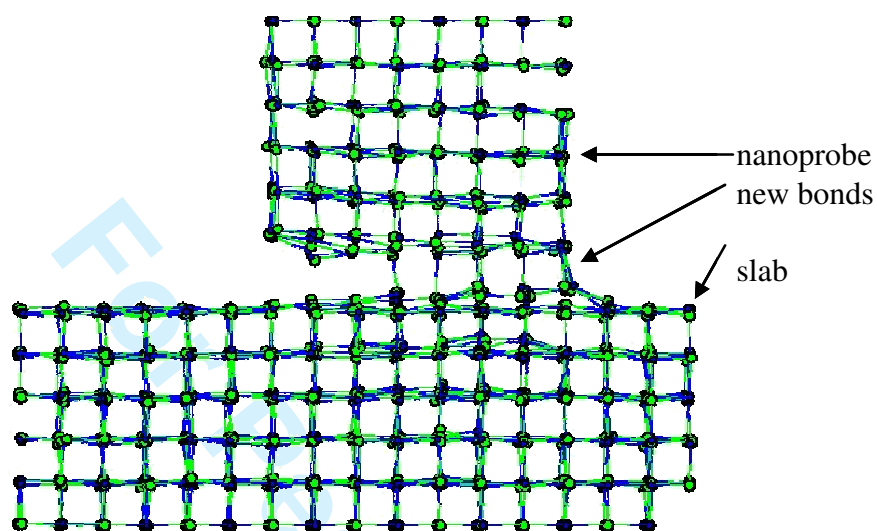


Fig 2 Molecular dynamics model of a sodium chloride 8x8 atom probe approaching a slab of NaCl to form new bonds with the surface atoms

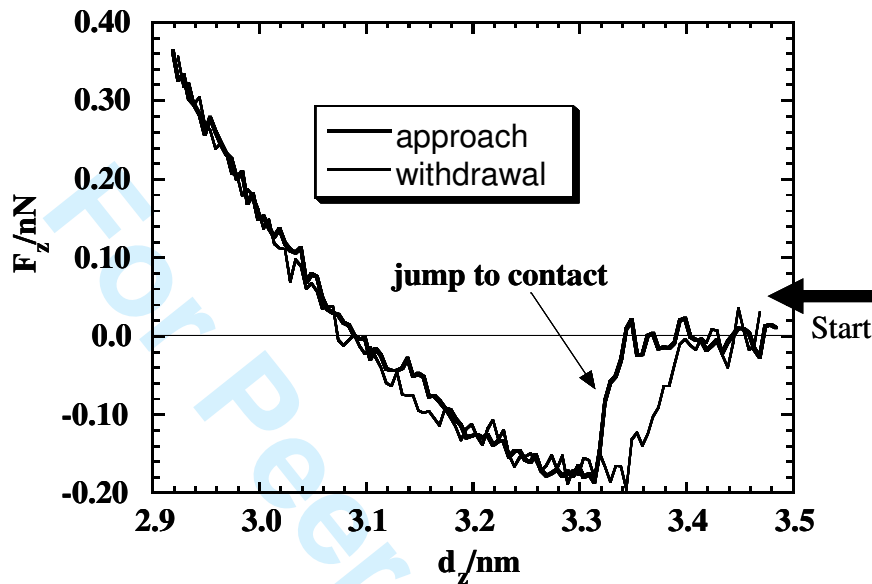


Fig 3 Force per ion versus distance curves for approach from right to left and withdrawal of the 8x8 NaCl nanoprobe showing the jump to contact and the equilibrium at zero force

