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► **To cite this version:**

Oliver Musshoff, Martin Odening, Wei Xu. Management of Climate Risks in Agriculture - Will Weather Derivatives Permeate?. Applied Economics, 2009, pp.1. 10.1080/00036840802600210 . hal-00582260

**HAL Id: hal-00582260**

**<https://hal.science/hal-00582260v1>**

Submitted on 1 Apr 2011

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**Management of Climate Risks in Agriculture - Will Weather Derivatives Permeate?**

Journal:	<i>Applied Economics</i>
Manuscript ID:	APE-07-0509.R1
Journal Selection:	Applied Economics
Date Submitted by the Author:	17-Sep-2008
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JEL Code:	G32 - Financing Policy Capital and Ownership Structure < G3 - Corporate Finance and Governance < G - Financial Economics, Q12 - Micro Analysis of Farm Firms, Farm Households, and Farm Input Markets < Q1 - Agriculture < Q - Agricultural and Natural Resource Economics, Q54 - Climate Natural Disasters < Q5 - Environmental Economics < Q - Agricultural and Natural Resource Economics
Keywords:	Weather derivatives, precipitation risk, hedging effectiveness, local basis risk, geographical basis risk



# Management of Climate Risks in Agriculture

## - Will Weather Derivatives Permeate?

It is a matter of common knowledge that weather represents the major source of uncertainty in crop production. It is to be expected that weather fluctuations will increase in the future due to climate change. Traditionally, farmers tried to protect themselves against weather-related yield variations by buying insurances. More recently, there has been a discussion regarding the use of weather derivatives to safeguard against volumetric risks. Although weather derivatives display advantages over traditional insurances, there is only a relatively small market for these products in agriculture. This is partly attributed to the fact that it is unclear whether and to what extent weather derivatives are a useful instrument of risk management in agriculture. This study applies real yield and weather data from northeast Germany in order to quantify the risk-reducing effect that can be achieved in wheat production by using precipitation options. To do so stochastic simulation is used. The hedging effectiveness is controlled by the contract design (index, strike level, tick size). However, the local basis risk and the geographical basis risk remain with the farmer. We separate both causes of basis risk and reveal the extent of each. This enables conclusions regarding the design of weather derivatives; thus the question dealt with here is relevant both for farmers and for potential sellers of weather derivatives.

## I. Introduction

Weather is an important production factor and at the same time one of the greatest sources of risk in agriculture. Perhaps, the most obvious impact of weather is on crop production (cf. e.g., Isik and Devadoss, 2006). There is scarcely a year in which there are no drought periods or extreme precipitation in the most diverse regions of the world leading to crop failures. The impact of the weather risk is not limited to crop production. The performance of livestock farms, the turnover of processors, the use of pesticides and fertilizers as well as the demand for many food products also depends on weather. Hence, large parts of the agribusiness are affected by weather risks.

It is expected that fluctuations in temperature and rainfall will increase in the wake of global climate change and thereby the volumetric risk will rise further. At the same time, the susceptibility of farms to risk will rise as a result of the increasing capital intensity of agriculture and the associated increasing debt ratio. Therefore, it will become increasingly necessary for farmers to insure themselves against weather risks.

Farmers have always been confronted with risks. In the past, farmers tried to protect themselves against the negative economic consequences of bad weather events by using on-farm risk management instruments like choosing less weather-dependent production activities, choosing a widely diversified production program, procuring overcapacities or investing in technologies to control the environment (e.g. irrigation technologies). Additionally, farmers have tried to share risks through buying damage-based insurances (cf. e.g., Mishra and Goodwin, 2006). Agricultural policy support (e.g., direct government aids in response to natural calamities and disasters) can also yield an insurance effect (cf. e.g., Thompson *et al.*, 2004).

From the end of the 1990s onwards, there has been a discussion about the use of index-based instruments, also called weather derivatives, as a new instrument to safeguard against volumetric risks (cf. Tigler and Butte, 2001; Cao *et al.*, 2003; Berg *et al.*, 2004; Jewson *et al.*, 2005). Weather derivatives are financial market products, such as futures, options or swaps, which allow exchanging weather risks. They are related to objectively measurable weather variables (temperature, rainfall, wind etc.). Until now, weather derivatives have been used mainly by energy companies. Trading of weather derivatives also occurs predominantly in the over-the-counter (OTC) market. This means that the contracting parties have to establish their contract specification bilaterally. As a contractual partner for a farmer wishing to be insured against in-

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4 sufficient rainfall during the growth phase of crops, for instance, the tourist industry (e.g., theme  
5 parks) can be considered, which exhibits a contrary risk exposure with regard to rainfall. How-  
6 ever, weather derivatives also offer attractive opportunities for institutional investors such as in-  
7 surers or banks to diversify a portfolio, since the weather-related risks are only correlated rela-  
8 tively weakly with the systematic risk of a national economy.  
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13 Whereas traditional damage-based insurances predominantly protect against damages from  
14 catastrophic events (e.g. hail), weather derivatives can be designed to release payments even for  
15 less drastic events (e.g. insufficient rainfall). A holder of a traditional insurance must also prove  
16 the damage in order to obtain indemnity payments. Unlike conventional damage-based instru-  
17 ments, the hedge from weather derivatives results from payments which are tied to weather  
18 variables that are measured objectively at a specified location; that is, weather derivatives are not  
19 impact-oriented, but cause-oriented. Weather derivatives thus offer administrative advantages  
20 over traditional insurances. Furthermore, weather derivatives, unlike insurances (cf. e.g., Jin *et*  
21 *al.*, 2005), are not affected by moral hazard problems and adverse selection. Therefore, weather  
22 derivatives have the advantage of relatively low transaction costs.  
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32 Although (i) agriculture is directly dependent on the weather, (ii) experts point out numer-  
33 ous potential applications of weather derivatives especially because of the advantages named  
34 above (cf. Turvey, 2001; Skees, 2002), and (iii) there have already been some promising practi-  
35 cal experiences in the USA and Canada, the market for weather derivatives in agriculture is cur-  
36 rently still relatively small. This may partly be accounted for by the fact that farmers are not yet  
37 familiar with using weather derivatives. Another problem is that different valuation methods for  
38 weather derivatives can provide different prices. A possible consequence is that no unique price  
39 is found which market participants consider to be fair. The market then lacks liquidity and there  
40 is consequently a lack of orientation for other potential market participants. Another possible  
41 obstacle to their application can be seen in the basis risk which remains with the farmer when he  
42 uses weather derivatives, and which means that yield variations are not compensated exactly by  
43 corresponding payoffs from the weather derivative. One cause of the basis risk is that yield  
44 variations are generally not perfectly correlated with the relevant weather variable (local basis  
45 risk). For example, the weather derivative could refer to the rainfall sum at the place of produc-  
46 tion in May, although e.g. the rainfall at other time periods, the timing of the rainfall and the  
47 temperature also influence the yield in the crop production. On the other hand, there is a geo-  
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graphical basis risk. In this context, this means the non-insurable risk which results from the difference between the weather event at the reference point of the derivative and the site of agricultural production. Although this aspect is not so important for temperature-related instruments, it cannot be neglected in the analysis of the hedging effectiveness of rainfall derivatives, as there is a high spatial variability of rainfall.

