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Tests and Confidence Intervals for a Class of Scientometric, Technological and Economic Specialisation Ratios

Torben Schubert¹² and Hariolf Grupp³

Abstract: In economic, scientometric, and innovation research, often so-called specialisation indices are used. These indices measure comparative strengths or weaknesses as well as specialisation profiles of the observation units with respect to certain criteria, such as patenting and publication or trade activities. They allow question like: Is Germany specialised in the export of motor vehicles? Or is the UK specialised in biotech patents? Unfortunately, little is known about their statistical properties, which makes valid inferencing difficult. In this article we prove asymptotic normality for a certain class of scientometric, technological, and some economic, though non-monetary, specialisation indices. We provide asymptotic confidence intervals and demonstrate in an example how to obtain statistically sound results. We will also address the problem of normalisation of these indicators. All procedures proposed are provided in an add-on package for R statistical environment.

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1 Introduction

Information about countries' scientific, technological, or economic performance is often required for various reasons. The specific strengths and weaknesses are commonly assessed by indicators. Thus, for example, a country's patent count will be interpreted as a measure of its technological capacity (Blind and Jungmittag, 2005, Jang et al., 2008). Other studies focus on scientific publications to assess a country's scientific performance (Garcia-Castrillo et al., 2002). Apart from using simple counts as performance measures, also specialisation ratios, describing a country's profile (e.g. specialisation in high-tech or low-tech patents; specialisation in natural science or social science publications; export and import profiles), are widely applied (e.g. Jensen, 2002, De Benedictis et al., 2008)

Originally specialisation ratios were introduced in the context of the analyis of trade flows. Among the early indicators are the Revealed Export Advantage (RXA) and the Revealed Import Advantage (RMA) (Keesing, 1965). Another example is the the Revealed Comparative Advantage (RCA) (see Balassa, 1965, 1977, Wolter, 1977, De Benedictis and Tamberi, 2001, for a discussion). Other indicators that describe trade flows emerge from the phenomenon of intra-industry trade (IIT). The earliest indicator measuring IIT is the Grubel-Lloyd Index (GLI) (Grubel and Lloyd, 1971, 1975). Many more IIT indicators have been developed in this branch of research (an overview can be found in Brülhart (1994)).⁴ Later on, in technometric and scientometric research similar indicators originated from the methodogical ideas of the RMA, the RXA, and the RCA, such as the Revealed Patent Advantage (RPA) and the Revealed Literature Advantage (RLA) (Grupp, 1998, pp. 157 - 158, 216 - 219). Indicators also emerged in economic analysis, including the Revealed Trade Mark Advantage (RTMA) and the Revealed Norms and Standards

⁴ Note for now that the GLI and, related to it, other IIT indicators are not really specialisation ratios, as they are discussed in this paper. This will become clear later on.

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Specialisation (RNSS). Additionally, the TRIS database containing national regulations of EUmembers has been used to calculate the Revealed Regulation Specialisation (RRS).⁵ All these indicators have a neutral value which indicates neither above nor below average specialisation. Values below the neutral value are a sign of under-specialisation, whereas values above the neutral indicate over-specialisation.

Due to their easy construction and interpretability they have awakened growing interest in various fields of research, as they provide information about the relative strengths of certain units in measuring specialisation without reference to size. Nonetheless, in a statistical sense, specialisation ratios are complex sample functions, for which the stochastic properties are largely unknown. While there is a formula to calculate some form of "parametric imprecision" (Engelsman and van Raan, 1990), the inability to determine their statistical distribution makes interpretation a cumbersome endeavour, often subjected to intuition or rules of thumb. In the following we will provide the asymptotic distribution for a specific class of specialisation ratios. Commonly, though not exclusively, these specialisation ratios will be technometric or scientometric.

The rest of the paper is organised as follows. Section 2 presents the most common specialisation ratios, to provide an intuition for the interpretation of these indicators. In view of their importance we will also describe the trade-related monetary specialisation ratios, although they are not covered by the statistical analysis of this paper. Section 3 summarises the main statistical results. The derivations may be found in the appendix. Section 4 presents an empirical example and some considerations of robustness with respect to classification decisions. Section 5 concludes.

⁵ http://ec.europa.eu/enterprise/tris/.

2 Common Specialisation Ratios

In this section, we discuss the most common indicators and their meaning in order to provide the reader with a feeling for this type of indicators. We also discuss which indicators meet the conditions needed for the statistical analysis and which do not. Before we do so, we introduce a technical definition and the requirements formally:

Technical Definition: A specialisation ratio is a measure which divides a ratio describing some feature of unit under consideration by an identically constructed ratio corresponding to a reference unit.