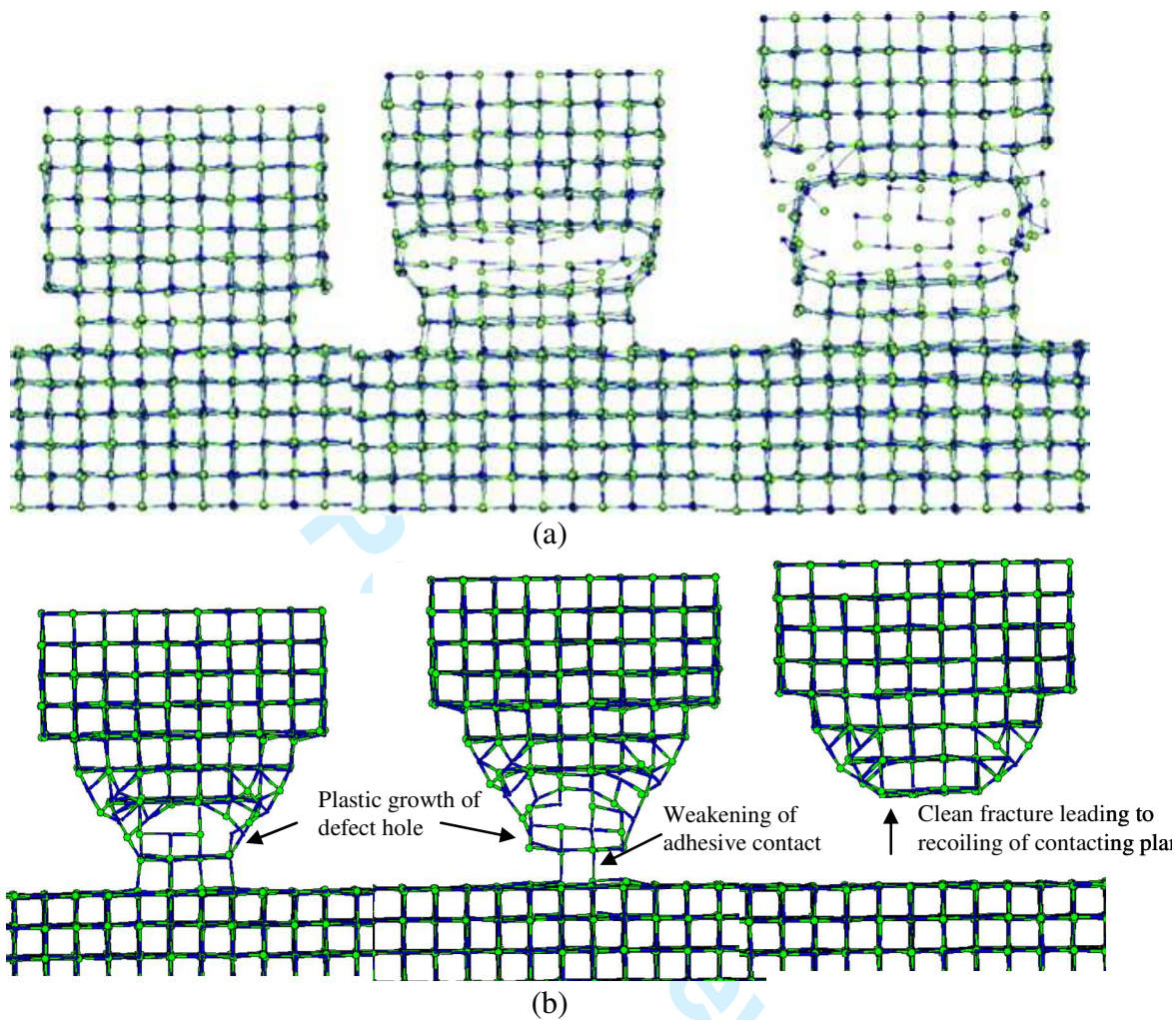


Fig 4 (a) Major plastic deformation observed in the 8x8 contact model of the pyramidal NaCl nanoparticle. (b) Computed results for 4x4 NaCl contact show clean detachment with minor plastic deformation