An increasing number of publications investigate the usefulness of weather derivatives as a risk management instrument in agribusiness. Previous studies have focussed on the one hand on theoretical questions of pricing weather derivatives and on the other hand on analysing temperature-related instruments (cf. van Asseldonk, 2003; Richards *et al.*, 2004; Manfredo and Richards, 2005; Turvey, 2005). For agricultural applications, rainfall-related instruments ought to play a greater role. Hitherto, however, there have been very few publications especially on the analysis of the hedging effectiveness of precipitation-based instruments (cf. Turvey, 2001; Stoppa and Hess, 2003). As yet, therefore, it is unclear whether weather derivatives will permeate in agriculture (Edwards and Simmons, 2004).

The aim of this study is to clarify the risk-reducing effect of using rainfall options, specifically by considering wheat production in northeast Germany by means of a with/without derivative comparison. Special attention will be given to quantifying the basis risk, which will be divided into the previously mentioned components (i) local basis risk and (ii) geographical basis risk. The separation of the basis risk, which to our knowledge has not been treated previously in literature, will provide important findings for the design of weather derivatives and their potential for usage in agriculture. Thus, the questions dealt with here will be relevant both for farmers and for potential sellers of weather derivatives.

The remainder of the paper is structured as follows: In Section II, the database and methodical procedure are described. In Section III, the analysis of the hedging effectiveness of rainfall options for a representative cash crop farm in northeast Germany is carried out. The paper ends with conclusions for the design of weather derivatives (Section IV).

## II. Data and methodical procedure

Grain production in northeast Germany, Brandenburg in particular, is highly affected by rainfall risk. During the important grain-yield months of April to June, the rainfall sum in Brandenburg was between 64 and 258 mm over the last 20 years (at an average of 141 mm and a standard deviation of 46 mm) - measured at the Berlin-Brandenburg central weather station in Berlin-

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4 Tempelhof. The grain yields have fluctuated similarly, due to the sandy soil possessing little  
5 water-storing capacity and a lack of artificial irrigation facilities. Currently there exists no op-  
6 portunity of insuring against yield losses caused by rainfall. During the drought years 2000 and  
7 2003, disaster relief was even granted by the government on account of the extreme harvest  
8 failures, in order to protect farms against insolvency. Of course, such government supports are  
9 not always be guaranteed. Therefore, there is a pronounced interest among affected farmers for  
10 a routine form of hedging weather-related risks.  
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17 For a farm-specific analysis of the hedging effectiveness of weather derivatives, a represen-  
18 tative cash crop farm with approximately 850 ha of acreage operating in the Federal State of  
19 Brandenburg, more precisely in Ketzin, is considered. The farmer wishes to be insured against  
20 weather-related yield losses in wheat production. Wheat is the major production activity with a  
21 crop proportion of more than one third. Without a weather station or a suitable contractual part-  
22 ner, it is difficult for the farmer to obtain a derivative which refers directly to the weather on site  
23 of production. Nonetheless, it is assumed that derivatives which refer to the rainfall measured at  
24 the weather station in Berlin-Tempelhof are available on the OTC market. Ketzin is situated  
25 about 39 km west of Berlin-Tempelhof. Both causes of basis risk which have previously been  
26 outlined are evident here: on the one hand, a number of weather variables influence the wheat  
27 yield while the payoff of the derivative and the indemnity payments is solely derived from rain-  
28 fall. On the other hand, Ketzin is 39 km away from Berlin-Tempelhof, which means that the  
29 rainfall in each location can be completely different in principle. Thus, even if the agricultural  
30 production were only dependent on the rainfall, indemnity payments and yield failure could still  
31 be different on account of the spatial distance.  
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46 In order to evaluate the hedging effectiveness of weather derivatives, a weather variable  
47 must first be specified and the production function must be estimated in which the weather is  
48 not - as is usual - a part of the error term, but a non-controllable (though measurable) production  
49 factor. Derivatives, which refer to the weather variable in the production function, are then  
50 specified. Before the hedging effectiveness of weather derivatives can be quantified, the deriva-  
51 tives - which do not yet exist but which could be available in principle - must be priced. The  
52 elements of a farm-specific analysis of the hedging effectiveness of weather derivatives are  
53 summarized in Fig. 1.  
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4 **Fig. 1 about here**  
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10 *On the specification of the weather variables*

11 Previous publications on rainfall-related derivatives have tended to refer to an accumulation in-  
12 dex (cf. Turvey, 2001; Skees *et al.*, 2001; Stoppa and Hess, 2003; Vedenov and Barnett, 2004).  
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14 The cumulative rainfall index  $I_T^C$  corresponds to the rainfall sum within a specific time period:  
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$$16 I_T^C = \sum_{t=1}^x y_t \quad (1)$$

17 Here,  $y_t$  indicates the rainfall on day  $t$  and  $x$  indicates the length of the accumulation period.  
18

19 Alternatively, the rainfall deficit index  $I_T^D$  is suggested here, which expresses the timing of  
20 rainfall in addition to the quantity:<sup>1</sup>  
21

$$22 I_T^D = \sum_{\tau=1}^z \min \left( 0, \sum_{t=(\tau-1) \cdot s+1}^{\tau \cdot s} y_t - y^{min} \right) \quad (2)$$