Statistical Conditions: (a) The quantities concerned are measured on an absolute scale.⁶ (b) The specialisation ratio can be interpreted as a fraction of fractions.⁷

To begin with, any indicator adhering to the technical definition and the statistical conditions is a specialisation ratio that falls in the class of indicators for which we are able to determine the asymptotic distribution by the methodology used in this paper.

We start our review of the most common specialisation indicators with those that either fail the technical definition or the statistical conditions (or both). Among the earliest specialisation ratios is the Revealed Comparative Advantage (RCA) – a measure for comparative advantage – which is given by⁸

$$RCA_{ik} = \left(E_{ik} / I_{ik}\right) / \left(\sum_{h} E_{hk} / \sum_{h} I_{hk}\right)$$
(1)

⁶ Note that quantities that can be measured on an absolute scale have a natural unit. In our context this will imply that the quantities can be counted (for example, patents).

⁷ The technical definition only requires it to be a ratio of ratios.

⁸ Check that the technical definition applies.

where E and I denote exports and imports in a given product group and a given country. The RCA compares the export to import ratio of some country i for product group k to that of the reference group of countries. A value greater than 1 is indicative of a comparative advantage the country i has with respect to product group k, while a value below 1 is a sign of a comparative disadvantage. Concerning requirements (a) and (b), neither the numerator nor the denominator is assured to be between zero and one, so that none is a fraction. Further, the quantities of the RCA fail the condition of having a natural unit. This is easy to see, by considering the following idea: a count measure could be derived by taking each euro as an individual element. Unfortunately, though unit stepped, this is not unique since the imports or exports could also be measured in yen or dollars. By changing the scale we would also change the number of counts.

The Revealed Export Advantage (RXA) – a measure for export specialisation – and the Revealed Import Advantage (RMA) – a measure for import specialisation – are defined as⁹

$$RXA_{ik} = \left(E_{ik} / \sum_{j} E_{ij}\right) / \left(\sum_{h} E_{hk} / \sum_{h} \sum_{j} E_{hj}\right)$$
(2)

and

$$RMA_{ik} = \left(I_{ik} / \sum_{j} I_{ij}\right) / \left(\sum_{h} I_{hk} / \sum_{h} \sum_{j} I_{hj}\right)$$
(3)

For instance, if the RMA is greater than unity, then country i imports more of product group k in comparison to own total imports than does the reference group of countries compared to its total imports. Country i imports more of product group k, relatively, than does the rest of the world. Clearly, the fractions condition is met. Unfortunately, both the RMA and the RXA fail the natural unit condition for the same reason as the RCA does.

9 In this definition $\sum_{j} E_{ij}$ denotes total exports of country *i*.

Despite these more traditional trade indicators, many advances have been made in measuring intra-industry trade (ITT). The earliest indicator of this type is the Grubel-Lloyd-Index (GLI), which we will shortly discuss here. The GLI is defined by following formula:

$$GLI_{ik} = \frac{\sum_{j} \left(E_{ij} + I_{ij} \right) - \left| \sum_{j} E_{ij} - \sum_{j} I_{ij} \right|}{\sum_{j} \left(E_{ij} + I_{ij} \right)}$$
(4)

where the notation is the same as above. The index takes a value of unity whenever all trade is intra-industrial and zero if all trade is inter-industrial. In fact, the GLI is not a specialisation ratio, as this was defined previously (see the technical definition). The reason for mentioning it here is the problem of aggregation bias, which has a parallel in what will be discussed later in Section 4.2. For the sake of completeness, it shall be noted that neither condition (a) nor condition (b) applies.

We now turn to indicators that meet the technical definition and the statistical requirements. The Revealed Patent Advantage (RPA) – a measure for technological specialisation proxied by patents – and the Revealed Literature Advantage (RLA) – a measure of science specialisation proxied by scientific publications – are defined very similarly to the RXA and the RMA. Take the RLA, for instance:

$$RLA_{ik} = \left(P_{ik} / \sum_{j} P_{ij}\right) / \left(\sum_{h} P_{hk} / \sum_{h} \sum_{j} P_{hj}\right)$$
(5)

where P denotes publications. A value of above 1 means that the fraction of publication in discipline k (e.g. biotechnology) of country i (say, the UK) is greater than the respective fraction of the reference region (e.g. the world). To put it in simple terms: the UK gives, in this hypothetical example, much greater relative emphasis to biotechnology compared to the rest of the world. Thus the fraction condition is met, as with the RMA and the RXA. Also, the *number of publications* is a natural integer stepped unit. The same holds true for the RPA. Other measures with

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identical properties are specialisation ratios based on trade marks (RTMA), norms and standards (RNSS), and technical regulation (RRS), which are certainly economic rather than scientometric or technological indicators.