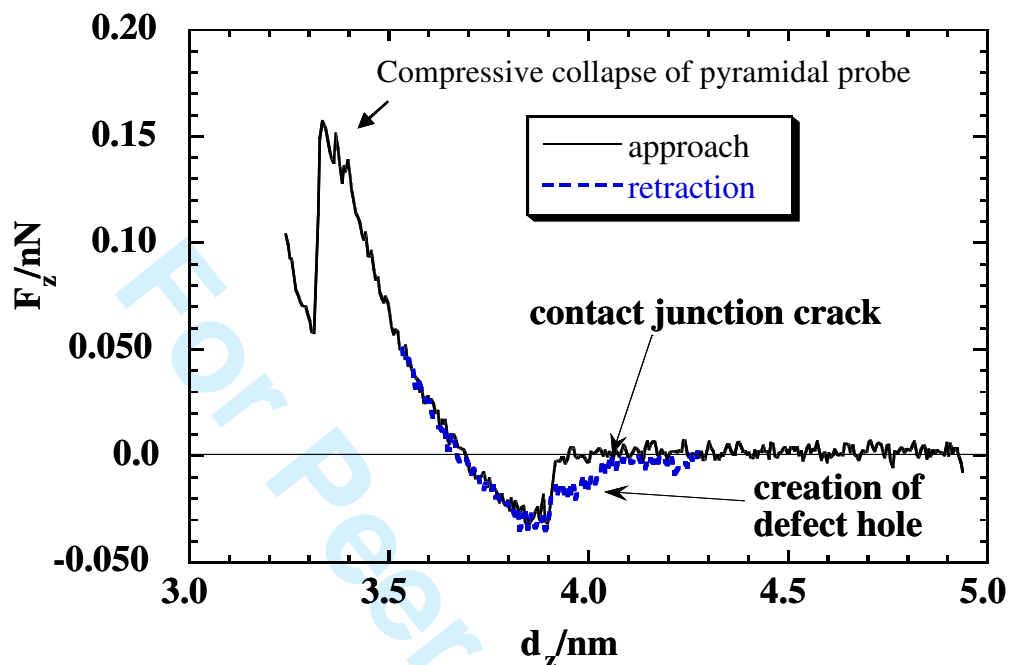


Fig 5 Force per ion in 10x10 rigid layer vs displacement curve for pyramidal 4x4 NaCl probe. The jump to contact appears perfectly elastic but the pull-off dissipates energy without raising the force significantly. The stress required for compressive collapse was much higher.

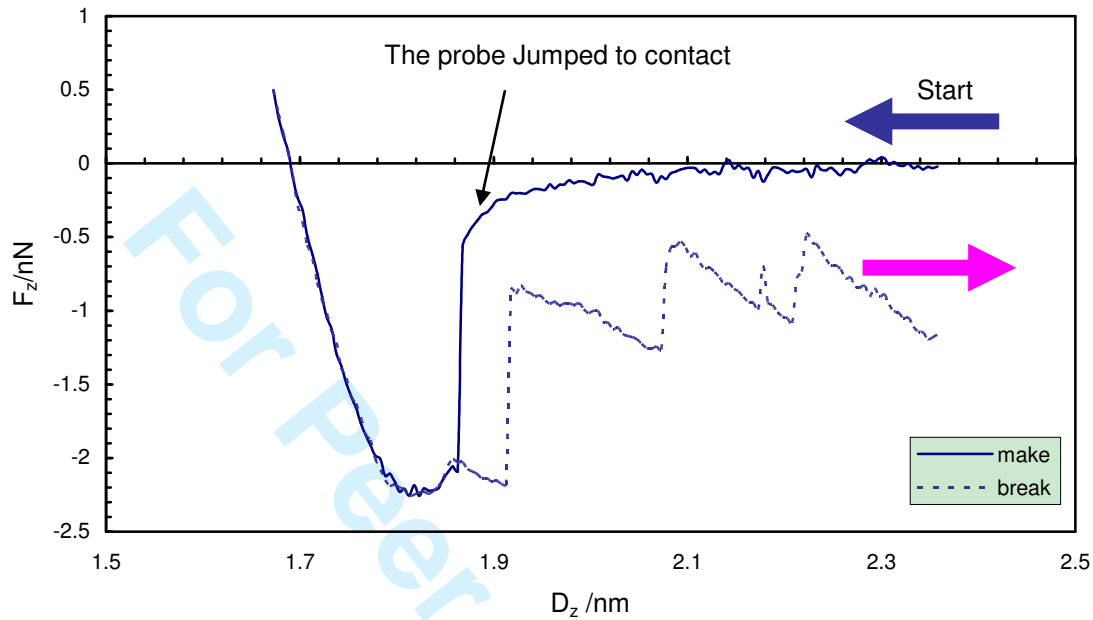


Fig 6 Force per 10x10 ion vs displacement curve for 6x6 pyramidal MgO probe showing that the jump to contact was perfectly elastic. The pull-off was at the same force but dissipated energy plastically. The steps in the breaking curve were due to sudden motion of defects within the nanoprobe, which remained attached to the slab.