23 This index measures the shortfall of the rainfall sum in an  $s$ -days period relative to a reference  
24 level  $y^{min}$ . This shortfall is cumulated over  $z$  periods. Hence, the construction principle is  
25 similar to that of degree-day-indices, which are widely used for the specification of temperature  
26 derivatives (cf. e.g. Alaton *et al.*, 2002; Zeng, 2000a).  
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31 *On the estimation of the production function*  
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33 For the considered cash crop farm yield data for winter wheat over a period from 1993 to 2006  
34 are available. Fourteen observations seem to be a poor database for the estimation of the yield  
35 model. However, a longer time series is not available for the new federal states in Germany in  
36 general and Brandenburg in particular, since production took place under totally different condi-  
37 tions prior to German reunification. Furthermore, it should also be noted that the yield data sur-  
38 vey was not performed in accordance with the wheat variety, even though certain wheat varie-  
39 ties are better suited to regions with low rainfall such as Brandenburg and are preferred there for  
40 cultivation. Using statistical tests, no significant trend can be found for the wheat yields.  
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59 <sup>1</sup> This definition may appear unusual since the rainfall deficit index will take negative values. However, the defini-  
60 tion is convenient for the present application because then the relationship between yield and rainfall deficit index  
is similar to that between yield and rainfall sum index.



Using daily rainfall data measured at the weather station in Berlin-Tempelhof, the rainfall indices described in (1) and (2) for the years 1993 ( $T - 14$ ) to 2006 ( $T - 1$ ) are calculated. To specify the relationship between the rainfall sum or rainfall deficit index observed in Berlin-Tempelhof  $I_b$  and the wheat yield observed for the farm in Ketzin  $\tilde{Q}_b$ , a linear-limitational (Leontief) production function seems most suitable:<sup>2</sup>

$$\tilde{Q}_b = \begin{cases} a_0 + a_1 \cdot I_b + \varepsilon_b, & \text{if } I_b < a_2 \\ a_3 + \varepsilon_b, & \text{otherwise} \end{cases}, \text{ with } b = T - 14, T - 13, \dots, T - 1 \text{ and } \varepsilon_b \sim N[0, \sigma_\varepsilon] \quad (3)$$

“~” makes it clear that the yield at the farm location in Ketzin is meant, whereas the weather index is related to weather data measured in Berlin-Tempelhof ( $I_b$  instead of  $\tilde{I}_b$ ).  $a_0$ ,  $a_1$ ,  $a_2$  and  $a_3$  describe the parameters of the production function to be estimated. When  $a_1 > 0$ , then drought-related yield losses are to be expected for the rainfall index below  $a_2$  mm. If values for the rainfall index are above  $a_2$  mm the expected wheat yield corresponds to  $a_3$  dt/ha.  $\varepsilon_b$  indicates the normally distributed error term with a standard deviation of  $\sigma_\varepsilon$ . It should be noted that this error term expresses both the local basis risk and the geographical basis risk: on the one hand, the yield-explaining weather index only refers to rainfall in a specific accumulation period. On the other hand, the production function is determined on the basis of yield data at the site of production and the weather event at the reference weather station.

There is some back coupling between the estimation of the production function and the precise specification of the rainfall indices, since weather variables are sought which are correlated as highly as possible to production output. Variant calculations are used to examine which reference period delivers the “best” rainfall sum index and which reference period allows the “best” rainfall deficit index. In order to do so, systematic variations for  $x$  as well as for  $z$  and  $s$  are carried out.  $y^{\min}$  was selected so as to provide a maximum correlation between the wheat yield and the deficit index.

Table 1 shows the parameter estimates and the explanatory power for selected production functions. Measured at  $R^2$ , the best rainfall sum index for the accumulation period June and the best rainfall deficit index for the accumulation period April to June are obtained. It should be noted that the explanatory power between the wheat yield and the best rainfall deficit index

<sup>2</sup> Several further functional forms for the yield model have been tested; in particular a quadratic and a logarithmic production functions. Nonetheless, the linear-limitational production function showed the best fit in terms of  $R^2$  for the empirical data and both rainfall indices. It should be noted that this result cannot be generalized. VEDENOV and BARNETT (2004) point out that a suitable yield-rainfall-model is dependent on type of variety and region.

( $R^2 = 0.48$ ) is considerably higher than that between the wheat yield and the best rainfall sum index ( $R^2 = 0.15$ ).

### Table 1 about here

The specification of derivatives which refer to the best rainfall sum or rainfall deficit index is described in the following.

#### *On the specification of the weather derivatives*

The revenue function of wheat production can be derived from the production function. As only volumetric risks are to be considered, it is assumed that the wheat price  $P$  is fixed by a forward contract and amounts to 10 €/dt. A derivative is now constructed respectively for the best rainfall sum index and the best rainfall deficit index in such a way that it compensates for expected revenue fluctuations precisely by corresponding payoffs. For a linear-limitational production function this can be achieved using an option. The payoff for a (European) put option corresponds to:

$$F_T = \max(S - I_T, 0) \cdot V \quad (4)$$

At expiry time  $T$  the put option generates a positive payoff  $F_T$  when the rainfall index  $I_T$  is below the strike level  $S$ . If the strike level is above the index, the payoff is zero. The tick size  $V$  monetizes the positive difference between  $S$  and  $I_T$ .