In summary, the procedures discussed subsequently work well, whenever quantity describing the feature can be (uniquely) counted and classified. This applies for example for the RPA, the RLA, the RTMA, the RNSS, and the RRS, but not for he RXA, the RMA or the RCA and not for any kind of monetary indicator such as the GLI. So the main restriction in an economic sense is that the indicators must be non-monetary.

Another issue concerns interpretability. The fact that all these indicators range between zero and infinity with neutral value at 1 makes interpretation a cumbersome endeavour. Symmetric and normalised indices are easier to understand. Therefore, often the symmetrifying second order Moebius transformation in the form $(r^2-1)/(r^2+1)$, where *r* is the respective specialisation index, is embarked upon (Grupp, 1994, pp. 187 onwards). The transformed index then ranges from -1 to +1 with a neutral value ("no specialisation") at 0. However, there is a large class of similar Moebius transformations,¹⁰ and to our knowledge, there is no mathematical solution to determine the optimal transformation so far.¹¹ In the following analysis we adopt the second order our results hold for any differentiable transformation, which is true for any transformation common to the literature.

¹⁰ Note that $(r^k - 1)/(r^k + 1)$ for any k > 0 has the same properties. Apart from the Moebius transformations there are others with identical normalisation properties.

¹¹ Also confirmed in a private communication from Dr. Markus von Ins, CEST, Switzerland, on September 11, 2006.

3 Asymptotic Results

In this section we briefly present the main theorems derived in this paper. The proofs are given in the Appendix. All of the procedures are implemented in the R-package SRinference (current version: 1.1) freely available under http://www.isi.fhg.de/p/mitarbeiter/tos.html, which does not require much statistical knowledge to use it. Additionally, a user guide is provided, which introduces the basic features of the package to the user. Therefore, for the application-oriented reader these derivations may be skipped as well as the theorems in Section 3. Instead, Section 4 gives an empirical example. This should help to make application and interpretation more accessible.

Let us first introduce some definitions. We will refer to 'unit' when we mean the unit having certain attributes. We will denote as 'objects' the attributes which may take certain values. For example, when we talk about Germany's strength in publishing reviewed articles in the field of natural sciences, Germany is the unit while a given reviewed article is the object (which either belongs to natural sciences or not).

The theorems only present the (asymptotic) distributions of the statistics under consideration. In any case, this is enough for our purpose because once their distribution is known to be normal, it is straightforward to define valid tests and confidence intervals, following the spirit of usual ttests or t-based intervals.

We define the following variates:

 X_{ij} A random variable, which is 1, whenever object *i* for unit *j* belongs to the field under consideration and 0 otherwise¹²

¹² We use either k or v throughout the text to denote the subjects under consideration. Also note that by defining an individual object we make use of the 'absolute scale' condition.

 $\sum_{i=1}^{n_j} X_{ij}$ A random variable which counts the number of all objects for unit *j* which belong

to the field under consideration

When different times are concerned, the objects and their number will be denoted by X_{ij}^k and n_j^k where the superscript indicates the time period.

During applied work it is often necessary to determine if a country is specialised e.g. in patenting activity in the chemical industry field. However, for values of the RPA close to zero, it is hard to maintain that the observed deviation is not just coincidental. Therefore a one-sample test is useful to determine whether the observed effect is not just noise. The result of Theorem 1 allows such inference, including, of course, the construction of confidence intervals.

Theorem 1 (One Sample Inference): If i) n_j is non-random for all j, ii) X_{ij} is independent of X_{hl} whenever both variates denote different objects, iii) when n increases, also each n_j grows, such that $n/n_j \rightarrow const$, iv) the function used to transform the linear indicator is differentiable around the estimated value, v) (a) the objects have a natural unit and (b) the indicator has a fraction of fractions meaning, then the transformed specialisation ratio is asymptotically normal and \sqrt{n} -consistent with a variance that can be consistently estimated from the data.

Especially assumption **ii**) is very strong. It essentially assumes away any kind of economic reasons for dependence. Taking the example of patenting activity, it means that regional clustering of industrial (and therefore innovative) activity is neglected, despite the fact that its existence is widely accepted in the literature (Krugman, 1991). There are a multitude of reasons for that, including spill-overs, endowment with natural or human resources, demand and supply side externalities resulting from transportation costs, pathdependence, etc. Yet the independence assumption is unavoidable from a statistical point of view (see Appendix). The reader is encouraged to

decide if in a specific application this assumption seems justified or if it is too strong. This will also depend on how strong regional interdependencies are believed to be.