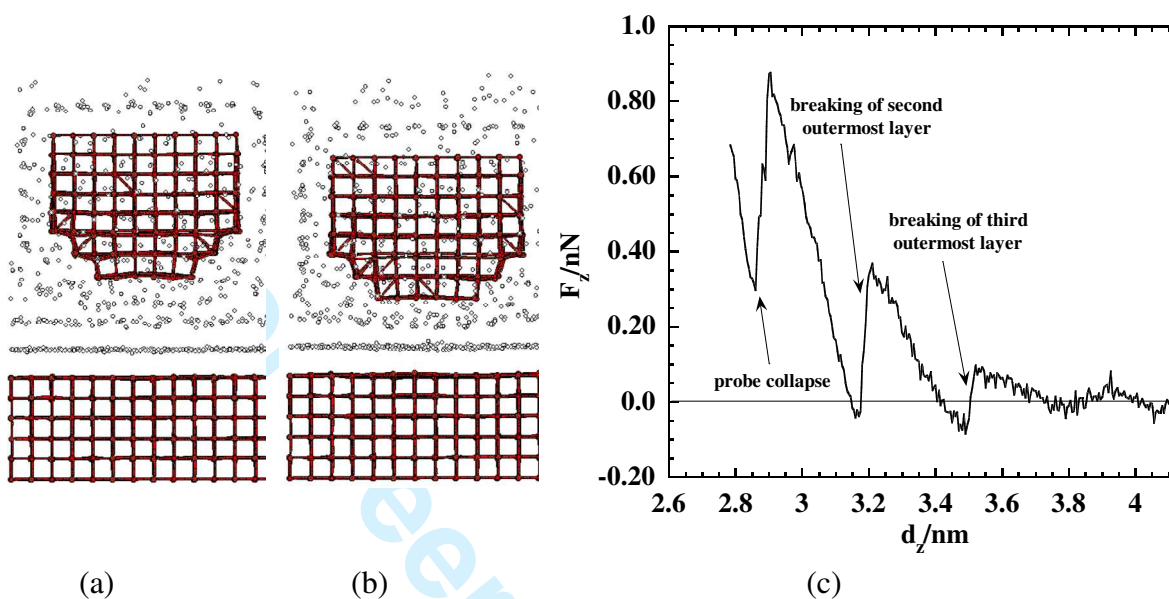


Fig 7 a),b) Stills from a movie of molecular dynamics model of 6x6 MgO pyramidal probe approaching an MgO slab coated with a monolayer of xenon molecules at 100K; c) force distance curve approaching from right to left, showing steps as molecules are squeezed out.