One put option relates to the cumulative index  $I_T^C$  which is measured in June 2007 at the weather station at Berlin-Tempelhof. The second put option refers to the rainfall deficit index  $I_T^D$  between the 7-day rainfall measured at the weather station in Berlin-Tempelhof and 7.4 mm cumulated during the period April to June 2007. Farmers can obtain each of the two options in July 2006. In order to design the options in such a way that their payoff is complete inversely to the expected revenues from the wheat production (per ha), strike level and tick size must be selected as follows:  $S = a_2$  and  $V = a_1 \cdot P$ .<sup>3</sup> As illustrated in Fig. 2, the options deliver

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<sup>3</sup> It should be noted that an option cannot be designed in such a way that its payoff is correlated perfectly negatively to the expected revenue from the production, if production function did not display a linear-limitational function form. To insure the production risk for a linear production function, a future can be used. For more complex production functions, several weather derivatives can be combined. In this way, a combination of put *and* call options

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4 a payoff for yield-reducing rainfall. However, there is no payoff if the weather is suitable for  
5 yield-formation.  
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9 **Fig. 2 about here**  
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13 The contract specifications for the rainfall options which are considered here are summa-  
14 rized in Table 2.  
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19 **Table 2 about here**  
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25 *On the calculation of the option price*  
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27 If farmers wish to insure their revenue in wheat production by using a rainfall option, they must  
28 first spend the option price. As the options are not market-traded, their price must also be de-  
29 termined. Unfortunately, the preference-independent valuation procedures developed in the fi-  
30 nancial option pricing theory cannot be used, since the rainfall index which forms the basis of a  
31 rainfall option is non-tradable (cf. Jewson *et al.*, 2005: 28-34; Richards *et al.*, 2004). In order to  
32 avoid the difficulties which are therefore associated with pricing weather derivatives, the price  
33 of both options is calculated as a “fair premium” in an actuarial sense, i.e. the profit expected  
34 from the option trade is precisely zero for both parties. Since therefore neither a risk premium  
35 from the seller or buyer nor transaction costs are taken into account, the option price can simply  
36 be calculated as the expected payoff of the option discounted with risk-free interest rate  $r$  :  
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$$46 F_0 = E(F_T) \cdot \exp(-r \cdot \Delta t) \quad (5)$$

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48 where  $\Delta t$  is the maturity of the option.  
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50 The fair premium can basically be determined by means of analytical procedures, historical  
51 simulation (burn analysis), index value simulation or daily simulation. Analytical procedures  
52 like the Black-Scholes formula require restrictive assumptions e.g. regarding the distribution for  
53 the weather variable underlying the derivative (cf. Hull, 2006). Option prices determined by  
54 means of historical simulation as a non-parametric procedure can be very imprecise, because for  
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60 could be suitable for a quadratic production function. In the “left area” (“right area”) of the production function,  
the put option (the call option) insures against volumetric risks.

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4 instance the length of the data series is too short to obtain a good approximation of the theoret-  
5 cal distribution for the weather index (Zeng, 2000b). Using the daily simulation based on a  
6 model for the daily rainfall, the volatility of the rainfall and thus the option price are systemati-  
7 cally underestimated (cf. Dubrovsky *et al.*, 2004; Odening *et al.*, 2007). Therefore, the index  
8 value simulation is used here.  
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13 Using daily rainfall data which were measured in Berlin-Tempelhof between 1948 and  
14 2006, the respective value for the rainfall index is calculated for each year. In the result, 59 em-  
15 pirical observations are available for each index. The MS-EXCEL-Add-In BEST-FIT is used to  
16 test which assumption regarding the distribution of the index is adequate. According to the  
17 standard tests (Chi-Square, Kolmogorov-Smirnov and Anderson-Darling test), the lognormal  
18 distribution shows the best fit to empirical distribution for the rainfall sum index and the  
19 Weibull distribution delivers the best fit for the rainfall deficit index; whereas only distributions  
20 were considered which did not permit a change of sign of the uncertain variable. In the context  
21 of the index value simulation, a value is randomly drawn 10 000 times from the estimated dis-  
22 tribution for the rainfall index.<sup>4</sup> In each simulation run the payoff of the option is determined in  
23 accordance with (4). The discounted average payoff of the derivative corresponds to the fair  
24 premium (cf. (5)). Using a risk-free interest rate  $r$  of 5%, the fair premium amounts to 108.1 €  
25 for the rainfall sum index and 56.8 € for the rainfall deficit index.  
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40 *On the estimation of the hedging effectiveness*

#### 41 **General procedure**

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43 The risk-reducing effect which can be attained by using weather derivatives is usually quanti-  
44 fied by a comparison of the revenue distribution with and without having a derivative (cf. e.g.  
45 Vedenov and Barnett, 2004). Without a derivative, the revenue from wheat production  $R_0$  (in  
46 €/ha) related to the time of buying the derivative corresponds to the wheat yield (in dt/ha) mul-  
47 tiplied by the wheat price (in €/dt) and the discounting factor:<sup>5</sup>  
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55 <sup>4</sup> Regarding the number of required simulation runs, Haug (1998: 40), e.g., stipulates that at least 10 000 runs  
56 should be carried out. For technical details describing how to use stochastic simulation to model a wide variety of  
57 distributions with established software packages see e.g. Winston (1998).

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59 <sup>5</sup> We are only focussing on the risk-reducing effect of weather derivatives in wheat production, i.e. we abstract  
60 from cross effects resulting from the fact that the payoff of a weather derivative is correlated with the yields of  
several crops.

$$R_0 = \tilde{Q}_T(I_T) \cdot P \cdot \exp(-r \cdot \Delta t) \quad (6)$$

With a derivative, the revenue  $R_0'$  (in €/ha) is to be calculated as follows:

$$R_0' = R_0 + F_T(I_T) \cdot \exp(-r \cdot \Delta t) - F_0 \quad (7)$$

If farmers wishing to be insured against volumetric risks using a derivative, at first, they have to pay the purchase price  $F_0$ . Afterwards, farmers receive in addition to the revenue from wheat production  $R_0$  the payoff of the derivative  $F_T$ , whose level - just like the success of the production (cf. (3)) - is dependent on the weather variable  $I_T$ .