Very often we would like to test whether two specialisation ratios are significantly different or not. For example, we might like to know if Italy's specialisation in astrophysical publications is significantly different from that of Portugal. This is also possible as indicated in Theorem 2.

Theorem 2 (Two Sample Inference): Under the conditions of Theorem 1, the difference of the transformed specialisation ratio is asymptotically normal and \sqrt{n} -consistent with a variance that can be consistently estimated from the data.

Sometimes changing structures in time are relevant. We may, for example, want to know if the patent specialisation of the UK concerning biotechnology has significantly changed over time. Theorem 3 gives conditions under which we can test for this.

Theorem 3 (Time Change Inference): If **i**) n_j^k is non-random for all j and $k \in \{s, t\}$, **ii**) X_{ij}^k is independent of X_{hl}^v whenever both variates denote different objects, **iii**) when n^t increases, also each n_j^t and n_j^s grows, such that $n^t/n_j^s \rightarrow const$ and $n^t/n_j^t \rightarrow const$, **iv**) the function used to transform the linear indicator is differentiable around the estimated value, **v**) (a) the objects have a natural unit and (b) the indicator has a fraction of fractions meaning, then the difference of the transformed specialisation ratios in time is asymptotically normal and \sqrt{n} -consistent with a variance that can be consistently estimated from the data.

In essence, Theorems 1-3 define ways to construct confidence intervals and tests for the statistics discussed (let these be denoted as T_n) by approximating the finite sample distribution with its asymptotic counterpart. However, simulation studies have shown that this approximation may be quite imprecise if the sample size is small. We therefore provide a bootstrap procedure which has

better rates of convergence (Hall, 1992, Horrowitz, 2001). In essence, this will make inference much more precise in small samples. The consistency results are summarised in Theorem 4.

Theorem 4 (Bootstrap Inference): Under the respective conditions of Theorems 1-3 the resampling bootstrap distribution of any of the statistics T_n is a consistent estimate of the true distribution.

From a practical point of view, in small samples we recommend the use of the estimator described in Theorem 4 (function *SRboottest* in the R-package). However, with large enough samples $(n > 200 \text{ and } n_j > 15 \text{ for all } j)$, the analytical tests and confidence intervals from Theorems 1-3 give a reasonably good approximation (function *SRtest* in the R-package). Under these conditions time savings should outweigh the higher precision of the bootstrap method.



4 An Empirical Example and the Problem of Classification

In this section we present an empirical application and discuss the robustness of the procedure with respect to the definition of the classes.

4.1 A Short Empirical Example

 To save space, we present only the case of one sample inference. We use the asymptotic test from Theorem 1. In any case, the other procedures work in very much the same manner.

For the empirical example we use patent data on 11 countries gathered for a study of the catchingup process of several of Germany's world market competitors in the context of the Technological Performance Report 2006 prepared for the German Ministry of Education and Research.

One task of this study was to describe the technological profile of these catching-up countries by their patenting profile.¹³ The results for the profile of patenting activity are depicted in Figure 1.

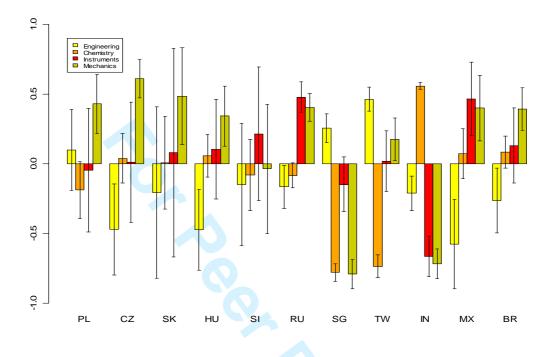
¹³ To do this, specialisation ratios as described above were used along with the second order Moebius transformation. The latter bounds the specialisation ratio to the interval -1 and 1. A zero indicates that the country average is identical with the reference group average (often the world average) while positive values indicate above average und negative below average specialisation.



55 56

57 58

59 60 Figure 1: Patent Profile for 11 catching-up countries in 2003 (including 95%-confidence intervals)



The main results can be summarised as follows. The eastern European countries (Poland, Czech Republic, Slovakia, Hungary, and Russia) have somewhat similar profiles, putting high weight on mechanics. This means that they are still, to some degree, in the production tradition of the Warsaw Pact. Slightly different profiles are apparent for Slovenia, Slovakia, Hungary, and Russia which are specialised in instruments. However, we also see that only the Russian specialisation in instruments is statistically significant, which indicates that the results for the other three countries are not overwhelmingly reliable. Though not applying to Slovenia, where none of the estimated specialisation ratios is statistically significant from zero, the similar profiles across the Eastern European countries are largely real effects. The non-significance in the Slovenian case might have two reasons. First, it does not have a very sharp profile. So indeed, Slovenia might follow a rather

'generalist' patenting strategy. Second, Slovenia's patent counts are very low. Therefore, the precision of the specialisation ratios is limited. The bands for India, on the contrary, are very narrow, because the total number of India's patents is relatively large (1202).