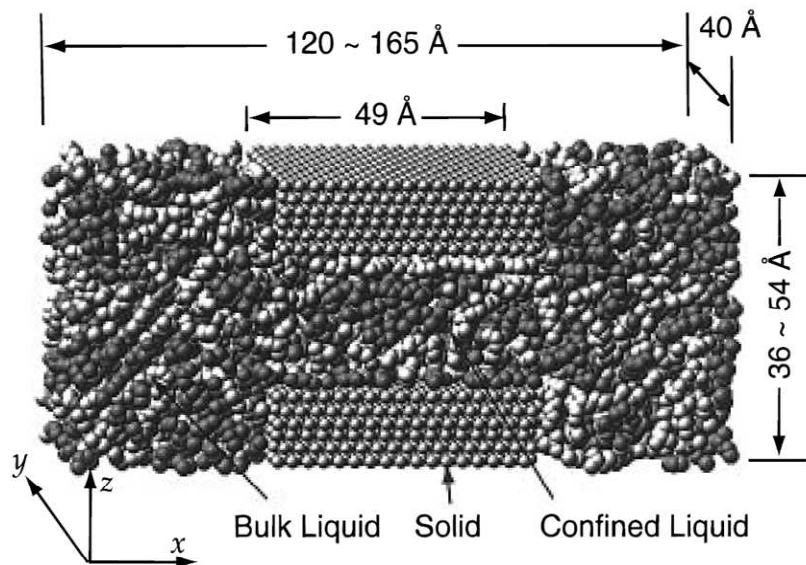
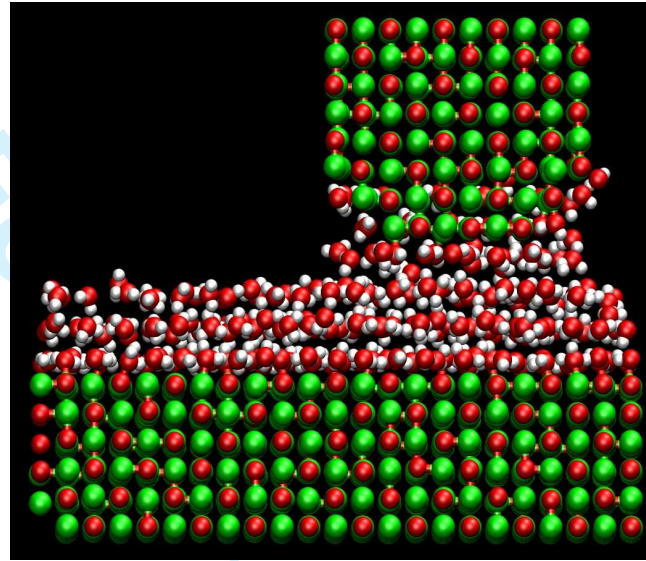
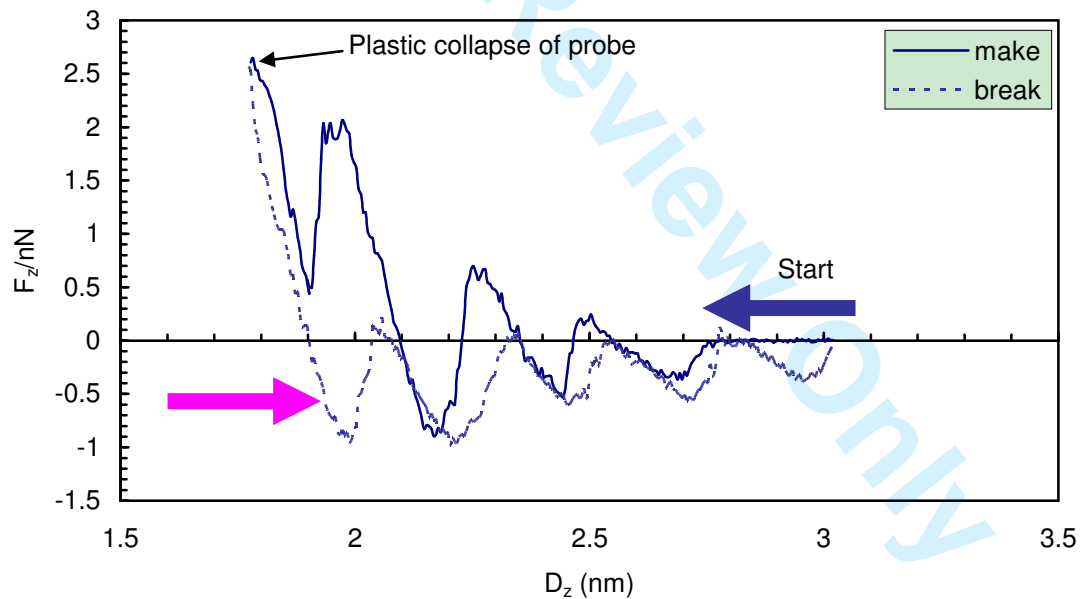


Fig 8 Molecular dynamics model of Gao et al (1997) showing the flat parallel plate configuration with liquid in between; the solid surfaces were infinite in the y direction.





(a)



(b)

Fig 9a) Pyramidal 6x6 MgO probe moving towards an MgO slab covered with 3 layers of water molecules; b) force distance curve revealing the filling of the gap then the oscillations as three layers of water were squeezed out, leaving one layer resisting removal, showing hysteresis