### On the separation of the basis risk

To separate the basis risk and its causes, three scenarios are considered when estimating the hedging effectiveness of rainfall options; two of these scenarios are synthesized in order to work on the specific effects. As the option is always related to the rainfall at the reference weather station Berlin-Tempelhof, the three scenarios are not distinguished with regard to the option price  $F_0$  and the payoff of the option  $F_T$ , but only in determining the production success of wheat production in  $T$ :

- In the first hypothetical scenario it is assumed that there is no basis risk. It is supposed that the location of the agricultural production is not in Ketzin, but in the immediate vicinity of the reference weather station in Berlin-Tempelhof ( $Q_T$  instead of  $\tilde{Q}_T$ ) and that the relationship between yield and rainfall index is not influenced by random effects ( $\varepsilon_T = 0$ ). Technically, the wheat yield in scenario 1  $Q_T^1$  is derived directly from the rainfall index in Berlin-Tempelhof:

$$Q_T^1 = \begin{cases} a_0 + a_1 \cdot I_T, & \text{if } I_T < a_2 \\ a_3, & \text{otherwise} \end{cases} \quad (8)$$

- In the second hypothetical scenario, the fact that the wheat production takes place 39 km away from the reference weather station is taken into account (geographical basis risk). However, it is further assumed that the relationship between yield and rainfall index at the site of production is purely deterministic ( $\varepsilon_T = 0$ ). Technically, the wheat yield in scenario 2  $\tilde{Q}_T^2$  is directly derived from the rainfall index at the site of production in Ketzin ( $\tilde{I}_T$  instead of  $I_T$ ):

$$\tilde{Q}_T^2 = \begin{cases} a_0 + a_1 \cdot \tilde{I}_T, & \text{if } \tilde{I}_T < a_2 \\ a_3, & \text{otherwise} \end{cases} \quad (9)$$

The value for the rainfall index in Ketzin  $\tilde{I}_T$  is derived from the value for the rainfall index in Berlin-Tempelhof  $I_T$  while taking a correlation yet to be determined into consideration (see below).

- In the third scenario, the spatial distance between the reference weather station and the site of production as well as the stochastic relationship between yield and rainfall are taken into consideration (geographical basis risk and local basis risk). Technically, the wheat yield in scenario 3  $\tilde{Q}_T^3$  is derived from the relevant value for the rainfall index at the reference weather station Berlin-Tempelhof and while taking into consideration the error term of the production function  $\varepsilon_T$ , which expresses both basis risks:

$$\tilde{Q}_T^3 = \begin{cases} a_0 + a_1 \cdot I_T + \varepsilon_T, & \text{if } I_T < a_2 \\ a_3 + \varepsilon_T, & \text{otherwise} \end{cases} \quad (10)$$

To determine the distribution for the revenues without option (cf. (6)) and with option (cf. (7)) in the three scenarios, the stochastic simulation (10 000 simulation runs) is used.

### Decorrelation analysis

Usually, one would quantify geographical basis risk (second scenario) by means of comparing the hedging effectiveness of weather derivatives based on weather data measured at the production site versus taken weather data some distance apart. Unfortunately, for the showcased farm in Brandenburg weather data measured on the production location are not available. For that reason we have to replace actual weather data by randomly generated values using an appropriate correlation coefficient. This correlation coefficient is derived from a statistically estimated decorrelation function.

In order to estimate the correlation between the rainfall index at the site of production and the rainfall index at the reference weather station, data is used from 23 weather stations in Berlin and Brandenburg from 1983 to 2003, all located within a 100 km radius of Berlin-Tempelhof and relatively uniformly distributed over the area. The correlation coefficients  $\rho_{i,j}$  between the values for the rainfall index at the weather stations  $i$  and  $j$  are determined. Then the distances  $d_{i,j}$  between the individual weather stations are calculated. On the basis of the correlation coefficients and each respective distance a so-called decorrelation function can be estimated.

Rubel (1996) suggests the following non-linear decorrelation function for modelling spatial correlation for rainfall in Europe:<sup>6</sup>

$$\rho_{i,j} = c_1 \cdot \exp(-c_2 \cdot d_{i,j}^{c_3}) \quad (11)$$

For the best rainfall sum index we find  $c_1 = 0.94$ ,  $c_2 = 0.0033$ ,  $c_3 = 0.88$  and for the best rainfall deficit index  $c_1 = 0.92$ ,  $c_2 = 0.0012$ ,  $c_3 = 1.11$ . The  $R^2$  is 0.24 for the rainfall sum index and 0.48 for the rainfall deficit index. The scatter diagram shown in Fig. 3 makes it clear, however, that the relationship between distance and correlation becomes more diffuse as the distance increases, that is the scatter plot reveals heteroscedasticity. It is also apparent that - as expected - the correlation between the rainfall index at two weather stations decreases with the distance. At a distance of 39 km between Berlin-Tempelhof and production location in Ketzin the rainfall sum index has an expected correlation of 0.87 and the rainfall deficit index has an expected correlation of 0.86.

**Fig. 3 about here**

Since the correlation coefficient is derived from the decorrelation analysis it implies an estimation error. This estimation error is not taken into account in the subsequent analysis of the hedging effectiveness. Actually, we calculate only the hedging effectiveness for an average correlation. The geographical basis risk and the hedging effectiveness of an individual farm can differ from the depicted values. However, there is no systematic over- or underestimation of the results as long as the estimated correlation is unbiased.

### III. Results

In Table 3 the expected value, the standard deviation and selected percentiles of the revenue distribution are given for all three scenarios in order to assess the hedging effectiveness of the two rainfall options described above. The situation without and with insurance by a rainfall option is considered for each scenario. Fig. 4 illustrates the revenue distributions for selected scenarios.

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<sup>6</sup> The de-correlation function is invariant regarding direction. Thus, topographical differences potentially influencing precipitation are neglected. In Brandenburg, topographical conditions play to the assumption of a correlation independent of location and direction.