Analogous to the eastern European cluster there is definitely a South American cluster of Mexico and Brazil, which also share similar profiles. To some extent, Singapore and Taiwan also have similarities.

So the main conclusion of this analysis could be that in fact regional clusters of technological specialisation do exist, that are shaped by regional, technological or cultural proximity and possibly by comparable factor and human capital endowments.

However, knowledge about statistical confidence is still absolutely necessary, in order to separate real effects from purely random ones. The same applies to time change inference. This can help to detect significant changes in country profiles earlier or prevent researchers from interpreting noise as relevant changes.

4.2 Influence of the Classification

Motivated by the well-known aggregation bias inherent to the construction of the GLI,¹⁴ it is worthwhile asking what is likely to happen, if the classes of the previous example (engineering, chemistry, instruments, and mechanics) were disaggregated. Intuitively, it can be expected that the significance of specialisation is likely to decrease, because estimations will become less precise. If this were true, then disaggregating patent classes would have a very similar effect to the

¹⁴ Aggregation bias in this context means that IIT is overestimated and vanishes after disaggregation The reason is the 'opposite sign effect'. (Gray, 1979, Greenaway, 1983, Tharakan, 1984, Balassa, 1987, Doroodian et al., 1999, Bahmani-Oskooee and Harvey, 2006).

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aggregation bias, though for a very different reason. This question is of special relevance, because classification is largely arbitrary.

Referring to the empirical example of the previous subsection, the chosen level with only four classes is rather broad. Since the International Patent Classification (version 7) contains about 85,000 classes, we could have relied on a much more detailed analysis.

We will demonstrate that the asymptotic variance will increase with the number of the classes considered, implying a decrease of precision and significance. In any case, finding an analytical solution in the general case seems very hard. Therefore we consider only a special case in which, after still tedious calculations, an easy closed form expression pertains.

Taking the test of Theorem 1 along with the second order Moebius transformation, we assume that for a given class, no subject is over- or under-specialised and that each subject holds an identical number of objects. Further, we assume that all classes have the same probability that an object belongs to them both before and after disaggregation.

These assumptions result in the following simplifications:

$$\pi_{1} = \pi_{2} = \dots = \pi_{J} = \pi = \frac{1}{K}$$

$$n_{1} / n = n_{2} / n = \dots = n_{J} / n = \frac{1}{J}$$
(6)

where K and J are the number of classes and the number of subjects. Taking the expression for the asymptotic variance of test in Theorem 1¹⁵, we see that

$$\sigma_I^2 = n \sum_{j=1}^J \left(\frac{dI}{dr} \frac{\partial r}{\partial \pi_j} \right)^2 \frac{\pi_j (1 - \pi_j)}{n_j}$$

¹⁵ Equation (10) of the Appendix.

$$= \left(\frac{dI}{dr}\right)^{2} \frac{K-1}{K^{2}} J \sum_{j=1}^{J} \left(\frac{\partial r}{\partial \pi_{j}}\right)^{2}$$

$$= \left(\frac{dI}{dr}\right)^{2} \frac{K-1}{K^{2}} J \left[\left(\frac{\pi}{\pi^{2}} \frac{1}{J}\right)^{2} (J-1) + \left(\left(\frac{\pi}{\pi^{2}} \frac{1}{J}(J-1)\right)^{2}\right) \right]$$

$$= \left(\frac{4r}{(r^{2}+1)^{2}}\right)^{2} (K-1)(J-1)$$

$$= (K-1)(J-1)$$
(7)

where the last line follows from the assumption of no specialisation, i.e. r = 1. This indicates that the asymptotic standard error increases by the order 1/2 in the number of classes. Therefore, disaggregating too much will increase the asymptotic variance and for any given sample size will result in a drop in significance.

However, unlike the aggregation bias known from the GLI, this is not a measurement bias, but purely a statistical problem of finite samples, which vanishes asymptotically for any finite number of classes.

Still, it should be stressed that the definition of classes should follow an economically sensible understanding and should result in a manageable number of classes, because otherwise the precision of the specialisation ratios is lost.

Conclusion

Specialisation ratios are in wide use concerning science, technology and trade assessment. Up to now, little was known about their statistical reliability. In order to progress in this field, we proved asymptotical normality for a certain type of non-monetary specialisation ratios. We used this knowledge to provide asymptotic confidence intervals and tests for the one and two-sample problem and the two-sample time change problem, whose critical values converge at usual rates, obtained from first order asymptotics. We showed in an empirical example how this knowledge can be applied to obtain statistically sound results. As specialisation ratios are a widely accepted und frequently used tool in economics, scientometrics, and technometrics, we believe that these new inferencing techniques are extremely relevant to any user of such indicators. In order to guarantee fast dissemination, we implemented each method proposed in an add-on package for R

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Appendix

Proof of Theorem 1:

Under conditions i) and ii) we have

$$X_{ik} \sim B(1, \pi_k)$$
 with $E(X_{ik}) = \pi_k$, $V(X_{ik}) = \pi_k(1 - \pi_k)$ (1)

as well as

$$\sum_{i=1}^{n_j} X_{ij} \sim B(n_j, \pi_j) \text{ with } E\left(\sum_{i=1}^{n_j} X_{ij}\right) = n_j \pi_j, \ V\left(\sum_{i=1}^{n_j} X_{ij}\right) = n_j \pi_j (1 - \pi_j) \qquad \forall j \quad (2)$$

Check that the true value of the linear specialisation ratio can be defined by:

$$r = E\left(n_k^{-1}\sum_{i=1}^{n_k} X_{ik}\right) / E\left(n^{-1}\sum_{j=1}^{J}\sum_{i=1}^{n_j} X_{ij}\right) = \frac{\pi_k}{\sum_{j=1}^{J}\frac{n_j}{n}\pi_j} \equiv \frac{\pi_k}{\pi}$$
(3)

This can be estimated by using the corresponding sample shares. To establish the asymptotics of the estimator $\hat{r} = \pi_k / \pi$, we first show that the estimated shares are normal.

We have:

$$n_{j}^{-1}\sum_{i=1}^{n_{j}}X_{ij} \xrightarrow{d} N\left(\pi_{j}, \frac{\pi_{j}(1-\pi_{j})}{n_{j}}\right)$$

$$\tag{4}$$

which follows from the central limit theorem. The linear indicator is thus a function of J asymptotically normal variables. We use the mean value expansion (see Hayashi, 2000, Wooldridge, 2002) to derive the following statement:

$$\hat{r} = r + \frac{\partial r}{\partial \pi} \Delta \pi$$
(5)

where
$$\partial r / \partial \overline{\pi} = \left(-\pi_k \frac{n_i}{n} / \pi^2, ..., \left(\pi - \frac{n_k}{n} \pi_k \right) / \pi^2, ... - \pi_J \frac{n_J}{n} / \pi^2 \right)$$
 is the gradient evaluated at
values for the shares caught between the true and the estimated. Also, note that
 $\Delta \pi = \left(\pi_1 - \pi_1, ..., \pi_J - \pi_J \right)^{'}$. We obtain:
 $\sqrt{n} \left(\hat{r} - r \right) = \frac{\partial r}{\partial \overline{\pi}} \sqrt{n} \Delta \pi + o_p (1)$
 $\stackrel{d}{\rightarrow} N \left(0, \frac{\partial r}{\partial \overline{\pi}} \operatorname{cov} \left(\sqrt{n} \pi \right) \frac{\partial r'}{\partial \overline{\pi}} \right)$ (6)

From independence stated in ii) we find that the covariance matrix is diagonal:

$$\operatorname{cov}\left(\sqrt{n}\,\pi\right) \equiv V = diag\left(\frac{n}{n_1}\pi_1(1-\pi_1), \dots, \frac{n}{n_J}\pi_J(1-\pi_J)\right)$$
(7)

Thus we conclude that $\Delta \pi$ is \sqrt{n} -consistent when **iii**) holds. The variance can be calculated by straightforward matrix multiplication

$$\left(\partial r / \partial \overline{\pi}\right) V \left(\partial r / \partial \overline{\pi}\right) = n \sum_{j=1}^{J} \left(\frac{\partial r}{\partial \pi_j}\right)^2 \frac{\pi_j (1 - \pi_j)}{n_j}$$
(8)

Now, again by the delta method under **iv**) any of the transformed versions is also normal. Let the transformation function be denoted by $I: \ ^+ \rightarrow [a,b]$, where [a,b] is some interval on , possibly even itself. Then we use the mean value theorem to get:

$$\sqrt{n}\left(\hat{I}-I\right) = \left(\frac{dI}{dr}\frac{\partial r}{\partial \pi_{1}}, \dots, \frac{dI}{dr}\frac{\partial r}{\partial \pi_{J}}\right)\sqrt{n}\Delta\pi + o_{p}\left(1\right) \xrightarrow{d} N\left(0, \sigma_{I}^{2}\right)$$
(9)

with

$$\sigma_I^2 = n \sum_{j=1}^J \left(\frac{dI}{dr} \frac{\partial r}{\partial \pi_j} \right)^2 \frac{\pi_j (1 - \pi_j)}{n_j}$$
(10)

The important point with (9) and (10) is that we can treat \hat{I} as approximately normal with $N(I, \sigma_I^2/n)$, where σ_I^2 is a consistent estimator of σ_I^2 usually obtained by replacing (π_k, π) with the sample shares.