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4 **Table 3 about here**  
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7 **Fig. 4 about here**  
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11 It is apparent first of all that there is no difference between the expected values for the revenue without and with the option. This is because the option price was calculated as a fair premium, therefore the insurance in average “brings as much as it costs”. With regard to the hedging effectiveness of an option, the following can be established:  
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- 18 • Scenario 1: When there is no basis risk (site of production in immediate vicinity of reference weather station and deterministic relationship between yield and weather index), farmers can completely eliminate the revenue risk of wheat production by buying a put option on the rainfall sum or rainfall deficit index. This is possible because the payoff of the option is correlated perfectly negatively to the revenue from the wheat production (cf. Fig. 2).  
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- 28 • Scenario 2: When it is taken into consideration that the site of the agricultural production is 39 km away from the reference weather station, the revenue distribution without the option is unchanged in comparison to scenario 1, because the same distribution underlies the rainfall index in Ketzin as that in Berlin-Tempelhof (cf. footnote 6). Nonetheless, the standard deviation of the revenue in wheat production can only be reduced by about 45% using the put option on the rainfall sum index or on the rainfall deficit index. Eventually, there may be cases in which farmers obtain a payoff from the option even though no yield loss could be registered (and vice versa), because the rainfall in Ketzin is different from that in Berlin-Tempelhof. In comparison to the results from scenario 1, it is evident that the risk-reducing effect of the option decreases with increasing distance from the reference weather station.  
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- 47 • Scenario 3: When both the geographical basis risk and a stochastic relationship between yield and rainfall index are realistically taken into consideration, the standard deviation of the revenue in wheat production can only be reduced by 10% by buying the put option on the rainfall sum index. That is to say, the hedging effectiveness of a put option on the best rainfall sum index is nearly completely eroded when the geographical basis risk and the local basis risk are considered; even though the option was explicitly tailored to the revenue function of the farm. Using the put option on the rainfall deficit index results in a 30% reduction of the standard deviation. The reason for the greater hedging effectiveness of the  
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4 rainfall option on the rainfall deficit index is that the explanatory power of the production  
5 function for the wheat yield depending on the rainfall deficit index is much higher than that  
6 depending on the rainfall sum index. The reduction of the hedging effectiveness of both op-  
7 tions, in comparison to scenario 2, is to be attributed to the additional consideration of the  
8 local basis risk.  
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#### 13 14 **IV. Conclusions and outlook**

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16 The model calculations have shown that by using rainfall options a very considerable risk-  
17 reducing effect can be obtained when the reference weather station is located in the immediate  
18 vicinity of the site of production and when there is a very close relationship between yield and  
19 rainfall index. That is, while not being able to avoid climate change on a farm-level, such in-  
20 struments could generate valuable support for those farming under risky conditions.  
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26 However, the model calculations also demonstrated that the basis risk has an extraordinarily  
27 high influence on the hedging effectiveness of rainfall options. When the site of agricultural  
28 production is only at a relatively small distance from the nearest reference weather station (e.g.  
29 39 km in the application available here), the hedging effectiveness is considerably reduced. If,  
30 in addition, an index which only shows a small correlation to the yield underlies the option (as  
31 is established here between the wheat yield and the rainfall sum index, which is often suggested  
32 in literature), the hedging effectiveness decreases even further.  
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39 One could be tempted to conclude from a low hedging effectiveness that the farmers' poten-  
40 tial demand would be low. However, such an interpretation would disregard the difference be-  
41 tween effectiveness and efficiency. The potential demand for a weather derivative results from  
42 the ratio of its costs and its benefits. Derivatives which are based on simple indices and which  
43 display low effectiveness lead to a lower willingness-to-pay on the part of the farmers. How-  
44 ever, as a result of their lower transaction costs they can also be provided at lower prices. We  
45 can, therefore, not a priori conclude that weather derivatives with a low hedging effectiveness  
46 are "inapplicable" or that they do not have a trading potential.  
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54 However, if potential sellers of rainfall options wish to increase the hedging effectiveness,  
55 they should permit a dense network of weather stations as reference points and a widely diversi-  
56 fied spectrum of differently specified weather derivatives. Of course, it is inconceivable that de-  
57 rivatives will be offered for every weather station. The demand for products of this kind would  
58 certainly be too low. A compromise could be to select the average derived from the values of a  
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4 rainfall index at several weather stations as a weather variable underlying the option. The rec-  
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ommendation for offering differently specified weather derivatives affects the derivative type  
on the one hand (cf. footnote 3) and the design of the index, the tick size and the strike level on  
the other hand. Many reference weather stations and weather derivatives designed in very dif-  
ferent ways result in a fragmentation of the demand.

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There is a further need for research with regard to the specification of the payoff function of  
an option. Rainfall sum indices dominating the scientific discussion until now are not suffi-  
ciently target-orientated in the opinion of many producers. An alternative suggestion was made  
here in the form of a rainfall deficit index. From an agronomic viewpoint, however, it could also  
be advisable to incorporate not only the rainfall but also the temperature, the wind etc. in the in-  
dex underlying the option. In this way, for instance, allowance could be made for a situation in  
which low rainfall at high temperatures would lead to higher yield losses than at lower tempera-  
tures. Another task of research concerns the question which was consciously avoided here,  
namely of valuing weather derivatives.