Proof of Theorem 2:

Define $\Delta I \equiv I_v - I_k = I_v (r_v (\pi_v, \pi)) - I_k (r_k (\pi_k, \pi))$. It is easy to verify that:

$$\sqrt{n}\left(\Delta I - \Delta I\right) = \frac{\partial \Delta I}{\partial \overline{\pi}} \sqrt{n} \Delta \pi + o_p(1) \xrightarrow{d} N\left(0, \frac{\partial \Delta I}{\partial \overline{\pi}} V \frac{\partial \Delta I}{\partial \overline{\pi}}\right)$$
(11)

where we obtain the gradient of ΔI by:

$$\frac{\partial \Delta I}{\partial \overline{\pi}} = \left(-\frac{dI_{v}}{dr_{v}} \frac{\pi_{v}}{\pi^{2}} + \frac{dI_{k}}{dr_{k}} \frac{\pi_{k}}{\pi^{2}}, ..., \frac{dI_{v}}{dr_{v}} \frac{\pi - \pi_{v} \frac{n_{v}}{n}}{\pi^{2}} + \frac{dI_{k}}{dr_{k}} \frac{\pi_{k} \frac{n_{v}}{n}}{\pi^{2}}, ..., -\frac{dI_{v}}{dr_{v}} \frac{\pi_{v} \frac{n_{s}}{n}}{\pi^{2}} + \frac{dI_{k}}{dr_{k}} \frac{\pi_{v} \frac{n_{s}}{n}}{\pi^{2}} \right) (12)$$

as well as V is given by

$$\left(\partial\Delta I / \partial\overline{\pi}\right) V \left(\partial\Delta I / \partial\overline{\pi}\right) = n \sum_{j=1}^{J} \left(\frac{\partial\Delta I}{\partial\pi_j}\right)^2 \frac{\pi_j (1 - \pi_j)}{n_j}$$
(13)

Proof of Theorem 3:

To compare indicators over time is conceptually very much the same. The proof follows along the lines of that of Theorem 2. We therefore omit most of it. However, since ΔI consists of twice as many different estimators for the sample shares, the variance is slightly different:

$$\sigma_I^2 = n^t \sum_{j=1}^J \left[\left(\frac{\partial I^s}{\partial \pi_j^s} \right)^2 \frac{\pi_j^s (1 - \pi_j^s)}{n_j^s} + \left(\frac{\partial I^t}{\partial \pi_j^t} \right)^2 \frac{\pi_j^t (1 - \pi_j^t)}{n_j^t} \right]$$
(14)

where the derivatives of the transformations are collected in the following vector:

$$\frac{\partial \Delta I}{\partial \overline{\pi}} = \left(-\frac{dI^{t}}{dr^{t}} \frac{\pi_{k}^{t} \frac{n_{k}^{t}}{n^{t}}}{\pi^{t^{2}}}, \dots, \frac{dI^{t}}{dr^{t}} \frac{\pi^{t} - \pi_{k}^{t} \frac{n_{k}^{t}}{n^{t}}}{\pi^{t^{2}}}, \dots, -\frac{dI^{t}}{dr^{t}} \frac{\pi_{k}^{s} \frac{n_{k}^{t}}{n^{s}}}{\pi^{s^{2}}}, \dots, -\frac{dI^{s}}{dr^{s}} \frac{\pi^{s} - \pi_{k}^{s} \frac{n_{k}^{s}}{n^{s}}}{\pi^{s^{2}}}, \dots, \frac{dI^{s}}{dr^{s}} \frac{\pi_{k}^{s} \frac{n_{k}^{s}}{n^{s}}}{\pi^{s^{2}}}, \dots, -\frac{dI^{s}}{dr^{s}} \frac{\pi^{s} - \pi_{k}^{s} \frac{n_{k}^{s}}{n^{s}}}{\pi^{s^{2}}}, \dots, \frac{dI^{s}}{dr^{s}} \frac{\pi_{k}^{s} \frac{n_{k}^{s}}{n^{s}}}{\pi^{s^{2}}}$$

Proof of Theorem 4:

We will not discuss the testing problem explicitly because a confidence interval that entails the value of the null hypothesis is indicative of a non-ejection decision with the corresponding test. First, we will define the bootstrap algorithm and then argue why it is consistent.