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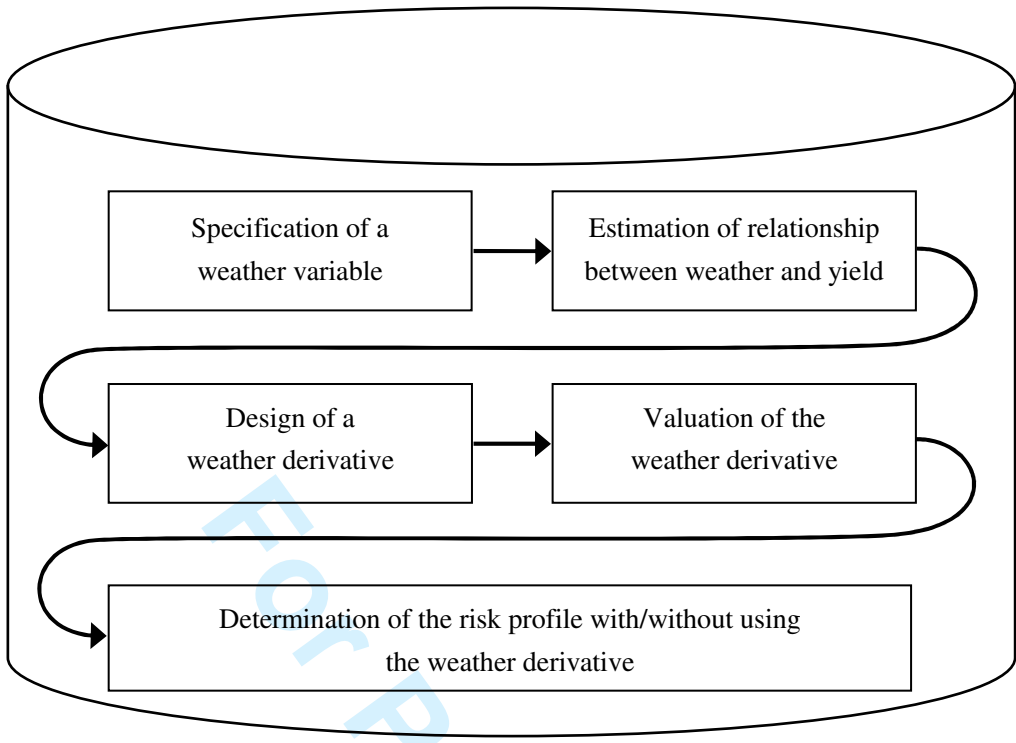
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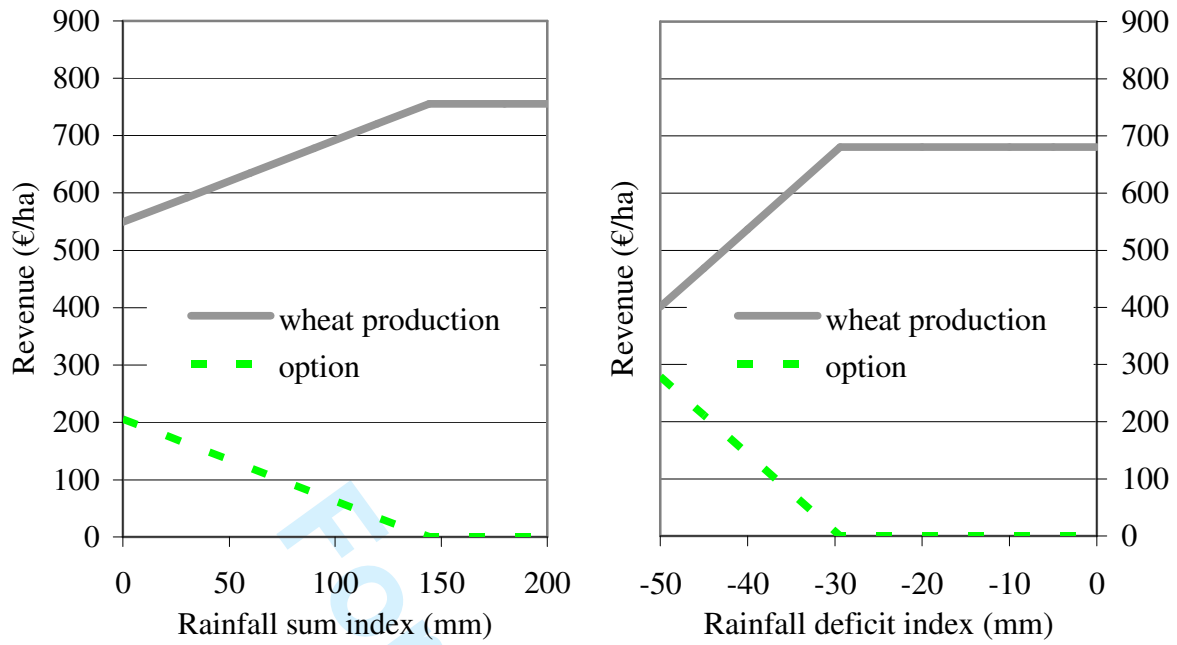
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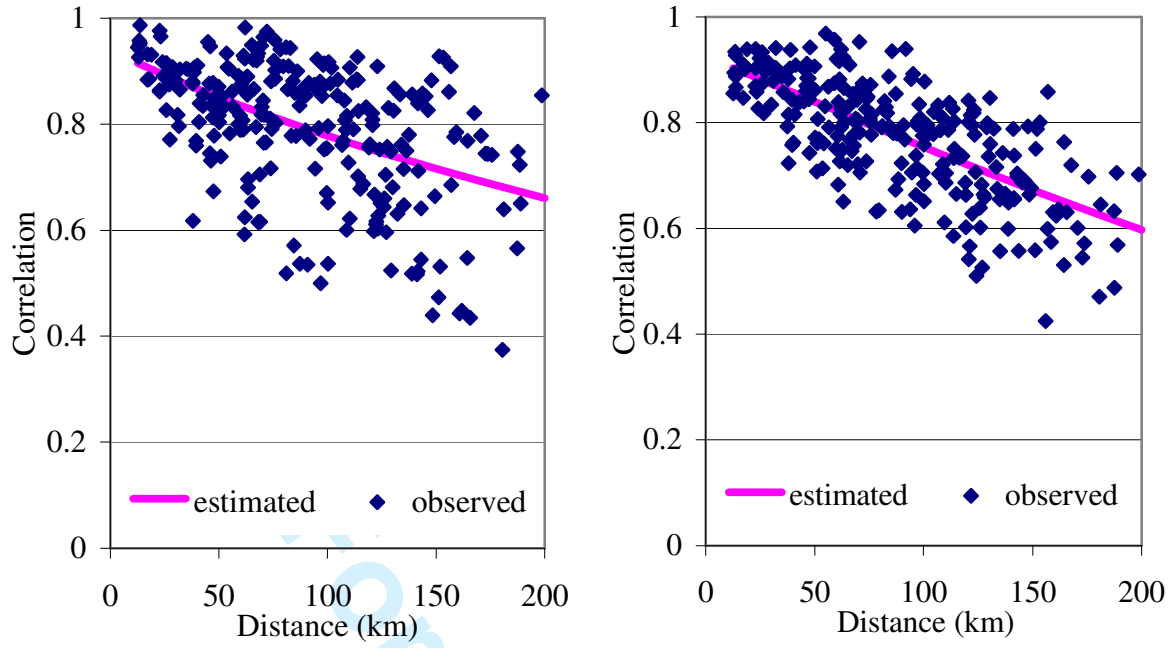


**Fig. 1. Elements in a farm-specific analysis of the hedging effectiveness of weather derivatives**

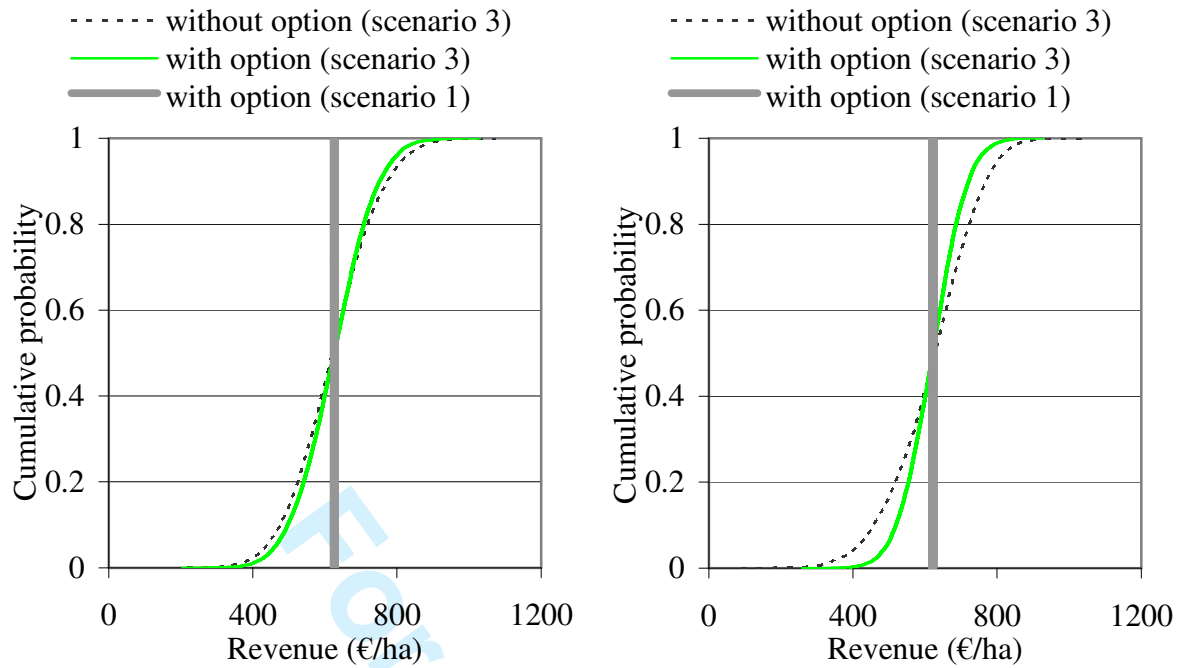


**Fig. 2. Revenue from wheat production and payoff of option depending on the rainfall sum index (left) and the rainfall deficit index (right)**

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**Fig. 3. Decorrelation analysis for the rainfall sum index (left) and the rainfall deficit index (right)**



**Fig. 4. Revenue distributions without and with insurance for the rainfall sum index (left) and the rainfall deficit index (right)**



Table 1. Estimates for different production functions\*

Period	Rainfall sum index				Rainfall deficit index				
	Jan. – June	April – June	May – June	June	Jan. – June	April – June	April – June	April – June	June
$x$	181	91	61	<b>30</b>	–	–	–	–	–
$z$	–	–	–	–	26	19	<b>13</b>	11	4
$s$	–	–	–	–	7	5	<b>7</b>	9	7
$y^{min}$	–	–	–	–	7.5	2.9	<b>7.4</b>	22.1	7.5
$a_0$	0 (0.00)	0 (0.00)	50.9 (4.91)	<b>54.9</b> (8.10)	88.5 (6.84)	137.9 (13.17)	<b>107.8</b> (8.81)	87.8 (4.96)	81.8 (15.67)
$a_1$	0.28 (5.23)	0.58 (7.23)	0.10 (1.20)	<b>0.14</b> (1.38)	0.38 (2.06)	3.73 (6.40)	<b>1.35</b> (3.62)	0.22 (1.45)	1.98 (3.81)
$a_2$	233.1	109.6	220.1	<b>144.3</b>	-39.8	-19.0	<b>-29.4</b>	-53.6	-7.1
$a_3$	64.6 (1.11)	64.1 (3.88)	73.7 (1.37)	<b>75.5</b> (2.68)	73.4 (2.08)	67.1 (2.38)	<b>68.0</b> (2.15)	76.0 (1.91)	67.7 (2.80)
$\sigma_\varepsilon$	10.2	11.0	11.1	<b>10.9</b>	9.9	8.7	<b>8.7</b>	10.8	9.0
$R^2$	0.10	0.09	0.13	<b>0.15</b>	0.30	0.47	<b>0.48</b>	0.17	0.43

\* The t-values are given in parentheses. The critical t-value is 1.81 or 1.37 at a probability of error of 5 or 10%.

**Table 2. Specification of rainfall options under consideration**

	<b>Option 1</b>	<b>Option 2</b>	
Weather index	Designation	Cumulative rainfall index	Rainfall deficit index
	Reference point	Rainfall data at the weather station in Berlin-Tempelhof	Rainfall data at the weather station in Berlin-Tempelhof
	Accumulation period	June	April – June
	Calculation	$I_T^C = \sum_{t=1}^{30} y_t$	$I_T^D = \sum_{\tau=1}^{13} \min\left(0, \sum_{t=(\tau-1)\cdot 7+1}^{\tau\cdot 7} y_t - 7.4\right)$
Option type	(European) put	(European) put	
Strike level $S$	144.3 mm	-29.4 mm	
Tick size $V$	1.4 €/index point	13.5 €/index point	
Maturity $\Delta t$	1 year (01.07.2006 to 30.06.2007)	1 year (01.07.2006 to 30.06.2007)	
Expiry time $T$	2007	2007	
Payoff $F_T$	$\max(144.3 - I_T^C, 0) \cdot 1.4$	$\max(-29.4 - I_T^D, 0) \cdot 13.5$	

**Table 3. Parameters for revenue distributions of wheat production without and with insurance (in €/ha)**

		Scenario 1		Scenario 2		Scenario 3		
Local basis risk		without		without		with		
Geographical basis risk		without		with		with		
Rainfall option		without	with	without	with	without	with	
Rainfall sum index	Expected value	620	620	620	620	620	620	
	Standard deviation	49	0	49	27	117	104	
	Percentile	5%	558	620	558	574	429	446
		10%	565	620	565	588	471	485
		50%	608	620	608	620	619	620
		90%	702	620	702	652	771	755
95%		728	620	728	666	815	793	
Rainfall deficit index	Expected value	599	599	599	599	599	599	
	Standard deviation	84	0	84	51	119	83	
	Percentile	5%	417	599	417	509	381	461
		10%	471	599	471	537	441	492
		50%	656	599	656	599	610	599
		90%	656	599	656	661	740	706
95%		656	599	656	690	773	737	