- Given $X_j = (X_{j1}, ..., X_{jn_j})$ for all *j*, calculate θ_n , where θ_n is one of the estimators described in Theorem 1-3.
- Draw from each vector X_j n_j elements randomly with replacement. From this form the bootstrap sample $X_j^* = \left(X_{j1}^*, \dots, X_{jn_j}^*\right)$.
- Calculate $|T_n^*| = |\sqrt{n} (\theta_n^* \theta_n) / s_n^*|$ for the two-sided alternative or

 $T_n^* = \sqrt{n} \left(\theta_n^* - \theta_n\right) / s_n^*$, where θ_n^* and s_n^* are the bootstrap point estimator and its corresponding standard deviation. The latter will be calculated by one of equations (10), (13) or (14).¹⁶

- Repeat the last two steps very often.¹⁷ Take from the resulting bootstrap EDF the $1-\alpha$ -quantile, $z_{n,\alpha/2}^*$.
- Define the bootstrap confidence interval as $\theta_n \pm z_{n,\alpha/2}^* s_n / \sqrt{n}$, where s_n can be calculated by one of (10), (13) or (14) based on the original sample.

It should be noted that this approach follows a non-parametric re-sampling strategy, which might seem curious at first sight, because we have specified a parametric distribution. However, since the binomial distribution has only two outcomes (success and failure), both techniques have identical statistical properties, which is not the case with any other common statistical distribution.

Concerning consistency, it is shown by Beran and Ducharme (1992) that we need to meet three conditions:

- $\sup_{x} \|F(x) F(x)\| \to 0$, i.e. that the EDF converges uniformly to the CDF.
- $G_{\infty}(x, F)$, denoting the asymptotic CDF of the statistic, is continuous.

¹⁶ In fact, we could use a nested bootstrap to determine the variance. But this is computationally even more intensive. Since we are in the lucky situation of having an asymptotic expression for the variance it is better to use this for practical reasons (see e.g. Wassermann (2006)).

¹⁷ The precision increases with the number of bootstrap replications. Thus infinite replications would be ideal. Since this is impossible for reasons of finite computation time, a usual recommendation is to choose 1,000-5,000 replications.

• for each sequence $\{H_n\}$ out of properly defined neighbourhood of F, such that H_n converges to F, $\lim_{n \to \infty} G_n(x, H_n) = G_{\infty}(x, F)$.

Checking the second and third condition is absolutely standard. The second holds because we know that the distribution of the statistics under consideration are asymptotically N(0,1). Therefore, $G_{\infty}(x, F) = N(0, 1)$ in the one-sided interval and when we use the two-sided interval, $G_{\infty}(x,F) = HN(\sqrt{2/\pi}, \sqrt{(\pi-2)/\pi})^{18}$. Turning to the third condition, we use Polya's Theorem which states that for any X_n converging to X almost surely, if the corresponding distribution function Z_X is continuous, then $\lim_{n \to \infty} \sup_{x} \left(\left| Z_{X_n}(x) - Z_X(x) \right| \right) = 0$. Along with condition 2, we must have $\lim_{n\to\infty} \sup_{x} \left(\left| G_n(x, H_n) - G_\infty(x, F) \right| \right) = 0$, which implies the last condition. Combining this with the first condition (if it holds), it follows that $\lim_{n \to \infty} P\left(\sup_{x} \left(\left| G_n\left(x, F\right) - G_{\infty}\left(x, F\right) \right| \right) > \varepsilon \right) = 0.$ The first condition requires $\sup \|F(x) - F(x)\| \xrightarrow{p} 0$, where $F(\cdot)$ is vector of *J* distribution functions corresponding to the distribution of the objects in each of the *j* subjects. Because of the Glivenko-Cantelli Theorem we have component-wise convergence. However, with the Euclidean distance this is enough

(see also Serfling, 2002). Check that:

$$P\left(\sup_{x}\left\|F\left(x\right)-F\left(x\right)\right\|<\varepsilon\right)=P\left(\sup_{x}\left(\sum_{j=1}^{J}\left(F_{j}\left(x\right)-F_{j}\left(x\right)\right)^{2}\right)^{1/2}<\varepsilon\right)$$
$$\geq P\left(\sup_{x}\sum_{j=1}^{J}\left|F_{j}\left(x\right)-F_{j}\left(x\right)\right|<\varepsilon\right)\geq P\left(\sum_{j=1}^{J}\sup_{x_{j}}\left|F_{j}\left(x_{j}\right)-F_{j}\left(x_{j}\right)\right|<\varepsilon\right)\rightarrow1$$
(16)

Thus all conditions are met and the bootstrap is consistent.